

Assignment #3

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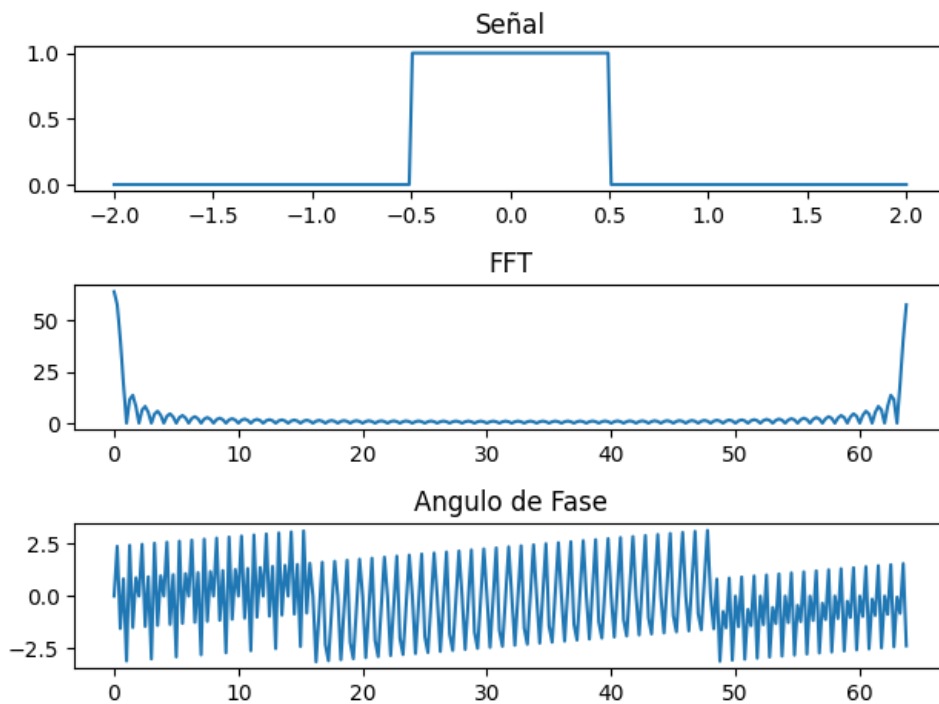
Course: *Introducción al Análisis de Fourier (Sep - Dec 2022)*

Professor: *Dr. Wilfrido Gómez-Flores*

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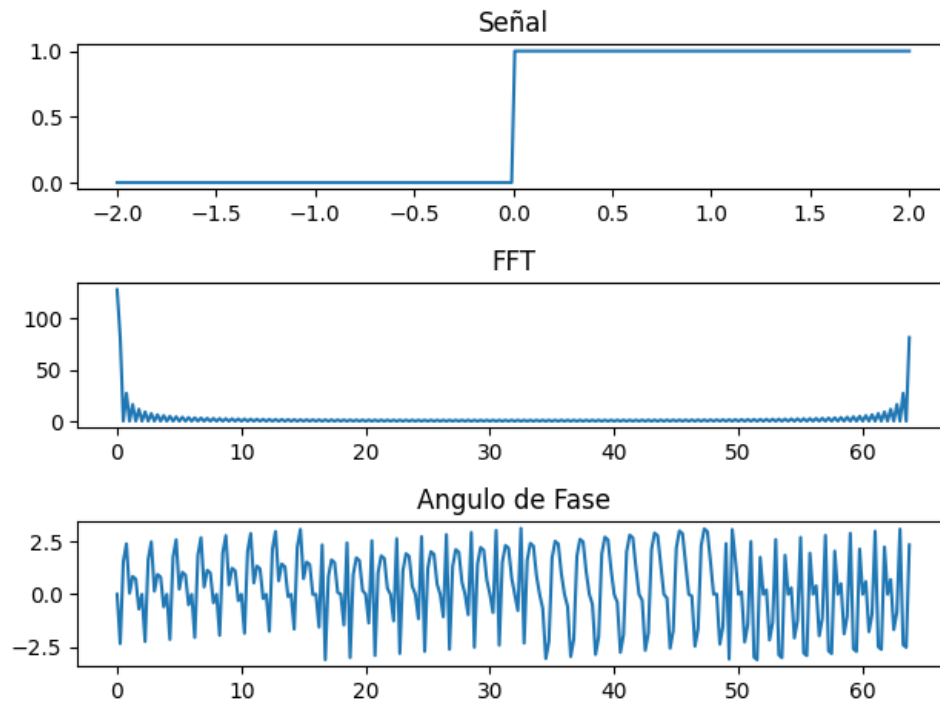
.....PULSO RECTANGULAR

$$f(t) = \begin{cases} 1, & |t| < \frac{\tau}{2} \\ 0, & |t| > \frac{\tau}{2} \end{cases}$$



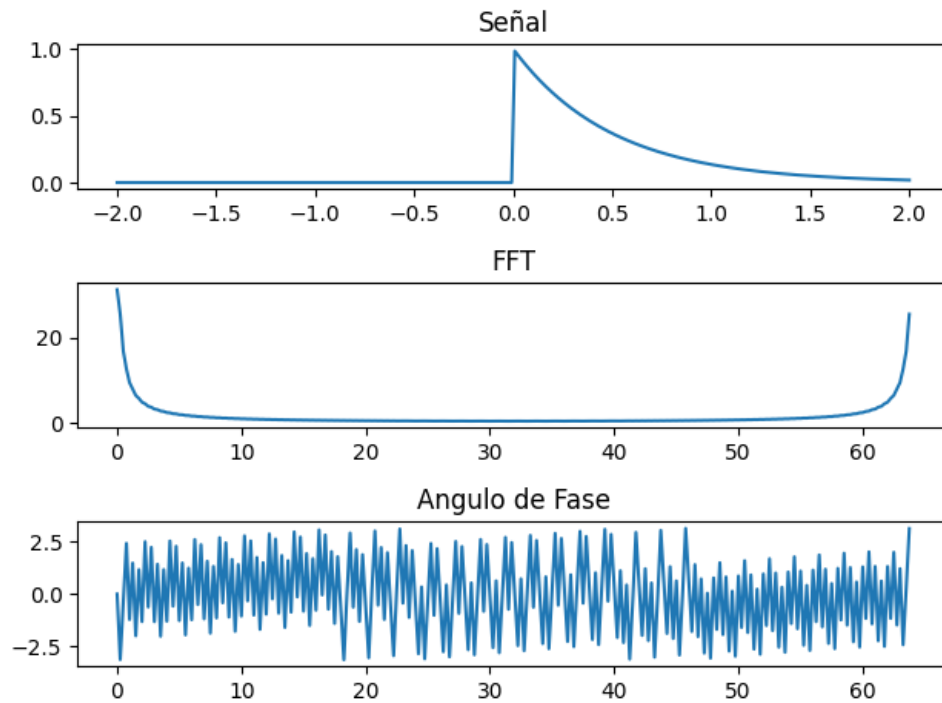
..... ESCALON UNITARIO

$$f(t) = \begin{cases} 1, & t > 0 \\ 0, & t < 0 \end{cases}$$



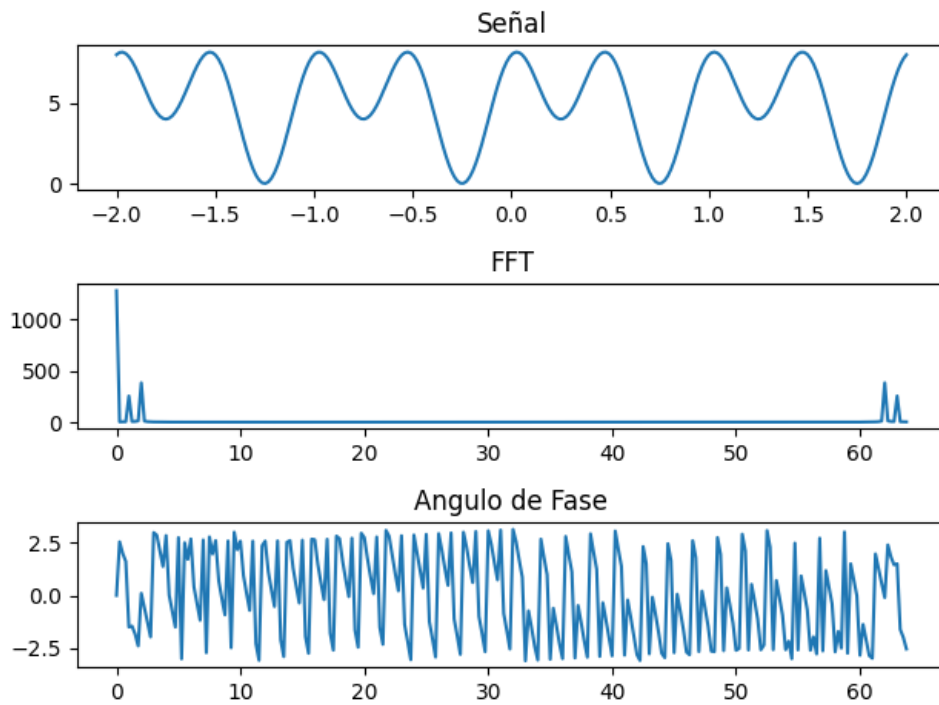
..... EXPONENCIAL

$$f(t) = \begin{cases} e^{-at}, & t > 0 \\ 0, & t < 0 \end{cases}$$



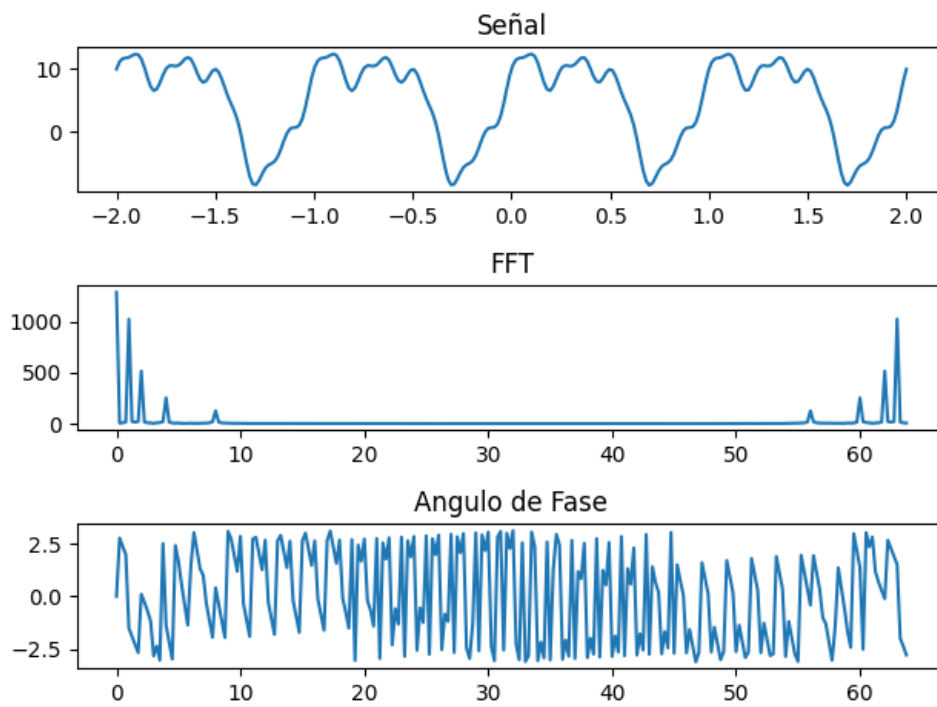
.....FUNCION A

$$f(t) = 5 + 2 * \cos(2 * \pi * t - \pi/2) + 3 * \cos(4 * \pi * t)$$



..... FUNCION B

$$f(t) = 5 + 8 * \cos(2 * \pi * t - \frac{\pi}{2}) + 4 * \cos(4 * \pi * t) + 2 * \cos(8 * \pi * t - \frac{\pi}{2}) + \cos(16 * \pi * t) + \\ + 2 * \cos(32 * \pi * t - \frac{\pi}{2})$$



..... Código python

```

1 def pulso_rectangular(t):
2     '''PULSO RECTANGULAR'''
3     return 1 * (abs(t) < 0.5)
4
5 def escalon_unitario(t):
6     '''ESCALON UNITARIO'''
7     return 1 * (t >= 0)
8
9 def exponencial(t):
10    '''FUNCION EXPONENCIAL'''
11    alpha = randrange(3)
12    return np.exp(-alpha * t) * (t > 0)
13
14 def funcion_a(t):
15    '''FUNCION A'''
16    return 5+2*np.cos((2*np.pi*t)-(np.pi/2)) + 3*np.cos(4*np.pi*t)
17
18 def funcion_b(t):
19    '''FUNCION B'''
20    return 5+8*np.cos((2*np.pi*t)-(np.pi/2))+4*np.cos(4*np.pi*t)+2*np.
    cos((8*np.pi*t)-(np.pi/2))+np.cos(16*np.pi*t)+2*np.cos((32*np.pi-(np.
    pi/2)))

```

Código 1: Dibujo de funciones

```

1 def FFT2(x):
2     ''' radix-2 FFT '''
3     x = np.array(x, dtype=float)
4     N = int(x.size)
5     n = np.log2(N)
6     d = 1
7     for i in range(1, int(n)):
8         w = np.exp(-(1j*2*np.pi)/(2*d))
9         for a in range(0, d-1):
10            b = 0
11            while(b<N-1):
12                wa=pow(w,a)
13                id1 = b+a+1
14                id2 = b+d+a+1
15                t_0 = x[id1] + (wa)*x[id2]
16                t_1 = x[id1] - (wa)*x[id2]
17                x[id1] = t_0
18                x[id2] = t_1
19                b = b+2*d
20
21            d = 2*d
22     return x

```

Código 2: FFT - radix2

```

1
2 def bit_reversal(data):
3     '''
4     gold rader - zero padding
5     :param data: array de datos
6     :return: array signal con zeros
7     '''
8     n = int(data.size)
9     j = 0
10    i = 0
11    while i < n-1:
12        k = n/2
13        if (i<j):
14            temp = data[int(i)]
15            data[int(i)] = data[int(j)]
16            data[int(j)] = temp
17        while(k<=j):
18            j = j-k
19            k = k/2
20        j = j+k
21        i += 1
22    return data

```

Código 3: Algoritmo Gold Rader