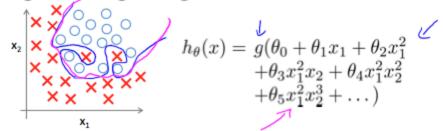
Regularized Logistic Regression

We can regularize logistic regression in a similar way that we regularize linear regression. As a result, we can avoid overfitting. The following image shows how the regularized function, displayed by the pink line, is less likely to overfit than the non-regularized function represented by the blue line:

Regularized logistic regression.



Cost function:

$$J(\theta) = -\left[\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)}))\right]$$

$$+ \frac{\lambda}{2m} \sum_{j=1}^{n} \bigotimes_{j=1}^{n} \bigotimes_{j=1}^{n} \left[\bigcirc_{i,j} \bigcirc_{i,\dots,j} \bigcirc_{n} \right]$$

Cost Function

Recall that our cost function for logistic regression was:

$$J(heta) = -rac{1}{m} \sum_{i=1}^m [y^{(i)} \; \log(h_ heta(x^{(i)})) + (1-y^{(i)}) \; \log(1-h_ heta(x^{(i)}))]$$

We can regularize this equation by adding a term to the end:

$$J(heta) = -rac{1}{m} \sum_{i=1}^m [y^{(i)} \; \log(h_ heta(x^{(i)})) + (1-y^{(i)}) \; \log(1-h_ heta(x^{(i)}))] + rac{\lambda}{2m} \sum_{j=1}^n heta_j^2$$

The second sum, $\sum_{j=1}^n \theta_j^2$ **means to explicitly exclude** the bias term, θ_0 . I.e. the θ vector is indexed from 0 to n (holding n+1 values, θ_0 through θ_n), and this sum explicitly skips θ_0 , by running from 1 to n, skipping 0. Thus, when computing the equation, we should continuously update the two following equations: