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Problem description

The requirement was to provide a parallel version of the Hopcroft-Karp algorithm for finding a maximum-cardinality matching in a Bipartite Graph. This implementation is a hybrid of message passing and shared memory paradigms, leveraging MPI and CUDA technologies. There are no constraints on the graph structure or memory allocation type, allowing for complete flexibility in data management.

Solution

In the proposed solution, the bipartite graph is generated randomly. Specifically, it is generated based on the number of nodes in each of the two parts. As a matter of simplicity and to better handle testing, given a pair of m (number of nodes in set X) and n (number of nodes in set Y), the generated graph is always the same.

2.1 MPI

The bipartite graph is generated and divided among the MPI processes. Each process is responsible for computing a local matching within its portion of the graph. This parallel execution enables the algorithm to leverage the computational resources of multiple processors simultaneously, thereby potentially speeding up the overall computation.

After computing the local matchings, the results need to be aggregated to determine the global maximum matching. MPI facilitates this aggregation through collective communication operations. Specifically, the local matchings from all processes are gathered to a designated root process (often process with rank 0). This root process then analyzes the collected data to identify the global maximum matching.

2.2 CUDA

The core of the Hopcroft-Karp algorithm is the breadth-first search (BFS) traversal, which is crucial for finding augmenting paths in the bipartite graph.

In CUDA, the BFS traversal is parallelized by assigning each vertex in set X of the bipartite graph to a separate CUDA thread.

This parallelization enables multiple BFS traversals to occur concurrently, with each CUDA thread exploring a different part of the graph simultaneously.

As a result, the computational workload is distributed across thousands of CUDA cores available on the GPU, leading to significant speedup compared to sequential execution on the CPU.

2.3 MPI & CUDA

By combining the distributed memory parallelism of MPI with the GPU acceleration of CUDA, the hybrid approach achieves a synergistic effect, enabling efficient parallelization of the Hopcroft-Karp algorithm on large-scale bipartite graphs. This approach leverages the scalability of MPI and the massive parallelism of GPUs, resulting in significant performance gains and scalability across heterogeneous computing platforms.

Experimental setup

3.1 Hardware

Architecture: x86_64 CPU op-mode(s): 32-bit, 64-bitAddress sizes: 43 bits physical, 48 bits virtual Byte Order: Little Endian CPU(s): On-line CPU(s) list: 0 - 3Vendor ID: AuthenticAMD Model name: AMD Ryzen 3 3250U with Radeon Graphics CPU family: 23 Model: 24 Thread(s) per core: 2 Core(s) per socket: Socket(s): 1 Stepping: 1 Frequency boost: enabled CPU(s) scaling MHz: 60% CPU max MHz: 2600,0000 CPU min MHz: 1400,0000 5190,28 BogoMIPS: fpu vme de pse tsc msr pae mce cx8 Flags: apic sep mtrr pge mca cmov pat pse36 clflush mmx fxsr sse sse2 ht syscall nx mmxext fxsr_opt pdpe1gb rdtscp lm constant_tsc rep_good nopl nonstop_tsc cpuid extd_apicid aperfmperf rapl pni pclmulqdq

monitor ssse3 fma cx16 sse4_1 sse4_2 movbe popcnt aes xsave avx f16c rdrand lahf_lm cmp_legacy svm extapic cr8_legacy abm sse4a misalignsse 3dnowprefetch osvw skinit wdt tce topoext perfctr_core perfctr_nb bpext perfctr_llc mwaitx cpb hw_pstate ssbd ibpb vmmcall fsgsbase bmi1 avx2 smep bmi2 rdseed adx smap clflushopt sha_ni xsaveopt xsavec xgetbv1 clzero irperf xsaveerptr arat npt lbrv svm_lock nrip_save tsc_scale vmcb_clean flushbyasid decodeassists pausefilter pfthreshold avic v_vmsave_vmload vgif overflow_recov succor smca sev sev_es

3.2 Memory Device

Array Handle: 0x0013

Error Information Handle: 0x001C

Total Width: 64 bits

Data Width: 64 bits

Size: 4 GB

Form Factor: SODIMM

Set: None

Locator: Bottom - Slot 2 (right)

Bank Locator: PO CHANNEL B

Type: DDR4

Type Detail: Synchronous Unbuffered (Unregistered)

3. EXPERIMENTAL SETUP

Speed: 2667 MT/s

Manufacturer: Kingston

Serial Number: E6629A6F

Asset Tag: Not Specified

Part Number: HP26D4S9S1ME-4

Rank: 1

Configured Memory Speed: 2400 MT/s

Minimum Voltage: 1.2 V

Maximum Voltage: 1.2 V

Configured Voltage: 1.2 V

3.3 Software

1

OS: Linux Ubuntu 6.5.0-21-generic.x86_64

GCC: gcc (Ubuntu 13.2.0-4ubuntu3) 13.2.0

Swap: 4GiB

Performance and SpeedUp

4.1 Performance

Regarding performance, testing was carried out for three dimensions of the graph: 10000 nodes, 20000 nodes, 30000 nodes. N.B. These numbers refer to the number of nodes in each of the two partitions. It was chosen to have the same number of nodes in each partition as a matter of simplicity. To ensure a fair veracity of the results, each test was run 10 times. Before showing the test results, it is important to specify that regarding MPI, the -O3 optimization of gcc was used and 4 MPI processes were used.

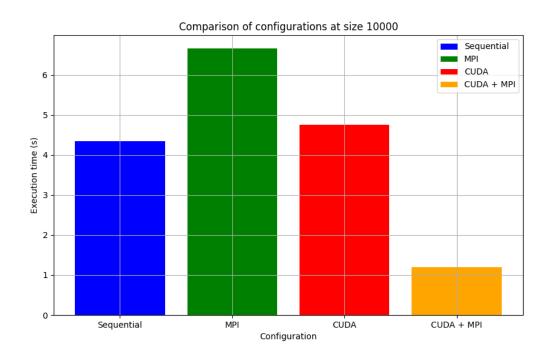


Figure 4.1: Comparison of configurations at size 10000

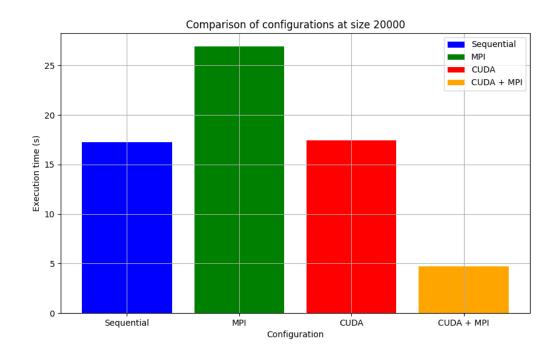


Figure 4.2: Comparison of configurations at size 20000

Regarding the 10000 and 20000 sizes, we can see that the performance of CUDA is similar to the serial version. The same is true for MPI, which is even worse than the serial version, this may be due to the overhead caused by synchronization and communication between processes.

However, we can see that the hybrid CUDA+MPI version increases performance dramatically and thus is the optimal choice.

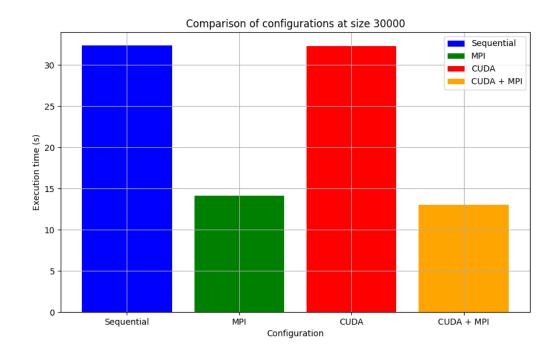


Figure 4.3: Comparison of configurations at size 30000

Finally, we can see that as the size increases, the version with MPI greatly increases performance. However, this argument does not apply to the version with CUDA. However, the hybrid version still turns out to be the best.

4.2 SpeedUp

MPI:

	Size		Speedup
-	:	-	:
	10000	1	0.6615
	20000	1	0.6863
ī	30000	ı	4 1096 l

CUDA:

	Size		Speedup	
-	:	-	:	١
	10000		0.9778	١
	20000		0.9864	١
I	30000	1	0.9925	

CUDA+MPI:

Ι	Size		Speedup			
:						
1	10000	1	3.905			
1	20000	1	4.7514			
1	30000	1	3.8701			

Looking at the speedup results for MPI, CUDA, and CUDA+MPI, we can observe some interesting findings:

MPI: The speedup obtained with MPI seems to be below 1 for all graph sizes, suggesting that parallel execution with MPI is actually slower than serial execution. This could be due to significant overhead caused by communication and synchronization between processes.

CUDA: Similarly, the speedup obtained with CUDA is below 1 for all graph sizes, although it is slightly higher than that of MPI. This might indicate that the parallel implementation with CUDA fails to fully exploit the capabilities of GPUs for relatively small data sizes. CUDA+MPI: On the other hand, the combined use of CUDA and MPI appears to provide higher speedup compared to individual implementations. For all graph sizes, the speedup

4. PERFORMANCE AND SPEEDUP

is above 1, indicating an improvement in performance over serial execution. However, the speedup seems to vary significantly across graph sizes, with better performance for larger sizes.

In general, these results suggest that the combined implementation of CUDA and MPI might be the best strategy for achieving optimal performance across a wide range of graph sizes, although scalability and optimization are still important for achieving better results.

Conclusions

Both MPI and CUDA implementations individually failed to achieve significant speedup over serial execution for the given graph sizes. This suggests that neither MPI nor CUDA alone could efficiently harness the parallel processing power for relatively small datasets. The combined use of CUDA and MPI demonstrated improved performance compared to individual implementations. CUDA leverages the parallel computing capabilities of GPUs, while MPI facilitates communication between processes. This combination allows for better utilization of resources and improved performance, especially for larger datasets where CUDA's GPU parallelism can be effectively exploited.

While CUDA+MPI showed promising results, the scalability of this approach should be further investigated. It's essential to determine whether the performance gains observed for larger datasets hold true as the dataset size continues to increase. Scalability is crucial for ensuring that the solution remains effective as the problem scales.

Optimization plays a crucial role in maximizing performance. This includes optimizing algorithms for parallel execution, minimizing communication overhead, and leveraging hardware-specific features for improved efficiency. Further optimization efforts could potentially enhance the performance of both individual and combined implementations. In conclusion, while individual implementations may struggle to achieve significant speedup for smaller datasets, a combined approach leveraging CUDA and MPI shows promise for improving performance, especially for larger datasets. However, optimization and scalability remain critical considerations for achieving optimal performance across different hardware architectures and dataset sizes.