

$$c) T(n) = 4T(n/2) + n$$

$$T(1) = 1$$

$$T(n) = 4T(n/2) + n$$

$$4T(n/2) = 4^2 T(n/2^2) + 4(n/2)$$

$$4^2 T(n/2^2) = 4^3 T(n/2^3) + 4(n/2^2)$$

↓

$$T(n) = 4^k T(n/2^k) + \sum_{i=0}^{k-1} \frac{4^i}{2^i} n \rightarrow \frac{2^{2i}}{2^i} = 2^i$$

$$T(n) = 4^k T(n/2^k) + \sum_{i=0}^{k-1} 2^i n$$

$$T(n) = \sum_{i=0}^{k-1} 2^i n$$

$$T(n) = n \cdot \sum_{i=0}^{k-1} 2^i$$

$$\frac{n}{2^k} = 1$$

$$n = 2^k$$

$$\sum_{i=0}^{k-1} 2^i + 2^{n+1} = 2^0 + \sum_{i=0}^{k-1} 2^{i+1}$$

$$\sum_{i=0}^{k-1} 2^i + 2^{n+1} = 1 + 2 \sum_{i=0}^{k-1} 2^i$$

$$\sum_{i=0}^{k-1} 2^i = 2^{k-1} - 1$$

$$T(n) = n \cdot (2^{k-1} - 1)$$

$$T(n) = 2 \cdot n^2 - n$$

Complexidade  $O(n^2)$