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THE SAD TRUTH ABOUT HAPPINESS SCALES

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The Sad Truth About Happiness Scales
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ABSTRACT

We show that, without strong auxiliary assumptions, it is impossible to rank groups by average happiness using survey data with a few potential responses. The categories represent intervals along some continuous distribution. The implied CDFs of these distributions will (almost) always cross when estimated using large samples. Therefore some monotonic transformation of the utility function will reverse the ranking. We provide several examples and a formal proof. Whether Moving-to-Opportunity increases happiness, men have become happier relative to women, and an Easterlin paradox exists depends on whether happiness is distributed normally or log-normally. We discuss restrictions that may permit such comparisons.

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1 Introduction

There is an extensive literature that relies on questions in which individuals are asked to report their happiness in a few ordered categories such as “very happy,” “pretty happy” or “not too happy.” We argue that with such scales it is essentially *never* possible to rank the overall happiness of two groups without strong auxiliary assumptions. Consequently, it is impossible to use such data to make scientifically valid statements of the form “people in country A are, on average, happier than people in country B” or that “married men are happier than single men” unless we believe that we know a great deal about the underlying distribution of happiness.

Our argument is simple. When placing themselves on a happiness scale that consists of a small number of points, people place their happiness or utility in a range.¹ For example, they describe themselves as “very happy” if their utility exceeds some critical value. Oswald (2008) refers to this as the reporting function. Any comparison of two groups presumes that the cutoffs for the groups are identical. If not, comparing the groups would be tantamount to declaring group A happier than group B because the proportion of As declaring themselves “quite happy” was greater than the proportion of Bs declaring themselves “ecstatically happy.”

If, for example, we have a scale with three categories (two cutoffs), we can, without apparent loss of generality, normalize the cutoffs to be 0 and 1. Given some belief about the full underlying distribution, such as that it is logistic or normal, we can estimate two parameters (e.g. the mean and variance) of the distribution from the distribution of the responses across categories.

Since we can calculate the mean, it might appear that we can compare average happiness. However, just as monotonic transformations of the utility function do not change choices under a revealed preference model of utility, monotonic transformations do not alter the category into which expressed utility or happiness falls. Therefore, unless the distribution of responses across categories enables us to conclude that one underlying distribution is greater than the other in the sense of first-order stochastic dominance, we cannot order the means. However, we will not be able to establish first-order stochastic dominance of the underlying distributions unless the estimated variances are identical, which is an essentially zero-probability event. Moreover, even if our estimates of the variance are identical, since

¹There is a literature (e.g. Frey and Stutzer, 2000) that distinguishes between utility as measured by revealed preference and happiness as reported in surveys. We view the underlying concepts as the same. Whether happiness or utility should be measured by revealed preference/willingness to pay or self-reports is a separate issues. Our point is merely that regardless of how utility or happiness is elicited, we cannot know more than the ranking of happiness.

both are merely estimates subject to error, our posterior that they are identical must still be 0.

Our argument is related to Oswald’s discussion of the reporting function. In an interesting experiment, he asks subjects to report their height on a continuous scale from 0 to 10. He finds that when the sample is split by sex, the response on the scale is roughly linear in actual height. There is, of course, between respondent variation, but we will mostly abstract from between person differences in the reporting function in what follows. Instead, we argue that there is a fundamental difference between height and happiness. The underlying variable height is measured on an interval scale. Regardless of whether the respondent uses metric or imperial measures, the reporting function will have the same shape. But happiness is ordinal. It is as if we could not agree whether height should be measured in centimeters, the log of centimeters or the exponential of centimeters.

In principle, this problem can be solved if we are willing to tie the happiness scale to some outcome measure. Bond and Lang (2014) develop interval measures of achievement by tying test scores to eventual completed education and to the associated expected wages. But as the parallel with their analysis of test scores shows, the conclusions we reach may depend on whether we relate the underlying happiness measure to the probability of committing suicide or some other outcome. Moreover it is not clear to us why in this case we would not prefer to measure the related outcomes directly. As discussed in section four, regardless of the concerns we raise about the measurement of happiness, the evidence is strong that Moving to Opportunity reduced symptoms of depression and improved other measures of psychological well-being.

The alternative approach, which is the one we will emphasize, is to place restrictions on the distribution of happiness in the population. However, this, too, raises difficulties. Our beliefs about what distributions are plausible are likely to depend on our beliefs about, among other things, the marginal utility of income. Yet, the relation between happiness and income is one of the key areas of debate in happiness research.

In the next section, we present a series of simple examples. We show first that even if happiness is normally distributed, shifting respondents from “not too happy” to “pretty happy” can *lower* our estimate of average happiness. We then provide an example which appears to avoid this problem: the distribution of responses over the three categories is higher in the sense of first-order stochastic dominance, and estimated mean utility for the group with more positive responses is higher. However, at one point in the utility distribution, a substantial minority of the second group has higher utility than the members in the first group. A simple monotonic transformation of the utility function (or happiness distribution) fits the data equally well but reverses the comparison of mean utilities. Finally, we further

show that when mean happiness is estimated assuming happiness is normally distributed, a common implicit assumption, one of two simple exponential transformations can reverse *any* reported happiness gap.

In the third section we prove our main result: **it is (almost) never possible to rank the mean happiness of two groups when the data are reported on a discrete ordinal scale**. We apply this result, in section four, to three findings from the happiness literature: the effect of Moving to Opportunity on happiness (Ludwig et. al, 2013); the decline in the relative happiness of women despite the dramatic progress they have made economically and socially since the 1970s (Stevenson and Wolfers, 2009), and the Easterlin paradox (Easterlin, 1973). We also investigate the impact of different distributional assumptions on comparisons more generally, by looking at the rank order of mean happiness by country. In the fifth and final section we discuss whether it is possible to weaken our result. We conclude that we can do so only under (perhaps overly) strong assumptions although we hold out some hope for a consensus on plausible restrictions on the happiness distribution which would permit strong conclusions in some cases.

2 Some Simple Examples

Suppose we ask a large number of people belonging to two groups to assess their happiness on a 3-point scale, and they respond as shown in example 1.

Example 1		
	Group A	Group B
Very happy	20	15
Pretty happy	25	30
Not too happy	55	55

The responses in group A are higher than those in group B in the sense of first-order stochastic dominance so that regardless of the values assigned to the three categories, two of which are in any event mere normalizations, group A will have higher average happiness than group B does.² However, increasingly researchers recognize that the three categories capture

²We focus on what we view as the more sophisticated approach in this literature which views these categories as capturing three parts of a continuum. We note, however, that is common for researchers to assign the values 0, 1 and 2 to the three categories, in which case, group A would have mean happiness .65 while group B would have mean happiness of only .6. Alternatively, they may perform a linear transformation by subtracting by the mean and dividing by the variance. This has no substantive impact on the results. These approaches assume that the three points on the scale represent known points on an interval scale,

a continuum. Therefore they are likely to estimate underlying happiness using ordered logit or probit. For a normal distribution of happiness with mean μ and standard deviation σ , textbook ordered probit will estimate μ/σ . Different computer packages use somewhat different normalizations to identify the model. We will use Stata which sets the constant term equal to zero and the variance to 1. Stata informs us that group B is .07 standard deviations less happy than group A if we use ordered probit. and about .08 standard deviations less happy if we use ordered logit.

But this conclusion is problematic because it assumes that the distribution of happiness differs between the two groups only through a shift in the mean. It is highly unlikely that a shift in the mean would induce only a shift between the top two categories and not one between the bottom two categories. Indeed this cannot happen with either the normal or logistic distribution. If there were roughly 400 observations in each group, a maximum likelihood estimator for either a normal or logistic distribution would reject the null hypothesis that the distributions differ only due to a shift in their mean.

Of course, we could estimate the ordered probit or logit separately for the two groups, but this makes it difficult to interpret the difference. When estimated on a single group with no explanatory variables, normalizing the constant to 0, as in Stata, sets the mean equal to 0. Therefore, we cannot find a difference in mean happiness between the two groups. Instead, we would conclude that for some unfathomable reason, members of group B declare themselves very happy only when their happiness exceeds 1.04 standard deviations above the mean while members of group A are very happy as long as their happiness exceeds .84 standard deviations above the mean although both groups declare themselves not too happy if their happiness is less than .13 deviations above the mean.

Needless to say, this is an unsatisfactory conclusion. The normalizations rule out differences in the true distributions of happiness, the very phenomenon we are trying to investigate. **A more reasonable assumption is that the members of groups A and B define the categories of happiness similarly but have both different means and standard deviations of happiness.** Without loss of generality (under the normality assumption), we set the cutoff between “not too happy” and “pretty happy” to 0 and the cutoff between the latter category and “very happy” to 1.

which, it will be clear we view as incorrect. There are even cases where such scales have been treated as ratio scales: “... the data revealed that those making \$55,000 were just 9 percent more satisfied than those making \$25,000.” (Dunn and Norton, 2013, p. xiv)

Given normality, we solve

$$\Phi\left(\frac{-\mu}{\sigma}\right) = .55 \quad (1)$$

$$\Phi\left(\frac{1-\mu}{\sigma}\right) = .80 \quad (2)$$

for group A and similarly for group B except that we replace .80 with .85.

We find that average utility is actually lower for group A at $-.18$ than for group B which has average utility $-.14$.³

To gain some intuition into this seemingly perverse result, consider a more extreme situation portrayed in example 2. In this case in both groups 55% are “not too happy” but the remaining 45% of group A are “very happy” whereas their counterparts in group B are only “pretty happy.” Given a normal distribution, the only way for no one to have happiness between 0 and 1 is for the variance to be infinite. With more observations to the left of 0 than to the right of it, as variance goes to infinity, mean utility goes to minus infinity. So, on average, group A is infinitely unhappy. In contrast, when nobody reports being “very happy,” the variance must be near zero. As the variance goes to zero, all observations are clustered very close to zero. Even though somewhat more people find themselves with happiness just below zero than just above it, they are all so close to zero that mean happiness among group B is also very close to zero.

Example 2		
	Group A	Group B
Very happy	45	0
Pretty happy	0	45
Not too happy	55	55

As the example may suggest, and it is straightforward to show, with the normal and logistic distributions, perverse examples arise when the median response lies at one of the extremes. In the happiness data for the United States, the median generally lies in the middle category. However, the normal and logistic distributions are both symmetric distributions. Asymmetric distributions can produce different results.

Even if estimated mean happiness changes in the same direction as the movement among categories, it will rarely be the case that the distributions of happiness can be ranked in the sense of first-order stochastic dominance. Consider example 3. Again group B appears to

³For the logistic distribution the means are $-.17$ and $-.13$.

be happier than group A. But let us assume that happiness is logistically distributed and normalize the cutoffs to 0 and 1 as before. Now our estimate of mean happiness for group B (.61) is indeed above the estimated mean for group A (.50), but the spread coefficient is also larger (.42 v .36) so that the happiness distributions cross at the 14th percentile. The results if we instead assume that happiness is normally distributed are similar.

Example 3		
	Group A	Group B
Very happy	.2	.28
Pretty happy	.6	.53
Not too happy	.2	.19

At first blush this may not seem problematic. Although neither group is happier in the sense of first-order stochastic dominance, we can still say, using either distribution, that group B is happier on average. Unfortunately, this conclusion relies on the assumption that we know the true distribution. Any monotonic transformation of the utility function is also a legitimate utility function. And given that the distributions cross, we can always define a new utility function/happiness distribution that fits the data equally well and for which the conclusion about mean utility is reversed. In example 3, starting from the normal distribution, we can redefine all utilities below -.163 to be

$$u^* = c(u + .163) - .163. \quad (3)$$

For c sufficiently positive, the estimates of average utility will be reversed.

In fact, perverse examples can even come from standard distributions. Suppose that we used ordinal data to estimate an underlying happiness distribution assuming normality. If we normalize the cut-points to 0 and 1, we will obtain a parameter for the mean, μ , and standard deviation, σ . Suppose we instead estimated a log-normal distribution, by transforming the utilities by e^X . Our new mean is

$$e^{\mu + .5\sigma^2}$$

If we are comparing two groups, one of which has a higher mean and the other a higher variance, this transformation alone could reverse the ranking obtained by the normal distribution. If not, we can raise the cut-point from 1 to c . This is equivalent to multiplying our data by c and thus would have no impact on the direction of the gaps when we estimate with the normal. However, the mean under the log-normal transformation becomes

$$\bar{\mu} = e^{c\mu + .5c^2\sigma^2} \quad (4)$$

There then will always be a c large enough to reverse the ranking.

What if one group has both a higher mean and higher variance when estimated normally? We can then transform the data by $-e^{-cX}$ to be left-skewed log-normal. The mean of happiness becomes

$$\bar{\mu} = -e^{-c\mu + .5c^2\sigma^2} \quad (5)$$

which is decreasing in σ . Thus there must be some c that will reverse the gap. It should be noted that in both cases these are just simple monotonic transformations of the utility function. Since happiness is ordinal, these transformations represent the responses equally well.⁴

There is a risk that our criticism will be confused with one that is trite. It is, of course, possible to argue that even though a lower proportion of group A than of group B is very happy, the As in this group are much happier than the Bs or that the unhappy Bs are much more unhappy than the unhappy As. But our argument is different. The allocation of the responses across the three categories strongly suggests that the variance of utility differs between the two groups. Therefore, one of the above possibilities should be recognized as highly likely.

Our focus is on reversals in the estimation of means. However, there is a small but growing literature discussed below that analyzes the dispersion of happiness. It is straightforward to generate plausible examples in which different assumptions about the distribution of happiness lead to different conclusions about relative variances. However, we make no claim that there is always an easy transformation that generates such a reversal.

Finally, we note that the *examples* do not require that utility be unbounded. Even if we believed that utility is uniformly distributed over some range, in all three examples the cumulative distributions of the utilities of the two groups would cross. However, with bounded utility, it is also possible to construct generic examples where the cdfs do not cross.

3 The General Argument

Assumption 1 *Utility u is unbounded.*

Assumption 2 *The cumulative distribution function $F(u)$ is continuous with $F'(u) > 0$.*

Assumption 3 *The cumulative distribution function can be written as a function of $(u - m)/s$ where u is the utility level, m is a measure of central tendency and s is a measure of spread.*

⁴It is worth noting that our analysis stands in sharp contrast with Hammond, Liberini and Proto (2011) who accept Pareto superiority as a normative principle but view stochastic dominance of subjective well-being as reported in categories as a necessary and sufficient condition for Pareto superiority.

In the case of the normal, m is the mean, s is the standard deviation. For the Cauchy distribution m is the median or mode, and s is a transformation of the entropy. Of course, in the case of the Cauchy distribution, it would not be meaningful to try to estimate mean utility. While not all distributions satisfying assumptions 1 and 2 will also satisfy assumption 3, depending on how one defines “standard,” most or all standard distributions do. These include the extreme value, logistic (including generalized logistic if the auxiliary parameters are held constant) and Laplace.

These three assumptions are sufficient to ensure the absence of first-order stochastic dominance except in a knife-edge case.

Proposition 1 *Under assumptions 1-3, if the happiness or utility of two groups is drawn from the same distribution except for the values of m and s , the cumulative distribution functions of utility for the groups cross at $-\infty < u^* < \infty$ unless s is identical for the two groups.*

Proof.

$$u^* = \frac{m_2 s_1 - m_1 s_2}{s_1 - s_2},$$

where 1 and 2 denote the two groups, which is finite for $s_1 \neq s_2$. ■

Remark 1 *Assumption 3 can be replaced with other assumptions. For example, if both distributions are symmetric, then one will have lower density at both $\pm\infty$ which is sufficient to ensure that first-order stochastic dominance fails.*

Remark 2 *Stochastic dominance can exist in three parameter models. If, for example, $F_i(x) = \left(1 + e^{-\frac{(x-m_i)}{s_i}}\right)^{-\tau_i}$, there are values of the parameters such that $F_a(x) \leq F_b(x), \forall x$. However, in general, even with four or more ordinal categories of response, three-parameter models cannot be estimated without additional restrictions that go beyond normalizations.*

We are now in a position to prove the major result of this paper.

Theorem 1 *Let $F\left(\frac{u-m_1}{s_1}\right)$ and $F\left(\frac{u-m_2}{s_2}\right)$ be the estimated cumulative distribution functions from categorical data on happiness. Then there is a transformation of the utility function that fits the data equally well but that reverses the ranking of the mean utilities.*

Proof. WLOG let $m_1 < m_2$. Let u^* represent the solution to $F\left(\frac{u-m_1}{s_1}\right) = F\left(\frac{u-m_2}{s_2}\right)$ and assume that $F\left(\frac{u'-m_1}{s_1}\right) > F\left(\frac{u'-m_2}{s_2}\right) \Leftrightarrow -\infty < u' < u^*$. Normalize the value of the lowest cutoff to be 0 so that $F\left(\frac{0-m_1}{s_1}\right)$ is the predicted proportion of type 1s in the lowest category

and similarly for type 2s and normalize the value of the highest cutoff to be 1 so that $1 - F\left(\frac{1-m_1}{s_1}\right)$ is the predicted proportion of type 1s in the highest category and similarly for type 2s. Choose any \tilde{u} such that $\tilde{u} < \min(0, u^*)$.

$$m_1 = \int_{-\infty}^{\tilde{u}} u F' \left(\frac{u - m_1}{s_1} \right) du + \int_{\tilde{u}}^{\infty} u F' \left(\frac{u - m_1}{s_1} \right) du \quad (6)$$

$$m_2 = \int_{-\infty}^{\tilde{u}} u F' \left(\frac{u - m_2}{s_2} \right) du + \int_{\tilde{u}}^{\infty} u F' \left(\frac{u - m_2}{s_2} \right) du. \quad (7)$$

Integration by parts, subtracting and noting that the cdfs are equal at $\pm\infty$ gives

$$m_2 - m_1 = \int_{-\infty}^{\tilde{u}} \left(F \left(\frac{u - m_2}{s_2} \right) - F \left(\frac{u - m_1}{s_1} \right) \right) du + \int_{\tilde{u}}^{\infty} \left(F \left(\frac{u - m_2}{s_2} \right) - F \left(\frac{u - m_1}{s_1} \right) \right) du$$

where the first integral is negative and the second is positive.

Replace u with $\gamma(u - \tilde{u}) + \tilde{u}$ for $u < \tilde{u}$, then we have

$$\begin{aligned} m'_2 - m'_1 &= \gamma \int_{-\infty}^{\tilde{u}} \left(F \left(\frac{u - m_2}{s_2} \right) - F \left(\frac{u - m_1}{s_1} \right) \right) du + \int_{\tilde{u}}^{\infty} \left(F \left(\frac{u - m_2}{s_2} \right) - F \left(\frac{u - m_1}{s_1} \right) \right) du \\ &= (\gamma - 1) \int_{-\infty}^{\tilde{u}} \left(F \left(\frac{u - m_2}{s_2} \right) - F \left(\frac{u - m_1}{s_1} \right) \right) du + m_2 - m_1 < 0 \\ &\Leftrightarrow \gamma > 1 - \frac{m_2 - m_1}{\int_{-\infty}^{\tilde{u}} \left(F \left(\frac{u - m_2}{s_2} \right) - F \left(\frac{u - m_1}{s_1} \right) \right) du}. \end{aligned}$$

■

Finally, we note that since the ordinal responses are reported in categories, in finite samples, depending on the number of observations from each group, there can be a positive probability that the estimated s will be the same for two independent samples. However, as the sample gets large, this probability gets small.

Remark 3 Let $L = \sum_{j \in G_i} \sum_c d_c \ln F_j^c(m_i, s_i)$ be the log-likelihood function of distribution $F(m, s)$ for group G_i from J independent observations of data d with C categories and let \hat{m}_i, \hat{s}_i be the parameter estimates that maximize the estimated likelihood, then

$$N^{.5}(\hat{s}_i - s_i) \rightarrow^d N(0, \sigma_s^2)$$

This remark follows from the standard properties of maximum-likelihood estimators. It follows directly that for large but finite samples, the estimated measures of spread will almost never be equal.

This, in turn, leads to our main result.

Conclusion 1 *If happiness (or utility) is reported using a discrete ordinal scale, in large samples it will (almost) never be possible to rank the mean happiness of two groups without additional restrictions on the nature of the happiness distribution.*⁵

4 Empirical Applications

4.1 Moving to Opportunity

Economists have long postulated that living in a poor neighborhood may make it more difficult to escape poverty. Motivated by this idea and the positive results of the Gautreaux desegregation program in Chicago,⁶ the Moving-to-Opportunity experiment targeted families living in public housing in high poverty areas. Eligible families were invited to apply for the chance to receive a Section 8 housing (rental assistance) voucher. Applicants were randomly assigned into three groups: no voucher (Control group), Section 8 voucher that could only be used in an area with a poverty rate below 10% (Experimental group), and a standard Section 8 voucher (Section 8 group).

The program has been assessed at multiple stages.⁷ A long-term follow-up (Ludwig et al, 2012, 2013) emphasizes that subjects in the experimental group were substantially happier than those in the control group. We reexamine the evidence for this conclusion.

The participants in the long-term MTO evaluation study were asked “Taken all together, how would you say things are these days – would you say that you are very happy, pretty happy, or not too happy?” The authors focus on the effect on the distribution of responses across categories. Nothing we write below can or will contradict the finding that MTO increases the proportion of individuals who report that they are “very happy” and reduces the proportion who say they are “not too happy.” If these are the socially relevant categories,

⁵The intuition behind this is relatively straightforward. Needless to say, if the true variances are not equal, then asymptotically the probability that the estimates differ by less than ε goes to 0 as the samples become large. Suppose, however, that $s_A = s_B = s$. Then $\hat{s}_A \rightarrow^d N(s, \sigma_A^2)$ and $\hat{s}_B \rightarrow^d N(s, \sigma_B^2)$. Define $\alpha = \hat{s}_A - \hat{s}_B$. Then since \hat{s}_A and \hat{s}_B are asymptotically independent normals, $\alpha \rightarrow^d N(0, \sigma^2)$ where $\sigma \equiv (\sigma_A + \sigma_B)$.⁵ The asymptotic density at $\alpha = 0$ is $(2\pi)^{-.5} \sigma^{-1}$. Since the density is maximized at 0, the probability that α falls in the range $-\varepsilon\sigma < \alpha < \varepsilon\sigma$ is less than $2\varepsilon\sigma (2\pi\sigma^2)^{-.5} = (2/\pi)^{.5} \varepsilon$ which can be made arbitrarily small for any sequence of σ approaching 0. We are grateful to Zhongjun Qu for providing us with this argument.

⁶The Gautreaux program came out of a court-ordered desegregation program in Chicago in the 1970s. See Rosenbaum (1995) for a detailed analysis.

⁷For the earliest evaluation, see Katz, Kling, and Liebman (2001). For an intermediate-term evaluation, see Kling, Liebman, and Katz (2007).

then there is no need to estimate a mean, or any other single summary measure of happiness. Thus, for example, we might believe that people are “not depressed,” “mildly depressed” or “severely depressed” and view variation in depression within these categories as unimportant. We take no position on the accuracy of this view of depression, but if we accept it, an intervention that reduces the proportion of severely and mildly depressed individuals reduces depression since variation in depression within categories is unimportant. We return to this point in our conclusions.

However, we believe that happiness should be viewed as continuous. Therefore, statements about mean happiness and not just the frequency of responses within categories are potentially relevant. Ludwig et al (2012, table S4) report intent-to-treat estimates on the experimental group using intervals of 1 unit between the categories, as is common in the literature, but also ordered probit and logit. For purposes of comparison with the literature, Ludwig et al not only show the effects on the distribution of responses but also consider the case where they assign values of 3, 2, and 1 to the three responses. In all three cases, they find positive effects on average happiness that fall just short of significance at the .05 level.

If we believed that happiness is normally distributed, normalizing the cutoffs to 0 and 1, we would find that the control group does have a lower mean (.44 v. .60). But, the control group also has a higher variance (.79 vs .63). The cdfs cross at the 83rd percentile, which is 1.20 units of happiness (and also in the extreme left tail of the distributions). Thus if we simply define a new utility function which increases the values of happiness above 1.20 we can reverse the mean happiness. This utility function would explain the data equally well.

Alternatively, we can perform an exponential transformation to get a log-normal distribution of happiness. Keeping our underlying cut-points fixed at 0 and 1, the exponential transformation will still show that the experimental group (2.22) is happier than the control group (2.14). But, as discussed in section 2, since the control group has a higher variance of happiness, we can raise their mean relative to the experimental group by raising the cut-point between pretty happy and very happy. If we raise our cut point to 1.33, or equivalently raise each individual’s happiness to the 1.33rd power after performing the exponential transformation, the mean utilities of the two groups are equal. As we show in figure 1, this amounts to a somewhat right-skewed distribution of happiness, meaning the differences among the happiest individuals are greater than the differences among the least happy. This utility function is just a monotonic transformation of the one underlying the normal distribution and thus fits the data equally well. Therefore, we cannot determine whether the causal effect of MTO on happiness is positive on average. One plausible interpretation of the data is that moving to a low poverty area reduced both the probability of being extremely unhappy and extremely happy.

One solution to this indeterminacy is to tie our assessment of (un)happiness to some other outcome variable. This is the approach we use in Bond and Lang (2014) where we scale test scores in a given grade by the eventual educational attainment of students with those test scores. The limited number of points on the happiness scale makes this difficult. This discreteness may be missing variation within the categories that represents important distinctions in happiness. But, compared with variation at the high end of the scale, variation in happiness at the low end of the scale might prove to be more closely correlated with other signs of psychological distress, which were also shown in Ludwig et al to be beneficially influenced by moving to a neighborhood with a lower poverty rate.

Thus, in settings where we do not have direct measures of psychological well-being, it *may* be possible, we are agnostic on this point, to use data from other settings such as MTO to scale happiness in a more compelling way. For MTO, the strongest evidence of positive psychological benefits comes from direct measures of the prevalence of psychological problems. Provided that these conditions are discrete rather than continuous, our concerns about happiness scales do not apply to such things as measures of depression.

4.2 The Paradox of Declining Female Happiness

One surprising result from the happiness literature, documented by Stevenson and Wolfers (2009), is that women’s happiness appears to have fallen relative to men’s from 1972-2006 despite the great social and economic progress women made during this period. Again, this result is easily reversed.

We use the publicly available file created by Stevenson and Wolfers from the General Social Survey (GSS), a nationally representative survey of social attitudes conducted annually or biennially since 1972. The GSS assesses subjective well being using responses to the question later adopted in the MTO study. While the question remains constant over time, its position in the survey does not, which could lead to biases in responses in different years.⁸ Stevenson and Wolfers use split-ballot experiments to modify the data to account for these differences.⁹

To simplify the analysis and ease exposition, we create two subgroups: those from the first five surveys (1972-1976) and those from the last five surveys (1998-2006) but can obtain similar results using the full time series. We display the distribution of happiness in these groups in Table 2. Using ordered probit, Stevenson and Wolfers found that women

⁸For example, Stevenson and Wolfers (2009) note that in every year but 1972, the question followed a question on marital happiness, which may cause differences in the impact of one’s marriage on his or her response to the general happiness assessment. See Smith (1990).

⁹For details of this process, see appendix A of Stevenson and Wolfers (2008b).

lost ground to men at the rate of .376 standard deviations per century. We confirm this result between the two subgroups; ordered probit estimates that women were .09 standard deviations less happy relative to men in the later sample than the early.

However, as discussed previously, ordered probit assumes that the variance of happiness is constant across sex and over time, an assumption we can easily reject. When we allow the variances to differ, we find women’s happiness has more variance than men’s and that the variance of happiness has declined over time. This is what one would expect from looking at the data. Most of the differences between the sexes and over time are due to there being more “very happy” women in the early years. When more people are “very happy” but there is no difference in the number “not too happy” the distribution must have higher variance to fit the data. Relaxing the constant variance assumption lowers the growth of the gap to .07.

Now, we transform the utility function by

$$\tilde{u} = -e^{-Cu} \tag{8}$$

so that the distribution of happiness is given by the left-skewed log normal distribution. Since their utility distribution has the highest variance under the normality assumption, choosing a C sufficiently large lowers the mean utility of women in the early period by more than it does men’s. As we show in Figure 2, for $C \geq 3.9$ women become happier over time relative to men, as one might expect given their social progress in the period. Large values of C will show large increases in relative female happiness.

Admittedly, when $C = 3.9$, the distribution is fairly skewed. This implies that utility differences among the unhappiest people are far greater than differences among the happiest. All happy people have happiness between 0.02 and 0, while 5% of the distribution has happiness below -250 . Of course, this distribution fits the data just as well as the normal. From the data alone it is difficult to argue that one utility distribution is clearly more plausible.

Further, this is just one scale and distribution based on a simple transformation under which women gain happiness relative to men. There are an infinite number of others, and more complex transformations may create distributions that are more intuitively appealing. Ultimately if we can gain consensus about plausible restrictions on the happiness distribution (e.g. skewness, kurtosis) or at least a reasonable loss function involving these moments, it may be possible in some cases to conclude that no plausible transformation will reverse a particular finding.

4.3 Easterlin Paradox

No question in the happiness literature has received more attention than the “Easterlin Paradox,” the observation that in some settings higher incomes do not appear correlated with higher levels of happiness. Easterlin (1973, 1974) found that income and subjective well-being assessments were strongly and positively correlated within a country in a given year, but not over time and across countries. This, and subsequent studies, led Easterlin (1994) to conclude, “Will raising the incomes of all increase the happiness of all? The answer to this question can now be given with somewhat greater assurance than twenty years ago. It is ‘no’.” Easterlin instead concludes that the weight of the evidence supports the conclusion that individuals judge their happiness relative to their peers and not on an absolute scale.

The paradox was recently called into question in a comprehensive study by Stevenson and Wolfers (2008a).¹⁰ They use ordered probit both across countries and over time within countries and find a strong relation between happiness and economic development. However, they find that the United States is an exception. Happiness has not increased despite substantial growth in per capita incomes. They attribute this to the substantial rise in income inequality over the last 30 years which occurred simultaneously with the rise in real GDP.

We match the GSS data from Stevenson and Wolfers (2009) with U.S. per capita real disposable income data from the 2013 Economic Report of the President to get a time series of national happiness and income data. Fixing the cut-points to 0 and 1, we estimate the two parameters of a normal distribution for each year using the GSS and regress the means on per capita disposable income. As we show in Figure 3, we do indeed find an Easterlin Paradox. Ordinary Least Squares estimates imply that a \$10,000 per capita increase in real disposable income is actually associated with a decrease in happiness in the United States of .02 units, although, with a p -value of only .11, it is not statistically significant.

However, figure 4 shows that we also estimate a strong negative relation between real per capita disposable income and the variance of happiness. A \$10,000 increase in per capita income is associated with a statistically significant .04 unit decrease in the standard deviation of happiness. This may be somewhat surprising given the increase in income inequality over the time period, but is what one would expect from the data and has been demonstrated previously by Stevenson and Wolfers (2008b) and Dutta and Foster (2013).¹¹ As real income has increased, fewer people report being very happy, but there is a zero to slightly negative change in the number of people who report being not too happy.

¹⁰See also Deaton (2008) who finds similar results from the Gallup World Poll using OLS on a basic 10-point scale.

¹¹Clark, Fleche and Senik (2014, forthcoming) argue that this is a standard pattern – growth reduces happiness inequality.

Since high-income periods have a lower mean and variance than low-income periods, we know that a left-skewed log normal distribution will reverse the trend. In fact, we do not need to skew the distribution that much. For values of $C \geq .45$ we find the expected positive relationship between income and happiness. In Figure 5, we show the distribution of happiness under this set of parameters in 2006. Here the cut-point values of happiness would be -1 to go from not too happy to pretty happy and $-.64$ to go from pretty happy to very happy. There is variation among the happiest and least happy individuals, although more so among the latter given the skewness of the distribution.

For $C > 2$, this positive relationship becomes statistically significant. We plot the $C = 2.05$ case in Figure 6. Here, a \$10,000 increase in real per capita disposable income is associated with a .22 unit increase in happiness. If we are willing to accept this amount of skewness in the happiness distribution, then raising the incomes of all does not raise the happiness of all but does raise average happiness. There are other distributions and transformations that replicate this result; there is no way to determine from the data which utility function is correct.

As in the case of MTO, if we are convinced that the response categories in the survey are the ones that are relevant for policy purposes, we can avoid this problem. However, unlike the case of the female happiness paradox where it *might* be possible to conclude that no plausible happiness distribution would reverse the result, it is evident that plausible (at least to us) distributions can reverse the basic finding.

4.4 Cross-Country Comparisons

In the previous sections, we found that three conclusions based on normally-distributed happiness assumptions could be reversed by simple log-normal transformations. In this subsection we explore the sensitivity of happiness comparisons to such transformations in general. Using data from the World Values Survey, we estimate mean happiness at the country level for a normal distribution, as well as a log-normal distribution with $C = 2, .5, -.5$, and -2 .¹²

The ordering of countries in Table 3 represents their happiness ranking when happiness is distributed normally, and the columns list their ranking under the different log-normal transformations. Although the actual degree of skewness varies across countries due to differences in the variance of the underlying normal distribution, moving from left to right in the columns represents moving from a relatively right-skewed to a relatively left-skewed

¹²In contrast with the other data we use, the World Values Survey elicits happiness responses on a 4-value scale: not at all happy, not very happy, quite happy, and very happy. Because the fraction of not at all happy responses is almost universally trivial, we combine these responses with those of not very happy to get a 3-point scale. This allows us to follow the same approach as in the previous three subsections.

distribution. Doing so has dramatic effects on the rank-ordering of happiness. The five happiest countries when happiness is right-skewed are Ghana, Guatemala, Mexico, Trinidad and Tobago, and South Africa. Three of these countries rank in the *bottom* ten when happiness is left-skewed, and only one (Mexico) ranks in the upper half. The top five under the extreme left-skewed distribution of happiness (New Zealand, Sweden, Canada, Norway, and Great Britain) fare relatively better under right-skewed happiness, though only Great Britain remains in the top ten. The rank-correlation between the log-normal transformations with $C = 2$ and $C = -2$ is .156.

There are some countries whose rank remains fairly stable throughout the distribution. Great Britain is the third happiest country under a normal distribution and has its rank vary between 2 and 8 under the skewed distributions. Moldova, the world's least happy country under the normal distribution, is never able to rise above 4th worst in the skewed transformations. These cases are counterbalanced by countries like Ghana and Ethiopia. Ghana ranges from the world's happiest to the world's 3rd least happy depending on whether happiness is right- or left-skewed. Ethiopia, the 10th least happy under the normal distribution, is able to rise as high as 7th when happiness is right-skewed, placing it above the United States, Australia, and Great Britain, among others.

The wide variation in ranking suggests that in most cases the amount of skewness allowed in the distribution can have substantial impacts on cross-group comparisons. Even the most skewed-distributions we explored here are not, to us, implausible. They involve a smaller exponential transformation than required to have a significant and positive relationship between average happiness and per capita income over time in the United States (see figure 5). We do find the ranking under the left-skewed distribution to be more in-line with our priors than the right-skew or the normal, though we stress there is nothing in the happiness data itself that would allow us to choose among the distributions. Interestingly, the right-skewed distributions would imply a strong negative correlation between per capita GDP, while the left-skewed implies a strong positive relation.¹³

5 Discussion and Conclusions

As we have demonstrated, key conclusions of happiness studies depend on assumptions about the underlying distribution of happiness, something about which the data can give us little or no guidance. Since the estimated cdfs (almost) always cross when we assume a particular

¹³Using 2005 data from the IMF on purchasing power parity equivalent per capita GDP, the coefficient on a regression of estimated mean happiness and the natural logarithm of per capita GDP is -4.79 for the right-skewed ($C = 2$) distribution and .60 for the left-skewed distribution ($C = -2$).

distribution of utility, there is always some transformation that preserves the rank order of individuals and changes the direction of the estimated gap in mean happiness.

Is there any way to create compelling cross-group comparisons?

Perhaps the simplest assumption one could make is to assume that we know the policy-relevant distribution of happiness. For instance, if we believe happiness is distributed normally, we can fix the cut-points between "not too happy", "pretty happy", and "very happy" and estimate the means and variances of each group through ordered probit.

It should be clear that the choice of a particular distribution almost inevitably implies taking a stand on some of the very issues that have been the focus of the happiness literature. Thus since wealth and income are highly skewed, a normal distribution of happiness would almost necessarily require the marginal utility of wealth or income to be sharply diminishing. We do not, however, rule out the possibility that the profession could achieve near consensus on some reasonable restrictions on the happiness distribution and that these restrictions would be adequate to allow us to reach strong conclusions about the ranking of mean happiness in some cases.

Of course, there are difficulties even if we can rank means. Unless we are very traditional utilitarians who wish to maximize the sum of utilities, we will still encounter problems for policy purposes. We may, many philosophers would argue should, care more about increases in utility at some parts of the distribution than at others. In this case, the Bond and Lang (2013) criticism of test scores applies directly.

An alternative solution is to declare the ordinal scale on which people report their happiness to be the policy-relevant one. Group A is happier than group B if its members' responses "stochastically dominate" B's using the categories provided in the question about self-assessed happiness. This approach has a great deal of intuitive appeal, and we confess that in some cases we are inclined to accept it. However, it is trivial to find examples where, using what appears to be a sensible partition of the data into three categories, groups appear to be ordered in the sense of stochastic dominance, but for which the means have the reverse order when the full underlying distribution is examined. For example, there are many occupations (e.g. actors) in which mean income is relatively high but most people in the occupation have very low incomes. Other occupations have high variance but also relatively low mean wages. When stochastic dominance fails using the full underlying distribution, it is possible to group wages (or other variables) so that using the grouped data, stochastic dominance appears to hold.

Of course, as the number of response categories becomes large, it becomes less plausible that a finer grid would reverse the conclusion that the group that appears to be happier in the sense of stochastic dominance has higher mean happiness. In the experiment described

earlier, Oswald asked participants to report their height on a continuous scale from 0 to 10. Assuming that there are no responses at the extreme, if all respondents use the same reporting function, then stochastic dominance is sufficient to ensure that the ranking of the means is independent of scale. It seems to us likely that if individual differences in the reporting function are independent of group membership, first order stochastic dominance will still be sufficient to rank means. However, we note that Oswald finds evidence that men and women use different reporting functions when converting their height to his scale. It is also not evident that repeated observations on the same individuals will address the problem of heterogeneity in the response function. In addition to the well-known problems associated with estimating fixed effects with ordinal data, it is not clear that we expect individual reporting functions to be stable over time. For example, in repeated cross-sections, immigrants show no improvement in their host-country language skills, but they report improvement when asked to compare their current and earlier language skills (Berman, Lang and Siniver, 2003).

One solution when working with ordinal scales is to relate them to some measurable outcome. In the traditional economics literature, we measure the utility of a good or outcome by willingness to pay, imperfectly captured by the equivalent or compensating variation. The happiness literature has called this approach into question and with it some basic assumptions, such as positive marginal utility of money. Invoking a monetary scale thus brings us to a Catch-22. We cannot answer the main questions of the happiness literature using the most obvious tool because the literature seeks to invalidate that very tool.

Finally, we note that our examples require different transformations to reverse the results in the literature. We showed that moving to a low poverty area reduces mean happiness if happiness is log normally distributed and strongly right skewed. But the Easterlin paradox is resolved for the United States if happiness follows a sufficiently left-skewed log normal distribution. It is not obvious that there is an assumption about the distribution that would reverse both results. It may be that we can reach sufficient consensus about which distributions are acceptable that we can make definitive statements in some cases.

One possibility is what we call the “Tolstoy assumption,” that there is far greater variation in unhappiness than in happiness.¹⁴ In other words, happiness is left skewed. In this case, it is very likely that MTO did raise happiness for those who moved to less impoverished areas. This is consistent with the standard assumption that expanding the choice set of rational agents should never *ex ante* decrease utility. But before drawing strong conclusions, we should be explicit about the requisite assumptions.

¹⁴We apologize to lovers of Russian literature for this deliberate misinterpretation of Anna Karenina – “All happy families are alike; each unhappy family is unhappy in its own way.”

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Figure 1: MTO Log-Normal Happiness Distribution with Equal Means

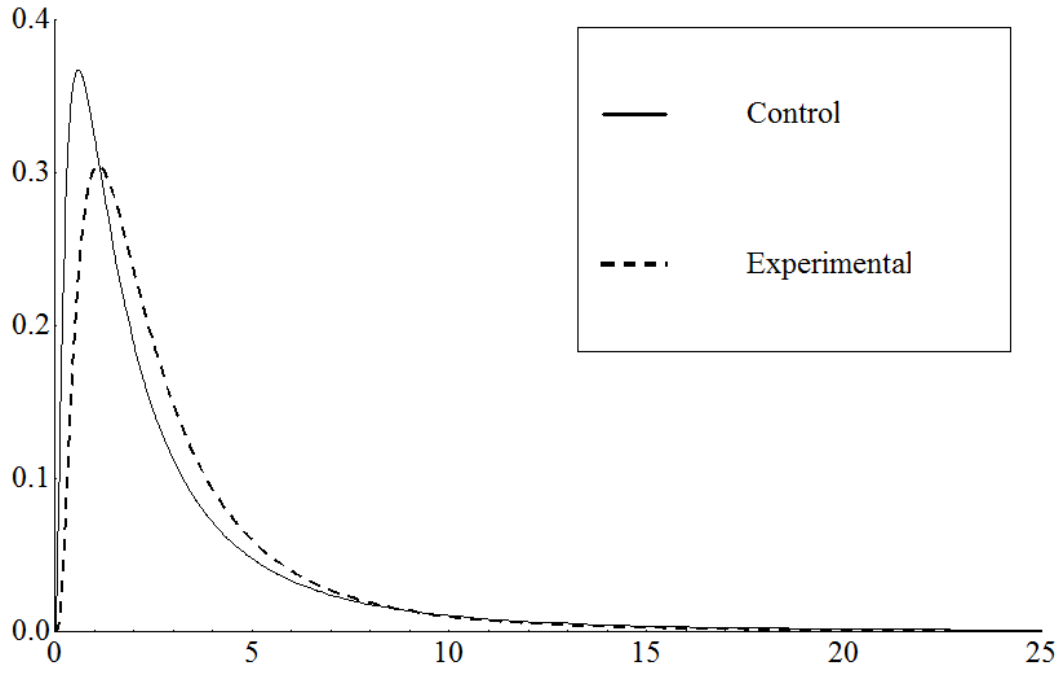


Figure 2: Trend in Female-Male Happiness Gap for Log-Normal Distributions

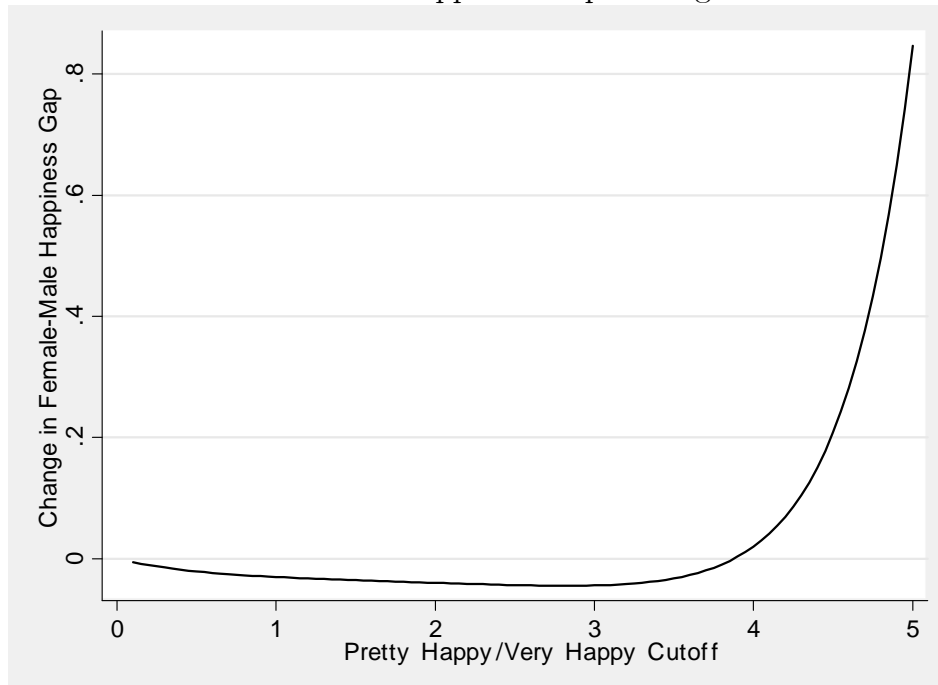


Figure 3: Mean Happiness and National Income, Normal Distribution

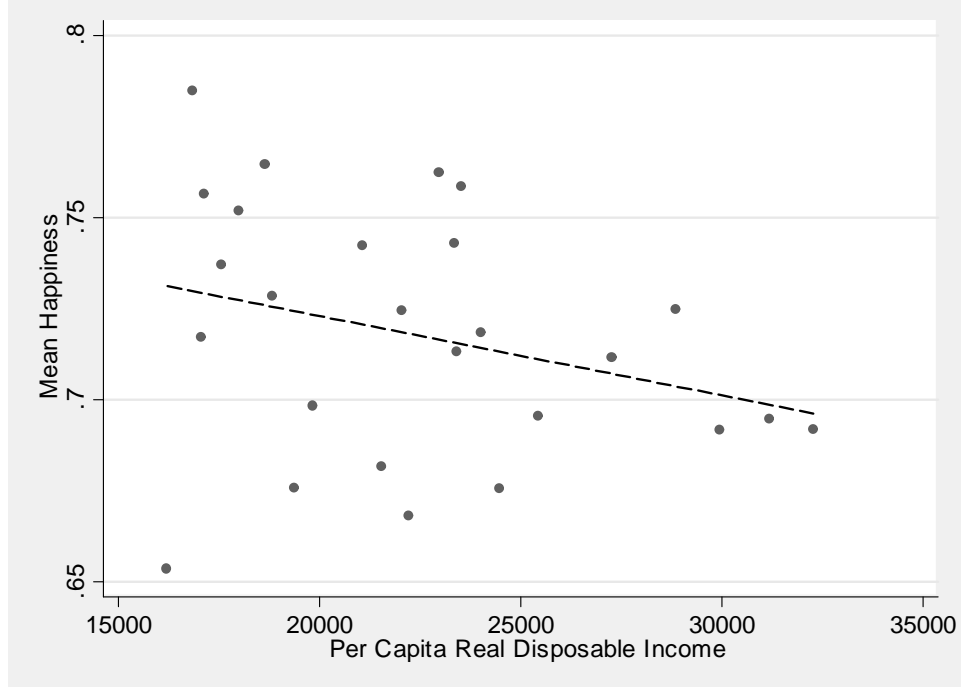


Figure 4: Standard Deviation of Happiness and National Income, Normal Distribution

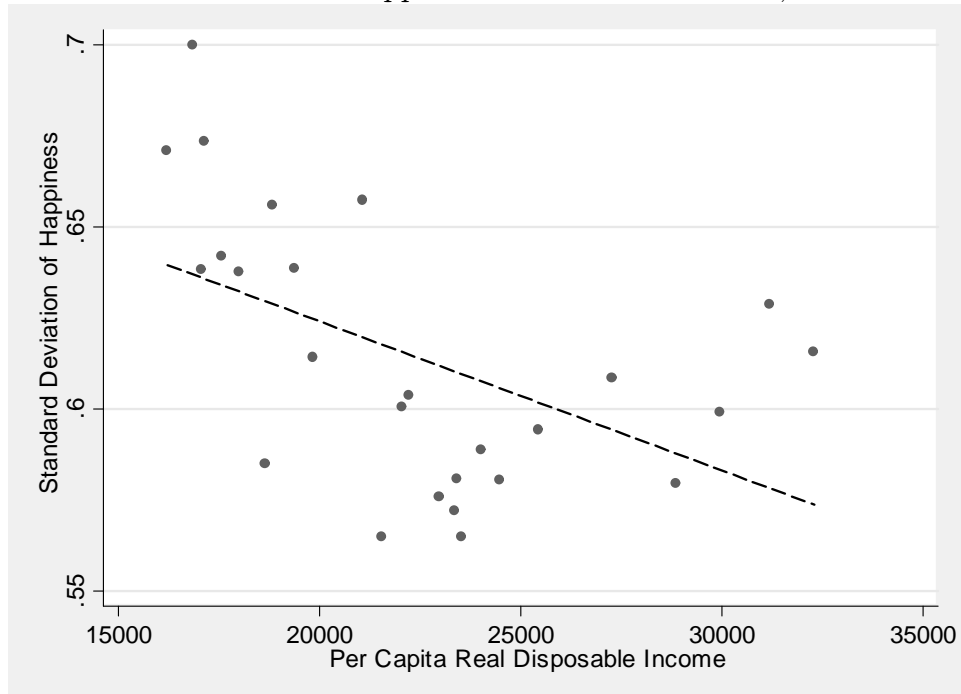


Figure 5: 2006 Log-Normal Distribution of Happiness with no Easterlin Paradox

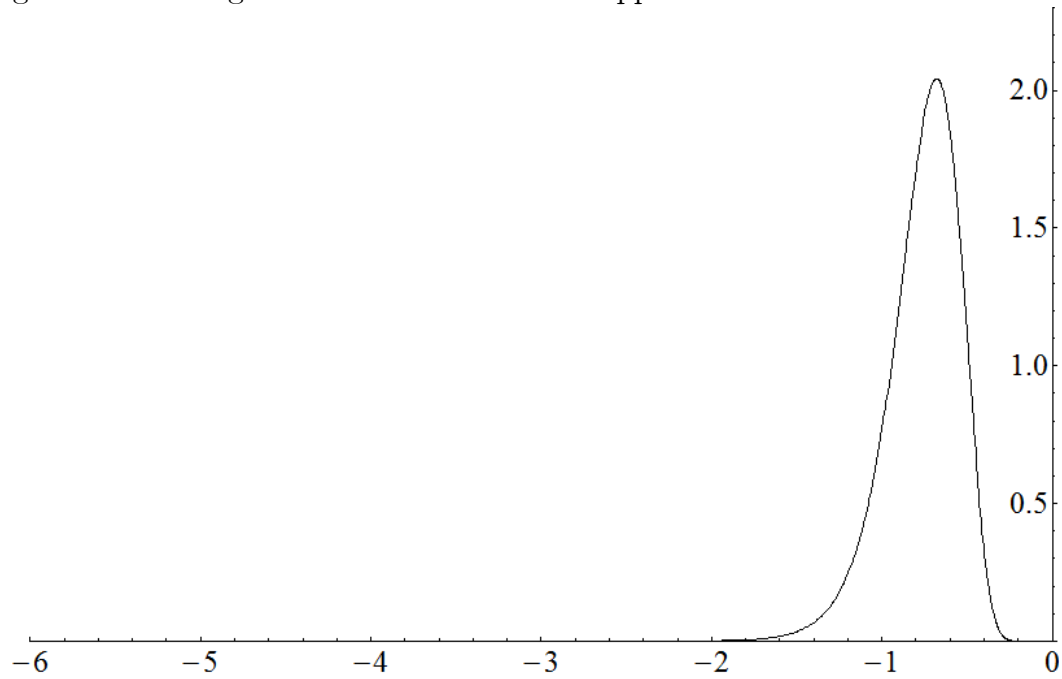


Figure 6: Mean Happiness and National Income, Log-Normal Distribution

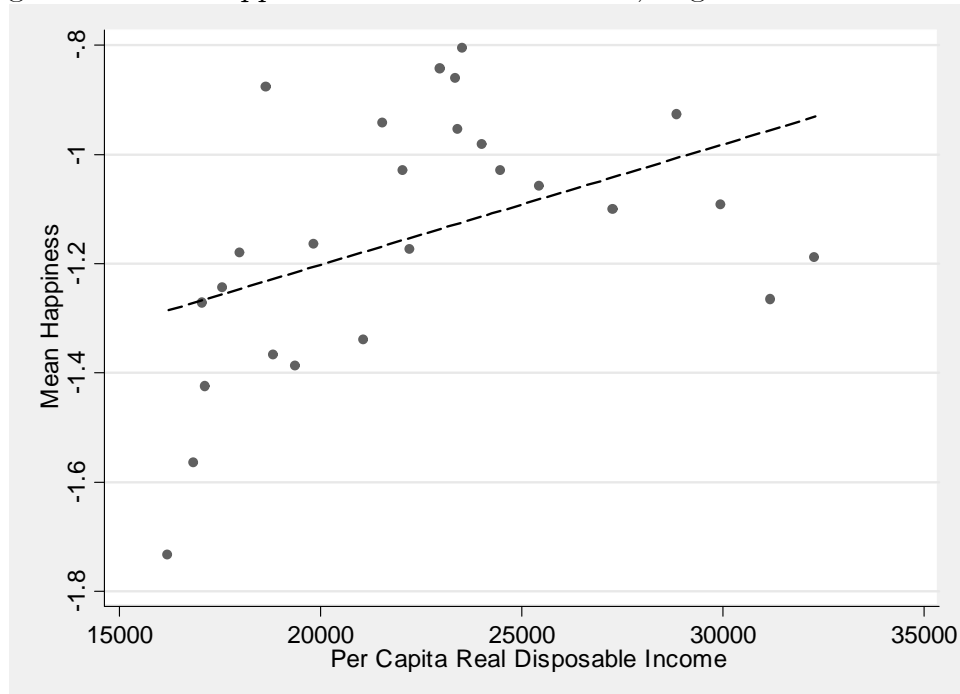


Table 1: Distribution of Happiness - Moving to Opportunities

	Control Compliers	Experimental Compliers
Very Happy	0.242	0.262
Pretty Happy	0.470	0.564
Not Too Happy	0.288	0.174

Source: Ludwig et al (2013), Appendix Table 7.

Experimental estimates are TOT.

Table 2: Distribution of Happiness - General Social Survey

	Male	Female
Panel A: 1972-1976		
Very Happy	0.337	0.384
Pretty Happy	0.530	0.493
Not Too Happy	0.132	0.122
Normal Mean	0.727	0.798
Normal Variance	0.424	0.471
Panel B: 1998-2006		
Very Happy	0.330	0.339
Pretty Happy	0.566	0.553
Not Too Happy	0.104	0.109
Normal Mean	0.742	0.748
Normal Variance	0.346	0.367

Source: General Social Survey Stevenson-Wolfers file.

Normal means and variances calculated from answers under assumption that happiness follows a normal distribution with separate means and variances

Table 3: Country Rankings of Mean Happiness under Log-Normal Distributions

	C=2	C=0.5	C=-0.5	C=-2.0
Mexico	3	2	1	20
Trinidad and Tobago	4	3	5	36
Great Britain	8	6	2	5
Ghana	1	1	26	55
Colombia	6	4	9	33
Canada	12	8	3	3
Sweden	19	9	4	2
Switzerland	14	10	7	8
Netherlands	15	11	8	6
New Zealand	27	14	6	1
Thailand	16	13	11	9
Guatemala	2	5	30	49
Norway	29	16	10	4
Malaysia	25	17	12	7
South Africa	5	7	31	48
France	20	19	15	17
Australia	22	20	14	13
United States	28	21	13	10
Mali	9	12	23	39
Turkey	11	15	20	29
Cyprus	13	18	19	26
Brazil	23	22	16	16
Argentina	24	23	22	23
Finland	32	24	18	14
Andorra	35	26	17	11
Japan	31	27	24	21
Indonesia	36	30	21	12
Uruguay	26	25	28	27
Jordan	30	28	27	24
Viet Nam	39	33	25	15
Poland	40	34	29	18
Chile	18	29	35	42

Table 3 Continued

Italy	44	39	32	22
Taiwan	38	38	34	30
Spain	45	41	33	19
Morocco	33	36	37	38
India	17	32	43	45
Burkina Faso	34	37	39	40
Germany	41	40	36	31
South Korea	46	45	38	25
Slovenia	43	43	41	35
Iran	42	44	42	37
China	37	42	45	43
Rwanda	47	46	40	28
Peru	10	35	48	53
Egypt	52	47	44	34
Hong Kong	55	49	46	32
Ethiopia	7	31	52	57
Ukraine	49	48	47	41
Russian Federation	51	52	49	44
Georgia	48	51	50	46
Serbia	53	53	51	47
Zambia	21	50	55	56
Bulgaria	50	54	53	52
Romania	56	55	54	50
Iraq	57	57	56	51
Moldova	54	56	57	54

Rank of estimated country mean happiness under various
log-normal transformations. Countries listed in order of
estimated mean happiness under normal distribution.

Source: World Values Survey 2005.