

Constant average
rate of change

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The function
graph is a line

Monotony of
functions

$$x \in \text{Dom}(f): f'(x) = 0$$

$$\frac{\Delta y}{\Delta x} = c$$

where c is a constant

The change of the dependent variable is a multiple of the change of the independent variable

Point on the graph where the function goes from decreasing to increasing or vice versa

They are critical point for the f'' graphic

The change in the dependent variable and the change in the independent variable are directly proportional

The instantaneous rate of change approaches a constant

$$f''(x) > 0 \text{ or } f''(x) < 0, \forall x \in I$$

Product Rule

$$(fg)'(x) = f'(x)g(x) + f(x)g'(x)$$

The relationship
between the
independent
variable and the
dependent variable
is linear

The graph of the
function is
increasing or
decreasing on an
interval I

The graph of the
function is
increasing or
decreasing on an
interval I

Points where the
instantaneous rate
of change of a
function is zero

If $x_1 < x_2$ then $f(x_1) < f(x_2)$
or $f(x_1) > f(x_2), \forall x_1, x_2 \in I$

$$f'(x) > 0 \text{ or } f'(x) < 0, \forall x \in I$$

They are critical points where exist a sign change of the first derivative

Points where exist a change in the concavity of the graph of the function

The instantaneous rate of change is always positive or always negative on an interval I

The tangent line to the graph of the function is increasing or decreasing

The concavity changes at an inflection point

Critical points

Critical Points

Chain Rule

$$(f \circ g)'(x) = f'(g(x))g'(x)$$

Study of the sign of
the first derivative
of a function

Local maximum
point or local
minimum point

Point on the graph
of a function
where an extreme
value is reached

Value of the domain where the tangent line to the graph of the function is horizontal

Inflection points

The graph of the function is concave up or concave down

Point of the domain where the slope of the line is zero

Points where the function does not present changes

Power rule
 $(x^n)' = nx^{n-1}$

Function's optimization	Function's optimization
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Points where the graph of f' has a horizontal tangent line	Global maximum point or global minimum point
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First or second derivative test/Modeling using derivatives	The instantaneous rate of change of f' is not constant
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Quotient rule

$$\left(\frac{f}{g}\right)'(x) = \frac{f'(x)g(x) - f(x)g'(x)}{g^2(x)}$$

Extreme points of
the graph of a
function

Points in the
domain of f where
exist a sign change
of f''

Points in the
domain of f where
exist a sign change
of f''

It is related to the
change of f'

The graph of the
function goes from
increasing faster (or
decreasing faster) to
increasing slower (or
decreasing slower)

Possible extreme
points of the graph
of f'

Addition and
subtraction rule

$$(f \pm g)'(x) = f'(x) \pm g'(x)$$

Concavities of the
graph of a function

Concavities of the
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Study of the sign
of the second
derivative of a
function

Implicit derivation
rule

