



# Model Representation II

To re-iterate, the following is an example of a neural network:

$$\begin{aligned}a_1^{(2)} &= g(\Theta_{10}^{(1)} x_0 + \Theta_{11}^{(1)} x_1 + \Theta_{12}^{(1)} x_2 + \Theta_{13}^{(1)} x_3) \\a_2^{(2)} &= g(\Theta_{20}^{(1)} x_0 + \Theta_{21}^{(1)} x_1 + \Theta_{22}^{(1)} x_2 + \Theta_{23}^{(1)} x_3) \\a_3^{(2)} &= g(\Theta_{30}^{(1)} x_0 + \Theta_{31}^{(1)} x_1 + \Theta_{32}^{(1)} x_2 + \Theta_{33}^{(1)} x_3) \\h_{\Theta}(x) = a_1^{(3)} &= g(\Theta_{10}^{(2)} a_0^{(2)} + \Theta_{11}^{(2)} a_1^{(2)} + \Theta_{12}^{(2)} a_2^{(2)} + \Theta_{13}^{(2)} a_3^{(2)})\end{aligned}$$

In this section we'll do a vectorized implementation of the above functions. We're going to define a new variable  $z_k^{(j)}$  that encompasses the parameters inside our  $g$  function. In our previous example if we replaced by the variable  $z$  for all the parameters we would get:

$$\begin{aligned}a_1^{(2)} &= g(z_1^{(2)}) \\a_2^{(2)} &= g(z_2^{(2)}) \\a_3^{(2)} &= g(z_3^{(2)})\end{aligned}$$

In other words, for layer  $j=2$  and node  $k$ , the variable  $z$  will be:

$$z_k^{(2)} = \Theta_{k,0}^{(1)} x_0 + \Theta_{k,1}^{(1)} x_1 + \cdots + \Theta_{k,n}^{(1)} x_n$$

The vector representation of  $x$  and  $z^j$  is:

$$\begin{array}{cc}x_0 & z_1^{(j)} \\x = \begin{matrix} x_1 \\ \vdots \\ x_n \end{matrix} & z^{(j)} = \begin{matrix} z_2^{(j)} \\ \vdots \\ z_n^{(j)} \end{matrix}\end{array}$$

Setting  $x = a^{(1)}$ , we can rewrite the equation as:

$$z^{(j)} = \Theta^{(j-1)} a^{(j-1)}$$