

"For loops" happens just once. happens @ end of body.

```
for (int i = 0; i < 10; i++) {
```

← "body"

checked before running body

```
// arbitrary state ments (including  
// other loops ...)  
}
```

Equivalent while loop:

```
→ int i = 0;  
while (i < 10) {  
    // state ments ...  
    i++;  
}
```

Exercise: read 2 integers, n, m and draw a $n \times m$ rectangle of '*' characters to std out.

E.g. if $n=3, m=4$

```
* * * *  
* * * *  
* * * *
```

New "technique": Brute force - leverage the speed of the computer to search through the entire space of solutions.

All that's needed: ① a test: "is x a solution?"
② a method to enumerate all possible solutions.

Brute force:

```
for (/  $x$  in possible solns /) {  
    if (/  $x$  passes test /) {  
        cout <<  $x$ ;  
        break; ←  
    }  
} ←
```

Example: compute the gcd of two integers m, n .

(GCD = greatest common divisor)

e.g. $\text{gcd}(10, 15) = 5$. $\left(\begin{array}{l} 10 = 2^1 \cdot 3^0 \cdot 5^1 \\ 15 = 2^0 \cdot 3^1 \cdot 5^1 \end{array} \right)$

Test for solution?

Warm up: test for common divisor?

How to check if one integer d divides another n ?

see if n/d has no remainder.

Note: the $\%$ operator gives you the remainder!

So, $\boxed{m \% d == 0} \iff d \text{ divides } m$

\therefore we can check to see if d is a common divisor of m, n via:

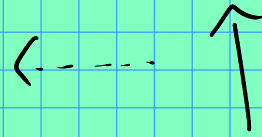
$$(m \% d == 0 \ \&\& \ n \% d == 0)$$

What about ②? List of candidates for $\text{gcd}(m, n)$?

Smallest value: 1

Largest value: $\min\{m, n\}$

Our list: $[1, 2, 3, \dots, \min\{m, n\}]$.



Idea: starting from largest candidate,
test it and count backwards.

First candidate that passes
is the gcd.