

Bra-ket notation

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The bra-ket notation, also called Dirac notation, is designed to make some operations of quantum mechanics easier. The notation uses angle brackets to denote vectors in a complex Hilbert space.

A **ket** is written as $|\psi\rangle$ and represents a column vector (state vector), while a **bra**, written as $\langle\phi|$ represents the conjugate transpose (row vector) of a ket.

The inner product (overlap) between two states is written as

$$\langle\phi|\psi\rangle,$$

and in quantum mechanics this expression is interpreted as the probability amplitude for a state ϕ to collapse onto ψ (the state ϕ is projected onto the state ψ).

The outer product, which forms an operator, is written as:

$$|\psi\rangle\langle\phi|$$