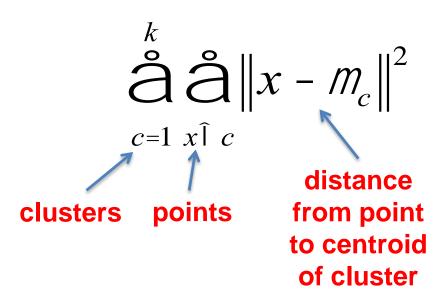
# A Quick Introduction to Machine Learning (K-means Clustering)

Lecturer: John Guttag

## K-means Clustering

Given a set of points X, and a positive integer k, partition X into k clusters such that it approximately minimizes the objective function



Minimizing the sum of the mean square differences

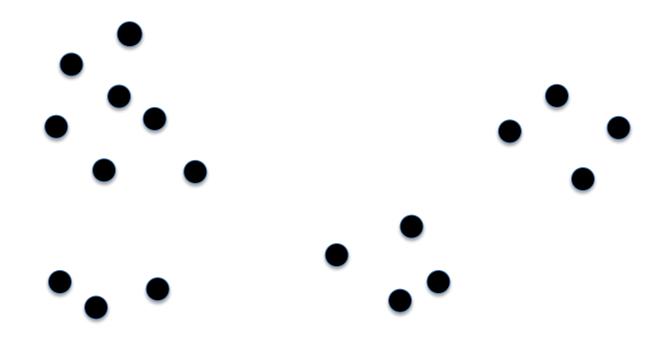
### K-means Algorithm

randomly choose k examples as centroids while true:

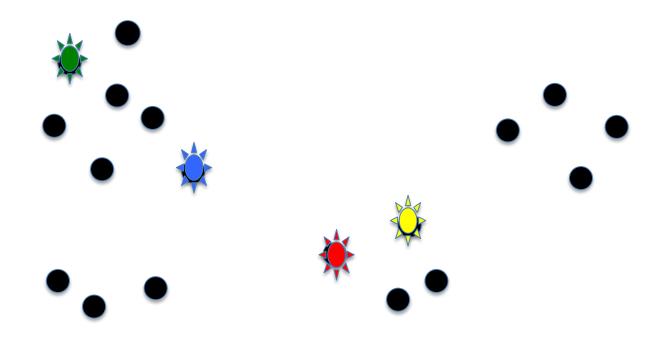
create k clusters by assigning each example to closest centroid compute k new centroids by averaging examples in each cluster if centroids don't change:

break

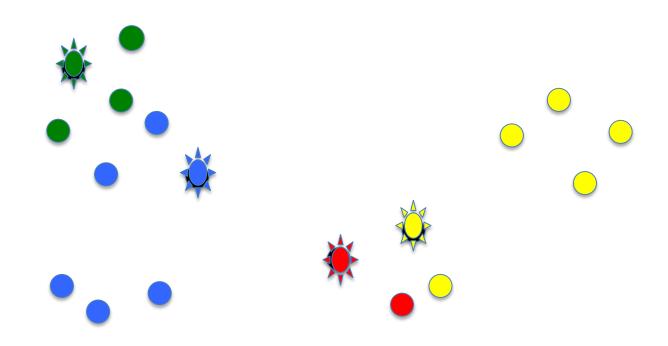
## **Example**

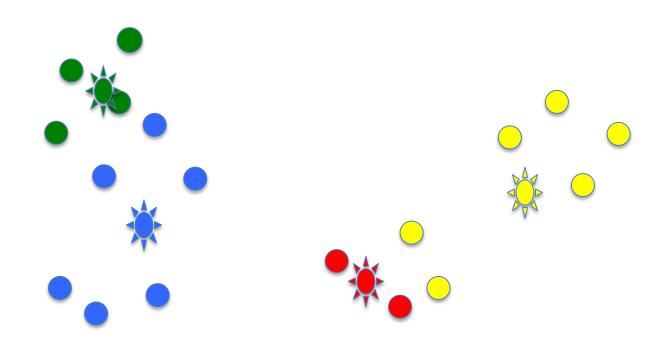


# Choose Initial Centroids (k = 4)

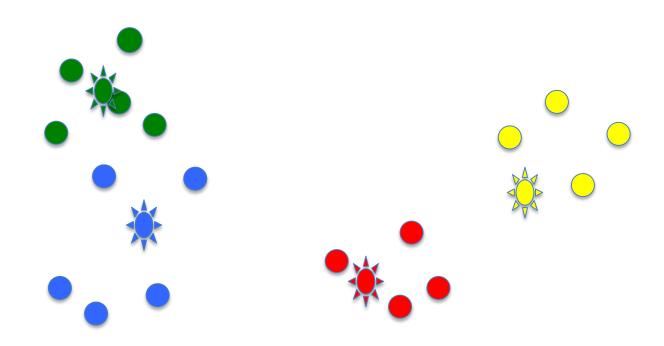


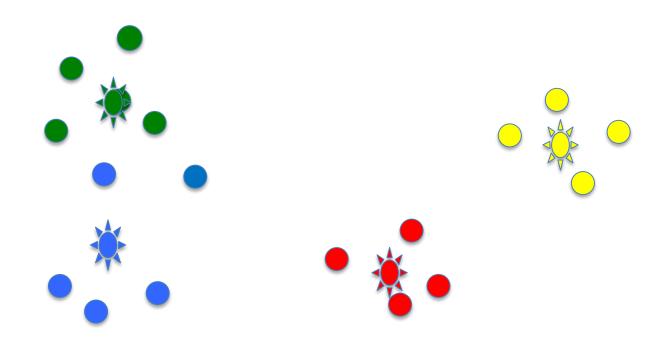
## **Assign Points to Clusters**



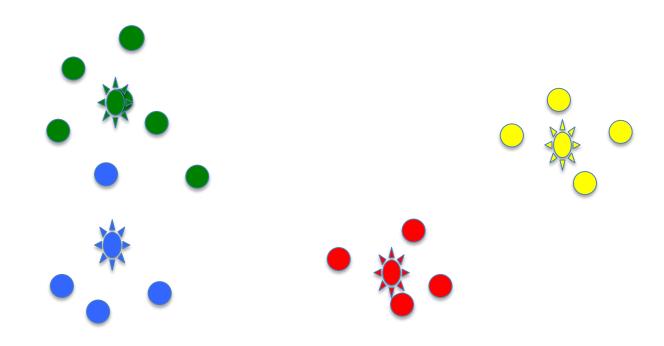


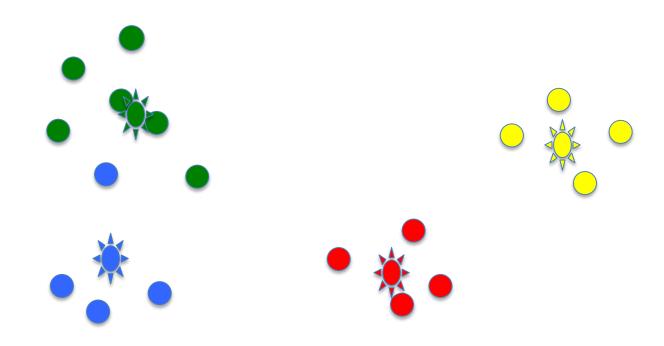
## Reassign Points to Clusters



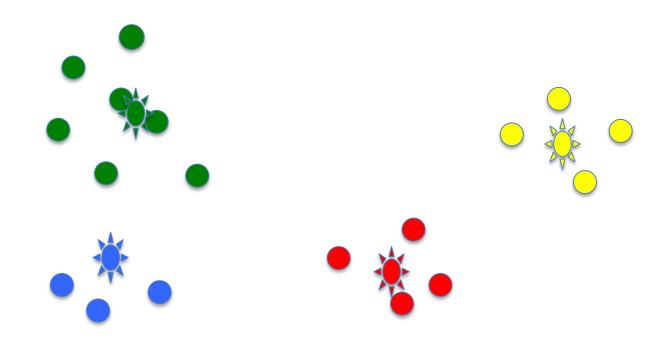


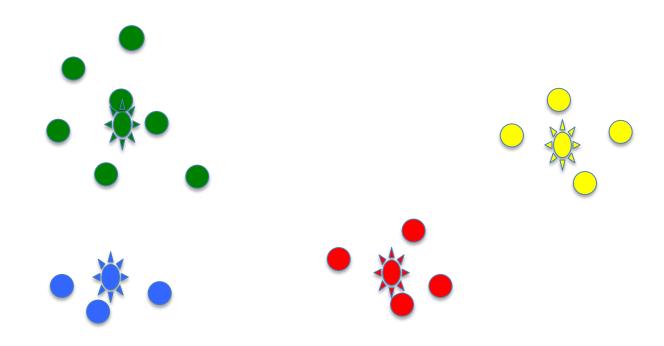
# **Reassign Points**



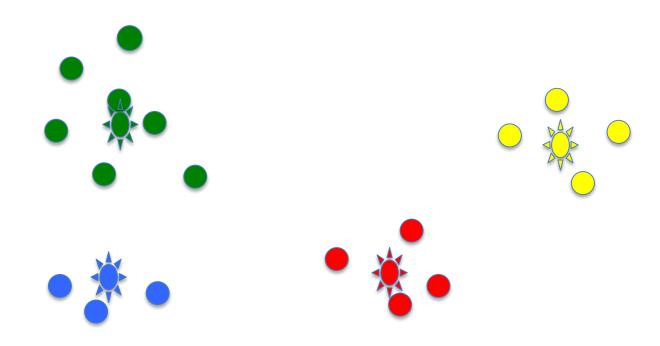


# **Reassign Points**





#### **No Points Move**

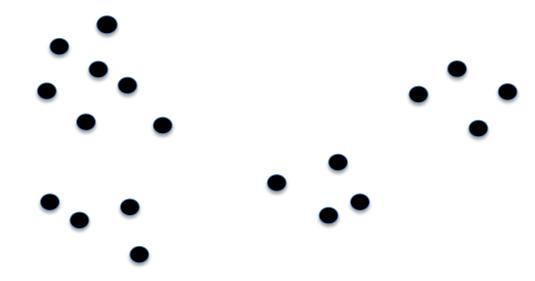


#### Issues with K-means

Final result can depend upon initial centroids

Greedy algorithm can find different local optima

Choosing the "wrong" k can lead to nonsense



## **Choosing K**

#### A priori knowledge about application domain

There are five different kinds of bacteria: k = 5There are two kinds of people in the world: k = 2

#### Search for a good k

Try different values of k, and evaluate quality of results

## **Choosing Centroids**

Try multiple random choices and choose best

## Finding the "Best" Solution

```
best = kMeans(points)
for t in range(numTrials):
    C = kMeans(points)
    if badness(C) < badness(best):
        best = C</pre>
```

$$V(c) = \mathop{\mathrm{a}}_{x \mid c} (mean(c) - x)^2$$
  $badness(C) = \mathop{\mathrm{a}}_{c \mid C} V(c)$ 

#### Hierarchical vs. K-means

Hierarchical looks at different numbers of clusters From 1 to n

K-means looks at many ways of creating k clusters

Hierarchical is slow

K-means is fast



Hierarchical is deterministic

K-means is non-deterministic

