



Information Retrieval

Dra. Mireya Paredes

Probabilistic Retrieval Model

Probability Ranking Principle:

Given a user query q and a document d_j in the collection, the probabilistic model tries to estimate the probability that the user will find the document d_j interesting (i. e. relevant).

Probabilistic Retrieval Model

1. Usage patterns to predict relevance [Maron and Kunhs 1960].
2. Usage of each term in the query as **clues** as to whether or not a document is **relevant**. [Robertson and Sparck Jones, 1976].

- Query $q(q1, q2)$
- Run q and retrieve top n documents (**let $n=5$**) d_i represents an arbitrary document



Assume **d_2** and **d_4** are relevant:

- $P(q1 \mid d_i \text{ is relevant}) = \frac{1}{2}$
- $P(q1 \mid d_i \text{ is not relevant}) = \frac{2}{3}$
- $P(q2 \mid d_i \text{ is relevant}) = 1$
- $P(q2 \mid d_i \text{ is not relevant}) = \frac{1}{3}$

Estimating the individual term weights

Robertson and Sparck Jones, 1976

INDEPENDENCE ASSUMPTIONS

I1 - The distribution of ***terms*** in ***relevant*** documents is ***independent*** and their distribution in all documents is independent.

I2 - The distribution of ***terms*** in ***relevant*** documents is ***independent*** and their distribution in non-relevant documents is independent.

Estimating the individual term weights

ORDERING PRINCIPLES

- O1.-** Probable **relevance** is based only on the presence of search terms in the documents.
- O2.-** Probable relevance is based on both the presence of search terms in documents and their absence from documents.

Four **Weights** are derived **I1, I2, O1, O2**

N = number of documents in the collection

R = number of **relevant** documents for a given query ***q***.

n = number of documents that contain term ***t***.

r = number of **relevant** documents that contain term ***t***.

Choosing I1 and O1 yields the following weight

$$\mathbf{w1} = \log \frac{\frac{r}{R}}{\frac{n}{N}}$$

Choosing I2 and O1 yields the following weight

$$\mathbf{w2} = \log \frac{\frac{r}{R}}{\frac{n-r}{N-R}}$$

Choosing **I1** and **O2** yields the following weight

$$\mathbf{w3} = \log \frac{\frac{r}{R-r}}{\frac{n}{N-n}}$$

Choosing **I2** and **O2** yields the following weight

$$\mathbf{w4} = \log \frac{\frac{r}{R-r}}{\frac{n-r}{(N-n)-(R-r)}}$$

Weight for incomplete relevant inf.

$$w = \log \frac{\frac{r+0.5}{(R-r)+0.5}}{\frac{(n-r)+0.5}{(N-n)-(R-r)+0.5}}$$

Q: “**gold silver truck**”

D1 = “Shipment of **gold** damaged in a fire”

D2 = “Delivery of **silver** arrived in a **silver truck**”

D3 = “Shipment of **gold** arrived in a **truck**”

<i>variable</i>	<i>gold</i>	<i>silver</i>	<i>truck</i>
N	3	3	3
n	2	1	2
R	2	2	2
r	1	1	2

N = number of documents in the collection

R = number of relevant documents for a given query **q**.

n = number of documents that contain term **t**.

r = number of relevant documents that contain term **t**.

Example: Term Weights

<i>term</i>	<i>w1</i>	<i>w2</i>	<i>w3</i>	<i>w4</i>
gold	-0.079	-0.176	-0.176	-0.477
silver	0.097	0.301	0.176	.477
truck	0.143	0.523	0.523	1.176

Example: Document Weights

<i>term</i>	<i>w1</i>	<i>w2</i>	<i>w3</i>	<i>w4</i>
D1	-0.079	-0.176	-0.176	-0.477
D2	0.240	0.824	0.699	1.653
D3	0.063	0.347	0.347	0.699

Disadvantages

- The need to guess the initial separation of documents into relevant and non-relevant sets.
- The fact that the method does not take into account the frequency
- Lack of length normalization.

Homework

- To study the topics we have seen so far because exam is after 4 lessons.
- To bring questions