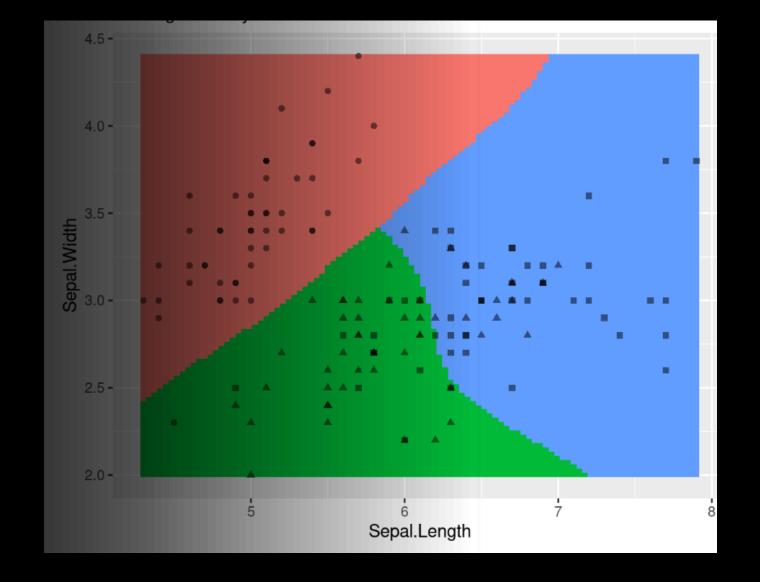
CS 5/7320 Artificial Intelligence

Learning from Examples

AIMA Chapter 19

By Michael Hahsler

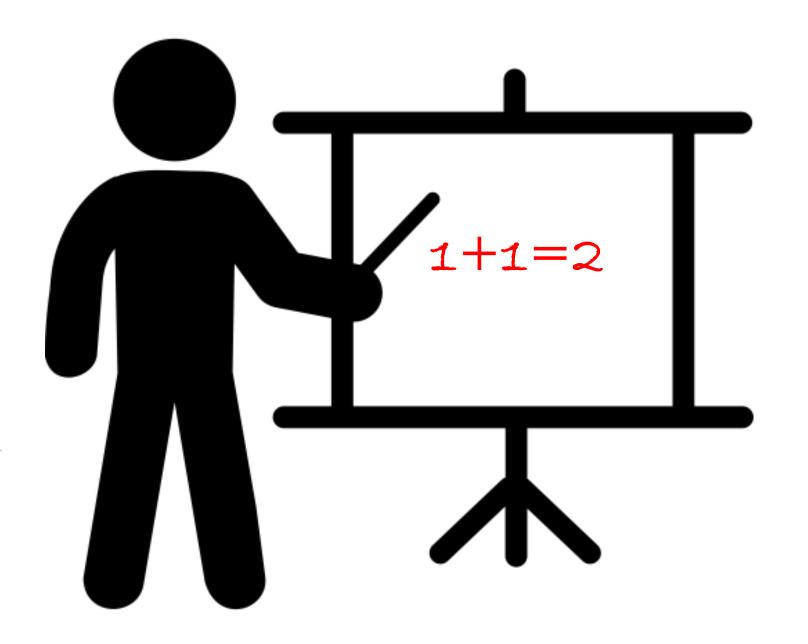
Based on slides by Dan Klein, Pieter Abbeel, Sergey Levine and A. Farhadi. All CS188 materials are at http://ai.berkeley.edu.



Learning from Examples: Machine Learning

- **Up until now:** hand-craft algorithms to make rational/optimal or at least good decisions. Examples: Search strategies, heuristics.
- **Learning**: Improve performance after making observations about the world. That is, learn what works and what doesn't.
- Machine learning: how to build a model from data/experience
 - Supervised Learning: Learn a function to map input to output. Examples:
 - Use a naïve Bayesian classifier to distinguish between spam/no spam
 - Learn a playout policy to simulate games (current board -> good move)
 - Reinforcement Learning: Learn from rewards/punishment (e.g., winning a game).
- Learning vs. hard coding the agent function
 - Designer cannot anticipate all possible future situations.
 - Designer may have examples but does not know how to program a solution.

Supervised Learning



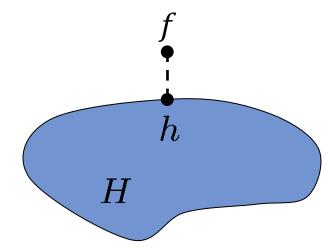
Supervised Learning

Examples

- Input-output pairs: $E = (x_1, y_1), ..., (x_i, y_i), ..., (x_N, y_N)$.
- We assume that the examples are produced iid (with noise and errors) from a target function y = f(x).

Learning problem

- Given a hypothesis space H
- Find a hypothesis $h \in H$ such that $\hat{y}_i = h(x_i) \approx y_i$
- That is, we want to approximate f by h using E.

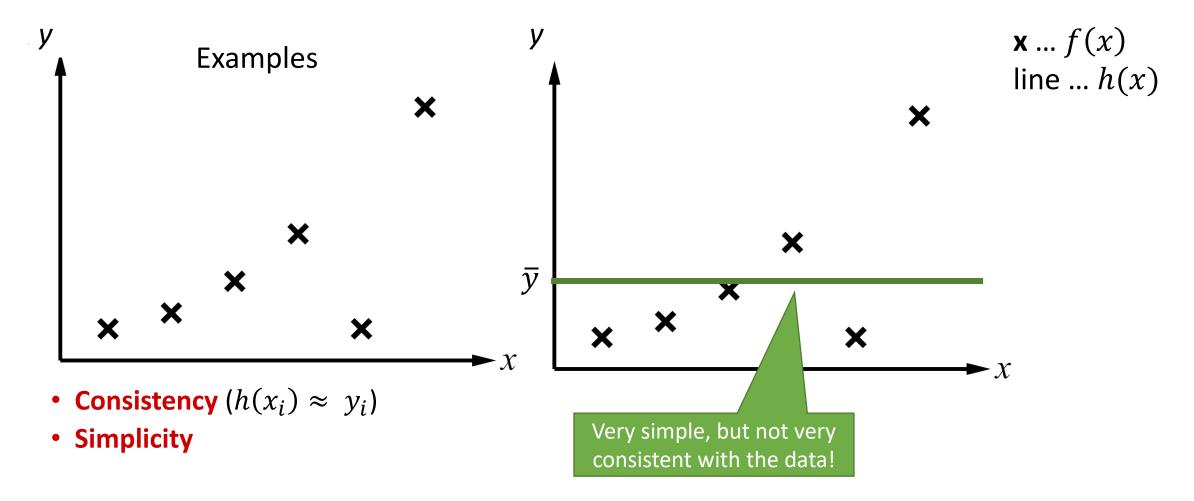


Includes

- Classification (outputs = class labels). E.g. x is an email and f(x) is spam / ham
- Regression (outputs = real numbers). E.g. x is a house and f(x) is its selling price

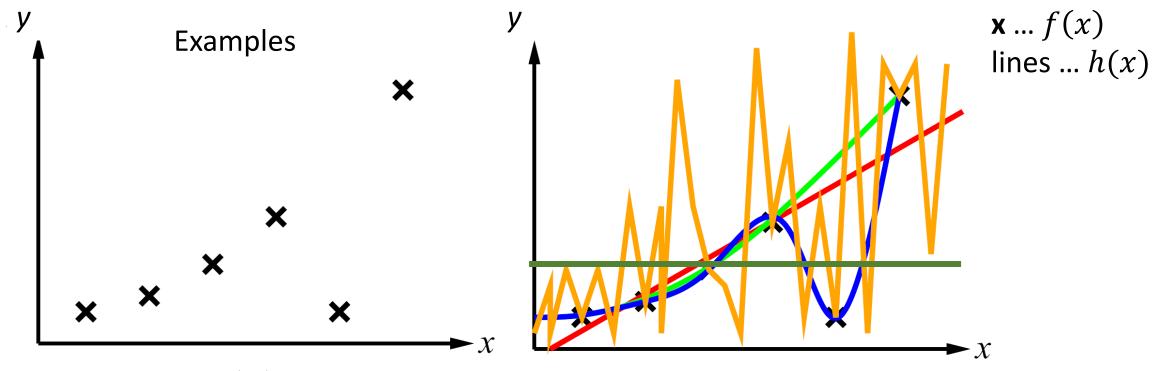
Consistency vs. Simplicity

Example: Curve fitting (regression, function approximation)



Consistency vs. Simplicity

Example: Curve fitting (regression, function approximation)



- Consistency $(h(x_i) \approx y_i)$
- Simplicity

Consistency and Loss

Goal of learning: Find a hypothesis that makes good predictions that are consistent with the examples $E = (x_1, y_1), ..., (x_i, y_i), ..., (x_N, y_N)$.

That is,
$$\hat{y} = h(x) \approx y$$
.

- Measure mistakes: Loss function $L(y, \hat{y})$

 - Absolute-value loss $L_1(y,\hat{y}) = |y \hat{y}|$ Squared-error loss $L_2(y,\hat{y}) = (y \hat{y})^2$ $0/1 \log s$ For Regression $L_0(y,\hat{y}) = 0 \text{ if } y = \hat{y}, \text{else } 1$ For Classification
- **Empirical loss:** average loss over the N examples in the dataset

$$EmpLoss_{L,E}(h) = \frac{1}{|E|} \sum_{(x,y) \in E} L(y,h(x))$$

Consistency and Loss

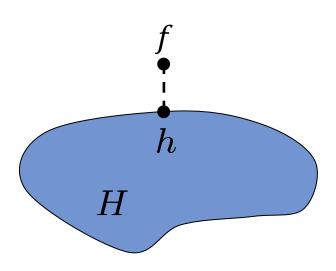
Empirical loss

$$EmpLoss_{L,E}(h) = \frac{1}{|E|} \sum_{(x,y) \in E} L(y,h(x))$$

Learning the best hypothesis

$$h^* = \underset{h \in H}{\operatorname{argmin}} EmpLoss_{L,E}(h)$$

- Reasons for $h^* \neq f$
 - a) Realizability: $f \notin H$
 - b) f is nondeterministic or examples are noisy
 - c) Computationally intractable to search all H



Example: Bayes Classifier

For 0/1 loss, the empirical loss is minimized by the model that predicts for each x the most likely class y.

$$h(x)^* = \operatorname*{argmax}_{y} P(Y = y \mid X = x)$$

This is equivalent (by Bayes' rule and dropping of P(x)) to:

$$h(x)^* = \underset{y}{\operatorname{argmax}} P(X = x \mid Y = y) P(y) = \underset{y}{\operatorname{argmax}} P(X, y)$$

The Bayes Classifier is optimal and guarantees the lowest possible error rate called the Bayes error rate.

Issue: Needs the complete joint probability which requires in the general case a probability table with one entry for each possible value for x. That is why we often use the naïve Bayes classifier, which is not optimal.

Simplicity

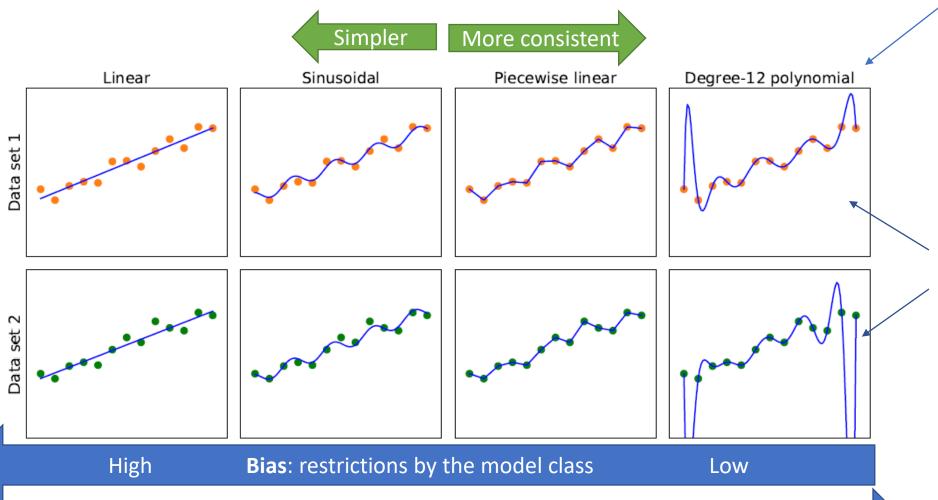
- **Ease of use**: Simpler hypotheses have fewer parameters and are easier to estimate.
- Generalization: How well does the hypothesis perform on new data?
 - We do not want the model to be too specific to the training examples (an issue called overfitting).
 - Simpler models typically generalize better to new examples.

How to achieve simplicity?

- a) Restrict H to simple models (e.g., independence assumption, linear models)
- b) Feature selection (use fewer variables)
- c) Regularization (penalize for complexity)

$$h^* = \underset{h \in H}{\operatorname{argmin}} \left[EmpLoss_{L,E}(h) + \underset{\text{Penalty term}}{\lambda} Complexity(h) \right]$$

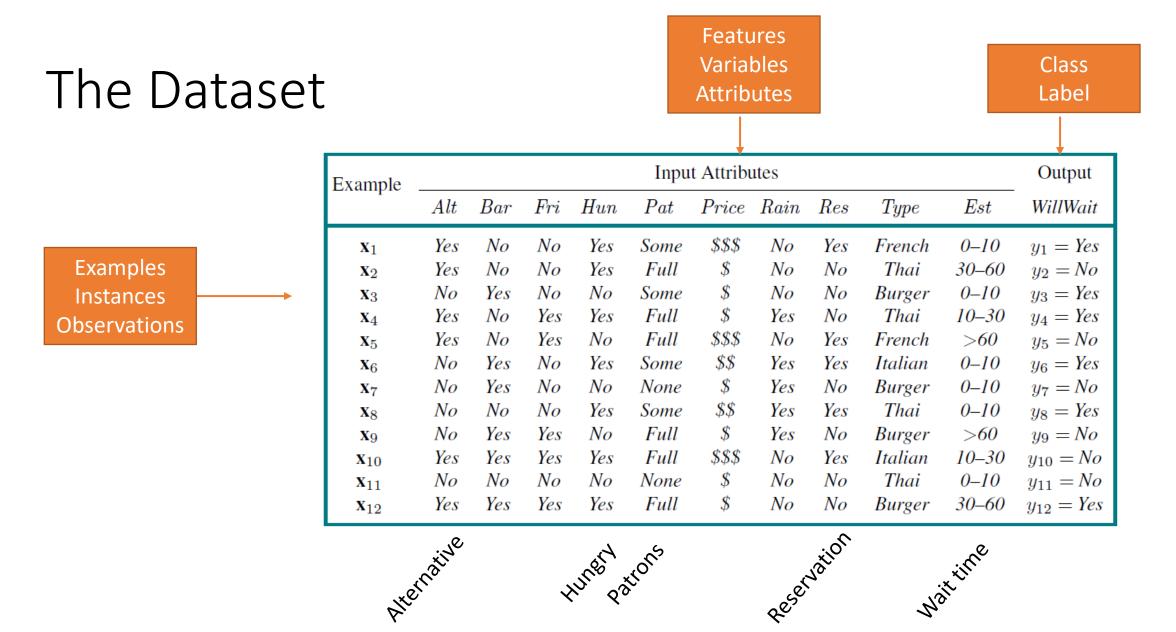
Model Selection: Bias vs. Variance



Two samples from the same function f (points) with the learned function h (lines).

ow Variance: difference in the model due to slightly different data. high

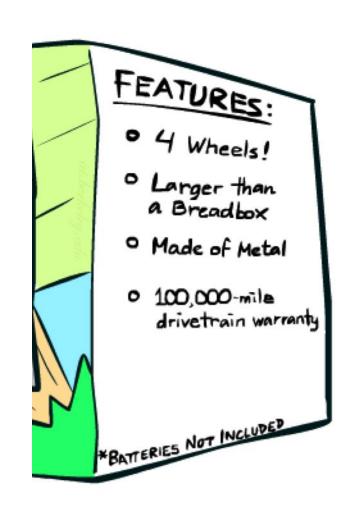
Data



Find a hypothesis (called "model") to predict the class given the features.

Feature Engineering

- Add information sources as new variables to the model.
- Add derived features that help the classifier (e.g., x^2).
- Example for Spam detection: In addition to words
 - Have you emailed the sender before?
 - Have 1000+ other people just gotten the same email?
 - Is the header information consistent?
 - Is the email in ALL CAPS?
 - Do inline URLs point where they say they point?
 - Does the email address you by (your) name?
- Feature Selection: Which features should be used in the model is a model selection problem (choose between models with different features).



Training and Testing



Model Evaluation

We want to test how well the model will perform on new data (i.e., how well it generalizes).

• Testing loss: Calculate the empirical loss for predictions on a testing data set T that is different from the data used for training.

$$EmpLoss_{L,T}(h) = \frac{1}{|T|} \sum_{(x,y) \in T} L(y,h(x))$$

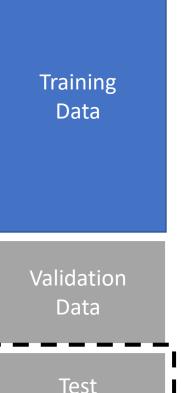
• For classification we often use the **accuracy** measure, the proportion of correctly classified test examples.

$$accuracy(h, T) = \frac{1}{|T|} \sum_{(x,y) \in T} [h(x) = y] = 1 - EmpLoss_{L_{0/1},T}(h)$$

Training a Model

• Models are "trained" (learned) on the training data (a part of the available data).

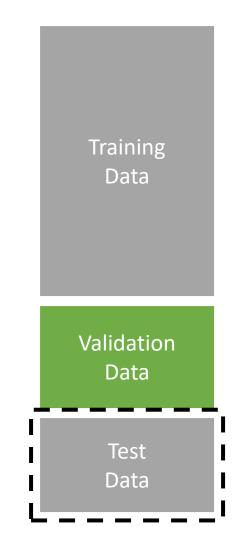
- Models have
 - Model parameters (the model): E.g., probabilities, weights, factors.
 - Hyperparameters: Choices for the algorithm used for learning. E.g., learning rate, regularization λ , maximal decision tree depth, selected features.
- The "Learner" (algorithm) tries to optimizes the model parameters given user-specified hyperparameters.
- We can learn models with different hyperparameters, but how do we know which set of hyperparameters is best?



Data

Hyperparameter Tuning/Model Selection

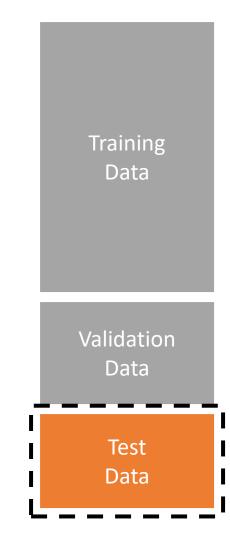
- Learn models using the training set and different hyperparameters.
- Often a grid of possible hyperparameter combinations or some greedy search is used.
- Evaluate the models using the **validation data** and choose the model with the best accuracy. Selecting the right type of model, hyperparameters and features is called **model** selection.
- Learn the final model using all training and validation data.
- Notes:
 - The validation set was not used for training, so we get generalization accuracy.
 - If no model selection is necessary, then no validation set is used.



Testing a Model

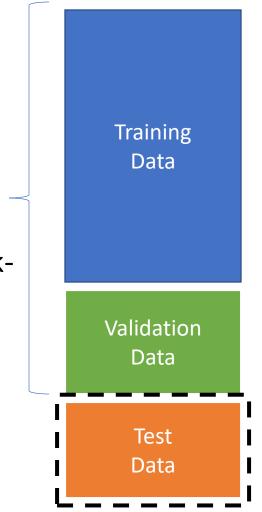
• After the hyper parameters are chosen, the final model is evaluated against the test set to estimate the model accuracy.

Very important: never "peek" at the test set during learning!

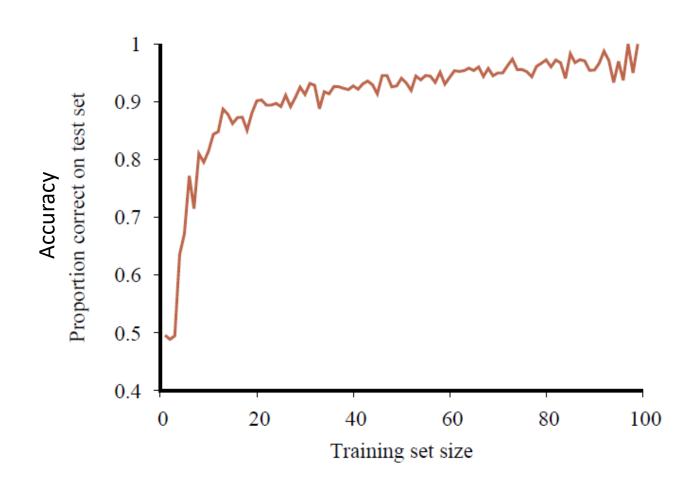


How to Split the Dataset

- Random splits: Split the data randomly in, e.g., 60% training, 20% validation, and 20% testing.
- k-fold cross validation: Use training & validation data better
 - split the training & validation data randomly into k folds.
 - For k rounds hold 1 fold back for testing and use the remaining k-1 folds for training.
 - Use the average error/accuracy as a better estimate.
 - Some algorithms/tools do that internally.
- **LOOCV** (leave-one-out cross validation): k = n used if very little data is available.



Learning Curve: The Effect the Training Data Size

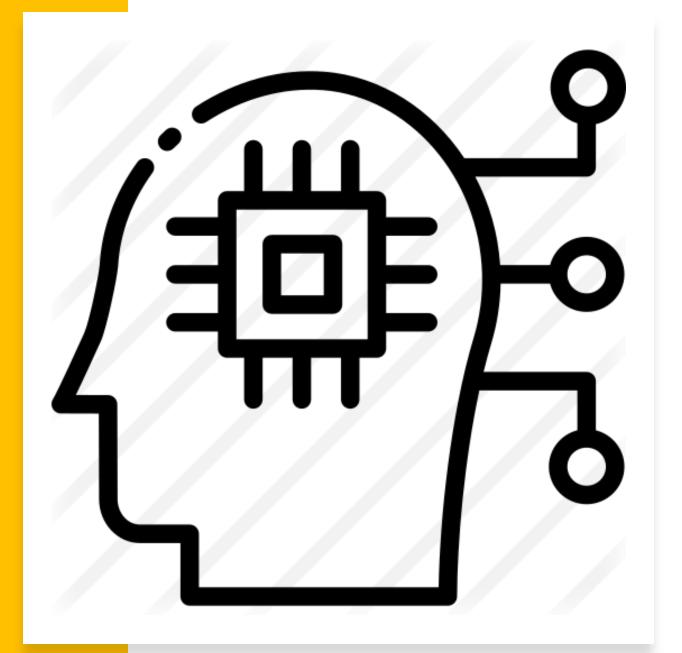


Accuracy of a classifier when the amount of available training data increases.

More data is better!

Comparing to a Baselines

- First step: get a baseline
 - Baselines are very simple "straw man" model.
 - Helps to determine how hard the task is.
 - Helps to find out what a "good" accuracy is.
- Weak baseline: The most frequent label classifier
 - Gives all test instances whatever label was most common in the training set.
 - Example: For spam filtering, give every message the label "ham."
 - Accuracy might be very high if the problem is skewed (called class imbalance).
 - Example: Calling everything "ham" gets already 66% right, so a classifier that gets 70% isn't very good...
- Strong baseline: For research, we typically compare to previous work as a baseline.



Types of Models

Regression: Predict a number

Classification: Predict a label



Regression: Linear Regression

Model:
$$h_{\mathbf{w}}(\mathbf{x}_{j}) = w_{o} + w_{1}x_{j,1} + \dots + w_{n}x_{j,n} = \sum_{i} w_{i}x_{j,i} = \mathbf{w}^{T}\mathbf{x}_{j}$$

Loss function: $L(w) = ||Xw - y||^2$

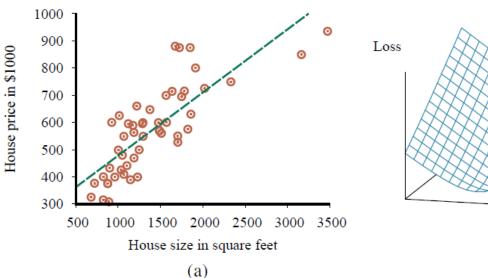
Squared error loss over the whole data matrix X

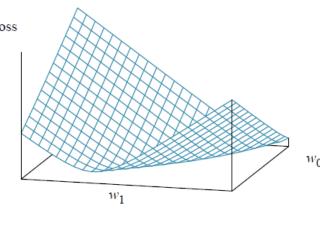
Gradient: $\nabla_{\boldsymbol{w}} L(\boldsymbol{w}) = 2\boldsymbol{X}^T(\boldsymbol{X}\boldsymbol{w} - \boldsymbol{y}) = 0$

The gradient $\nabla_{\mathbf{w}} L(\mathbf{w})$ is a vector of partial derivatives

Solution: $\mathbf{w}^* = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y}$

Pseudo inverse

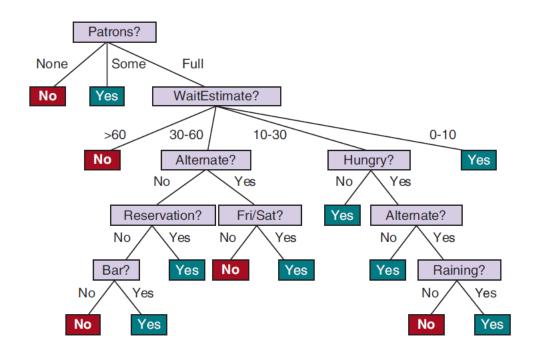




(b)

Decision Trees

Example	Input Attributes										Output
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	WillWait
\mathbf{x}_1	Yes	No	No	Yes	Some	\$\$\$	No	Yes	French	0–10	$y_1 = Yes$
\mathbf{x}_2	Yes	No	No	Yes	Full	\$	No	No	Thai	<i>30–60</i>	$y_2 = No$
\mathbf{x}_3	No	Yes	No	No	Some	\$	No	No	Burger	0-10	$y_3 = Yes$
\mathbf{x}_4	Yes	No	Yes	Yes	Full	\$	Yes	No	Thai	10-30	$y_4 = Yes$
\mathbf{x}_5	Yes	No	Yes	No	Full	<i>\$\$\$</i>	No	Yes	French	>60	$y_5 = No$
\mathbf{x}_6	No	Yes	No	Yes	Some	\$\$	Yes	Yes	Italian	0-10	$y_6 = Yes$
\mathbf{x}_7	No	Yes	No	No	None	\$	Yes	No	Burger	0-10	$y_7 = No$
\mathbf{x}_8	No	No	No	Yes	Some	\$\$	Yes	Yes	Thai	0-10	$y_8 = Yes$
X 9	No	Yes	Yes	No	Full	\$	Yes	No	Burger	>60	$y_9 = No$
\mathbf{x}_{10}	Yes	Yes	Yes	Yes	Full	\$\$\$	No	Yes	Italian	10-30	$y_{10} = No$
\mathbf{x}_{11}	No	No	No	No	None	\$	No	No	Thai	0-10	$y_{11} = No$
\mathbf{x}_{12}	Yes	Yes	Yes	Yes	Full	\$	No	No	Burger	<i>30–60</i>	$y_{12} = Yes$



- A sequence of decisions represented as a tree.
- Many implementations that differ by
 - How to select features to split?
 - When to stop splitting?
 - Is the tree pruned?
- Approximates a Bayesian classifier by

$$h(x) = \underset{v}{\operatorname{argmax}} P(Y = y \mid leafNodeMatching}(x))$$

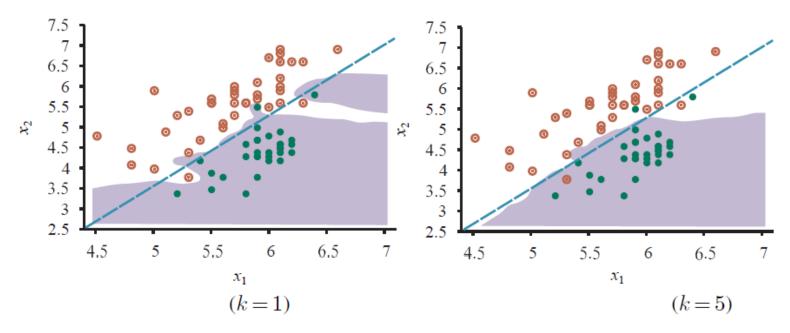
Naïve Bayes Classifier

• Approximates a Bayes classifier with the naïve assumption that all n features are conditional independent given the class.

$$h(x) = \underset{y}{\operatorname{argmax}} P(y) \prod_{i=1}^{n} P(x_i|y)$$

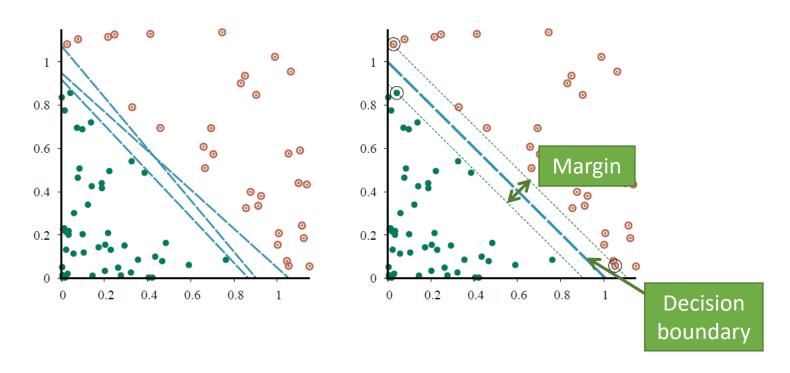
• We have only used discrete features so far, but it can be extended to continuous features.

K-Nearest Neighbors Classifier



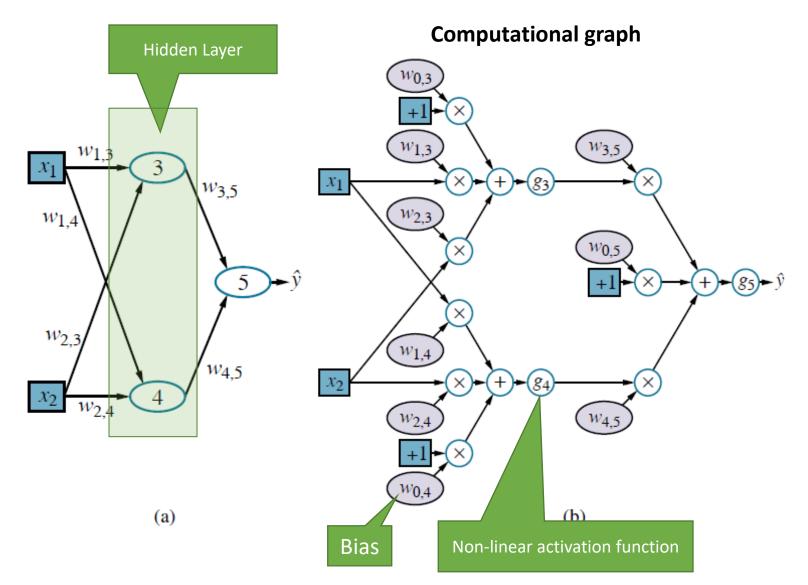
- Class is predicted by looking at the majority in the set of the k nearest neighbors.
- Neighbors are found using a distance measure (e.g., Euclidean distance between points).
- Approximates a Bayesian classifier by $h(x) = \operatorname{argmax} P(Y = y \mid neighborhood(x))$
- k is a hyperparameter. Larger k smooth the decision boundary.

Support Vector Machine (SVM)



- Linear classifier that finds the maximum margin separator using only the "support vectors" and quadratic optimization.
- The kernel trick can be used to learn non-linear decision boundaries.

Artificial Neural Networks/Deep Learning



- Represent $\hat{y} = f(x)$ as a network of weighted sums with non-linear activation functions (e.g., logistic, ReLU, tanh).
- Learn weights w from examples using backpropagation of prediction errors $|\hat{y} y|$ (gradient descend).
- ANNs can approximate any function (low bias).
 Regularization is typically used to avoid overfitting.
- **Deep learning** adds more layers (e.g., convolution layers)

Other Models and Methods

- Many other models exist
 - Generalized linear model (GLM): A model family that includes linear regression and the classification method logistic regression.
- Often used methods
 - Ensemble Learning: Use many models and combine the results (e.g., random forest, boosting).
 - Regularization: enforce simplicity by using a penalty for complexity.
 - Stochastic Gradient Descent (SGD): to find model parameters that minimizes the loss.
 - Kernel trick: Let a linear classifier learn non-linear decision boundaries (= a linear boundary in a high dimensional space).