

$$d) T(n) = T(n/2) + \log_2 n$$

$$T(1) = 1$$

$$T(n) = T(n/2) + \log_2 n$$

$$T(n/2) = T(n/2^2) + \log_2(n/2)$$

$$T(n/2^2) = T(n/2^3) + \log_2(n/2^2)$$

↓

$$T(n) = \underbrace{T(n/2^k)}_{T(1)} + \log_2(n/2^{k-1})$$

$$\frac{n}{2^k} = 1$$

$$k = \log_2 n$$

$$T(n) = T(1) + \sum_{i=0}^{k-1} \log_2(n/2^i)$$

$$T(n) = \sum_{i=0}^{k-1} \frac{\log_2 n}{\log_2 2^i}$$

$$T(n) = \sum_{i=0}^{k-1} \frac{\log_2 n}{i \log_2 2}$$

$$T(n) = \sum_{i=0}^{k-1} \frac{\log_2 n}{i}$$

$$T(n) = \log_2 n \left(\sum_{i=0}^{k-1} \frac{1}{i} \right) \rightarrow \text{Nunca Será maior que 1}$$

Domina o Somatório

$$T(n) = \log_2 n$$

Complexidade $O(\log_2 n)$