

# **Course M-GFP3: Imaging and non-imaging spectroscopy:Term Paper**

**Strategies to enhance predictive modeling of soil organic carbon (SOC) using the  
LUCAS topsoil spectral library.**

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# Outline

Structure

Authors

**Part I**

**Main**

# **1 Course M-GFP3: Imaging and non-imaging spectroscopy:**

Term Paper

Strategies to enhance predictive modeling of soil organic carbon (SOC) using the LUCAS topsoil spectral library.

## 2 Packages

```
# Use autoreload to automatically reload modules
%load_ext autoreload
%autoreload 2

import own_functions

import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import torch
import torch.nn as nn
import torch.optim as optim
from scipy.signal import savgol_filter
from scipy.stats import pearsonr
from sklearn.cross_decomposition import PLSRegression
from sklearn.decomposition import PCA
from sklearn.metrics import mean_squared_error, pairwise_distances
from sklearn.model_selection import cross_val_score, train_test_split
from sklearn.preprocessing import StandardScaler
import numpy as np
import torch
import torch.nn as nn
import torch.optim as optim
from sklearn.metrics import mean_squared_error, r2_score
from sklearn.model_selection import train_test_split
import geopandas as gpd
from autogluon.tabular import TabularDataset, TabularPredictor

import autogluon
```

## 3 Data

Data splitting (5 P):

- Split your data into a calibration data set (~70%) and an independent test data set (~30%).
- Show that both are representative of the full data set.
- For procedures with randomized approaches, please define and note the seed (in R: `set.seed( )`) to make the split reproducible for the instructors.
- From this point onward, the composition of the test data set must remain constant and unchanged for all subsequent tasks

### 3.1 Load and Clean

```
# Load data
data = pd.read_csv('data/France_spc.csv')

# Remove unnecessary column
data = data.drop(columns=['Unnamed: 0'])

print(f>Data rows: {data.shape[0]}, columns: {data.shape[1]}")
display(data.head())
```

Data rows: 2807, columns: 1000

	500	502	504	506	508	510	512	514	516	518
0	0.137399	0.139045	0.140758	0.142544	0.144388	0.146281	0.148221	0.150205	0.152239	0.154321
1	0.141740	0.142851	0.144007	0.145208	0.146450	0.147726	0.149025	0.150348	0.151702	0.153081
2	0.140713	0.142216	0.143778	0.145392	0.147053	0.148756	0.150488	0.152257	0.154059	0.155891
3	0.128922	0.129908	0.130919	0.131959	0.133019	0.134102	0.135196	0.136307	0.137433	0.138571
4	0.161760	0.163229	0.164741	0.166298	0.167895	0.169530	0.171194	0.172890	0.174611	0.176351



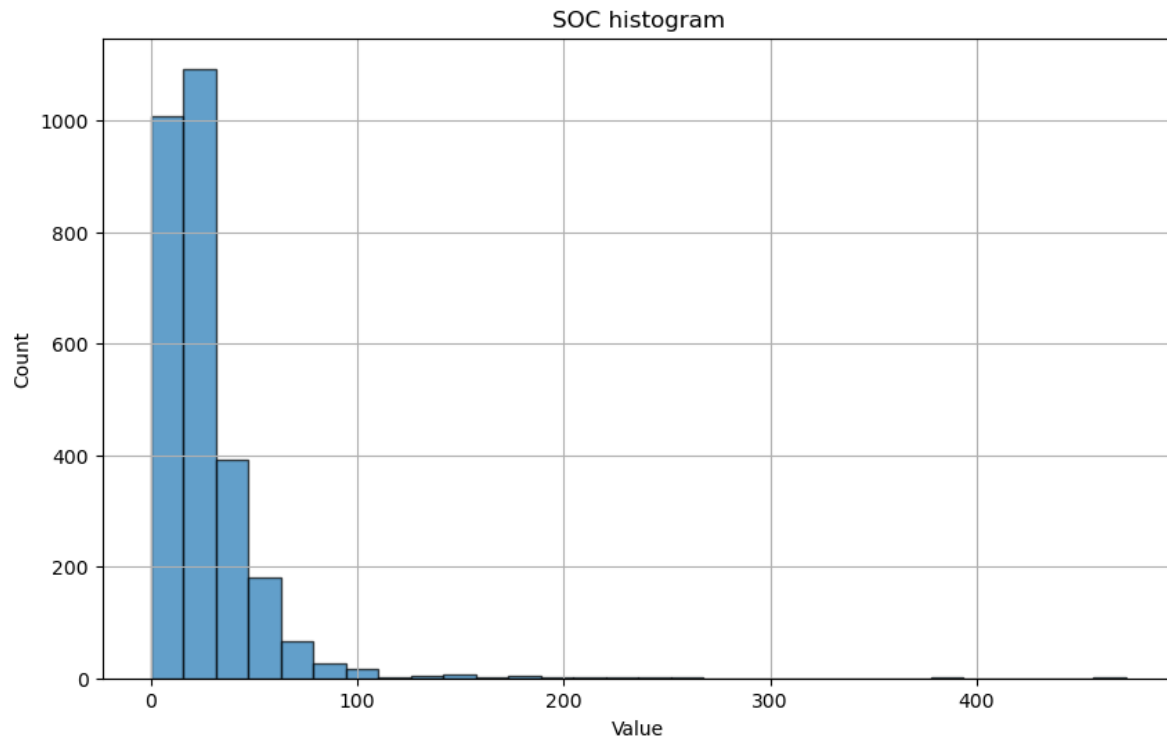
```
target_raw = pd.read_csv('data/France_lab.csv')
lat_lon = target_raw[['GPS_LAT', 'GPS_LONG']]
target = target_raw['SOC']
print(f"Target rows: {target.shape[0]}")
```

Target rows: 2807

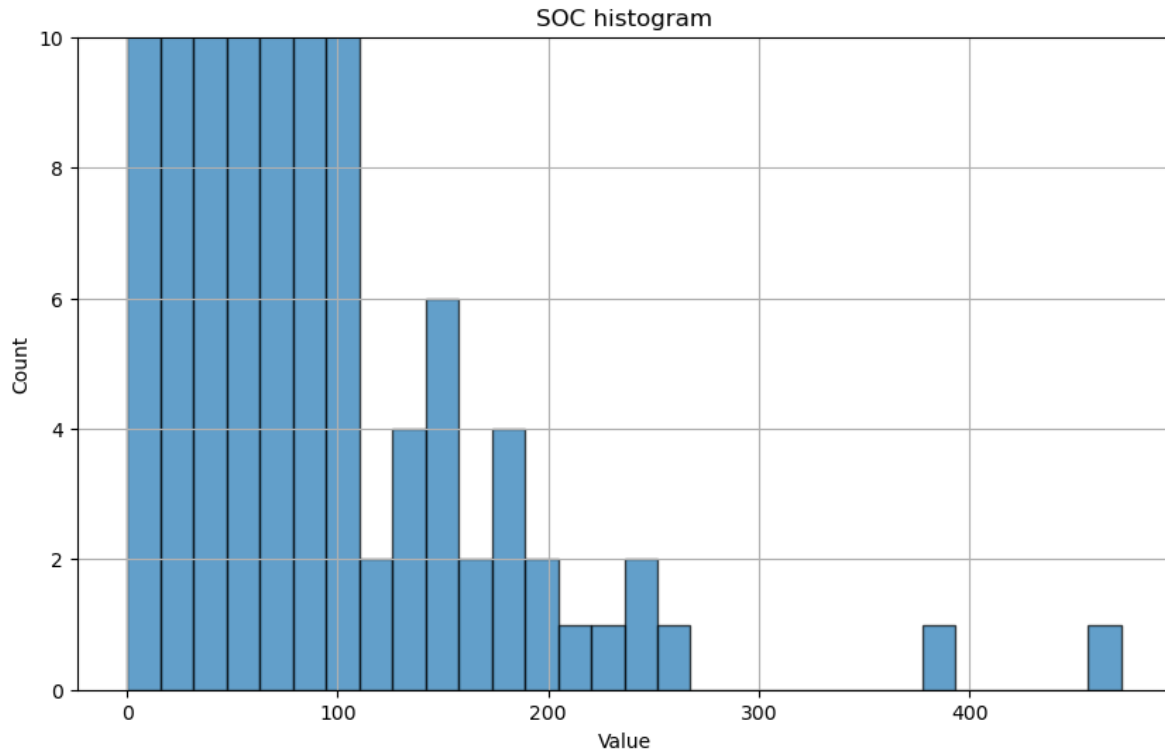
target\_raw

	Unnamed: 0	SAMPLE_ID	CLAY	SILT	SAND	SOC	CaCO3	N	P	K	CEC	C
0	1	10000	40.0	52.0	8.0	15.6	1	1.4	42.6	491.1	24.6	V
1	2	10001	26.0	18.0	56.0	19.8	1	1.6	19.5	279.1	20.6	V
2	3	10002	22.0	41.0	37.0	33.5	1	2.6	37.8	399.1	15.0	V
3	4	10004	27.0	47.0	26.0	66.1	21	6.6	147.7	1080.6	30.5	V
4	5	10005	16.0	32.0	52.0	38.1	0	2.6	49.6	293.9	7.8	V
...	...	...	...	...	...	...	...	...	...	...	...	...
2802	2803	9994	19.0	62.0	19.0	9.1	0	1.2	44.5	131.8	9.7	V
2803	2804	9995	16.0	41.0	42.0	13.4	0	1.4	33.0	184.4	7.2	V
2804	2805	9996	13.0	29.0	58.0	8.7	3	1.3	104.9	425.4	7.7	V
2805	2806	9997	20.0	38.0	42.0	30.6	0	3.0	56.1	107.8	12.6	V
2806	2807	9998	11.0	56.0	34.0	5.9	0	0.7	39.7	172.1	3.8	V

```
# plot soc histogram
plt.figure(figsize=(10, 6))
plt.hist(target, bins=30, edgecolor='k', alpha=0.7)
plt.title('SOC histogram')
plt.xlabel('Value')
plt.ylabel('Count')
plt.grid(True)
plt.show()
```



```
# plot soc histogram
plt.figure(figsize=(10, 6))
plt.hist(target, bins=30, edgecolor='k', alpha=0.7)
plt.title('SOC histogram')
plt.xlabel('Value')
plt.ylabel('Count')
plt.ylim((0,10))
plt.grid(True)
plt.show()
```



## 3.2 Sampling and Splitting

```
# Extract features and target as numpy array
X = data.values
y = target.values
```

```
### Sampling strategies
```

```
# Step 1: Generate or Load Data
```

```
np.random.seed(100) # Set seed for reproducibility
```

```
# Step 2: Random Split (70% Calibration, 30% Test)
```

```
X_train_random, X_test_random, y_train_random, y_test_random = train_test_split(X, y, test
```

```
print(f"Random Split: {X_train_random.shape[0]} training samples, {X_test_random.shape[0]}")
```

```
# Step 3: Apply Kennard-Stone to select 70% of the data
```

```
n_train = int(0.7 * X.shape[0])
```

```

# Get indices
ks_indices = own_functions.kennard_stone(X, n_train)

# Select Training data
X_train_ks = X[ks_indices,:]
y_train_ks = y[ks_indices]

# Select Test
test_indices = np.setdiff1d(np.arange(X.shape[0]), ks_indices)
X_test_ks = X[test_indices]
y_test_ks = y[test_indices]

print(f"Kennard-Stone: {X_train_ks.shape[0]} training samples, {X_test_ks.shape[0]} test samples")

# Step 4: PCA for Visualization
pca = PCA(n_components=2)

# Fit PCA on full data
X_pca = pca.fit_transform(X)

# Transform data
X_train_random_pca = pca.transform(X_train_random) # PCA on random calibration set
X_test_random_pca = pca.transform(X_test_random) # PCA on random test set
X_cal_ks_pca = pca.transform(X_train_ks) # PCA on Kennard-Stone calibration set
X_test_ks_pca = pca.transform(X_test_ks) # PCA on Kennard-Stone test set

```

Random Split: 1964 training samples, 843 test samples  
Kennard-Stone: 1964 training samples, 843 test samples

```

#TODO: Show that both test and train are representative of the full dataset

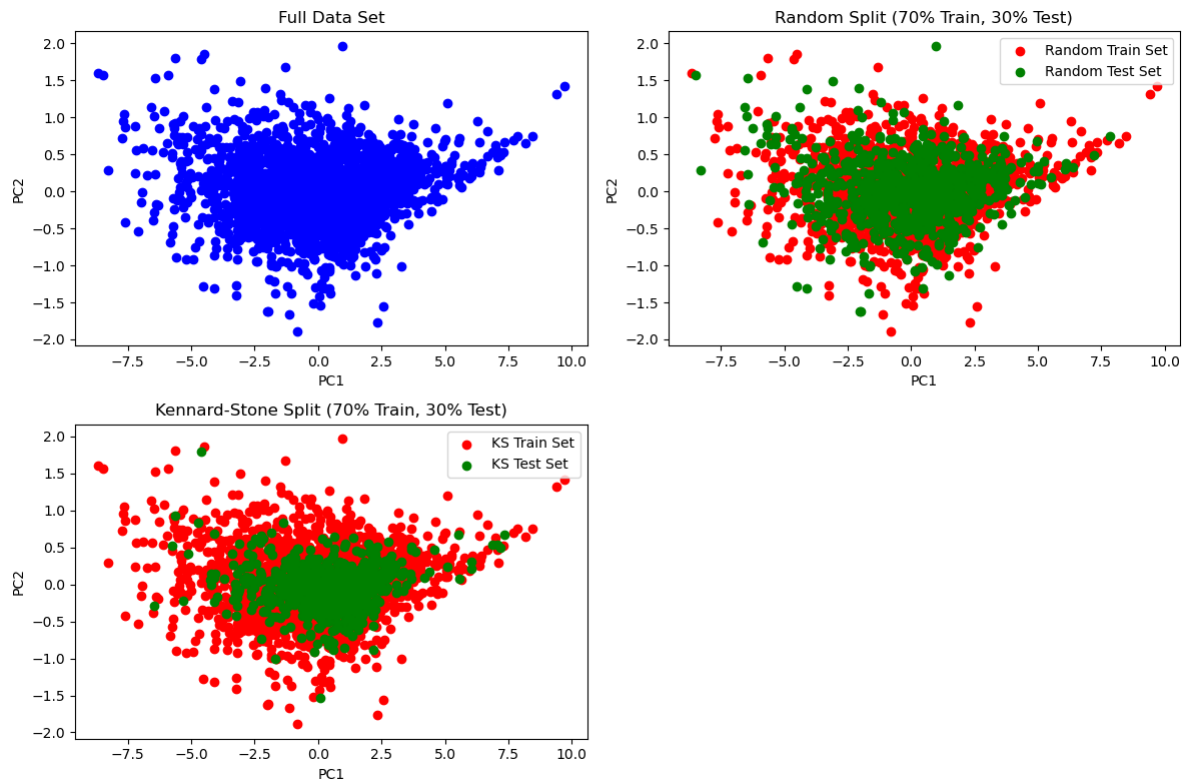
# Step 5: Plot Results
own_functions.plot_pca_comparison(X_full=X,
                                  X_train_random=X_train_random,
                                  X_test_random=X_test_random,
                                  X_train_ks=X_train_ks,
                                  X_test_ks=X_test_ks)

```

Random Split:

Train set shape: (1964, 1000)  
Test set shape: (843, 1000)

Kennard-Stone Split:  
Train set shape: (1964, 1000)  
Test set shape: (843, 1000)



```
X_train = X_train_ks  
y_train = y_train_ks  
  
X_test = X_test_ks  
y_test = y_test_ks
```

## 4 Basemodel

Baseline model (5 P): - Develop a global baseline PLSR model using the *calibration dataset* - (entire VNIR range from 500 nm to 2499 nm in steps of 2 nm) - *without* applying any *spectral preprocessing*. - The target variable is soil organic carbon (SOC). - Perform *internal optimization* to *determine* the *optimal number of latent PLS variables* - *report your selected value*. - Apply the optimized model\* to the independent test set. - *Compute the validation metrics* ( $R^2$ , RMSE, bias, and RPD) - *visualize\** the results in a *scatter plot* (observed vs. predicted values) - and assess the model's performance.

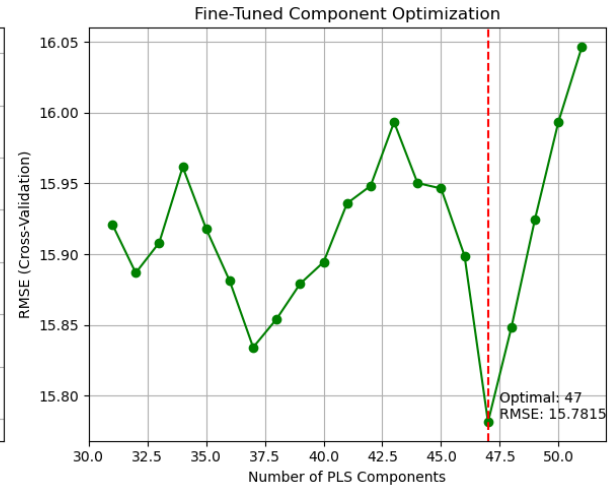
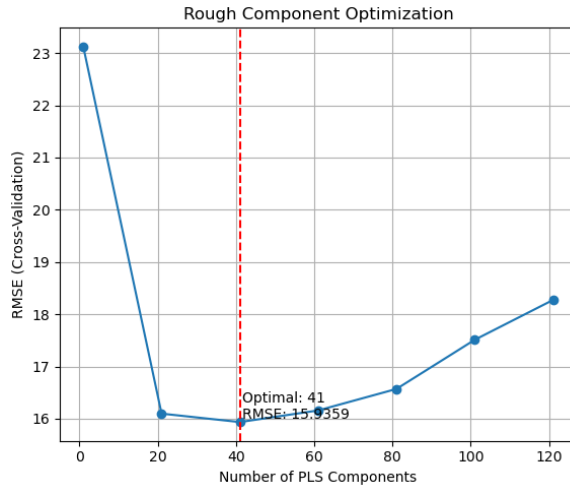
### 4.1 Finding optimal number of components

```
import own_functions

plsr_base_components = own_functions.optimize_pls_components(X_train=X_train,
                                                            y_train=y_train,
                                                            max_components=140,
                                                            step=20,
                                                            fine_tune=True,
                                                            show_progress=True,
                                                            plot_results=True
                                                            )
```

Rough Optimization: 0%| | 0/7 [00:00<?, ?it/s]

Fine Tuning: 0%| | 0/21 [00:00<?, ?it/s]



## 4.2 Evaluating Base Model

```
plsr_base_model = PLSRegression(n_components=plsr_base_components["optimal_n"])
plsr_base_model.fit(X_train, y_train)

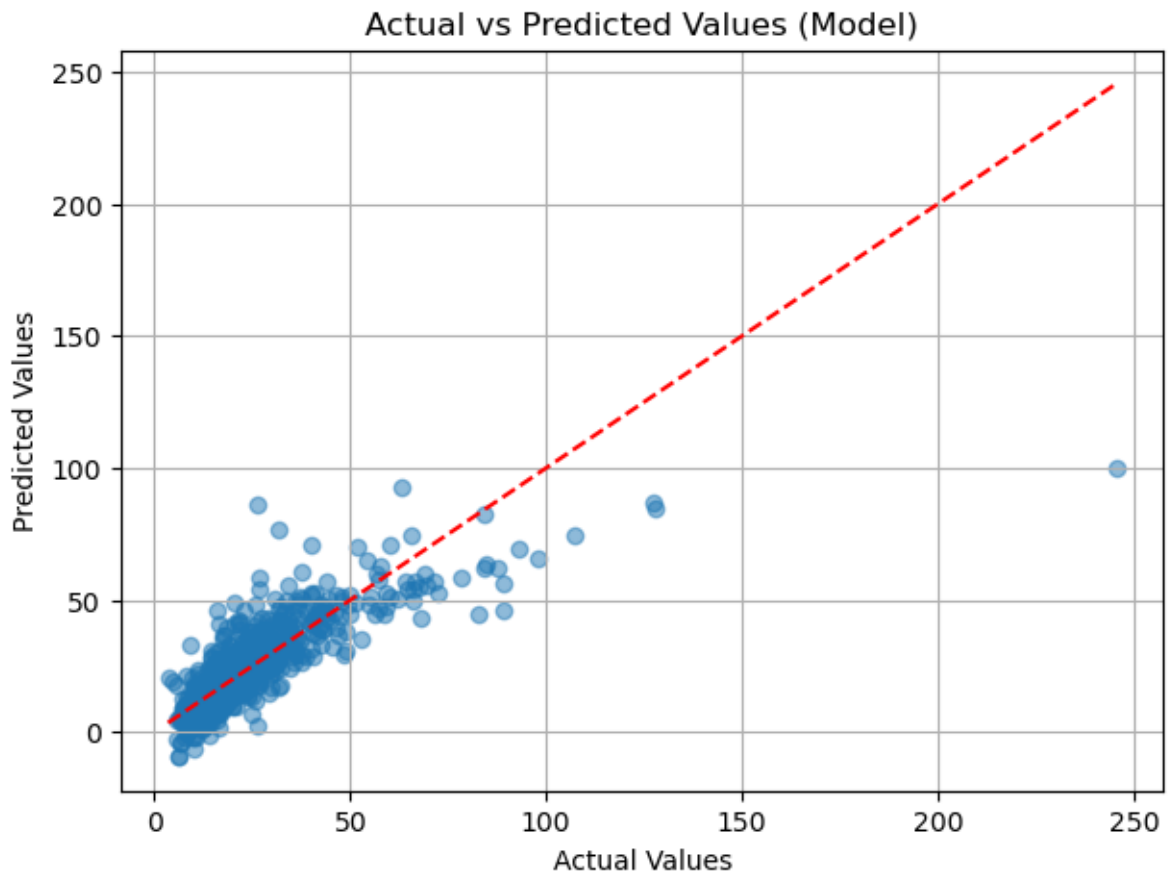
plsr_base_eval = own_functions.evaluate_model(plsr_base_model,
                                              X_test=X_test,
                                              y_test=y_test,
                                              print_metrics=True,
                                              show_plot=True
                                              )
```

Root Mean Squared Error (RMSE): 10.0547

$R^2$ : 0.6552

Bias: -0.1772

RPD: 1.7030





## 5 Model Improvement Strategies (5 P per strategy):

- Develop and evaluate three distinct strategies to improve the baseline model,
  - using the **same independent test set for validation**.
- For each strategy, report the validation metrics
  - ( $R^2$ , RMSE, bias, and RPD),
  - visualize the best result in a scatter plot (observed vs. predicted values)
  - assess the performance of these alternative models.
  - Use the same independent test set for all strategies to ensure that validation metrics are directly comparable.

IMPORTANT: Testing two or more spectral preprocessing methods is considered one strategy, not multiple strategies. Similarly, testing one or more alternative regression algorithms counts as one strategy, not multiple.

### 5.1 Varying Preprocessing Strategy

#### 5.1.1 Savitzky-Golay

```
#TODO: Is scaling necessary? - Does not seem to make a difference -> removed
```

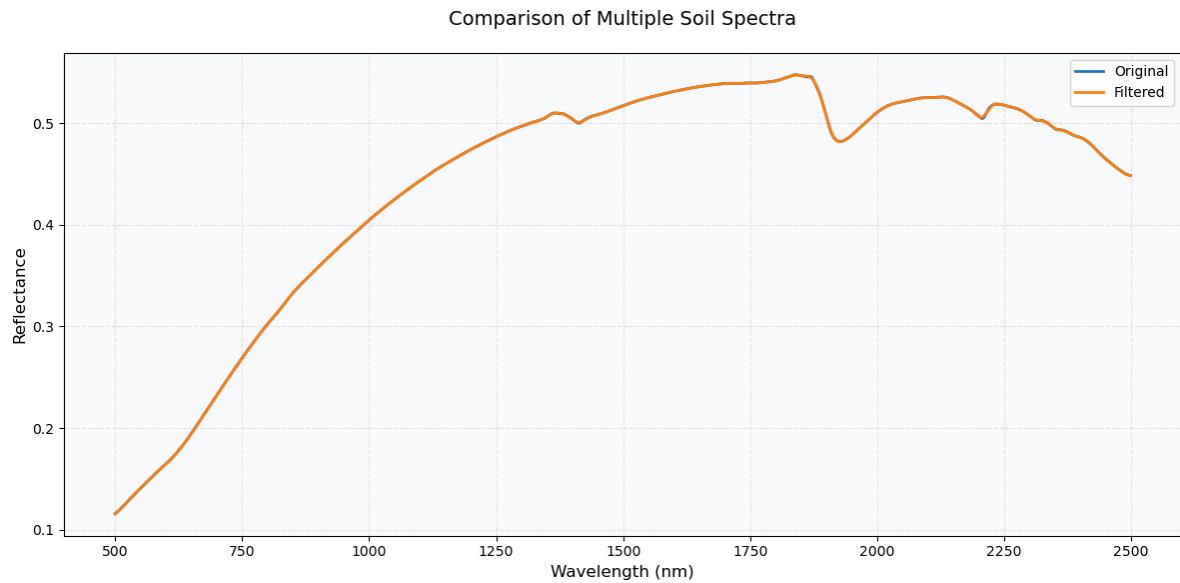
```
# Applying Savitzky-Golay filter to calibration and test data
```

```
X_train_sg = own_functions.apply_savitzky_golay(X_train, window_length=31, polyorder=4, de
```

```
X_test_sg = own_functions.apply_savitzky_golay(X_test, window_length=31, polyorder=4, deri
```

```
own_functions.plot_spectra_comparison(  
    X_train[2],  
    X_train_sg[2],  
    wavelengths=range(500, 2500, 2),  
    labels=['Original', 'Filtered'],  
    title='Comparison of Multiple Soil Spectra'
```

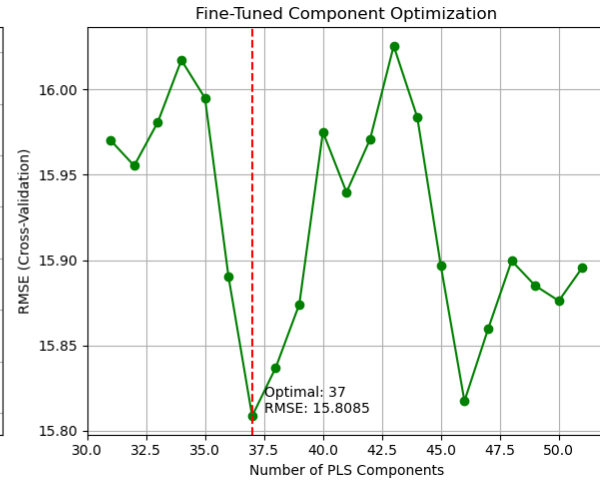
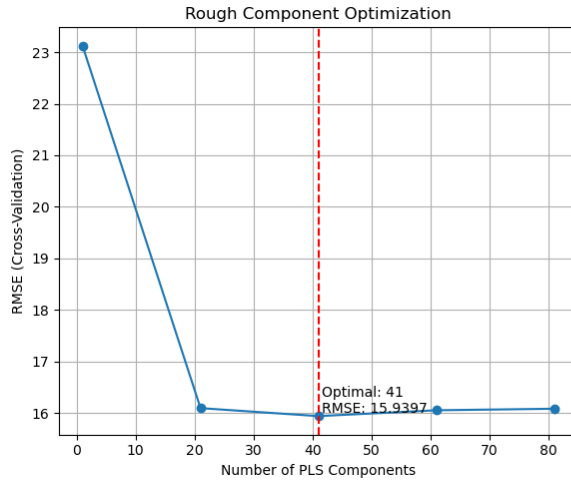
)



```
plsr_sgolay_components = own_functions.optimize_pls_components(X_train=X_train_sg,  
                                                                y_train=y_train,  
                                                                max_components=100,  
                                                                step=20,  
                                                                fine_tune=True,  
                                                                show_progress=True,  
                                                                plot_results=True  
                                                                )
```

Rough Optimization: 0%| | 0/5 [00:00<?, ?it/s]

Fine Tuning: 0%| | 0/21 [00:00<?, ?it/s]



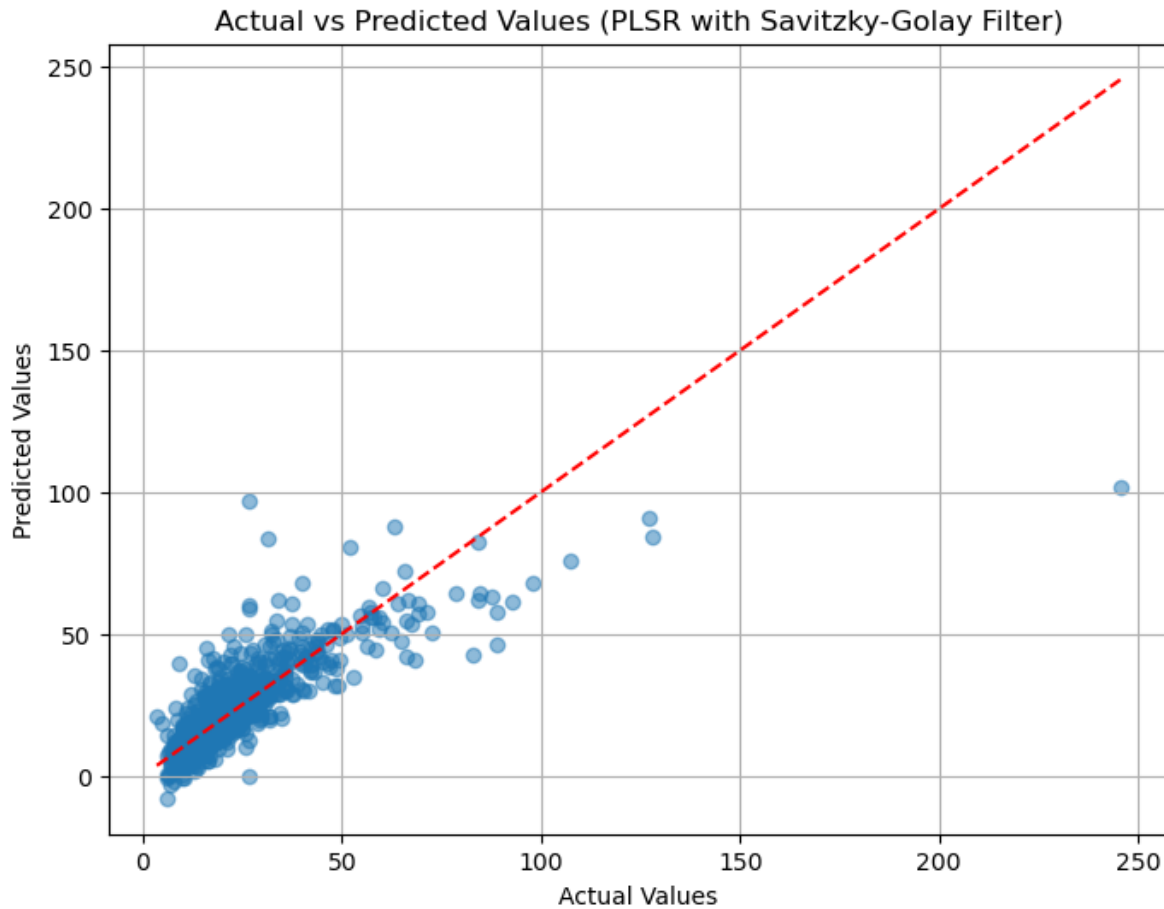
```

plsr_sg_model = PLSRegression(n_components=plsr_sgolay_components["optimal_n"])
plsr_sg_model.fit(X_train_sg, y_train)

plsr_sg_eval = own_functions.evaluate_model(plsr_sg_model,
                                            X_test=X_test_sg,
                                            y_test=y_test,
                                            print_metrics=True,
                                            show_plot=True,
                                            plot_kwargs={'model_name': 'PLSR with Savitzky-Golay Filter',
                                                         'figsize': (8, 6)}
                                            )

```

Root Mean Squared Error (RMSE): 10.1694  
 $R^2$ : 0.6473  
 Bias: -0.1207  
 RPD: 1.6838



### 5.1.2 Standard Normal Variate

```
import own_functions

# Applying Savitzky-Golay filter to calibration and test data
X_train_snv = own_functions.standard_normal_variate(X_train)
X_test_snv = own_functions.standard_normal_variate(X_test)

# Example usage with multiple spectra:
own_functions.plot_spectra_comparison(
    X_train[2],
    X_train_snv[2],
    wavelengths=range(500, 2500, 2),
```

```

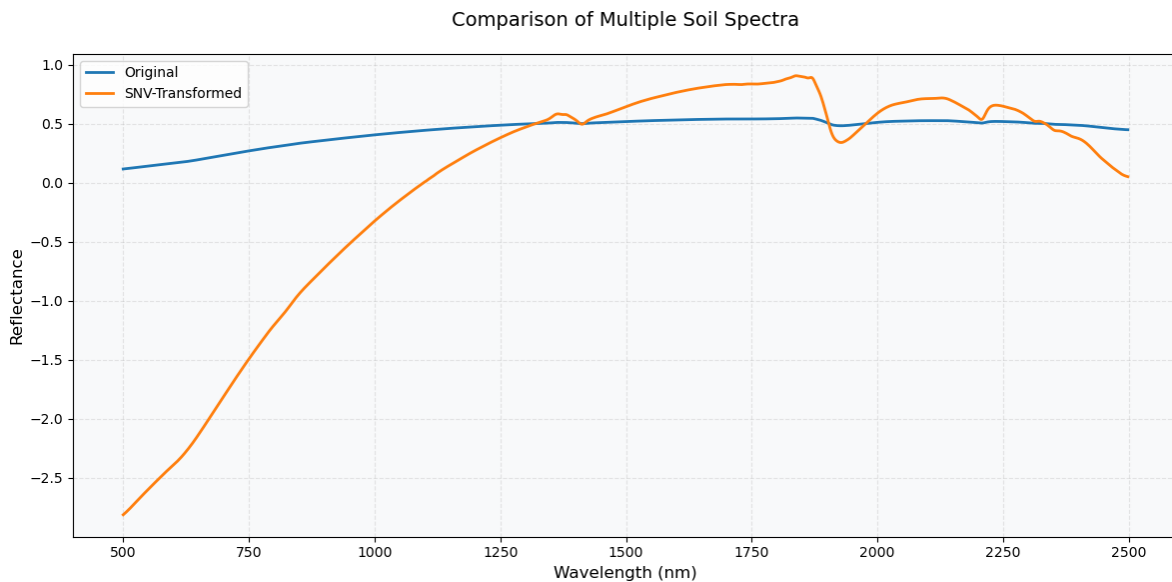
labels=['Original', 'SNV-Transformed'],
title='Comparison of Multiple Soil Spectra'
)

plsr_snv_components = own_functions.optimize_pls_components(X_train=X_train_snv,
                                                            y_train=y_train,
                                                            max_components=100,
                                                            step=20,
                                                            fine_tune=True,
                                                            show_progress=True,
                                                            plot_results=True
                                                            )

plsr_snv_model = PLSRegression(n_components=plsr_snv_components["optimal_n"])
plsr_snv_model.fit(X_train_snv, y_train)

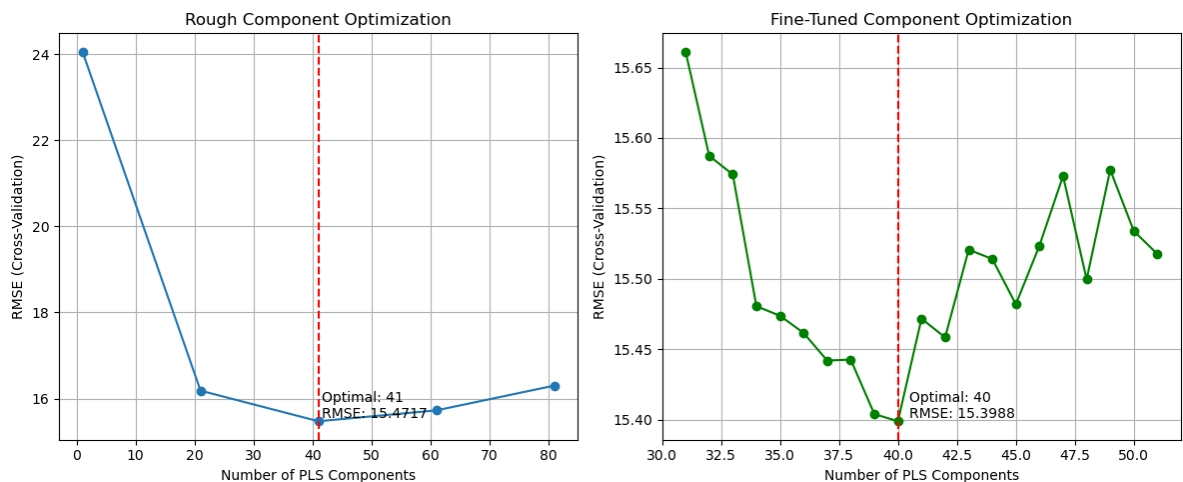
plsr_snv_eval = own_functions.evaluate_model(plsr_snv_model,
                                             X_test=X_test_snv,
                                             y_test=y_test,
                                             print_metrics=True,
                                             show_plot=True,
                                             plot_kwargs={'model_name': 'PLSR with SNV Preprocessing',
                                                           'figsize': (8, 6)}
                                             )

```



Rough Optimization: 0%| | 0/5 [00:00<?, ?it/s]

Fine Tuning: 0%| | 0/21 [00:00<?, ?it/s]

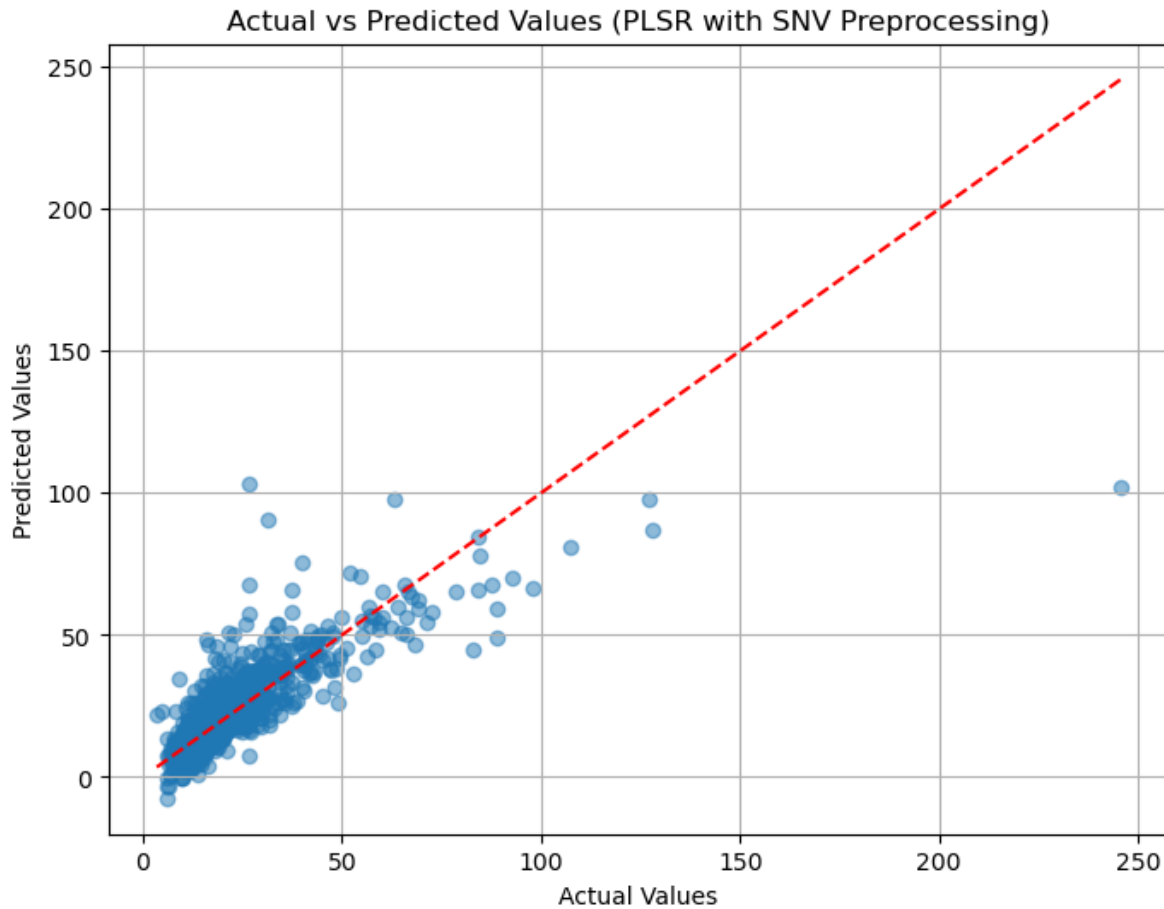


Root Mean Squared Error (RMSE): 10.1517

$R^2$ : 0.6485

Bias: 0.3009

RPD: 1.6867



### 5.1.3 Absorbance

```
# Calculate pseudo absorbance
X_train_absorb = np.log10(1/X_train)
X_test_absorb = np.log10(1/X_test)

# Plot Spectra
own_functions.plot_spectra_comparison(
    X_train[2],
    X_train_absorb[2],
    wavelengths=range(500, 2500, 2),
    labels=['Original', 'SNV-Transformed'],
    title='Comparison of Multiple Soil Spectra'
)
```

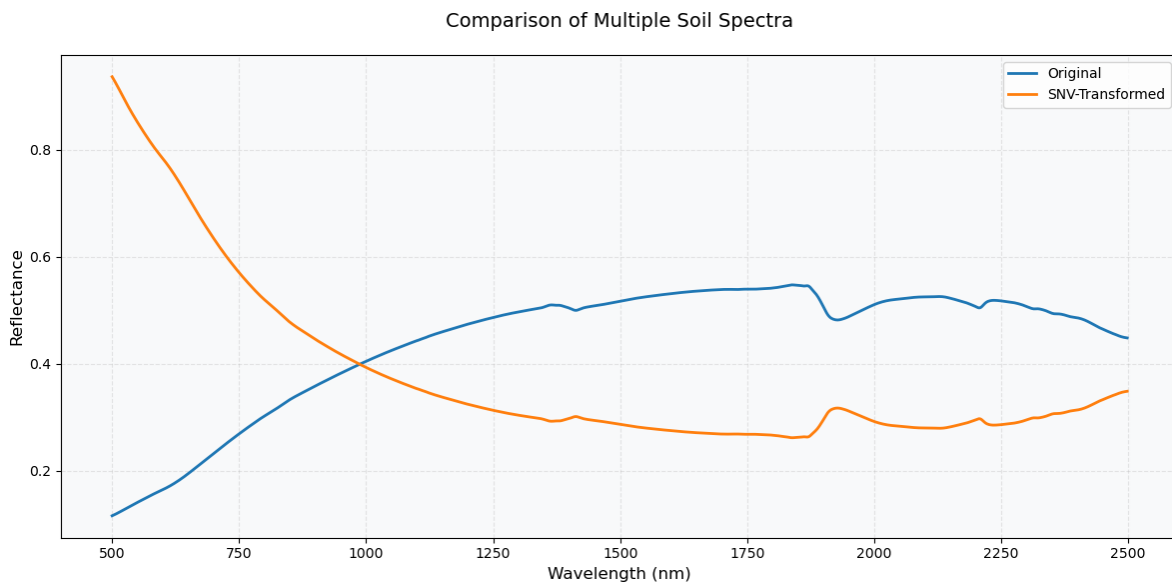
```

plsr_absorb_components = own_functions.optimize_pls_components(X_train=X_train_absorb,
                                                              y_train=y_train,
                                                              max_components=100,
                                                              step=20,
                                                              fine_tune=True,
                                                              show_progress=True,
                                                              plot_results=True
                                                              )

plsr_absorb_model = PLSRegression(n_components=plsr_absorb_components["optimal_n"])
plsr_absorb_model.fit(X_train_absorb, y_train)

plsr_absorb_eval = own_functions.evaluate_model(plsr_absorb_model,
                                                X_test=X_test_absorb,
                                                y_test=y_test,
                                                print_metrics=True,
                                                show_plot=True,
                                                plot_kwargs={'model_name': 'PLSR with abosrbances',
                                                                'figsize': (8, 6)}
                                                )

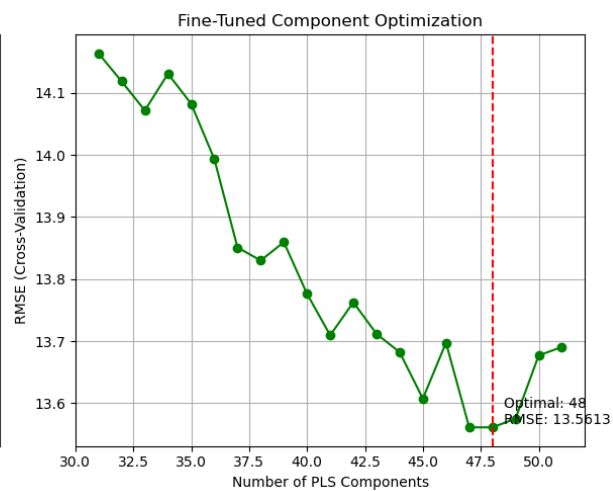
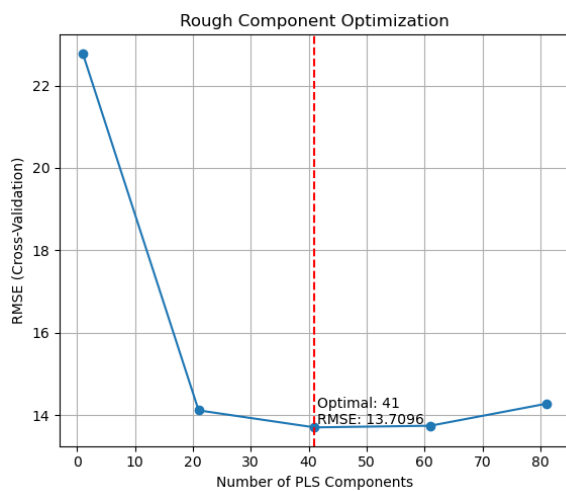
```



Rough Optimization: 0% | 0/5 [00:00<?, ?it/s]



Fine Tuning: 0% | 0/21 [00:00<?, ?it/s]

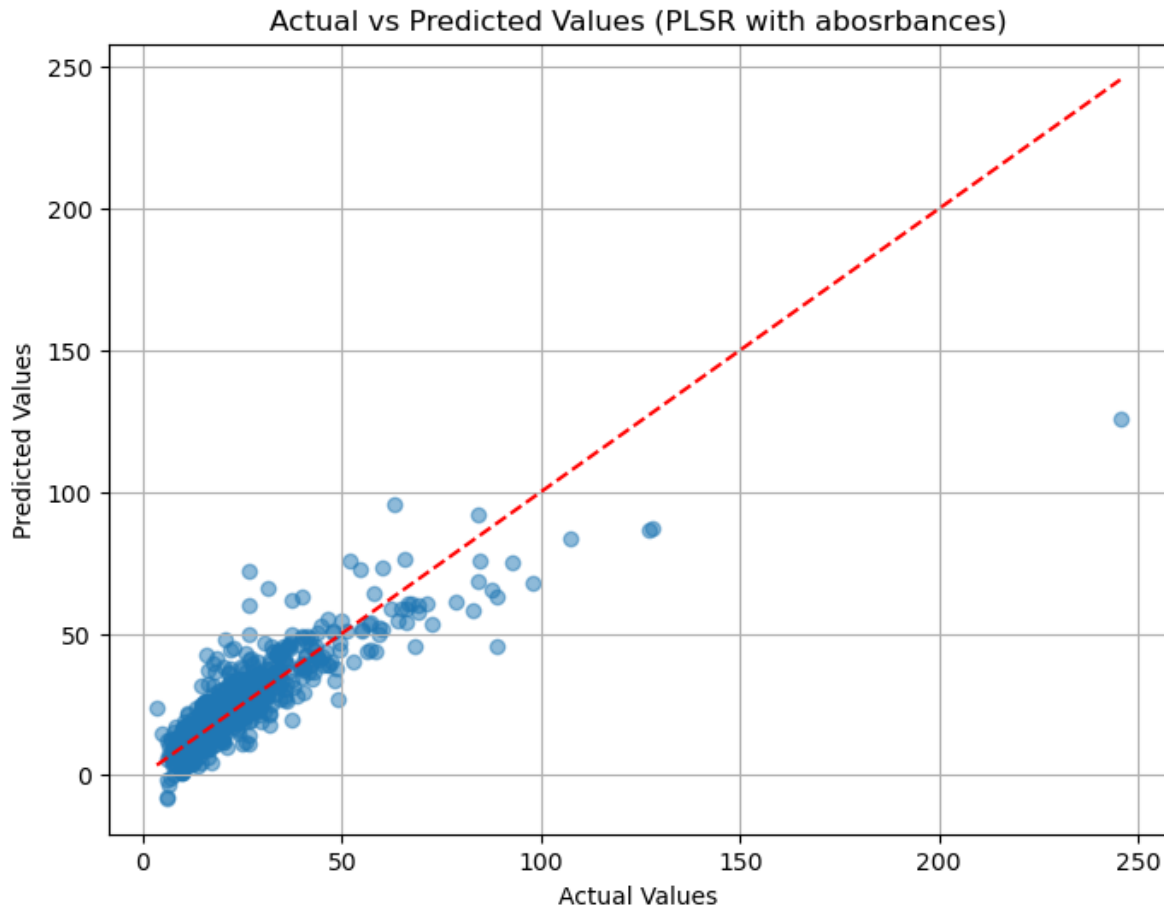


Root Mean Squared Error (RMSE): 8.6069

$R^2$ : 0.7474

Bias: 0.1506

RPD: 1.9895



## 5.2 Testing Different Models

Our next strategy is to test different models. We will test the following models: - LSTM -

### 5.2.1 Pytorch LSTM

```
import own_functions

# drop rate 0.2 best
# First split training data into train and validation sets
X_train_final, X_val, y_train_final, y_val = train_test_split(X_train_absorb, y_train,
                                                                test_size=0.2,
```

```
random_state=110)
```

```
# Training enhanced LSTM model
LSTM_base_model, history, metrics = own_functions.train_and_evaluate_lstm(
    X_train=X_train_final,
    X_val=X_val,
    X_test=X_test,
    y_train=y_train_final,
    y_val=y_val,
    y_test=y_test,
    hidden_size=256,
    num_layers=5,
    num_epochs=3000,
    learning_rate=0.001,
    patience=200, # Early stopping patience
    dropout=0.2,
)
```

```
# Evaluate LSTM model
_ = own_functions.evaluate_model(LSTM_base_model,
                                X_test=X_test_absorb, y_test=y_test,
                                print_metrics=True, show_plot=True)
```

```
Epoch [10/3000], Train Loss: 1323.3580, Val Loss: 2055.6138
Epoch [20/3000], Train Loss: 1073.8004, Val Loss: 1774.0663
Epoch [30/3000], Train Loss: 897.4761, Val Loss: 1591.5127
Epoch [40/3000], Train Loss: 804.3825, Val Loss: 1491.1821
Epoch [50/3000], Train Loss: 739.6238, Val Loss: 1418.3021
Epoch [60/3000], Train Loss: 691.6126, Val Loss: 1362.8917
Epoch [70/3000], Train Loss: 656.5456, Val Loss: 1321.1735
Epoch [80/3000], Train Loss: 631.4288, Val Loss: 1290.1431
Epoch [90/3000], Train Loss: 613.8032, Val Loss: 1267.3346
Epoch [100/3000], Train Loss: 601.7249, Val Loss: 1250.7620
Epoch [110/3000], Train Loss: 593.6379, Val Loss: 1238.8523
Epoch [120/3000], Train Loss: 588.3791, Val Loss: 1230.3783
Epoch [130/3000], Train Loss: 585.0749, Val Loss: 1224.3984
Epoch [140/3000], Train Loss: 583.0453, Val Loss: 1220.2046
Epoch [150/3000], Train Loss: 581.8547, Val Loss: 1217.2766
Epoch [160/3000], Train Loss: 581.1397, Val Loss: 1215.2374
Epoch [170/3000], Train Loss: 580.7720, Val Loss: 1213.8202
```

Epoch [180/3000], Train Loss: 580.5948, Val Loss: 1212.8375  
Epoch [190/3000], Train Loss: 580.4708, Val Loss: 1212.1587  
Epoch [200/3000], Train Loss: 580.4212, Val Loss: 1211.6929  
Epoch [210/3000], Train Loss: 580.3871, Val Loss: 1211.3760  
Epoch [220/3000], Train Loss: 580.3820, Val Loss: 1211.1633  
Epoch [230/3000], Train Loss: 580.3714, Val Loss: 1211.0229  
Epoch [240/3000], Train Loss: 580.3652, Val Loss: 1210.9321  
Epoch [250/3000], Train Loss: 580.3819, Val Loss: 1210.8749  
Epoch [260/3000], Train Loss: 580.3779, Val Loss: 1210.8401  
Epoch [270/3000], Train Loss: 580.3584, Val Loss: 1210.8195  
Epoch [280/3000], Train Loss: 580.3649, Val Loss: 1210.8080  
Epoch [290/3000], Train Loss: 580.3868, Val Loss: 1210.8020  
Epoch [300/3000], Train Loss: 580.3781, Val Loss: 1210.7992  
Epoch [310/3000], Train Loss: 580.3660, Val Loss: 1210.7980  
Epoch [320/3000], Train Loss: 580.3627, Val Loss: 1210.7976  
Epoch [330/3000], Train Loss: 580.3510, Val Loss: 1210.7976  
Epoch [340/3000], Train Loss: 580.3632, Val Loss: 1210.7977  
Epoch [350/3000], Train Loss: 580.3787, Val Loss: 1210.7981  
Epoch [360/3000], Train Loss: 580.3858, Val Loss: 1210.7982  
Epoch [370/3000], Train Loss: 580.3724, Val Loss: 1210.7983  
Epoch [380/3000], Train Loss: 580.3879, Val Loss: 1210.7983  
Epoch [390/3000], Train Loss: 580.3510, Val Loss: 1210.7983  
Epoch [400/3000], Train Loss: 580.3687, Val Loss: 1210.7983  
Epoch [410/3000], Train Loss: 580.3755, Val Loss: 1210.7983  
Epoch [420/3000], Train Loss: 580.3708, Val Loss: 1210.7982  
Epoch [430/3000], Train Loss: 580.3740, Val Loss: 1210.7983  
Epoch [440/3000], Train Loss: 580.3839, Val Loss: 1210.7985  
Epoch [450/3000], Train Loss: 580.3721, Val Loss: 1210.7986  
Epoch [460/3000], Train Loss: 580.3799, Val Loss: 1210.7988  
Epoch [470/3000], Train Loss: 580.3810, Val Loss: 1210.7986  
Epoch [480/3000], Train Loss: 580.3684, Val Loss: 1210.7986  
Epoch [490/3000], Train Loss: 580.3710, Val Loss: 1210.7985  
Epoch [500/3000], Train Loss: 580.3718, Val Loss: 1210.7985  
Epoch [510/3000], Train Loss: 580.3718, Val Loss: 1210.7985  
Epoch [520/3000], Train Loss: 580.3864, Val Loss: 1210.7986  
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Early stopping triggered at epoch 537

Final Test Metrics:

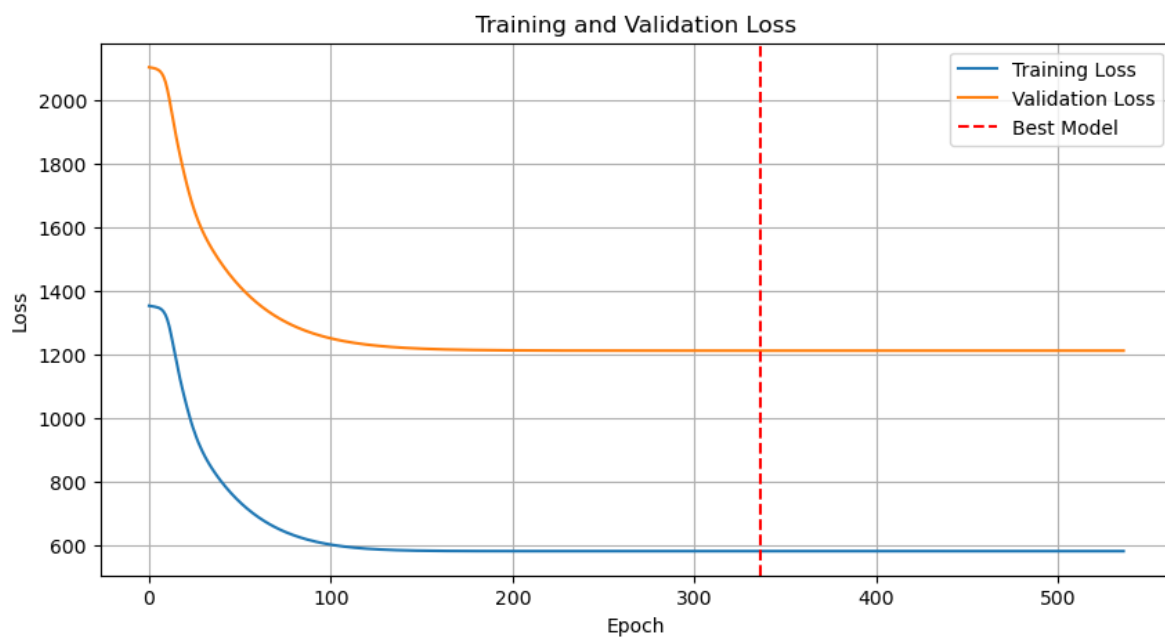
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rmse: 18.0296

r2: -0.1087

bias: 5.6444

rpd: 0.9497

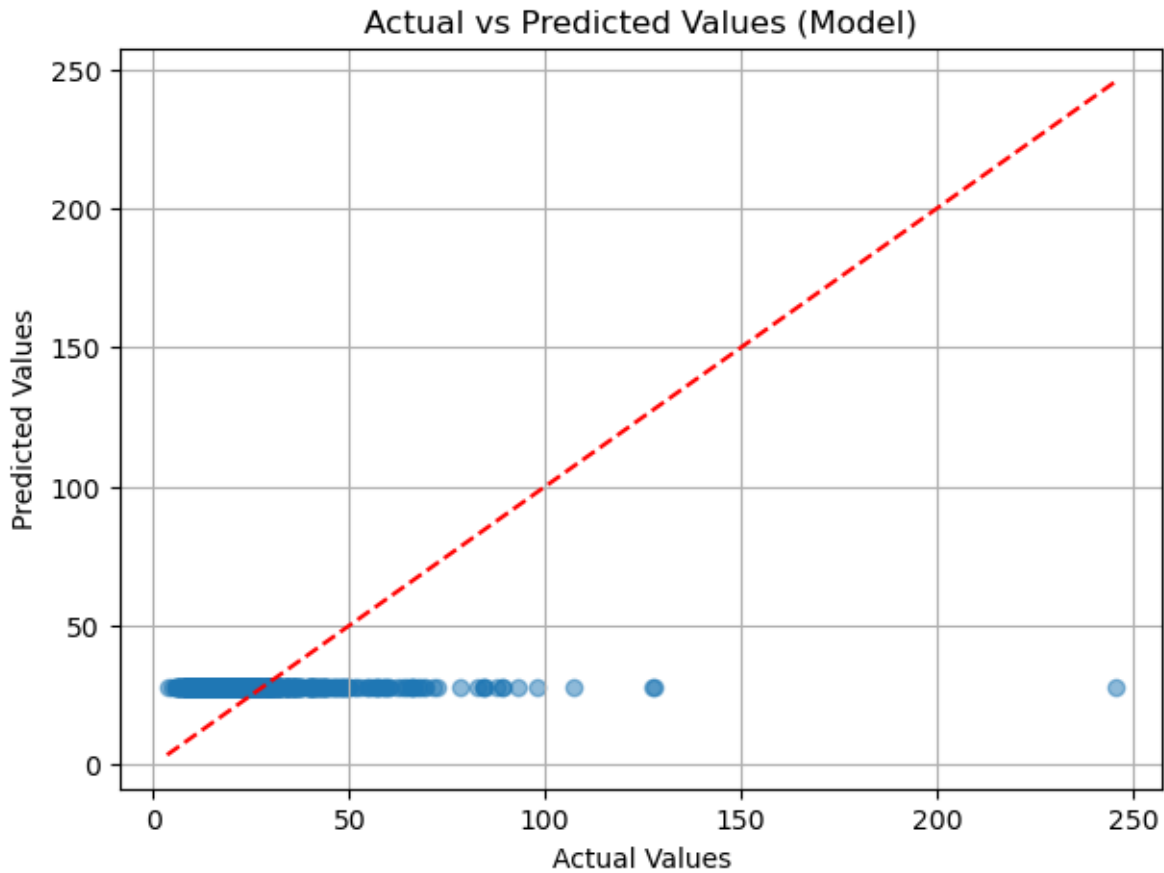


Root Mean Squared Error (RMSE): 18.0296

$R^2$ : -0.1087

Bias: 5.6444

RPD: 0.9497



### 5.2.2 LSTM with PLSR components

```
# Fit PLSR on the training data and transform the training set
X_train_pls = plsr_absorb_model.transform(X_train_absorb)

# Transform the test set using the fitted model (trained on the training set)
X_test_pls = plsr_absorb_model.transform(X_test_absorb)

# First split training data into train and validation sets
X_train_final, X_val, y_train_final, y_val = train_test_split(X_train_pls, y_train,
                                                                test_size=0.2,
                                                                random_state=42)

# Training enhanced LSTM model
```

```

LSTM_plsr_model, history, metrics = own_functions.train_and_evaluate_lstm(
    X_train=X_train_final,
    X_val=X_val,
    X_test=X_test_pls,
    y_train=y_train_final,
    y_val=y_val,
    y_test=y_test,
    hidden_size=256,
    num_layers=5,
    num_epochs=3000,
    learning_rate=0.001,
    patience=200, # Early stopping patience
    dropout=0.2
)

lstm_plsr_eval = own_functions.evaluate_model(LSTM_plsr_model,
                                              X_test=X_test_pls, y_test=y_test,
                                              print_metrics=True, show_plot=True)

```

```

Epoch [10/3000], Train Loss: 1476.9949, Val Loss: 1522.3971
Epoch [20/3000], Train Loss: 1298.9865, Val Loss: 1303.0087
Epoch [30/3000], Train Loss: 1055.8999, Val Loss: 1075.3479
Epoch [40/3000], Train Loss: 936.0597, Val Loss: 960.6909
Epoch [50/3000], Train Loss: 864.6968, Val Loss: 888.7760
Epoch [60/3000], Train Loss: 813.6223, Val Loss: 836.5993
Epoch [70/3000], Train Loss: 777.1158, Val Loss: 798.9126
Epoch [80/3000], Train Loss: 751.5482, Val Loss: 772.2037
Epoch [90/3000], Train Loss: 734.0804, Val Loss: 753.6362
Epoch [100/3000], Train Loss: 722.4227, Val Loss: 740.9803
Epoch [110/3000], Train Loss: 714.8896, Val Loss: 732.5262
Epoch [120/3000], Train Loss: 710.1119, Val Loss: 726.9906
Epoch [130/3000], Train Loss: 707.2158, Val Loss: 723.4321
Epoch [140/3000], Train Loss: 705.5001, Val Loss: 721.1772
Epoch [150/3000], Train Loss: 704.2849, Val Loss: 719.7388
Epoch [160/3000], Train Loss: 702.4864, Val Loss: 717.9755
Epoch [170/3000], Train Loss: 701.9086, Val Loss: 716.7893
Epoch [180/3000], Train Loss: 700.6622, Val Loss: 715.4919
Epoch [190/3000], Train Loss: 698.9515, Val Loss: 714.5274
Epoch [200/3000], Train Loss: 695.2794, Val Loss: 709.4814
Epoch [210/3000], Train Loss: 691.9188, Val Loss: 707.7747
Epoch [220/3000], Train Loss: 688.4955, Val Loss: 702.2612

```

Epoch [230/3000], Train Loss: 681.7617, Val Loss: 696.5450  
Epoch [240/3000], Train Loss: 660.8052, Val Loss: 670.4714  
Epoch [250/3000], Train Loss: 598.0337, Val Loss: 608.7620  
Epoch [260/3000], Train Loss: 578.2463, Val Loss: 587.5004  
Epoch [270/3000], Train Loss: 554.2938, Val Loss: 563.7514  
Epoch [280/3000], Train Loss: 534.7710, Val Loss: 544.4777  
Epoch [290/3000], Train Loss: 516.8218, Val Loss: 526.2027  
Epoch [300/3000], Train Loss: 501.3236, Val Loss: 509.9671  
Epoch [310/3000], Train Loss: 486.6131, Val Loss: 495.2682  
Epoch [320/3000], Train Loss: 473.3205, Val Loss: 481.4204  
Epoch [330/3000], Train Loss: 460.4038, Val Loss: 469.4686  
Epoch [340/3000], Train Loss: 449.8602, Val Loss: 459.4424  
Epoch [350/3000], Train Loss: 439.8952, Val Loss: 449.1520  
Epoch [360/3000], Train Loss: 430.5488, Val Loss: 440.9105  
Epoch [370/3000], Train Loss: 424.1036, Val Loss: 432.1590  
Epoch [380/3000], Train Loss: 414.9257, Val Loss: 424.5315  
Epoch [390/3000], Train Loss: 407.8018, Val Loss: 418.7832  
Epoch [400/3000], Train Loss: 402.1411, Val Loss: 410.3160  
Epoch [410/3000], Train Loss: 394.8529, Val Loss: 405.0167  
Epoch [420/3000], Train Loss: 388.8846, Val Loss: 398.1512  
Epoch [430/3000], Train Loss: 384.2500, Val Loss: 394.7275  
Epoch [440/3000], Train Loss: 378.3047, Val Loss: 386.6680  
Epoch [450/3000], Train Loss: 371.8717, Val Loss: 381.3099  
Epoch [460/3000], Train Loss: 367.6703, Val Loss: 377.8934  
Epoch [470/3000], Train Loss: 363.1318, Val Loss: 371.2940  
Epoch [480/3000], Train Loss: 358.1399, Val Loss: 365.4178  
Epoch [490/3000], Train Loss: 355.3999, Val Loss: 362.7246  
Epoch [500/3000], Train Loss: 351.4532, Val Loss: 356.0226  
Epoch [510/3000], Train Loss: 347.9709, Val Loss: 354.5867  
Epoch [520/3000], Train Loss: 342.6750, Val Loss: 349.2525  
Epoch [530/3000], Train Loss: 339.2817, Val Loss: 344.0117  
Epoch [540/3000], Train Loss: 336.5583, Val Loss: 341.4745  
Epoch [550/3000], Train Loss: 334.2585, Val Loss: 336.6165  
Epoch [560/3000], Train Loss: 330.9122, Val Loss: 333.5845  
Epoch [570/3000], Train Loss: 327.8176, Val Loss: 330.5784  
Epoch [580/3000], Train Loss: 323.5317, Val Loss: 326.8005  
Epoch [590/3000], Train Loss: 321.0453, Val Loss: 329.3196  
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Epoch [650/3000], Train Loss: 305.7915, Val Loss: 317.6821



Epoch [660/3000], Train Loss: 300.9412, Val Loss: 318.9722  
Epoch [670/3000], Train Loss: 299.0072, Val Loss: 315.4145  
Epoch [680/3000], Train Loss: 297.4985, Val Loss: 309.6865  
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Epoch [700/3000], Train Loss: 293.6654, Val Loss: 299.8304  
Epoch [710/3000], Train Loss: 289.3485, Val Loss: 303.7017  
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Epoch [730/3000], Train Loss: 285.0848, Val Loss: 300.4618  
Epoch [740/3000], Train Loss: 282.4811, Val Loss: 297.2863  
Epoch [750/3000], Train Loss: 281.5024, Val Loss: 298.2256  
Epoch [760/3000], Train Loss: 278.1667, Val Loss: 296.1386  
Epoch [770/3000], Train Loss: 276.5258, Val Loss: 290.8620  
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Epoch [1610/3000], Train Loss: 148.7325, Val Loss: 191.7266  
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Epoch [1670/3000], Train Loss: 142.2986, Val Loss: 193.4411  
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Epoch [1820/3000], Train Loss: 129.6214, Val Loss: 195.6850  
Epoch [1830/3000], Train Loss: 129.0399, Val Loss: 197.5882  
Epoch [1840/3000], Train Loss: 128.0919, Val Loss: 195.5797  
Epoch [1850/3000], Train Loss: 127.4352, Val Loss: 203.0794  
Epoch [1860/3000], Train Loss: 126.4132, Val Loss: 194.0215  
Epoch [1870/3000], Train Loss: 125.5426, Val Loss: 197.1165  
Epoch [1880/3000], Train Loss: 124.8665, Val Loss: 197.0638  
Epoch [1890/3000], Train Loss: 125.1311, Val Loss: 194.8841  
Epoch [1900/3000], Train Loss: 123.3983, Val Loss: 191.0178  
Epoch [1910/3000], Train Loss: 122.7461, Val Loss: 190.8943  
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Early stopping triggered at epoch 1929

Final Test Metrics:

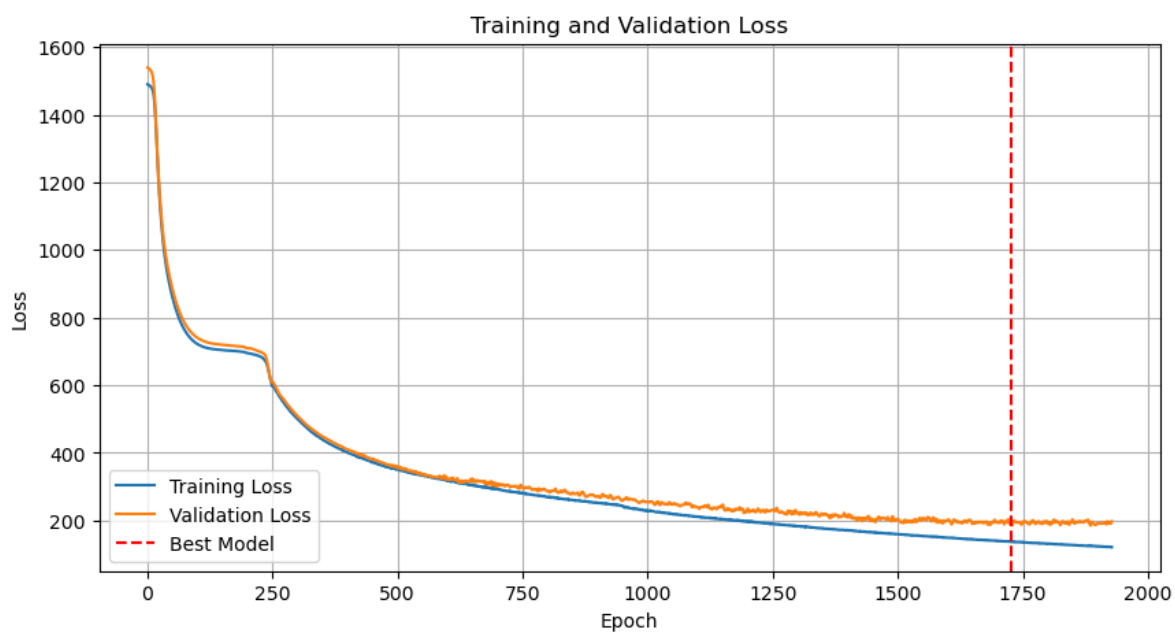
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rmse: 6.2590

r2: 0.8664

bias: -0.4263

rpd: 2.7358

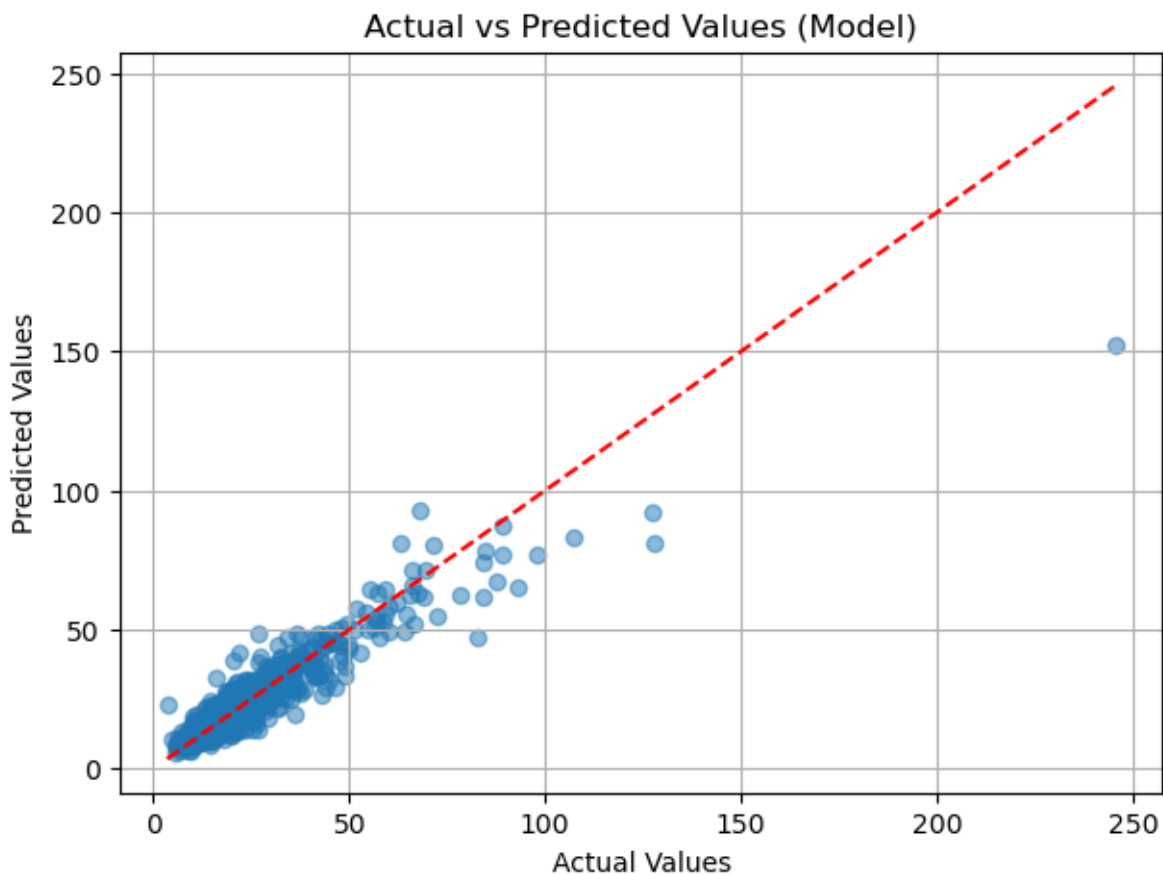


Root Mean Squared Error (RMSE): 6.2590

$R^2$ : 0.8664

Bias: -0.4263

RPD: 2.7358



```
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 42.557728 , 71.08807 , 11.561662 , 14.070908 , 11.60595 ,  
 25.278719 , 34.58436 , 55.678577 , 18.055357 , 29.36125 ,  
 15.464841 , 21.306545 , 32.019 , 37.875145 , 26.188683 ,  
 16.820736 , 19.33336 , 15.115097 , 22.25376 , 15.745544 ,  
 23.427172 , 19.380209 , 14.033683 , 22.273777 , 34.195057 ,  
 18.268261 , 23.87647 , 66.10261 , 8.18068 , 22.135567 ,  
 35.70045 , 34.375103 , 22.009825 , 10.3081255, 64.56007 ,  
 11.582939 , 33.773964 , 27.376707 , 22.735174 , 32.311417 ,  
 18.406734 , 11.532261 , 9.946317 , 21.073862 , 7.352037 ,

9.92745 , 11.493267 , 12.870199 , 14.933127 , 32.01177 ,  
 45.283333 , 73.98525 , 38.42441 , 12.110559 , 49.059174 ,  
 81.09719 , 83.09725 , 11.515052 , 10.613716 , 9.425875 ,  
 15.053785 , 11.198204 , 14.109471 , 16.43013 , 13.268848 ,  
 14.880234 , 11.496066 , 12.539433 , 10.828272 , 11.364031 ,  
 22.299456 , 57.5303 , 24.294947 , 30.799166 , 24.453077 ,  
 36.401577 , 33.175556 , 17.038424 , 54.710865 , 13.620868 ,  
 13.344478 , 10.450514 , 16.484327 , 12.338276 , 12.501667 ,  
 11.411373 , 10.65053 , 10.23892 , 13.390879 , 13.287432 ,  
 78.31412 , 52.026382 , 25.679058 , 20.801281 , 24.685266 ,  
 19.60126 , 15.513273 , 10.469099 , 29.268675 , 24.840525 ,  
 12.52013 , 13.321831 , 15.013981 , 12.054942 , 15.535204 ,  
 67.592415 , 30.433876 , 9.97851 , 10.85454 , 12.518485 ,  
 29.264061 , 18.526619 , 10.472612 , 21.11899 , 9.604242 ,  
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 21.561155 , 28.850647 , 20.65027 , 13.382404 , 34.131584 ,  
 32.803577 , 13.780179 , 21.297504 , 29.361448 , 10.924696 ,  
 24.954939 , 13.089909 , 11.966734 , 21.530884 , 18.162638 ,  
 17.628157 , 14.240722 , 13.82554 , 76.70651 , 20.598488 ,  
 21.106672 , 23.789173 , 14.234191 , 16.17023 , 13.023797 ,  
 21.559175 , 23.04782 , 25.382774 , 23.426039 , 26.01671 ,  
 25.898333 , 19.936064 , 42.268925 , 16.215971 , 22.49438 ,  
 28.955221 , 15.256432 , 11.647049 , 33.23688 , 30.278831 ,  
 19.921213 , 25.314432 , 23.099176 , 14.569479 , 20.45313 ,  
 23.968582 , 30.724693 , 37.12682 , 17.888708 , 27.445473 ,  
 31.41481 , 28.32174 , 20.045897 , 21.893892 , 31.875418 ,  
 30.181309 , 9.173586 , 14.383961 , 12.933123 , 12.062146 ,  
 8.49432 , 13.265076 , 15.042267 , 14.023979 , 12.988524 ,  
 11.633797 , 14.353547 , 13.184746 , 12.244453 , 11.846791 ,  
 8.773142 , 10.889131 , 15.910397 , 12.316376 , 11.074291 ,  
 14.244022 , 10.340889 , 10.828012 , 11.9963455 , 11.042196 ,  
 12.527097 , 11.771417 , 13.962059 , 12.521383 , 10.128203 ,  
 14.295046 , 16.339293 , 15.980588 , 14.465033 , 14.183508 ,  
 10.731536 , 13.665385 , 10.060436 , 15.951105 , 11.781576 ,  
 14.601776 , 15.322576 , 12.151108 , 14.645617 , 17.314589 ,  
 16.120483 , 12.621321 , 13.469178 , 12.316679 , 13.308516 ,  
 11.669124 , 20.7637 , 19.29775 , 44.364613 , 17.892675 ,  
 31.329645 , 14.989101 , 27.39985 , 36.21284 , 50.515804 ,  
 48.512833 , 80.331604 , 31.363312 , 23.124382 , 39.800762 ,  
 46.979366 , 40.606724 , 11.189964 , 46.88944 , 13.47703 ,  
 13.881943 , 27.77301 , 62.65966 , 31.963083 , 24.469461 ,  
 47.455463 , 25.022343 , 18.459959 , 25.76804 , 20.784414 ,  
 21.212088 , 10.94429 , 13.6669855 , 13.091532 , 13.261982 ,

15.874415 , 19.665571 , 26.65234 , 23.44771 , 16.414022 ,  
 14.419901 , 22.863268 , 13.897646 , 41.792107 , 38.90065 ,  
 45.915737 , 49.371555 , 31.315296 , 12.263399 , 30.963991 ,  
 62.731266 , 91.94937 , 28.759546 , 49.877666 , 12.539829 ,  
 37.474133 , 31.584576 , 38.961147 , 43.7233 , 29.491695 ,  
 11.212091 , 10.949663 , 16.365812 , 33.53551 , 11.266697 ,  
 14.327033 , 13.410329 , 16.326382 , 28.509527 , 16.585867 ,  
 20.788076 , 10.168418 , 24.822367 , 24.971884 , 22.246784 ,  
 28.665592 , 30.169128 , 28.447351 , 20.21415 , 26.229086 ,  
 14.376749 , 15.402897 , 16.336533 , 23.407915 , 22.655249 ,  
 63.2682 , 17.057951 , 27.14274 , 22.407038 , 21.540663 ,  
 17.228092 , 31.131224 , 10.427744 , 23.655306 , 30.84339 ,  
 29.72337 , 11.57591 , 12.629789 , 23.162363 , 152.12224 ,  
 17.37777 , 49.686085 , 38.217213 , 6.200782 , 17.491488 ,  
 16.955462 , 12.221439 , 76.69378 , 48.732212 , 21.174788 ,  
 16.974009 , 21.722109 , 13.397806 , 30.00752 , 21.883944 ,  
 23.188337 , 21.771322 , 26.45743 , 11.8614 , 13.528744 ,  
 12.325241 , 10.60121 , 17.709867 , 12.492927 , 56.40955 ,  
 18.475695 , 24.155245 , 15.563114 , 45.0291 , 30.906923 ,  
 50.523193 , 32.456066 , 18.669321 , 17.98613 , 18.244167 ,  
 40.597675 , 25.390787 , 43.51433 , 8.770008 , 15.551195 ,  
 26.492525 , 12.731497 , 19.182997 , 19.398142 , 12.086107 ,  
 13.844336 , 19.543814 , 19.663733 , 15.902086 , 32.211285 ,  
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 12.690422 , 12.499697 , 12.940079 , 8.934736 , 25.006073 ,  
 13.402452 , 20.573765 , 10.877329 , 8.093711 , 46.59967 ,  
 31.864634 , 40.02611 , 92.66779 , 55.76471 , 29.547998 ,  
 28.353556 , 13.127747 , 12.657144 , 13.203468 , 11.9830475 ,  
 13.63901 , 18.361464 , 10.321588 , 21.434431 , 11.251289 ,  
 11.940774 , 7.772327 , 15.981235 , 52.98866 , 28.60234 ,  
 31.327269 , 31.533604 , 21.875006 , 33.89951 , 28.973486 ,  
 39.061123 , 38.50964 , 28.725042 , 17.768194 , 23.66232 ,  
 19.722464 , 41.921757 , 13.648109 , 14.257262 , 21.89126 ,  
 28.267046 , 19.048292 , 62.88085 , 26.106714 , 19.2394 ,  
 43.560993 , 33.579353 , 29.373468 , 38.420246 , 32.79838 ,  
 44.19013 , 26.640135 , 22.966896 , 9.720984 , 29.09915 ,  
 17.466688 , 23.847116 , 10.286739 , 20.243505 , 20.899103 ,  
 17.164846 , 16.400167 , 16.076075 , 43.09666 , 18.647457 ,  
 24.760546 , 16.414967 , 10.573597 , 64.85003 , 32.896515 ,  
 36.177402 , 26.318235 , 36.60629 , 23.404049 , 20.402998 ,  
 47.446392 , 17.466173 , 23.769876 , 27.580992 , 21.75085 ,



```

19.234144 ,    8.928478 ,   17.079042 ,   12.365701 ,   15.504739 ,
13.988066 ,   10.963501 ,   13.514893 ,   13.434107 ,   15.218806 ,
24.524042 ,   11.149149 ,   19.497814 ,    9.400767 ,   13.035424 ,
12.362514 ,   10.787676 ,   11.530916 ,   13.42346 ,   15.611746 ,
16.465837 ,   12.452387 ,   12.5047035,    9.955307 ,   10.32907 ,
11.770672 ,    9.714632 ,    8.639699 ,   11.256895 ,   12.542776 ,
29.973228 ,   10.900404 ,   10.462853 ,   15.404116 ,   11.440291 ,
30.112501 ,   33.4202 ,    32.812374 ,   14.718645 ,   18.706034 ,
37.01601 ,   24.778025 ,   15.86528 ,   10.593363 ,    9.654915 ,
10.702266 ,   13.184469 ,   11.963707 ,    8.914192 ,   10.309573 ,
13.888376 ,   11.595388 ,   13.254608 ,   10.734537 ,   12.481808 ,
10.862255 ,   13.951749 ,    9.38986 ,   14.535303 ,   22.987494 ,
13.209288 ,   11.008216 ,   17.189978 ,   13.156677 ,    9.673297 ,
 9.575037 ,   11.499191 ,   20.667397 ,   10.748065 ,   11.618143 ,
11.314845 ,    9.421642 ,   11.200173 ,   15.538531 ,   13.054743 ,
11.124045 ,   27.843306 ,   19.899363 ,   13.265014 ,   13.903096 ,
22.426582 ,   12.584957 ,   31.101923 ,   15.389742 ,   17.344656 ,
11.272923 ,    6.3225145,   21.726652 ,   26.79259 ,   43.22578 ,
13.940535 ,   35.361294 ,   20.470942 ,   37.4109 ,   13.69034 ,
62.067455 ,   10.295662 ,   14.320028 ,    6.2013874,    9.615353 ,
10.193489 ,   12.932112 ,    9.54437 ,   13.768511 ,   31.721369 ,
13.790487 ,   30.009695 ,   38.537945 ,   81.00288 ,    9.594304 ,
14.1083355,   24.776472 ,   17.041985 ,   14.905752 ,   16.416456 ,
 9.9295635,   25.22701 ,    8.273629 ], dtype=float32),
'rmse': 6.259019974514894,
'r2': 0.8663901085255814,
'bias': -0.4263318489454818,
'rpdc': 2.735777001992952}

```

### 5.2.3 Plsr + AutoML

```

# Convert numpy arrays to DataFrame with wavelength columns
wavelengths = range(500, 2500, 2) # Your wavelength range
train_df = pd.DataFrame(X_train_pls, columns=range(1, X_train_pls.shape[1] + 1))
test_df = pd.DataFrame(X_test_pls, columns=range(1, X_train_pls.shape[1] + 1))

# Add target variable
train_df['SOC'] = y_train
test_df['SOC'] = y_test

```

```

# More advanced configuration with safety measures
auto_predictor = TabularPredictor(
    label='SOC',
    problem_type="regression",
    eval_metric='root_mean_squared_error',
).fit(
    train_df,
    presets='best_quality',
    num_gpus=0,
    num_cpus=1,
    memory_limit='auto',
    auto_stack=False,
    verbosity=2
)

print(f"predictor path is {auto_predictor.path}")
# Show leaderboard
print("\nModel Leaderboard:")
print(auto_predictor.leaderboard(test_df))

```

predictor path is c:\Users\luis\_\Desktop\Alles\Uni\Leipzig\WS\_24\_25\spectroscopy\final\_proje

Model Leaderboard:

	model	score_test	score_val	eval_metric \
0	NeuralNetFastAI_r191	-6.465653	-7.858265	root_mean_squared_error
1	WeightedEnsemble_L2	-6.565789	-7.667403	root_mean_squared_error
2	CatBoost_r137	-7.100844	-10.370113	root_mean_squared_error
3	CatBoost	-7.319287	-9.634744	root_mean_squared_error
4	CatBoost_r177	-7.464913	-9.398295	root_mean_squared_error
5	NeuralNetFastAI	-7.833119	-8.503627	root_mean_squared_error
6	CatBoost_r13	-8.104972	-8.996269	root_mean_squared_error
7	CatBoost_r9	-8.638408	-9.252907	root_mean_squared_error
8	XGBoost	-8.678744	-11.231818	root_mean_squared_error
9	XGBoost_r33	-9.264493	-10.793384	root_mean_squared_error
10	RandomForestMSE	-10.015084	-12.752302	root_mean_squared_error
11	ExtraTrees_r42	-10.321236	-12.743379	root_mean_squared_error
12	ExtraTreesMSE	-10.338205	-12.501554	root_mean_squared_error
13	KNeighborsUnif	-11.313581	-14.232448	root_mean_squared_error
14	NeuralNetFastAI_r102	-11.314371	-13.623935	root_mean_squared_error
15	KNeighborsDist	-11.326214	-14.656925	root_mean_squared_error

	pred_time_test	pred_time_val	fit_time	pred_time_test_marginal	\
0	0.062636	0.025176	9.271056	0.062636	
1	0.193922	0.033624	1533.309282	0.021792	
2	0.080354	0.006184	367.305470	0.080354	
3	0.063215	0.005027	482.195087	0.063215	
4	0.027581	0.006836	86.732648	0.027581	
5	0.040360	0.002593	3.638255	0.040360	
6	0.109494	0.008448	1524.012893	0.109494	
7	0.057354	0.025461	1030.988951	0.057354	
8	0.031350	0.008112	11.257859	0.031350	
9	0.109050	0.012634	55.511277	0.109050	
10	0.215906	0.480414	4.535789	0.215906	
11	0.216460	0.122088	1.322315	0.216460	
12	0.212351	0.099897	1.110185	0.212351	
13	0.036509	0.023081	0.022188	0.036509	
14	0.130343	0.071021	15.547421	0.130343	
15	0.029869	0.024546	0.022627	0.029869	

	pred_time_val_marginal	fit_time_marginal	stack_level	can_infer	\
0	0.025176	9.271056	1	True	
1	0.000000	0.025332	2	True	
2	0.006184	367.305470	1	True	
3	0.005027	482.195087	1	True	
4	0.006836	86.732648	1	True	
5	0.002593	3.638255	1	True	
6	0.008448	1524.012893	1	True	
7	0.025461	1030.988951	1	True	
8	0.008112	11.257859	1	True	
9	0.012634	55.511277	1	True	
10	0.480414	4.535789	1	True	
11	0.122088	1.322315	1	True	
12	0.099897	1.110185	1	True	
13	0.023081	0.022188	1	True	
14	0.071021	15.547421	1	True	
15	0.024546	0.022627	1	True	

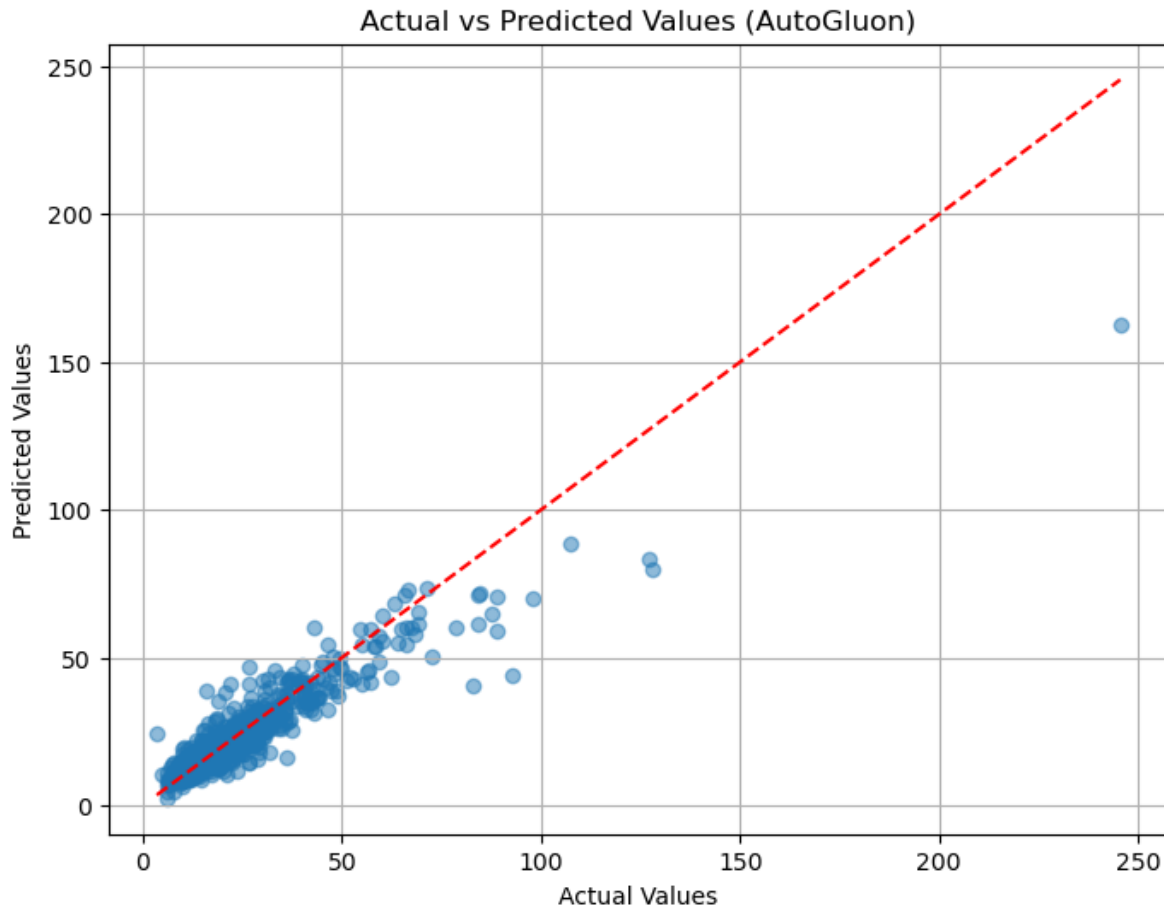
	fit_order
0	9
1	16
2	13
3	4
4	8
5	6

6	15
7	10
8	7
9	11
10	3
11	12
12	5
13	1
14	14
15	2

```
# Get predictions and evaluate
y_pred_auto = auto_predictor.predict(test_df.drop(columns=['SOC']))

# Evaluate using your existing function
autogluon_eval = own_functions.evaluate_model(
    auto_predictor,
    X_test=test_df.drop(columns=['SOC']),
    y_test=test_df['SOC'],
    print_metrics=True,
    show_plot=True,
    plot_kwargs={'model_name': 'AutoGluon', 'figsize': (8, 6)}
)
```

Root Mean Squared Error (RMSE): 6.5658  
 $R^2$ : 0.8530  
 Bias: -0.5860  
 RPD: 2.6080



## 5.3 Strategy 3: Testing auxillary spectral data

### 5.3.1 DLR Spectral Data

<https://geoservice.dlr.de/eoc/ogc/stac/v1/collections/S2-soilsuite-europe-2018-2022-P5Y>

Remove Points without results. Check for MREF vs SRC.

Add parameters to training and test data of the plsr absorbance latent variables.

```
dlr_data = gpd.read_parquet("data/auxiliary_data_results_full_updated.parquet")
# Set pandas display options to show all rows and columns
pd.set_option('display.max_rows', 100) # Show all rows
pd.set_option('display.max_columns', None) # Show all columns
```

```
pd.set_option('display.width', 1000) # Set width to avoid wrapping
```

```
dlr_data
```

	y	x	spatial_ref	time	MREF_B02	MREF_B03	MREF_B04	MREF_B05
0	2548010.0	3902010.0	3035	2018-03-01	567	927	946	1516
1	2545990.0	3908010.0	3035	2018-03-01	399	688	706	1206
2	2555990.0	3907990.0	3035	2018-03-01	556	936	937	1369
3	2537990.0	3899990.0	3035	2018-03-01	232	466	446	934
4	2577990.0	3896010.0	3035	2018-03-01	431	766	805	1357
...	...	...	...	...	...	...	...	...
2800	2636010.0	3598010.0	3035	2018-03-01	446	753	731	1300
2801	2869990.0	3372010.0	3035	2018-03-01	298	620	463	1110
2802	2620010.0	3788010.0	3035	2018-03-01	485	803	833	1367
2803	2795990.0	3357990.0	3035	2018-03-01	498	752	882	1234
2804	2910010.0	3566010.0	3035	2018-03-01	485	779	916	1301

```
dlr_measurements = ["MREF_B02", "MREF_B03", "MREF_B04", "MREF_B05", "MREF_B06", "MREF_B07",
                    "MREF-STD_B02", "MREF-STD_B03", "MREF-STD_B04", "MREF-STD_B05", "MREF-STD_B06", "MREF-STD_B07",
                    # "SRC_B02", "SRC_B03", "SRC_B04", "SRC_B05", "SRC_B06", "SRC_B07",
                    # "SRC-STD_B02", "SRC-STD_B03", "SRC-STD_B04", "SRC-STD_B05", "SRC-STD_B06", "SRC-STD_B07",
                    # "SRC-CI95_B02", "SRC-CI95_B03", "SRC-CI95_B04", "SRC-CI95_B05", "SRC-CI95_B06", "SRC-CI95_B07",
                    # "SFREQ-BSF" #, "SFREQ-BSC", "SFREQ-VPC"
                    ]
```

```
original_ks_indices = ks_indices
original_test_indices = test_indices
```

```
# Create a mapping from original indices to rows in the auxiliary data
point_to_row = dict(zip(dlr_data['point_index'], dlr_data.index))
```

```
# Filter indices to only include those with data in dlr_data
valid_ks_indices = [idx for idx in original_ks_indices if idx in point_to_row]
valid_test_indices = [idx for idx in original_test_indices if idx in point_to_row]
```

```
# Map original indices to row positions in dlr_data
mapped_ks_indices = [point_to_row[idx] for idx in valid_ks_indices]
mapped_test_indices = [point_to_row[idx] for idx in valid_test_indices]
```

```

# Now use these mapped indices to select data
dlr_train_ks = dlr_data.iloc[mapped_ks_indices]
dlr_test_ks = dlr_data.iloc[mapped_test_indices]

# Calculate indices
indices_train_ks = own_functions.compute_indices(dlr_train_ks)
indices_test_ks = own_functions.compute_indices(dlr_test_ks)

# Combine indices with original data
dlr_train_ks = pd.concat([dlr_train_ks[dlr_measurements], indices_train_ks], axis=1)
dlr_test_ks = pd.concat([dlr_test_ks[dlr_measurements], indices_test_ks], axis=1)

# Print shapes
print(f"Original indices: {len(original_ks_indices)} training, {len(original_test_indices)} test")
print(f"Valid indices with aux data: {len(valid_ks_indices)} training, {len(valid_test_indices)} test")

```

Original indices: 1964 training, 843 test  
Valid indices with aux data: 1962 training, 843 test

```

# # select only relevant columns
# dlr_train_ks = dlr_train_ks[dlr_measurements].values
# dlr_test_ks = dlr_test_ks[dlr_measurements].values
dlr_train_ks = dlr_train_ks.values
dlr_test_ks = dlr_test_ks.values

# Print number of rows containing NaN values
print(f"NaN values in DLR Train data: {np.isnan(dlr_train_ks).sum()}")

dlr_train_ks = np.nan_to_num(dlr_train_ks, nan=0, posinf=0, neginf=0)
dlr_test_ks = np.nan_to_num(dlr_test_ks, nan=0, posinf=0, neginf=0)

print(f"Auxillary DLR Train data shape: {dlr_train_ks.shape}")
print(f"Auxillary DLR Test data shape: {dlr_test_ks.shape}")

```

NaN values in DLR Train data: 48  
Auxillary DLR Train data shape: (1962, 38)  
Auxillary DLR Test data shape: (843, 38)

```

# Map from original index to position in X_train_absprb
original_to_train_pos = {orig_idx: train_pos for train_pos, orig_idx in enumerate(ks_indices)}

# Find the positions in X_train_absprb that correspond to valid_ks_indices
train_absprb_positions = []
for idx in valid_ks_indices:
    if idx in original_to_train_pos:
        train_absprb_positions.append(original_to_train_pos[idx])

# Now use these positions to select from X_train_absprb
X_train_absprb_dlr = X_train_absorb[train_absprb_positions, :]
y_train_dlr = y_train[train_absprb_positions]

# Do the same for test data
original_to_test_pos = {orig_idx: test_pos for test_pos, orig_idx in enumerate(test_indices)}

test_absprb_positions = []
for idx in valid_test_indices:
    if idx in original_to_test_pos:
        test_absprb_positions.append(original_to_test_pos[idx])

X_test_absprb_dlr = X_test_absorb[test_absprb_positions, :]
y_test_dlr = y_test[test_absprb_positions]

# Print shapes
print(f"X_train_absorb_dlr shape: {X_train_absprb_dlr.shape}")
print(f"X_test_absprb_dlr shape: {X_test_absprb_dlr.shape}")
print(f"y_train_dlr shape: {y_train_dlr.shape}")
print(f"y_test_dlr shape: {y_test_dlr.shape}")

```

```

X_train_absorb_dlr shape: (1962, 1000)
X_test_absprb_dlr shape: (843, 1000)
y_train_dlr shape: (1962,)
y_test_dlr shape: (843,)

```

```

# Add the auxiliary data to the PLSR transformed data
X_train_combined = np.hstack((X_train_absprb_dlr, dlr_train_ks))
X_test_combined = np.hstack((X_test_absprb_dlr, dlr_test_ks))

# Print shapes
print(f"X_train_combined shape: {X_train_combined.shape}")

```



```
print(f"X_test_combined shape: {X_test_combined.shape}")
```

X\_train\_combined shape: (1962, 1038)

X\_test\_combined shape: (843, 1038)

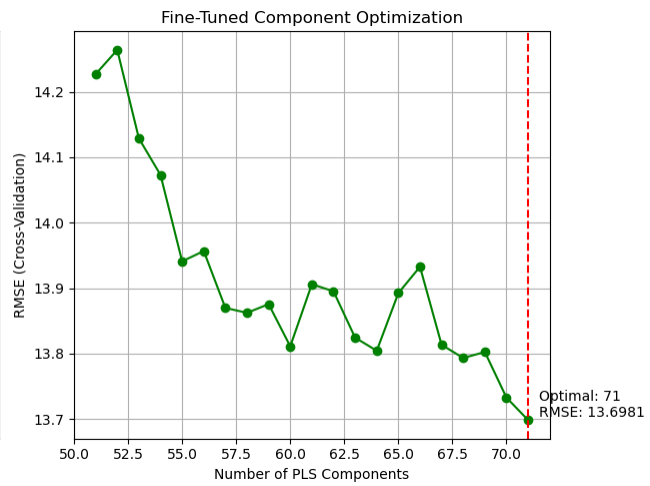
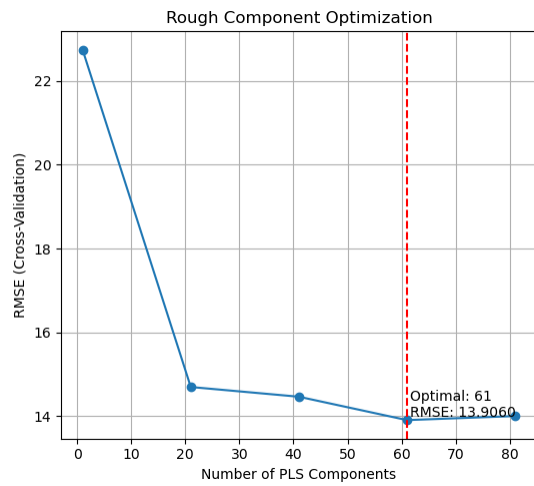
```
plsr_dlr_components = own_functions.optimize_pls_components(X_train=X_train_combined,
                                                            y_train=y_train_dlr,
                                                            max_components=100,
                                                            step=20,
                                                            fine_tune=True,
                                                            show_progress=True,
                                                            plot_results=True
                                                            )
```

```
plsr_absorb_dlr_model = PLSRegression(plsr_dlr_components["optimal_n"])
plsr_absorb_dlr_model.fit(X_train_combined, y_train_dlr)
```

```
plsr_absorb_dlr_eval = own_functions.evaluate_model(plsr_absorb_dlr_model,
                                                    X_test=X_test_combined,
                                                    y_test=y_test_dlr,
                                                    print_metrics=True,
                                                    show_plot=True,
                                                    plot_kwargs={'model_name': 'PLSR with abosrbances',
                                                                    'figsize': (8, 6)}
                                                    )
```

Rough Optimization: 0%| | 0/5 [00:00<?, ?it/s]

Fine Tuning: 0%| | 0/21 [00:00<?, ?it/s]

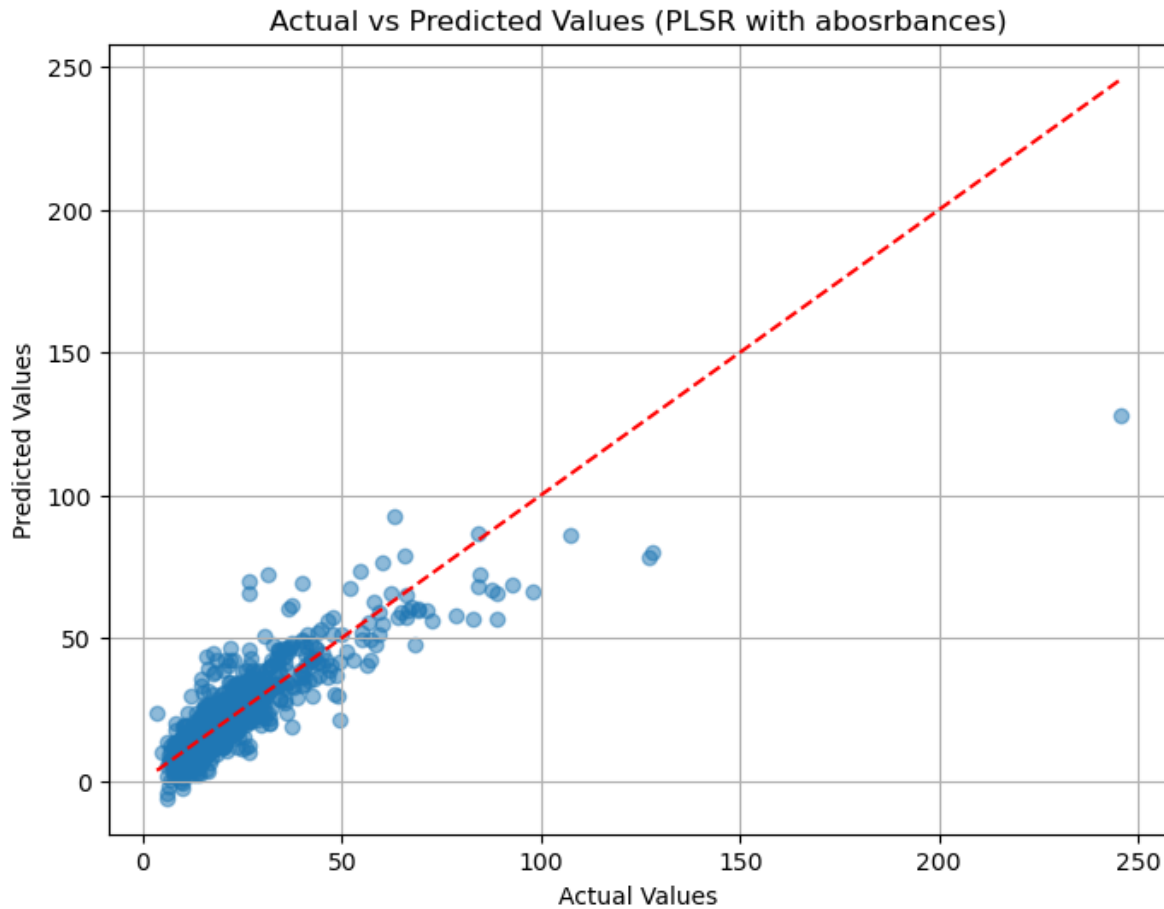


Root Mean Squared Error (RMSE): 8.9545

$R^2$ : 0.7265

Bias: 0.2841

RPD: 1.9123



```
# transform the data using plsr_absorb_dlr_model
X_train_plsr_absorb_dlr = plsr_absorb_dlr_model.transform(X_train_combined)
X_test_plsr_absorb_dlr = plsr_absorb_dlr_model.transform(X_test_combined)

# First split training data into train and validation sets
X_train_final, X_val, y_train_final, y_val = train_test_split(X_train_plsr_absorb_dlr, y_train_combined,
                                                                test_size=0.2,
                                                                random_state=42)

# Training enhanced LSTM model
LSTM_plsr_dlr_model, history, metrics = own_functions.train_and_evaluate_lstm(
    X_train=X_train_final,
    X_val=X_val,
    X_test=X_test_plsr_absorb_dlr,
```

```

    y_train=y_train_final,
    y_val=y_val,
    y_test=y_test_dlr,
    hidden_size=256,
    num_layers=5,
    num_epochs=3000,
    learning_rate=0.001,
    patience=200, # Early stopping patience
    dropout=0.2
)

lstm_plsr_eval = own_functions.evaluate_model(LSTM_plsr_dlr_model,
                                              X_test=X_test_plsr_absorb_dlr, y_test=y_test_dlr,
                                              print_metrics=True, show_plot=True)

```

```

Epoch [10/3000], Train Loss: 1540.5464, Val Loss: 1257.4043
Epoch [20/3000], Train Loss: 1344.9900, Val Loss: 1036.0135
Epoch [30/3000], Train Loss: 1098.5538, Val Loss: 813.5641
Epoch [40/3000], Train Loss: 986.3824, Val Loss: 711.8333
Epoch [50/3000], Train Loss: 917.4670, Val Loss: 647.8571
Epoch [60/3000], Train Loss: 866.9979, Val Loss: 601.1006
Epoch [70/3000], Train Loss: 830.6962, Val Loss: 567.8345
Epoch [80/3000], Train Loss: 805.1898, Val Loss: 544.7816
Epoch [90/3000], Train Loss: 787.6553, Val Loss: 529.2339
Epoch [100/3000], Train Loss: 775.8893, Val Loss: 519.0675
Epoch [110/3000], Train Loss: 768.2424, Val Loss: 512.6531
Epoch [120/3000], Train Loss: 763.3832, Val Loss: 508.7702
Epoch [130/3000], Train Loss: 760.3764, Val Loss: 506.5227
Epoch [140/3000], Train Loss: 758.4575, Val Loss: 505.1368
Epoch [150/3000], Train Loss: 757.2153, Val Loss: 503.8857
Epoch [160/3000], Train Loss: 755.8500, Val Loss: 499.4169
Epoch [170/3000], Train Loss: 753.3842, Val Loss: 498.8031
Epoch [180/3000], Train Loss: 751.7171, Val Loss: 495.5575
Epoch [190/3000], Train Loss: 749.3278, Val Loss: 493.8198
Epoch [200/3000], Train Loss: 745.2280, Val Loss: 490.5216
Epoch [210/3000], Train Loss: 740.8985, Val Loss: 486.6480
Epoch [220/3000], Train Loss: 731.9058, Val Loss: 475.0211
Epoch [230/3000], Train Loss: 712.8406, Val Loss: 456.1924
Epoch [240/3000], Train Loss: 654.4607, Val Loss: 397.9888
Epoch [250/3000], Train Loss: 630.2448, Val Loss: 376.5938
Epoch [260/3000], Train Loss: 607.6003, Val Loss: 358.4547

```

Epoch [270/3000], Train Loss: 585.6476, Val Loss: 338.9770  
 Epoch [280/3000], Train Loss: 566.1488, Val Loss: 322.1868  
 Epoch [290/3000], Train Loss: 549.3708, Val Loss: 309.4305  
 Epoch [300/3000], Train Loss: 532.5668, Val Loss: 296.8417  
 Epoch [310/3000], Train Loss: 519.7497, Val Loss: 284.9230  
 Epoch [320/3000], Train Loss: 505.5452, Val Loss: 273.9857  
 Epoch [330/3000], Train Loss: 493.5374, Val Loss: 264.8949  
 Epoch [340/3000], Train Loss: 484.1887, Val Loss: 256.2636  
 Epoch [350/3000], Train Loss: 473.1741, Val Loss: 249.6683  
 Epoch [360/3000], Train Loss: 465.3259, Val Loss: 243.4194  
 Epoch [370/3000], Train Loss: 456.6234, Val Loss: 236.2714  
 Epoch [380/3000], Train Loss: 449.8513, Val Loss: 230.1771  
 Epoch [390/3000], Train Loss: 441.3017, Val Loss: 223.6157  
 Epoch [400/3000], Train Loss: 433.4195, Val Loss: 220.1736  
 Epoch [410/3000], Train Loss: 427.6105, Val Loss: 214.7301  
 Epoch [420/3000], Train Loss: 422.0114, Val Loss: 213.1962  
 Epoch [430/3000], Train Loss: 414.6510, Val Loss: 206.7473  
 Epoch [440/3000], Train Loss: 407.7838, Val Loss: 203.2201  
 Epoch [450/3000], Train Loss: 402.4257, Val Loss: 199.4562  
 Epoch [460/3000], Train Loss: 396.7086, Val Loss: 196.9667  
 Epoch [470/3000], Train Loss: 390.8503, Val Loss: 193.0206  
 Epoch [480/3000], Train Loss: 386.5664, Val Loss: 189.7172  
 Epoch [490/3000], Train Loss: 381.8917, Val Loss: 187.7487  
 Epoch [500/3000], Train Loss: 376.5102, Val Loss: 182.8676  
 Epoch [510/3000], Train Loss: 371.9299, Val Loss: 178.7989  
 Epoch [520/3000], Train Loss: 366.1584, Val Loss: 175.5018  
 Epoch [530/3000], Train Loss: 361.6959, Val Loss: 173.6944  
 Epoch [540/3000], Train Loss: 356.5685, Val Loss: 171.1390  
 Epoch [550/3000], Train Loss: 351.8480, Val Loss: 169.6963  
 Epoch [560/3000], Train Loss: 347.9784, Val Loss: 165.1118  
 Epoch [570/3000], Train Loss: 344.4390, Val Loss: 163.6105  
 Epoch [580/3000], Train Loss: 340.5009, Val Loss: 161.4051  
 Epoch [590/3000], Train Loss: 337.0747, Val Loss: 159.3816  
 Epoch [600/3000], Train Loss: 333.2801, Val Loss: 157.3070  
 Epoch [610/3000], Train Loss: 329.4747, Val Loss: 155.0859  
 Epoch [620/3000], Train Loss: 325.9943, Val Loss: 152.1785  
 Epoch [630/3000], Train Loss: 323.2853, Val Loss: 151.4859  
 Epoch [640/3000], Train Loss: 319.2904, Val Loss: 148.9192  
 Epoch [650/3000], Train Loss: 316.3323, Val Loss: 147.7457  
 Epoch [660/3000], Train Loss: 312.4438, Val Loss: 146.3408  
 Epoch [670/3000], Train Loss: 309.1076, Val Loss: 143.9397  
 Epoch [680/3000], Train Loss: 306.0854, Val Loss: 143.7634  
 Epoch [690/3000], Train Loss: 303.6172, Val Loss: 142.2303

Epoch [700/3000], Train Loss: 300.4765, Val Loss: 141.3450  
Epoch [710/3000], Train Loss: 297.2296, Val Loss: 139.1321  
Epoch [720/3000], Train Loss: 293.1558, Val Loss: 133.8564  
Epoch [730/3000], Train Loss: 291.3673, Val Loss: 132.3879  
Epoch [740/3000], Train Loss: 289.5096, Val Loss: 131.1984  
Epoch [750/3000], Train Loss: 285.8670, Val Loss: 127.8757  
Epoch [760/3000], Train Loss: 283.5089, Val Loss: 126.0784  
Epoch [770/3000], Train Loss: 280.9081, Val Loss: 127.8975  
Epoch [780/3000], Train Loss: 277.1148, Val Loss: 127.4610  
Epoch [790/3000], Train Loss: 275.3409, Val Loss: 127.2116  
Epoch [800/3000], Train Loss: 272.9195, Val Loss: 122.2731  
Epoch [810/3000], Train Loss: 270.0008, Val Loss: 119.5473  
Epoch [820/3000], Train Loss: 268.3408, Val Loss: 118.9863  
Epoch [830/3000], Train Loss: 265.6374, Val Loss: 117.0228  
Epoch [840/3000], Train Loss: 263.4792, Val Loss: 116.3368  
Epoch [850/3000], Train Loss: 261.1463, Val Loss: 114.9678  
Epoch [860/3000], Train Loss: 258.1842, Val Loss: 113.9380  
Epoch [870/3000], Train Loss: 256.4466, Val Loss: 111.2624  
Epoch [880/3000], Train Loss: 253.9297, Val Loss: 110.3496  
Epoch [890/3000], Train Loss: 251.4222, Val Loss: 109.4902  
Epoch [900/3000], Train Loss: 249.0736, Val Loss: 107.4268  
Epoch [910/3000], Train Loss: 247.4741, Val Loss: 107.8101  
Epoch [920/3000], Train Loss: 245.3165, Val Loss: 107.8644  
Epoch [930/3000], Train Loss: 243.1395, Val Loss: 106.0409  
Epoch [940/3000], Train Loss: 241.0189, Val Loss: 105.7801  
Epoch [950/3000], Train Loss: 239.6714, Val Loss: 104.6199  
Epoch [960/3000], Train Loss: 237.4846, Val Loss: 101.2453  
Epoch [970/3000], Train Loss: 234.7814, Val Loss: 101.6119  
Epoch [980/3000], Train Loss: 233.5699, Val Loss: 101.5904  
Epoch [990/3000], Train Loss: 231.6402, Val Loss: 99.9985  
Epoch [1000/3000], Train Loss: 229.6795, Val Loss: 98.4479  
Epoch [1010/3000], Train Loss: 227.5080, Val Loss: 97.6271  
Epoch [1020/3000], Train Loss: 226.2702, Val Loss: 96.4655  
Epoch [1030/3000], Train Loss: 224.1594, Val Loss: 96.8722  
Epoch [1040/3000], Train Loss: 222.3503, Val Loss: 93.1366  
Epoch [1050/3000], Train Loss: 220.5237, Val Loss: 95.1915  
Epoch [1060/3000], Train Loss: 219.4306, Val Loss: 92.7521  
Epoch [1070/3000], Train Loss: 217.0003, Val Loss: 91.0391  
Epoch [1080/3000], Train Loss: 215.0062, Val Loss: 92.9009  
Epoch [1090/3000], Train Loss: 212.7579, Val Loss: 89.9007  
Epoch [1100/3000], Train Loss: 211.8514, Val Loss: 88.0061  
Epoch [1110/3000], Train Loss: 210.1269, Val Loss: 85.9341  
Epoch [1120/3000], Train Loss: 208.7714, Val Loss: 91.5790

Epoch [1130/3000], Train Loss: 206.4010, Val Loss: 90.6554  
 Epoch [1140/3000], Train Loss: 204.3830, Val Loss: 89.6532  
 Epoch [1150/3000], Train Loss: 203.6959, Val Loss: 89.2974  
 Epoch [1160/3000], Train Loss: 201.4929, Val Loss: 88.8583  
 Epoch [1170/3000], Train Loss: 200.3690, Val Loss: 84.1039  
 Epoch [1180/3000], Train Loss: 197.8281, Val Loss: 85.3187  
 Epoch [1190/3000], Train Loss: 196.5895, Val Loss: 85.1077  
 Epoch [1200/3000], Train Loss: 195.0304, Val Loss: 85.1213  
 Epoch [1210/3000], Train Loss: 194.0274, Val Loss: 80.5765  
 Epoch [1220/3000], Train Loss: 192.9698, Val Loss: 82.4580  
 Epoch [1230/3000], Train Loss: 190.5625, Val Loss: 79.4048  
 Epoch [1240/3000], Train Loss: 188.9924, Val Loss: 81.8780  
 Epoch [1250/3000], Train Loss: 187.3711, Val Loss: 81.3156  
 Epoch [1260/3000], Train Loss: 185.7895, Val Loss: 82.0416  
 Epoch [1270/3000], Train Loss: 185.1033, Val Loss: 81.3030  
 Epoch [1280/3000], Train Loss: 183.4679, Val Loss: 77.2549  
 Epoch [1290/3000], Train Loss: 181.8413, Val Loss: 78.1357  
 Epoch [1300/3000], Train Loss: 180.1181, Val Loss: 79.9820  
 Epoch [1310/3000], Train Loss: 178.8289, Val Loss: 75.7877  
 Epoch [1320/3000], Train Loss: 177.4787, Val Loss: 78.2868  
 Epoch [1330/3000], Train Loss: 175.8099, Val Loss: 78.2056  
 Epoch [1340/3000], Train Loss: 174.2967, Val Loss: 76.2412  
 Epoch [1350/3000], Train Loss: 173.4266, Val Loss: 73.7899  
 Epoch [1360/3000], Train Loss: 171.6779, Val Loss: 76.7758  
 Epoch [1370/3000], Train Loss: 170.3346, Val Loss: 75.5946  
 Epoch [1380/3000], Train Loss: 168.8669, Val Loss: 74.0210  
 Epoch [1390/3000], Train Loss: 167.3740, Val Loss: 72.5895  
 Epoch [1400/3000], Train Loss: 166.0790, Val Loss: 71.5685  
 Epoch [1410/3000], Train Loss: 164.8049, Val Loss: 71.9062  
 Epoch [1420/3000], Train Loss: 163.7440, Val Loss: 72.5149  
 Epoch [1430/3000], Train Loss: 162.1865, Val Loss: 74.8183  
 Epoch [1440/3000], Train Loss: 160.9719, Val Loss: 72.8818  
 Epoch [1450/3000], Train Loss: 160.1599, Val Loss: 72.2733  
 Epoch [1460/3000], Train Loss: 159.6580, Val Loss: 71.9436  
 Epoch [1470/3000], Train Loss: 157.3667, Val Loss: 70.6574  
 Epoch [1480/3000], Train Loss: 156.1098, Val Loss: 70.6578  
 Epoch [1490/3000], Train Loss: 155.0821, Val Loss: 72.4272  
 Epoch [1500/3000], Train Loss: 153.7685, Val Loss: 68.9280  
 Epoch [1510/3000], Train Loss: 152.5436, Val Loss: 70.6565  
 Epoch [1520/3000], Train Loss: 151.6387, Val Loss: 67.5730  
 Epoch [1530/3000], Train Loss: 150.6447, Val Loss: 68.7568  
 Epoch [1540/3000], Train Loss: 149.8463, Val Loss: 69.0988  
 Epoch [1550/3000], Train Loss: 148.3323, Val Loss: 68.6356

Epoch [1560/3000], Train Loss: 146.8783, Val Loss: 66.5376  
 Epoch [1570/3000], Train Loss: 145.7830, Val Loss: 68.7561  
 Epoch [1580/3000], Train Loss: 144.7695, Val Loss: 67.1103  
 Epoch [1590/3000], Train Loss: 143.6030, Val Loss: 67.5270  
 Epoch [1600/3000], Train Loss: 142.4209, Val Loss: 67.8633  
 Epoch [1610/3000], Train Loss: 141.7666, Val Loss: 66.5600  
 Epoch [1620/3000], Train Loss: 140.4418, Val Loss: 67.7374  
 Epoch [1630/3000], Train Loss: 139.2329, Val Loss: 70.1780  
 Epoch [1640/3000], Train Loss: 139.0233, Val Loss: 67.3184  
 Epoch [1650/3000], Train Loss: 137.2160, Val Loss: 65.6899  
 Epoch [1660/3000], Train Loss: 136.1907, Val Loss: 68.1165  
 Epoch [1670/3000], Train Loss: 135.7569, Val Loss: 65.2837  
 Epoch [1680/3000], Train Loss: 134.5427, Val Loss: 65.4321  
 Epoch [1690/3000], Train Loss: 133.5053, Val Loss: 64.5273  
 Epoch [1700/3000], Train Loss: 132.7533, Val Loss: 66.5384  
 Epoch [1710/3000], Train Loss: 132.0370, Val Loss: 68.9226  
 Epoch [1720/3000], Train Loss: 130.9869, Val Loss: 67.9919  
 Epoch [1730/3000], Train Loss: 130.3685, Val Loss: 65.8093  
 Epoch [1740/3000], Train Loss: 128.9625, Val Loss: 66.5856  
 Epoch [1750/3000], Train Loss: 127.8757, Val Loss: 63.5284  
 Epoch [1760/3000], Train Loss: 127.2936, Val Loss: 63.4254  
 Epoch [1770/3000], Train Loss: 126.4377, Val Loss: 64.9431  
 Epoch [1780/3000], Train Loss: 125.1934, Val Loss: 65.1679  
 Epoch [1790/3000], Train Loss: 124.5525, Val Loss: 64.6615  
 Epoch [1800/3000], Train Loss: 124.3395, Val Loss: 63.8481  
 Epoch [1810/3000], Train Loss: 123.4211, Val Loss: 66.0345  
 Epoch [1820/3000], Train Loss: 122.2801, Val Loss: 64.0493  
 Epoch [1830/3000], Train Loss: 121.5827, Val Loss: 63.5406  
 Epoch [1840/3000], Train Loss: 120.9762, Val Loss: 64.8369  
 Epoch [1850/3000], Train Loss: 120.1384, Val Loss: 63.7654  
 Epoch [1860/3000], Train Loss: 119.0760, Val Loss: 64.8412  
 Epoch [1870/3000], Train Loss: 118.3706, Val Loss: 66.1343  
 Epoch [1880/3000], Train Loss: 117.5391, Val Loss: 63.1404  
 Epoch [1890/3000], Train Loss: 117.0470, Val Loss: 64.0964  
 Epoch [1900/3000], Train Loss: 115.9382, Val Loss: 64.4309  
 Epoch [1910/3000], Train Loss: 115.0538, Val Loss: 64.1527  
 Epoch [1920/3000], Train Loss: 114.5444, Val Loss: 65.5393  
 Epoch [1930/3000], Train Loss: 113.6631, Val Loss: 65.1711  
 Epoch [1940/3000], Train Loss: 113.4395, Val Loss: 67.2524  
 Epoch [1950/3000], Train Loss: 112.1825, Val Loss: 64.2757  
 Epoch [1960/3000], Train Loss: 112.1844, Val Loss: 64.3860  
 Epoch [1970/3000], Train Loss: 111.3415, Val Loss: 63.7314  
 Epoch [1980/3000], Train Loss: 110.6227, Val Loss: 64.0904



Epoch [1990/3000], Train Loss: 109.3487, Val Loss: 64.2847  
Epoch [2000/3000], Train Loss: 108.9872, Val Loss: 63.1711  
Epoch [2010/3000], Train Loss: 107.8140, Val Loss: 65.8118  
Epoch [2020/3000], Train Loss: 107.0848, Val Loss: 65.5678  
Epoch [2030/3000], Train Loss: 107.0298, Val Loss: 67.7580  
Epoch [2040/3000], Train Loss: 105.8401, Val Loss: 64.5578  
Epoch [2050/3000], Train Loss: 105.5651, Val Loss: 65.6982  
Epoch [2060/3000], Train Loss: 105.2389, Val Loss: 64.8927  
Epoch [2070/3000], Train Loss: 103.9555, Val Loss: 64.0075  
Epoch [2080/3000], Train Loss: 103.1114, Val Loss: 67.7239  
Epoch [2090/3000], Train Loss: 102.6616, Val Loss: 67.5062  
Epoch [2100/3000], Train Loss: 102.9571, Val Loss: 67.2030  
Epoch [2110/3000], Train Loss: 101.0403, Val Loss: 66.6137  
Epoch [2120/3000], Train Loss: 100.5723, Val Loss: 68.2896  
Epoch [2130/3000], Train Loss: 99.5712, Val Loss: 66.7092  
Epoch [2140/3000], Train Loss: 99.5899, Val Loss: 64.0705  
Epoch [2150/3000], Train Loss: 99.4821, Val Loss: 67.0173  
Epoch [2160/3000], Train Loss: 98.4651, Val Loss: 67.6521  
Epoch [2170/3000], Train Loss: 97.5777, Val Loss: 64.8495  
Epoch [2180/3000], Train Loss: 97.1009, Val Loss: 65.3012  
Epoch [2190/3000], Train Loss: 96.2967, Val Loss: 67.1722  
Epoch [2200/3000], Train Loss: 95.9820, Val Loss: 69.6837  
Early stopping triggered at epoch 2202

Final Test Metrics:

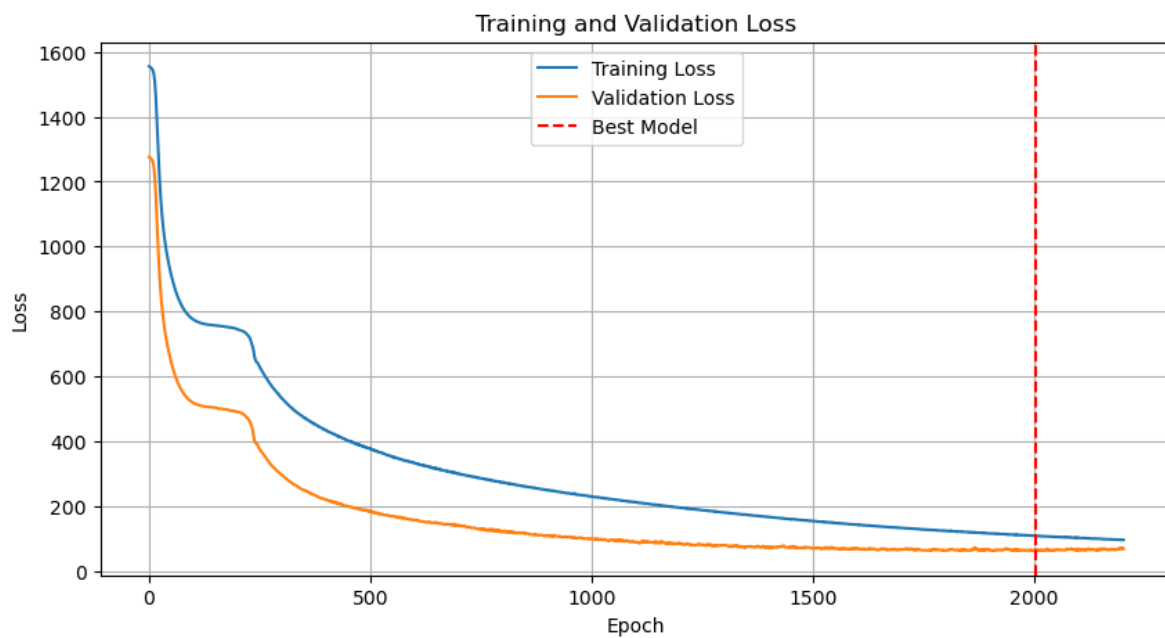
test\_loss: 37.0165

rmse: 6.0841

r2: 0.8738

bias: -0.3307

rpd: 2.8144

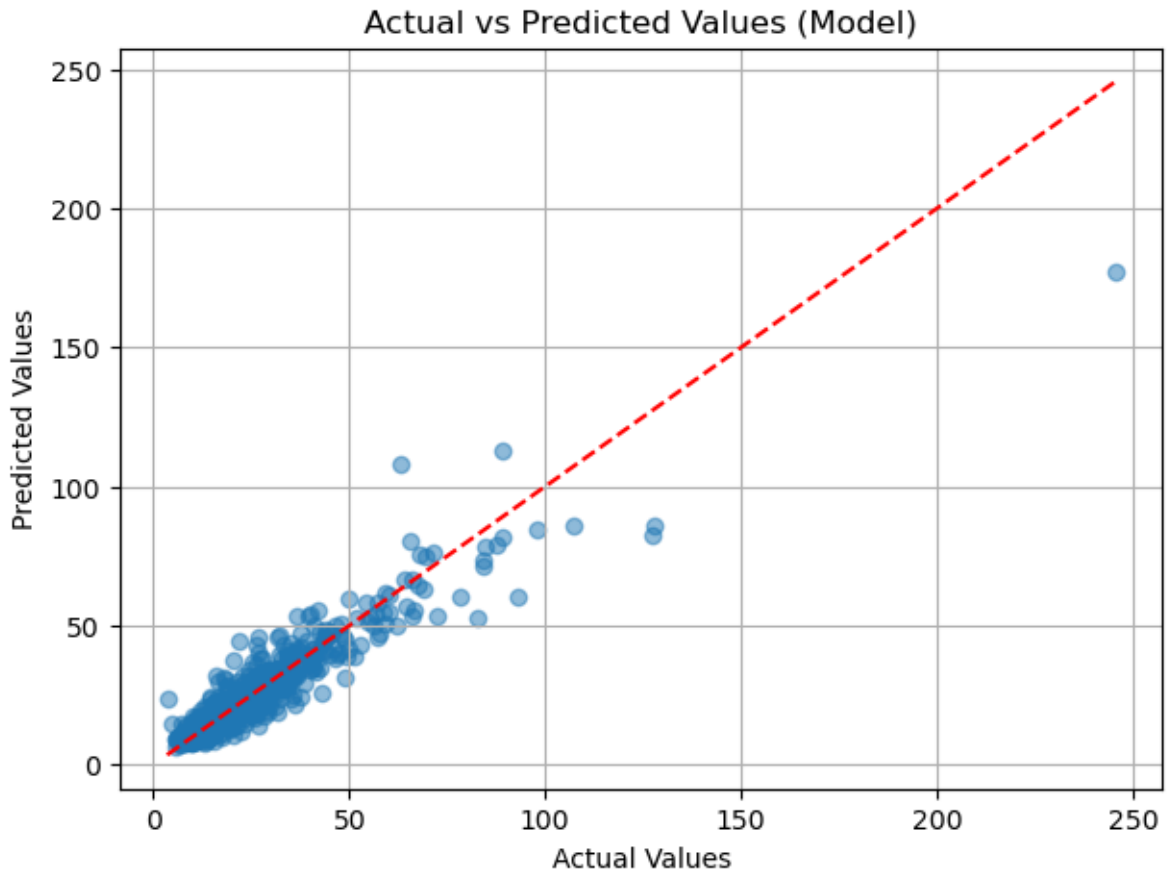


Root Mean Squared Error (RMSE): 6.0841

$R^2$ : 0.8738

Bias: -0.3307

RPD: 2.8144



### 5.3.2 ISRIC Soil Data

<https://www.isric.org/explore/soilgrids>

```
# read pd from csv
isric_data = pd.read_csv('data/soilgrids_parallel.csv')
isric_data.head()
```

	point_index	lon	lat	bdod_0_to_5cm_mean	bdod_5_to_15cm_mean	bdod_15_to_...
0	1	4.584692	45.816720	125.0	134.0	141.0
1	0	4.680379	45.893933	128.0	138.0	141.0
2	3	4.601575	45.908022	133.0	140.0	144.0
3	2	4.671533	45.983716	129.0	139.0	143.0
4	6	4.439863	46.224665	102.0	116.0	121.0

```
# check if any lon is 88.8888 and lat is 88.8888
isric_data[isric_data['lon'].isin([88.888888])]
```

	point_index	lon	lat	bdod_0_to_5cm_mean	bdod_5_to_15cm_mean	bdod_15_to_30cm_mean
511	513	88.888888	88.888888	NaN	NaN	NaN
933	935	88.888888	88.888888	NaN	NaN	NaN

```
isric_measurements = ["bdod_0_to_5cm_mean", "bdod_5_to_15cm_mean", "bdod_15_to_30cm_mean",
                      "clay_0_to_5cm_mean", "clay_5_to_15cm_mean", "clay_15_to_30cm_mean",
                      "phh2o_0_to_5cm_mean", "phh2o_5_to_15cm_mean", "phh2o_15_to_30cm_mean",
                      "sand_0_to_5cm_mean", "sand_5_to_15cm_mean", "sand_15_to_30cm_mean",
                      "silt_0_to_5cm_mean", "silt_5_to_15cm_mean", "silt_15_to_30cm_mean"]
```

```
# Create a mapping from original indices to rows in the isriciliary data
point_to_row = dict(zip(isric_data['point_index'], isric_data.index))
```

```
# Filter indices to only include those with data in isric_data
valid_ks_indices = [idx for idx in original_ks_indices if idx in point_to_row]
valid_test_indices = [idx for idx in original_ks_indices if idx in point_to_row]
```

```
# Map original indices to row positions in isric_data
mapped_ks_indices = [point_to_row[idx] for idx in valid_ks_indices]
mapped_test_indices = [point_to_row[idx] for idx in valid_test_indices]
```

```
# Now use these mapped indices to select data
isric_train_ks = isric_data.iloc[mapped_ks_indices]
isric_test_ks = isric_data.iloc[mapped_test_indices]
```

```
# Print shapes
print(f"Original indices: {len(ks_indices)} training, {len(test_indices)} test")
print(f"Valid indices with isric data: {len(valid_ks_indices)} training, {len(valid_test_indices)} test")
```

```
# select only relevant columns
isric_train_ks = isric_train_ks[isric_measurements].values
isric_test_ks = isric_test_ks[isric_measurements].values
```

```
isric_train_ks = np.nan_to_num(isric_train_ks, nan=0, posinf=0, neginf=0)
isric_test_ks = np.nan_to_num(isric_test_ks, nan=0, posinf=0, neginf=0)
```

```
print(f"Auxillary isric Train data shape: {isric_train_ks.shape}")
print(f"Auxillary isric Test data shape: {isric_test_ks.shape}")
```

Original indices: 1964 training, 843 test  
Valid indices with isric data: 1964 training, 843 test  
Auxillary isric Train data shape: (1964, 15)  
Auxillary isric Test data shape: (843, 15)

```
original_train_indices = ks_indices # These are the indices used to create X_train_pls

# Map from original index to position in X_train_pls
original_to_train_pos = {orig_idx: train_pos for train_pos, orig_idx in enumerate(original_train_indices)}

# Find the positions in X_train_pls that correspond to valid_ks_indices
train_pls_positions = []
for idx in valid_ks_indices:
    if idx in original_to_train_pos:
        train_pls_positions.append(original_to_train_pos[idx])

# Now use these positions to select from X_train_pls
X_train_pls_isric = X_train_absorb[train_pls_positions, :]
y_train_isric = y_train[train_pls_positions]

# Do the same for test data
original_test_indices = test_indices # These are the indices used to create X_test_pls
original_to_test_pos = {orig_idx: test_pos for test_pos, orig_idx in enumerate(original_test_indices)}

test_pls_positions = []
for idx in valid_test_indices:
    if idx in original_to_test_pos:
        test_pls_positions.append(original_to_test_pos[idx])

X_test_pls_isric = X_test_absorb[test_pls_positions, :]
y_test_isric = y_test[test_pls_positions]

# Print shapes
print(f"X_train_pls_isric shape: {X_train_pls_isric.shape}")
print(f"X_test_pls_isric shape: {X_test_pls_isric.shape}")
print(f"y_train_isric shape: {y_train_isric.shape}")
print(f"y_test_isric shape: {y_test_isric.shape}")
```

```

# Add the isriciliary data to the PLSR transformed data
X_train_combined = np.hstack((X_train_pls_isric, isric_train_ks))
X_test_combined = np.hstack((X_test_pls_isric, isric_test_ks))

# standardize the data
scaler = StandardScaler()
X_train_combined = scaler.fit_transform(X_train_combined)
X_test_combined = scaler.transform(X_test_combined)

# Print shapes
print(f"X_train_combined shape: {X_train_combined.shape}")
print(f"X_test_combined shape: {X_test_combined.shape}")

```

```

X_train_pls_isric shape: (1964, 1000)
X_test_pls_isric shape: (843, 1000)
y_train_isric shape: (1964,)
y_test_isric shape: (843,)
X_train_combined shape: (1964, 1015)
X_test_combined shape: (843, 1015)

```

```

plsr_isric_components = own_functions.optimize_pls_components(X_train=X_train_combined,
                                                             y_train=y_train_isric,
                                                             max_components=100,
                                                             step=20,
                                                             fine_tune=True,
                                                             show_progress=True,
                                                             plot_results=True
                                                             )

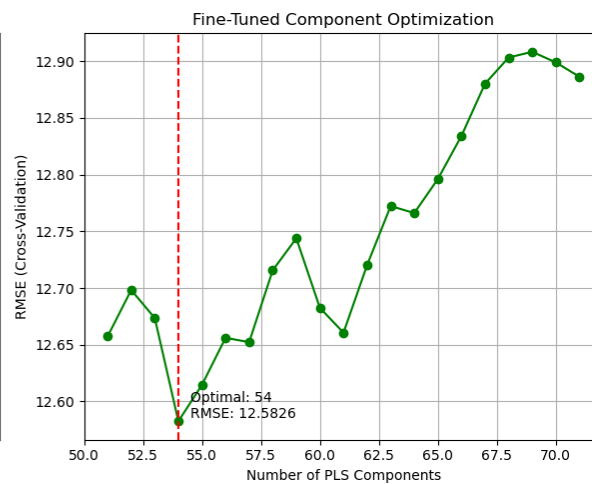
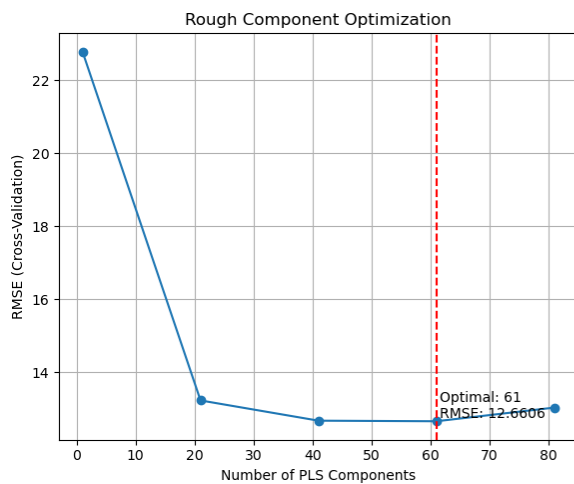
plsr_absorb_aux_model = PLSRegression(n_components=plsr_isric_components["optimal_n"])
plsr_absorb_aux_model.fit(X_train_combined, y_train_isric)

plsr_absorb_aux_eval = own_functions.evaluate_model(plsr_absorb_aux_model,
                                                    X_test=X_test_combined,
                                                    y_test=y_test_isric,
                                                    print_metrics=True,
                                                    show_plot=True,
                                                    plot_kwargs={'model_name': 'PLSR with abosrbances',
                                                                    'figsize': (8, 6)}
                                                    )

```

Rough Optimization: 0% | 0/5 [00:00<?, ?it/s]

Fine Tuning: 0% | 0/21 [00:00<?, ?it/s]

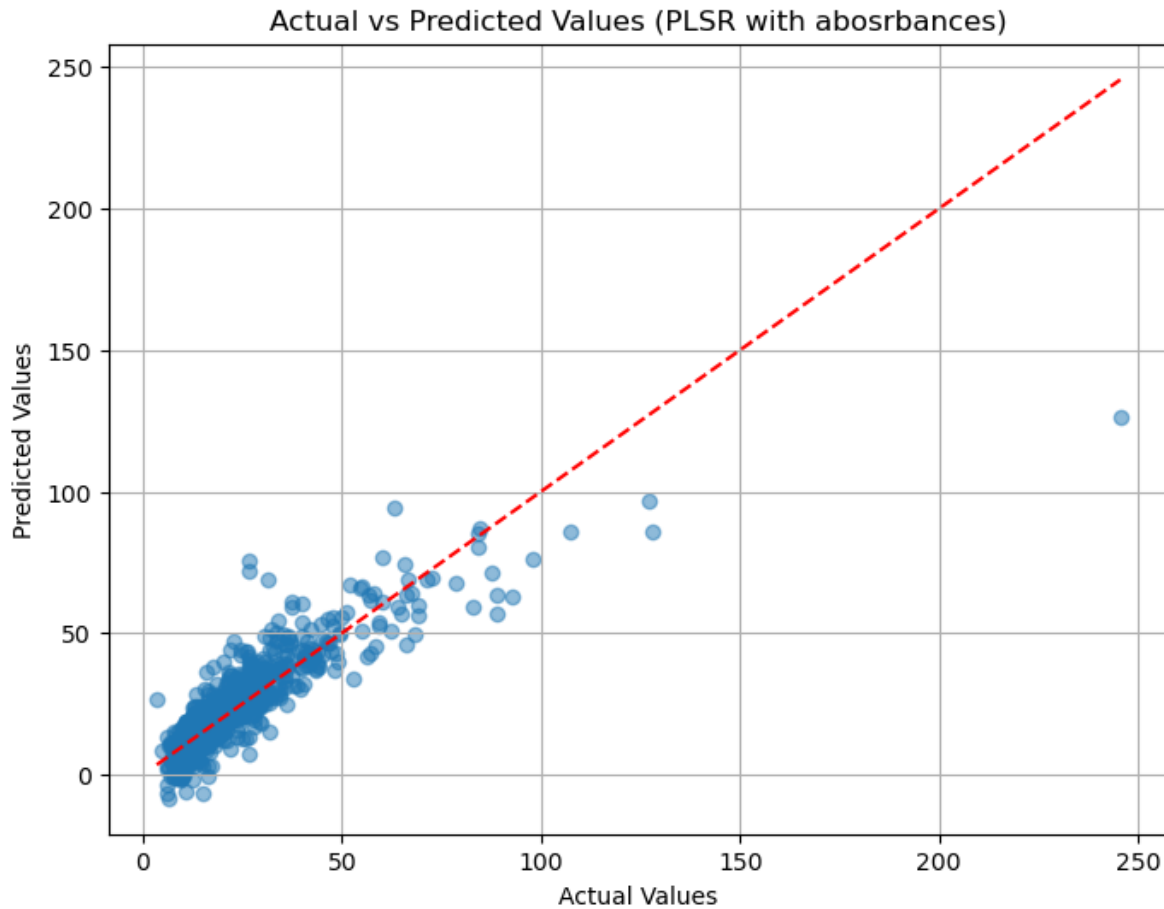


Root Mean Squared Error (RMSE): 8.7390

$R^2$ : 0.7395

Bias: 0.7804

RPD: 1.9594



```
X_train_comb_plsr = plsr_absorb_aux_model.transform(X_train_combined)
X_test_comb_plsr = plsr_absorb_aux_model.transform(X_test_combined)
```

```
# First split training data into train and validation sets
```

```
X_train_final, X_val, y_train_final, y_val = train_test_split(X_train_comb_plsr, y_train_i
                                                                test_size=0.2,
                                                                random_state=42)
```

```
# Training enhanced LSTM model
```

```
LSTM_aux_model, history, metrics = own_functions.train_and_evaluate_lstm(
    X_train=X_train_final,
    X_val=X_val,
    X_test=X_test_comb_plsr,
    y_train=y_train_final,
```



```

        y_val=y_val,
        y_test=y_test_isric,
        hidden_size=256,
        num_layers=5,
        num_epochs=4000,
        learning_rate=0.001,
        patience=300, # Early stopping patience
        dropout=0.2
    )

lstm_eval = own_functions.evaluate_model(LSTM_aux_model,
                                         X_test=X_test_comb_plsr, y_test=y_test_isric,
                                         print_metrics=True, show_plot=True)

# First split training data into train and validation sets
X_train_final, X_val, y_train_final, y_val = train_test_split(X_train_comb_plsr, y_train_i
                                                                test_size=0.2,
                                                                random_state=42)

# Training enhanced LSTM model
LSTM_aux_model, history, metrics = own_functions.train_and_evaluate_lstm(
    X_train=X_train_final,
    X_val=X_val,
    X_test=X_test_comb_plsr,
    y_train=y_train_final,
    y_val=y_val,
    y_test=y_test_isric,
    hidden_size=256,
    num_layers=5,
    num_epochs=4000,
    learning_rate=0.001,
    patience=200, # Early stopping patience
    dropout=0.2
)

lstm_eval = own_functions.evaluate_model(LSTM_aux_model,
                                         X_test=X_test_comb_plsr, y_test=y_test_isric,
                                         print_metrics=True, show_plot=True)

```

Epoch [10/4000], Train Loss: 1475.2972, Val Loss: 1519.5110  
Epoch [20/4000], Train Loss: 1280.4115, Val Loss: 1283.1000  
Epoch [30/4000], Train Loss: 1040.9993, Val Loss: 1062.2501  
Epoch [40/4000], Train Loss: 929.5973, Val Loss: 954.4364  
Epoch [50/4000], Train Loss: 861.1890, Val Loss: 885.2343  
Epoch [60/4000], Train Loss: 811.6935, Val Loss: 834.5779  
Epoch [70/4000], Train Loss: 775.9415, Val Loss: 797.5146  
Epoch [80/4000], Train Loss: 750.5928, Val Loss: 770.7653  
Epoch [90/4000], Train Loss: 732.1863, Val Loss: 751.7930  
Epoch [100/4000], Train Loss: 718.9263, Val Loss: 738.2095  
Epoch [110/4000], Train Loss: 709.2322, Val Loss: 727.8226  
Epoch [120/4000], Train Loss: 702.1847, Val Loss: 720.2368  
Epoch [130/4000], Train Loss: 696.5098, Val Loss: 714.1851  
Epoch [140/4000], Train Loss: 691.6286, Val Loss: 708.9233  
Epoch [150/4000], Train Loss: 686.7952, Val Loss: 703.0333  
Epoch [160/4000], Train Loss: 676.5783, Val Loss: 696.5714  
Epoch [170/4000], Train Loss: 660.6702, Val Loss: 671.7918  
Epoch [180/4000], Train Loss: 611.3018, Val Loss: 620.0627  
Epoch [190/4000], Train Loss: 585.4724, Val Loss: 594.4952  
Epoch [200/4000], Train Loss: 562.5011, Val Loss: 571.0565  
Epoch [210/4000], Train Loss: 542.8493, Val Loss: 551.1712  
Epoch [220/4000], Train Loss: 525.5701, Val Loss: 534.1605  
Epoch [230/4000], Train Loss: 509.3923, Val Loss: 518.1349  
Epoch [240/4000], Train Loss: 495.3281, Val Loss: 503.3998  
Epoch [250/4000], Train Loss: 482.5118, Val Loss: 490.0721  
Epoch [260/4000], Train Loss: 470.3756, Val Loss: 478.1037  
Epoch [270/4000], Train Loss: 458.9582, Val Loss: 467.4412  
Epoch [280/4000], Train Loss: 448.4810, Val Loss: 456.5381  
Epoch [290/4000], Train Loss: 438.2216, Val Loss: 447.2844  
Epoch [300/4000], Train Loss: 428.8750, Val Loss: 438.7708  
Epoch [310/4000], Train Loss: 420.6180, Val Loss: 429.9001  
Epoch [320/4000], Train Loss: 412.1140, Val Loss: 421.0419  
Epoch [330/4000], Train Loss: 405.7183, Val Loss: 414.2930  
Epoch [340/4000], Train Loss: 396.6264, Val Loss: 406.5574  
Epoch [350/4000], Train Loss: 390.4545, Val Loss: 399.5245  
Epoch [360/4000], Train Loss: 383.7248, Val Loss: 393.4516  
Epoch [370/4000], Train Loss: 378.0196, Val Loss: 389.2910  
Epoch [380/4000], Train Loss: 372.8172, Val Loss: 380.0265  
Epoch [390/4000], Train Loss: 368.0840, Val Loss: 374.1557  
Epoch [400/4000], Train Loss: 362.7235, Val Loss: 374.2974  
Epoch [410/4000], Train Loss: 357.2463, Val Loss: 369.5172  
Epoch [420/4000], Train Loss: 352.7180, Val Loss: 360.7042  
Epoch [430/4000], Train Loss: 347.9333, Val Loss: 355.6990

Epoch [440/4000], Train Loss: 343.2024, Val Loss: 351.0757  
Epoch [450/4000], Train Loss: 340.2503, Val Loss: 346.8278  
Epoch [460/4000], Train Loss: 335.1614, Val Loss: 343.3439  
Epoch [470/4000], Train Loss: 332.5359, Val Loss: 339.5449  
Epoch [480/4000], Train Loss: 329.0076, Val Loss: 334.6169  
Epoch [490/4000], Train Loss: 324.6738, Val Loss: 330.5406  
Epoch [500/4000], Train Loss: 321.7654, Val Loss: 327.0572  
Epoch [510/4000], Train Loss: 318.4358, Val Loss: 322.8938  
Epoch [520/4000], Train Loss: 315.3759, Val Loss: 318.9895  
Epoch [530/4000], Train Loss: 312.0256, Val Loss: 315.3359  
Epoch [540/4000], Train Loss: 309.3525, Val Loss: 312.6183  
Epoch [550/4000], Train Loss: 305.9377, Val Loss: 309.1159  
Epoch [560/4000], Train Loss: 302.1337, Val Loss: 304.8154  
Epoch [570/4000], Train Loss: 299.8845, Val Loss: 300.7813  
Epoch [580/4000], Train Loss: 297.0800, Val Loss: 298.9834  
Epoch [590/4000], Train Loss: 294.7407, Val Loss: 294.9838  
Epoch [600/4000], Train Loss: 291.3507, Val Loss: 292.5641  
Epoch [610/4000], Train Loss: 289.1307, Val Loss: 288.1119  
Epoch [620/4000], Train Loss: 286.0616, Val Loss: 284.8908  
Epoch [630/4000], Train Loss: 283.8226, Val Loss: 281.2082  
Epoch [640/4000], Train Loss: 280.8970, Val Loss: 279.6353  
Epoch [650/4000], Train Loss: 278.5081, Val Loss: 277.2468  
Epoch [660/4000], Train Loss: 275.2970, Val Loss: 272.4575  
Epoch [670/4000], Train Loss: 274.0508, Val Loss: 269.8115  
Epoch [680/4000], Train Loss: 272.5681, Val Loss: 267.6024  
Epoch [690/4000], Train Loss: 270.0841, Val Loss: 264.0202  
Epoch [700/4000], Train Loss: 267.5056, Val Loss: 259.1208  
Epoch [710/4000], Train Loss: 265.4495, Val Loss: 255.3375  
Epoch [720/4000], Train Loss: 263.1166, Val Loss: 255.2786  
Epoch [730/4000], Train Loss: 260.1707, Val Loss: 255.9149  
Epoch [740/4000], Train Loss: 259.7098, Val Loss: 251.5681  
Epoch [750/4000], Train Loss: 257.0754, Val Loss: 245.3743  
Epoch [760/4000], Train Loss: 254.6993, Val Loss: 241.7000  
Epoch [770/4000], Train Loss: 252.8703, Val Loss: 241.0565  
Epoch [780/4000], Train Loss: 250.8164, Val Loss: 239.1893  
Epoch [790/4000], Train Loss: 248.8749, Val Loss: 235.0323  
Epoch [800/4000], Train Loss: 246.8988, Val Loss: 233.9730  
Epoch [810/4000], Train Loss: 245.4286, Val Loss: 232.6353  
Epoch [820/4000], Train Loss: 243.8551, Val Loss: 228.9728  
Epoch [830/4000], Train Loss: 241.4019, Val Loss: 227.3049  
Epoch [840/4000], Train Loss: 239.5529, Val Loss: 225.8664  
Epoch [850/4000], Train Loss: 238.2764, Val Loss: 223.2610  
Epoch [860/4000], Train Loss: 236.8090, Val Loss: 218.5238

Epoch [870/4000], Train Loss: 235.2233, Val Loss: 217.4158  
Epoch [880/4000], Train Loss: 233.4767, Val Loss: 217.7320  
Epoch [890/4000], Train Loss: 231.6711, Val Loss: 217.3340  
Epoch [900/4000], Train Loss: 229.3501, Val Loss: 213.9813  
Epoch [910/4000], Train Loss: 228.2005, Val Loss: 213.6611  
Epoch [920/4000], Train Loss: 226.3165, Val Loss: 210.5754  
Epoch [930/4000], Train Loss: 224.4331, Val Loss: 209.2676  
Epoch [940/4000], Train Loss: 223.2852, Val Loss: 207.7989  
Epoch [950/4000], Train Loss: 221.9013, Val Loss: 202.3709  
Epoch [960/4000], Train Loss: 219.8360, Val Loss: 202.4597  
Epoch [970/4000], Train Loss: 218.0010, Val Loss: 198.2457  
Epoch [980/4000], Train Loss: 217.1879, Val Loss: 195.3857  
Epoch [990/4000], Train Loss: 215.1354, Val Loss: 193.2548  
Epoch [1000/4000], Train Loss: 213.0206, Val Loss: 190.4581  
Epoch [1010/4000], Train Loss: 211.3067, Val Loss: 189.5974  
Epoch [1020/4000], Train Loss: 210.3573, Val Loss: 192.0776  
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Epoch [1040/4000], Train Loss: 206.9423, Val Loss: 185.5899  
Epoch [1050/4000], Train Loss: 205.1693, Val Loss: 183.4603  
Epoch [1060/4000], Train Loss: 203.9469, Val Loss: 180.7608  
Epoch [1070/4000], Train Loss: 202.3957, Val Loss: 181.2276  
Epoch [1080/4000], Train Loss: 201.4997, Val Loss: 178.1205  
Epoch [1090/4000], Train Loss: 199.6372, Val Loss: 176.5981  
Epoch [1100/4000], Train Loss: 198.5518, Val Loss: 175.3873  
Epoch [1110/4000], Train Loss: 196.8762, Val Loss: 174.3162  
Epoch [1120/4000], Train Loss: 196.2135, Val Loss: 173.3125  
Epoch [1130/4000], Train Loss: 194.3036, Val Loss: 171.3059  
Epoch [1140/4000], Train Loss: 193.0226, Val Loss: 168.4846  
Epoch [1150/4000], Train Loss: 192.0900, Val Loss: 166.3214  
Epoch [1160/4000], Train Loss: 190.3935, Val Loss: 165.6931  
Epoch [1170/4000], Train Loss: 189.0933, Val Loss: 164.7315  
Epoch [1180/4000], Train Loss: 187.7266, Val Loss: 162.8180  
Epoch [1190/4000], Train Loss: 186.9007, Val Loss: 161.8801  
Epoch [1200/4000], Train Loss: 185.7356, Val Loss: 159.2818  
Epoch [1210/4000], Train Loss: 184.4393, Val Loss: 158.2003  
Epoch [1220/4000], Train Loss: 182.7735, Val Loss: 156.4669  
Epoch [1230/4000], Train Loss: 181.4821, Val Loss: 156.6378  
Epoch [1240/4000], Train Loss: 180.7059, Val Loss: 155.0530  
Epoch [1250/4000], Train Loss: 179.2459, Val Loss: 153.8369  
Epoch [1260/4000], Train Loss: 178.3188, Val Loss: 151.6919  
Epoch [1270/4000], Train Loss: 176.9521, Val Loss: 151.7181  
Epoch [1280/4000], Train Loss: 176.0576, Val Loss: 150.8133  
Epoch [1290/4000], Train Loss: 174.3492, Val Loss: 148.9969

Epoch [1300/4000], Train Loss: 173.7594, Val Loss: 148.8919  
 Epoch [1310/4000], Train Loss: 172.7791, Val Loss: 146.5303  
 Epoch [1320/4000], Train Loss: 171.1582, Val Loss: 146.5997  
 Epoch [1330/4000], Train Loss: 170.5263, Val Loss: 144.1215  
 Epoch [1340/4000], Train Loss: 168.8886, Val Loss: 144.9699  
 Epoch [1350/4000], Train Loss: 167.9973, Val Loss: 141.2650  
 Epoch [1360/4000], Train Loss: 166.7077, Val Loss: 139.8877  
 Epoch [1370/4000], Train Loss: 166.2939, Val Loss: 141.3412  
 Epoch [1380/4000], Train Loss: 164.6947, Val Loss: 140.1218  
 Epoch [1390/4000], Train Loss: 163.4467, Val Loss: 139.7124  
 Epoch [1400/4000], Train Loss: 162.7966, Val Loss: 137.7644  
 Epoch [1410/4000], Train Loss: 161.7658, Val Loss: 137.4774  
 Epoch [1420/4000], Train Loss: 160.7231, Val Loss: 134.2698  
 Epoch [1430/4000], Train Loss: 159.4350, Val Loss: 136.2363  
 Epoch [1440/4000], Train Loss: 158.7151, Val Loss: 134.6639  
 Epoch [1450/4000], Train Loss: 157.6062, Val Loss: 134.2825  
 Epoch [1460/4000], Train Loss: 156.2660, Val Loss: 130.8835  
 Epoch [1470/4000], Train Loss: 155.9137, Val Loss: 132.7157  
 Epoch [1480/4000], Train Loss: 154.5379, Val Loss: 131.2435  
 Epoch [1490/4000], Train Loss: 153.7037, Val Loss: 129.6104  
 Epoch [1500/4000], Train Loss: 152.9774, Val Loss: 128.5560  
 Epoch [1510/4000], Train Loss: 151.7004, Val Loss: 128.6219  
 Epoch [1520/4000], Train Loss: 150.6979, Val Loss: 126.3337  
 Epoch [1530/4000], Train Loss: 150.1365, Val Loss: 124.1229  
 Epoch [1540/4000], Train Loss: 148.3528, Val Loss: 125.6940  
 Epoch [1550/4000], Train Loss: 147.9403, Val Loss: 122.5712  
 Epoch [1560/4000], Train Loss: 146.6510, Val Loss: 121.2221  
 Epoch [1570/4000], Train Loss: 145.8448, Val Loss: 120.7168  
 Epoch [1580/4000], Train Loss: 144.8011, Val Loss: 123.2362  
 Epoch [1590/4000], Train Loss: 144.2140, Val Loss: 120.5647  
 Epoch [1600/4000], Train Loss: 143.1090, Val Loss: 119.2540  
 Epoch [1610/4000], Train Loss: 142.0329, Val Loss: 118.6189  
 Epoch [1620/4000], Train Loss: 141.2752, Val Loss: 116.8923  
 Epoch [1630/4000], Train Loss: 140.4433, Val Loss: 115.1083  
 Epoch [1640/4000], Train Loss: 139.1991, Val Loss: 116.2727  
 Epoch [1650/4000], Train Loss: 138.7201, Val Loss: 115.9392  
 Epoch [1660/4000], Train Loss: 137.7895, Val Loss: 115.5939  
 Epoch [1670/4000], Train Loss: 136.5574, Val Loss: 114.0230  
 Epoch [1680/4000], Train Loss: 135.9528, Val Loss: 114.4975  
 Epoch [1690/4000], Train Loss: 135.2841, Val Loss: 110.6569  
 Epoch [1700/4000], Train Loss: 134.8039, Val Loss: 115.1600  
 Epoch [1710/4000], Train Loss: 133.5406, Val Loss: 110.0300  
 Epoch [1720/4000], Train Loss: 132.7553, Val Loss: 108.4593

Epoch [1730/4000], Train Loss: 132.0244, Val Loss: 108.3886  
 Epoch [1740/4000], Train Loss: 131.3950, Val Loss: 107.6691  
 Epoch [1750/4000], Train Loss: 130.6855, Val Loss: 108.7865  
 Epoch [1760/4000], Train Loss: 129.5622, Val Loss: 106.1223  
 Epoch [1770/4000], Train Loss: 129.0035, Val Loss: 105.5860  
 Epoch [1780/4000], Train Loss: 128.0325, Val Loss: 103.9554  
 Epoch [1790/4000], Train Loss: 127.5116, Val Loss: 105.6273  
 Epoch [1800/4000], Train Loss: 126.4400, Val Loss: 102.6399  
 Epoch [1810/4000], Train Loss: 125.6601, Val Loss: 103.3804  
 Epoch [1820/4000], Train Loss: 125.4416, Val Loss: 105.8067  
 Epoch [1830/4000], Train Loss: 124.9395, Val Loss: 101.2187  
 Epoch [1840/4000], Train Loss: 123.2253, Val Loss: 104.2556  
 Epoch [1850/4000], Train Loss: 122.7832, Val Loss: 100.3161  
 Epoch [1860/4000], Train Loss: 121.9710, Val Loss: 98.5214  
 Epoch [1870/4000], Train Loss: 121.3527, Val Loss: 98.5841  
 Epoch [1880/4000], Train Loss: 120.6299, Val Loss: 95.7500  
 Epoch [1890/4000], Train Loss: 120.6749, Val Loss: 99.3560  
 Epoch [1900/4000], Train Loss: 119.5486, Val Loss: 97.6784  
 Epoch [1910/4000], Train Loss: 118.3321, Val Loss: 92.3545  
 Epoch [1920/4000], Train Loss: 117.9050, Val Loss: 94.4123  
 Epoch [1930/4000], Train Loss: 117.2739, Val Loss: 93.1113  
 Epoch [1940/4000], Train Loss: 116.2846, Val Loss: 88.5482  
 Epoch [1950/4000], Train Loss: 115.8986, Val Loss: 90.9105  
 Epoch [1960/4000], Train Loss: 115.3080, Val Loss: 93.9559  
 Epoch [1970/4000], Train Loss: 114.3435, Val Loss: 90.4082  
 Epoch [1980/4000], Train Loss: 113.5336, Val Loss: 94.2318  
 Epoch [1990/4000], Train Loss: 113.4553, Val Loss: 96.8833  
 Epoch [2000/4000], Train Loss: 112.2931, Val Loss: 89.5048  
 Epoch [2010/4000], Train Loss: 111.6759, Val Loss: 94.6542  
 Epoch [2020/4000], Train Loss: 111.2247, Val Loss: 91.0629  
 Epoch [2030/4000], Train Loss: 110.4307, Val Loss: 91.1231  
 Epoch [2040/4000], Train Loss: 110.0050, Val Loss: 88.7316  
 Epoch [2050/4000], Train Loss: 109.2240, Val Loss: 89.3921  
 Epoch [2060/4000], Train Loss: 108.3593, Val Loss: 89.8433  
 Epoch [2070/4000], Train Loss: 108.1223, Val Loss: 90.3443  
 Epoch [2080/4000], Train Loss: 107.0611, Val Loss: 86.9198  
 Epoch [2090/4000], Train Loss: 106.6175, Val Loss: 88.7713  
 Epoch [2100/4000], Train Loss: 105.7518, Val Loss: 88.6444  
 Epoch [2110/4000], Train Loss: 105.7235, Val Loss: 89.7381  
 Epoch [2120/4000], Train Loss: 105.1024, Val Loss: 87.4743  
 Epoch [2130/4000], Train Loss: 104.1024, Val Loss: 86.6269  
 Epoch [2140/4000], Train Loss: 103.9082, Val Loss: 88.0413  
 Epoch [2150/4000], Train Loss: 102.7591, Val Loss: 85.2298

Epoch [2160/4000], Train Loss: 102.4836, Val Loss: 84.3741  
Epoch [2170/4000], Train Loss: 101.9873, Val Loss: 84.0700  
Epoch [2180/4000], Train Loss: 101.5353, Val Loss: 83.6846  
Epoch [2190/4000], Train Loss: 100.5013, Val Loss: 81.8236  
Epoch [2200/4000], Train Loss: 99.8078, Val Loss: 85.8560  
Epoch [2210/4000], Train Loss: 99.4545, Val Loss: 81.8619  
Epoch [2220/4000], Train Loss: 99.1633, Val Loss: 81.9100  
Epoch [2230/4000], Train Loss: 98.3155, Val Loss: 81.6756  
Epoch [2240/4000], Train Loss: 97.9388, Val Loss: 82.4595  
Epoch [2250/4000], Train Loss: 97.2953, Val Loss: 82.1583  
Epoch [2260/4000], Train Loss: 96.4588, Val Loss: 79.8386  
Epoch [2270/4000], Train Loss: 96.1209, Val Loss: 80.4036  
Epoch [2280/4000], Train Loss: 96.0188, Val Loss: 79.1964  
Epoch [2290/4000], Train Loss: 95.3891, Val Loss: 79.9859  
Epoch [2300/4000], Train Loss: 94.5486, Val Loss: 79.4242  
Epoch [2310/4000], Train Loss: 94.3102, Val Loss: 79.9428  
Epoch [2320/4000], Train Loss: 93.6289, Val Loss: 78.5922  
Epoch [2330/4000], Train Loss: 92.9661, Val Loss: 78.1629  
Epoch [2340/4000], Train Loss: 92.2733, Val Loss: 80.4315  
Epoch [2350/4000], Train Loss: 91.7731, Val Loss: 79.3922  
Epoch [2360/4000], Train Loss: 91.7519, Val Loss: 77.7873  
Epoch [2370/4000], Train Loss: 90.8322, Val Loss: 78.6464  
Epoch [2380/4000], Train Loss: 90.5798, Val Loss: 75.7892  
Epoch [2390/4000], Train Loss: 89.5495, Val Loss: 78.6463  
Epoch [2400/4000], Train Loss: 89.3860, Val Loss: 78.1047  
Epoch [2410/4000], Train Loss: 89.0039, Val Loss: 78.5845  
Epoch [2420/4000], Train Loss: 88.4657, Val Loss: 75.7842  
Epoch [2430/4000], Train Loss: 88.2265, Val Loss: 76.6274  
Epoch [2440/4000], Train Loss: 87.3137, Val Loss: 75.7389  
Epoch [2450/4000], Train Loss: 86.6753, Val Loss: 78.6994  
Epoch [2460/4000], Train Loss: 87.1207, Val Loss: 79.2834  
Epoch [2470/4000], Train Loss: 85.9596, Val Loss: 76.2952  
Epoch [2480/4000], Train Loss: 85.3464, Val Loss: 71.3577  
Epoch [2490/4000], Train Loss: 85.1605, Val Loss: 73.5715  
Epoch [2500/4000], Train Loss: 84.6268, Val Loss: 73.5383  
Epoch [2510/4000], Train Loss: 84.1133, Val Loss: 74.3282  
Epoch [2520/4000], Train Loss: 83.5839, Val Loss: 75.7406  
Epoch [2530/4000], Train Loss: 83.2210, Val Loss: 77.1210  
Epoch [2540/4000], Train Loss: 82.8623, Val Loss: 73.0023  
Epoch [2550/4000], Train Loss: 82.5890, Val Loss: 72.5696  
Epoch [2560/4000], Train Loss: 82.0369, Val Loss: 74.2347  
Epoch [2570/4000], Train Loss: 81.5016, Val Loss: 74.9981  
Epoch [2580/4000], Train Loss: 81.0995, Val Loss: 70.3764

Epoch [2590/4000], Train Loss: 80.6859, Val Loss: 71.5359  
Epoch [2600/4000], Train Loss: 80.6933, Val Loss: 73.4774  
Epoch [2610/4000], Train Loss: 80.5954, Val Loss: 72.4979  
Epoch [2620/4000], Train Loss: 79.7742, Val Loss: 71.6546  
Epoch [2630/4000], Train Loss: 79.9925, Val Loss: 73.2060  
Epoch [2640/4000], Train Loss: 78.7852, Val Loss: 73.0067  
Epoch [2650/4000], Train Loss: 78.2762, Val Loss: 71.2027  
Epoch [2660/4000], Train Loss: 77.8366, Val Loss: 70.4018  
Epoch [2670/4000], Train Loss: 77.6922, Val Loss: 69.2568  
Epoch [2680/4000], Train Loss: 76.9244, Val Loss: 73.6592  
Epoch [2690/4000], Train Loss: 76.8279, Val Loss: 73.0960  
Epoch [2700/4000], Train Loss: 76.0845, Val Loss: 72.2024  
Epoch [2710/4000], Train Loss: 76.2772, Val Loss: 72.3820  
Epoch [2720/4000], Train Loss: 75.3092, Val Loss: 71.8076  
Epoch [2730/4000], Train Loss: 75.1692, Val Loss: 69.2691  
Epoch [2740/4000], Train Loss: 74.9733, Val Loss: 69.8544  
Epoch [2750/4000], Train Loss: 74.5515, Val Loss: 74.4492  
Epoch [2760/4000], Train Loss: 74.0229, Val Loss: 71.0891  
Epoch [2770/4000], Train Loss: 73.5033, Val Loss: 71.6540  
Epoch [2780/4000], Train Loss: 73.3870, Val Loss: 70.4911  
Epoch [2790/4000], Train Loss: 72.5135, Val Loss: 71.0347  
Epoch [2800/4000], Train Loss: 72.2039, Val Loss: 73.5950  
Epoch [2810/4000], Train Loss: 72.3273, Val Loss: 70.3539  
Epoch [2820/4000], Train Loss: 72.8485, Val Loss: 72.0424  
Epoch [2830/4000], Train Loss: 71.7018, Val Loss: 70.4526  
Epoch [2840/4000], Train Loss: 70.7951, Val Loss: 73.2022  
Epoch [2850/4000], Train Loss: 70.1997, Val Loss: 72.3059  
Epoch [2860/4000], Train Loss: 69.9281, Val Loss: 71.0135  
Epoch [2870/4000], Train Loss: 69.8212, Val Loss: 72.1294  
Epoch [2880/4000], Train Loss: 69.2205, Val Loss: 70.7717  
Epoch [2890/4000], Train Loss: 69.1564, Val Loss: 72.5951  
Epoch [2900/4000], Train Loss: 68.2798, Val Loss: 71.3689  
Epoch [2910/4000], Train Loss: 68.0547, Val Loss: 71.6414  
Epoch [2920/4000], Train Loss: 67.5505, Val Loss: 72.8377  
Epoch [2930/4000], Train Loss: 67.5432, Val Loss: 71.0826  
Epoch [2940/4000], Train Loss: 67.1700, Val Loss: 72.1346  
Epoch [2950/4000], Train Loss: 66.7856, Val Loss: 70.2226  
Epoch [2960/4000], Train Loss: 66.1184, Val Loss: 70.9697  
Epoch [2970/4000], Train Loss: 66.1702, Val Loss: 74.3410  
Epoch [2980/4000], Train Loss: 65.8824, Val Loss: 73.6123  
Epoch [2990/4000], Train Loss: 65.5826, Val Loss: 73.1546  
Epoch [3000/4000], Train Loss: 65.1834, Val Loss: 70.7262  
Epoch [3010/4000], Train Loss: 64.7049, Val Loss: 71.1611



Epoch [3020/4000], Train Loss: 64.1906, Val Loss: 70.3399  
Epoch [3030/4000], Train Loss: 63.6143, Val Loss: 71.2310  
Epoch [3040/4000], Train Loss: 63.9896, Val Loss: 69.8181  
Epoch [3050/4000], Train Loss: 63.7118, Val Loss: 71.8857  
Epoch [3060/4000], Train Loss: 63.2881, Val Loss: 68.5068  
Epoch [3070/4000], Train Loss: 62.9631, Val Loss: 70.0213  
Epoch [3080/4000], Train Loss: 62.2313, Val Loss: 69.1991  
Epoch [3090/4000], Train Loss: 62.4382, Val Loss: 73.1480  
Epoch [3100/4000], Train Loss: 61.7150, Val Loss: 71.7592  
Epoch [3110/4000], Train Loss: 61.2196, Val Loss: 68.6339  
Epoch [3120/4000], Train Loss: 60.8892, Val Loss: 68.6813  
Epoch [3130/4000], Train Loss: 60.5875, Val Loss: 70.5614  
Epoch [3140/4000], Train Loss: 60.7052, Val Loss: 74.2106  
Epoch [3150/4000], Train Loss: 60.0216, Val Loss: 70.5668  
Epoch [3160/4000], Train Loss: 59.9391, Val Loss: 72.6791  
Epoch [3170/4000], Train Loss: 59.1286, Val Loss: 68.5612  
Epoch [3180/4000], Train Loss: 58.9806, Val Loss: 70.7640  
Epoch [3190/4000], Train Loss: 58.6160, Val Loss: 68.0443  
Epoch [3200/4000], Train Loss: 58.5205, Val Loss: 68.0781  
Epoch [3210/4000], Train Loss: 58.2038, Val Loss: 70.3584  
Epoch [3220/4000], Train Loss: 57.5880, Val Loss: 70.8389  
Epoch [3230/4000], Train Loss: 57.2102, Val Loss: 69.5093  
Epoch [3240/4000], Train Loss: 57.0882, Val Loss: 70.0921  
Epoch [3250/4000], Train Loss: 56.9717, Val Loss: 69.6033  
Epoch [3260/4000], Train Loss: 56.3433, Val Loss: 71.2625  
Epoch [3270/4000], Train Loss: 56.3955, Val Loss: 71.2912  
Epoch [3280/4000], Train Loss: 55.7468, Val Loss: 70.1235  
Epoch [3290/4000], Train Loss: 56.0993, Val Loss: 71.4007  
Epoch [3300/4000], Train Loss: 55.3590, Val Loss: 69.3364  
Epoch [3310/4000], Train Loss: 55.0446, Val Loss: 71.2662  
Epoch [3320/4000], Train Loss: 55.6800, Val Loss: 76.7160  
Epoch [3330/4000], Train Loss: 55.0863, Val Loss: 69.8083  
Epoch [3340/4000], Train Loss: 54.1134, Val Loss: 69.4163  
Epoch [3350/4000], Train Loss: 54.0234, Val Loss: 68.9033  
Epoch [3360/4000], Train Loss: 53.5544, Val Loss: 71.2739  
Epoch [3370/4000], Train Loss: 53.7395, Val Loss: 70.9363  
Early stopping triggered at epoch 3371

Final Test Metrics:

test\_loss: 32.5966

rmse: 5.7093

r2: 0.8888

bias: -0.2987

rpd: 2.9992

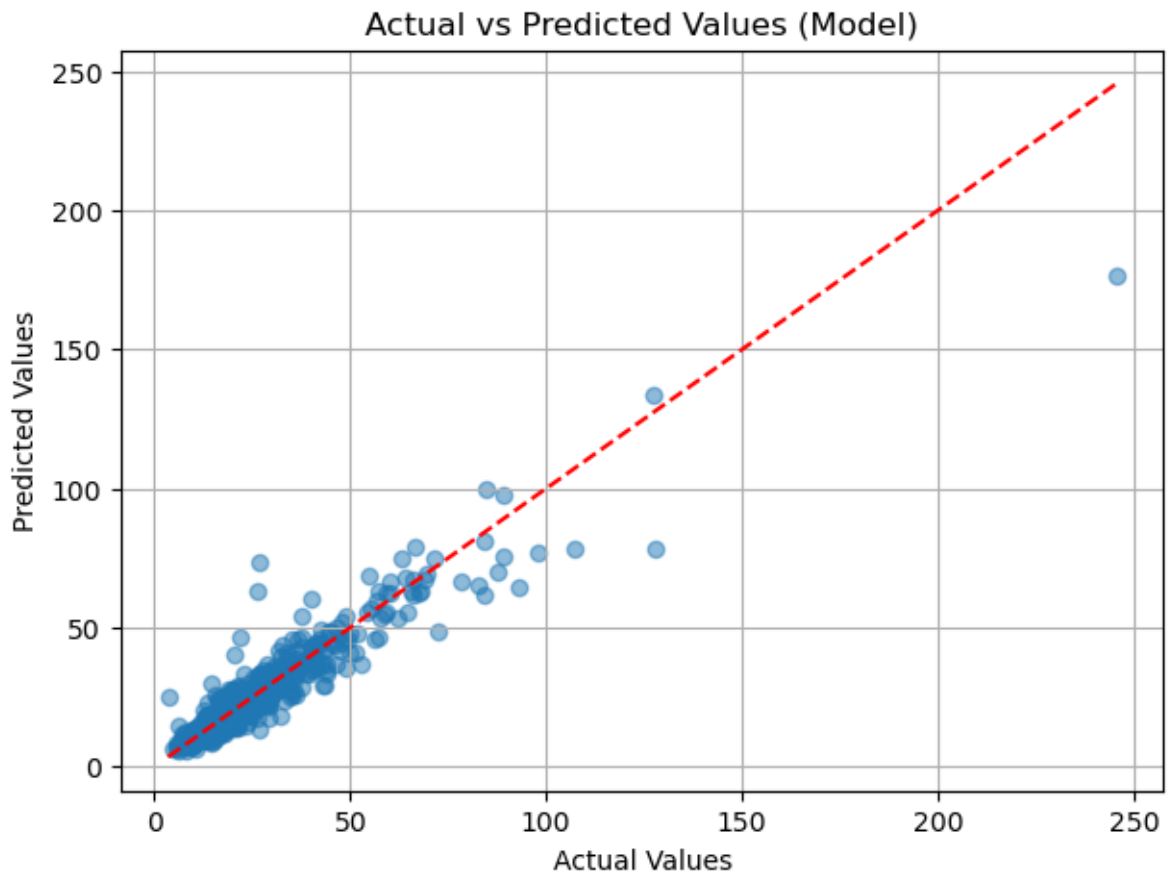


Root Mean Squared Error (RMSE): 5.7093

$R^2$ : 0.8888

Bias: -0.2987

RPD: 2.9992



#### 5.3.2.1 Test base lstm+plsr with lower samples

```
max(mapped_test_indices)
```

2801

```
X_test_test = X_test_pls[mapped_test_indices, :]
```

IndexError: index 844 is out of bounds for axis 0 with size 843

```
X_test_test.shape
```

(843, 48)

```
lstm_plsr_eval = own_functions.evaluate_model(LSTM_plsr_model,  
                                              X_test=X_test_pls, y_test=y_test,  
                                              print_metrics=True, show_plot=True)
```

## 6 Discussion of Results (5 P):

- Briefly discuss your results and interpret them based on the validation metrics for the test set.
- Compare your findings with those of published studies in a similar context.
- Evaluate whether soil VNIR reflectance spectroscopy could serve as a complementary approach for large-scale soil organic carbon assessment in Earth (system) science.

### **Additional Information:**

The length of the discussion section really depends on your results, but as a general guideline, I would expect it to be around one page.

- **Focus on:**
  - directly comparing your different modeling approaches
  - interpreting which performed best based on the validation metrics
- If the results are not as good as expected:
  - consider discussing possible reasons and suggesting ways to improve them
  - (you might find 1-2 examples from the literature helpful here).
- Additionally, you could compare your findings with similar studies that have attempted to model SOC (or related properties) at national or continental scales using spectroscopy—ideally referencing 2-3 relevant publications.
- Finally, reflect on whether and how soil VNIR spectroscopy could contribute to large-scale soil information systems.
  - This is a more theoretical aspect, and you are free in how you approach this point.
  - Important aspects to consider might include:
    - \* a) Model accuracy (What would be considered a good accuracy in this context?)
    - \* b) Data harmonization (Challenges when combining datasets from different providers)
    - \* c) Practical usability (Would end users require programming skills, etc.?)

A recent publication that could provide a useful overview is: Peng et al. (2025): Spectroscopic solutions for generating new global soil information (Link: <https://www.sciencedirect.com/science/article/pii/S2>

# **Part II**

# **Appendix**

## 7 Getting DLR Data

```
import rioxtarray as rxr
import xarray as xr
from odc.stac import load
import pystac_client
import pandas as pd
import geopandas as gpd
import matplotlib.pyplot as plt
import numpy as np
from shapely.geometry import Point
from concurrent.futures import ThreadPoolExecutor, as_completed
from tqdm import tqdm
import os

# Create cache directory
CACHE_DIR = "data/stac_data_cache_full"
os.makedirs(CACHE_DIR, exist_ok=True)

def create_bbox(lon, lat, step=0.000001):
    """Create a bounding box around a point."""
    return [lon - step, lat - step, lon + step, lat + step]

def get_stac_data_for_point(args):
    """Process a single point (for parallel execution)"""
    catalog, collection, measurements, point_idx, lon, lat, bbox_step = args

    # Check if cached result exists
    cache_file = f"{CACHE_DIR}/point_{lon}_{lat}.parquet"
    if os.path.exists(cache_file):
        try:
            return pd.read_parquet(cache_file)
        except Exception as e:
            print(f"Error reading cache file {cache_file}: {e}")
            pass # If cache read fails, continue with regular processing
```

```

try:
    # Create bounding box for this point
    bbox = create_bbox(lon, lat, bbox_step)

    # Search for items
    search = catalog.search(
        collections=collection,
        bbox=bbox,
        datetime="2018-03-01/2020-12-31"
    )

    # Convert search results to list
    items = list(search.items())

    if len(items) > 0:
        # Load the data
        dataset = load(
            items,
            measurements=measurements,
            bbox=bbox,
            resolution=20
        )

        # Convert to dataframe
        data_point = dataset.isel(time=0).to_dataframe().reset_index()

        # Add point metadata
        data_point['point_index'] = point_idx
        data_point['source_lon'] = lon
        data_point['source_lat'] = lat

        # Cache the result
        try:
            data_point.to_parquet(cache_file)
        except Exception as e:
            print(f"Error caching point {point_idx}: {e}")
            pass # If caching fails, continue anyway

        return data_point
    else:
        print(f"No items found for point {point_idx} ({lon}, {lat})")

```



```

        return None
    except Exception as e:
        print(f"Error processing point {point_idx}: {e}")
        return None

def get_all_auxiliary_data(catalog, collection, measurements, long_lat, bbox_step=0.000001):
    """Retrieve STAC data for all points using parallel processing."""

    # Prepare arguments for each point
    args_list = []

    # Create argument list for all points
    for i in range(len(long_lat)):
        args_list.append((
            catalog,
            collection,
            measurements,
            i, # Point index
            long_lat.iloc[i]['GPS_LONG'],
            long_lat.iloc[i]['GPS_LAT'],
            bbox_step
        ))

    # Process points in parallel
    results = []
    with ThreadPoolExecutor(max_workers=max_workers) as executor:
        # Submit all tasks and track with progress bar
        futures = [executor.submit(get_stac_data_for_point, args) for args in args_list]

        for future in tqdm(as_completed(futures), total=len(args_list), desc="Processing p
            result = future.result()
            if result is not None:
                results.append(result)

    # Combine all results
    if not results:
        print("No data retrieved!")
        return None

    points_df = pd.concat(results, ignore_index=True)

```

```

# Create geometry points for GeoDataFrame
geometry_points = [Point(x, y) for x, y in zip(points_df['x'], points_df['y'])]

# Convert to GeoDataFrame
points_gdf = gpd.GeoDataFrame(points_df, geometry=geometry_points, crs=3035)

return points_gdf

dlr_measurements = ["MREF_B02", "MREF_B03", "MREF_B04", "MREF_B05", "MREF_B06", "MREF_B07",
                    "MREF-STD_B02", "MREF-STD_B03", "MREF-STD_B04", "MREF-STD_B05", "MREF-STD_B06", "MREF-STD_B07",
                    "SRC_B02", "SRC_B03", "SRC_B04", "SRC_B05", "SRC_B06", "SRC_B07",
                    "SRC-STD_B02", "SRC-STD_B03", "SRC-STD_B04", "SRC-STD_B05", "SRC-STD_B06", "SRC-STD_B07",
                    "SRC-CI95_B02", "SRC-CI95_B03", "SRC-CI95_B04", "SRC-CI95_B05", "SRC-CI95_B06", "SRC-CI95_B07",
                    "SFREQ-BSF" #, "SFREQ-BSC", "SFREQ-VPC"
                    ]

# Load your data
target_raw = pd.read_csv('data/France_lab.csv')
long_lat = target_raw[['GPS_LONG', 'GPS_LAT']]

# Initialize STAC catalog
dlr_catalog = pystac_client.Client.open("https://geoservice.dlr.de/eoc/ogc/stac/v1")

# Define measurements (you can reduce this list if you don't need all bands)
# dlr_measurements = ["MREF_B02", "MREF_B03", "MREF_B04", "MREF_B08", "MREF_B11", "MREF_B12", "MREF_B13", "MREF_B14", "MREF_B15", "MREF_B16", "MREF_B17", "MREF_B18", "MREF_B19", "MREF_B20", "MREF_B21", "MREF_B22", "MREF_B23", "MREF_B24", "MREF_B25", "MREF_B26", "MREF_B27", "MREF_B28", "MREF_B29", "MREF_B30", "MREF_B31", "MREF_B32", "MREF_B33", "MREF_B34", "MREF_B35", "MREF_B36", "MREF_B37", "MREF_B38", "MREF_B39", "MREF_B40", "MREF_B41", "MREF_B42", "MREF_B43", "MREF_B44", "MREF_B45", "MREF_B46", "MREF_B47", "MREF_B48", "MREF_B49", "MREF_B50", "MREF_B51", "MREF_B52", "MREF_B53", "MREF_B54", "MREF_B55", "MREF_B56", "MREF_B57", "MREF_B58", "MREF_B59", "MREF_B60", "MREF_B61", "MREF_B62", "MREF_B63", "MREF_B64", "MREF_B65", "MREF_B66", "MREF_B67", "MREF_B68", "MREF_B69", "MREF_B70", "MREF_B71", "MREF_B72", "MREF_B73", "MREF_B74", "MREF_B75", "MREF_B76", "MREF_B77", "MREF_B78", "MREF_B79", "MREF_B80", "MREF_B81", "MREF_B82", "MREF_B83", "MREF_B84", "MREF_B85", "MREF_B86", "MREF_B87", "MREF_B88", "MREF_B89", "MREF_B90", "MREF_B91", "MREF_B92", "MREF_B93", "MREF_B94", "MREF_B95", "MREF_B96", "MREF_B97", "MREF_B98", "MREF_B99", "MREF_B100"]

# Define collection
dlr_collection = ["S2-soilsuite-europe-2018-2022-P5Y"]

# # Process all points (consider using a subset for testing: long_lat.iloc[:10])
# results = get_all_auxiliary_data(
#     catalog=dlr_catalog,
#     collection=dlr_collection,
#     measurements=dlr_measurements,
#     long_lat=long_lat,
#     bbox_step=0.000001,
#     max_workers=4 # Adjust based on your CPU and bandwidth
# )

# # Save the results

```

```
# if results is not None:
#     results.to_parquet("data/auxiliary_data_results_full.parquet")
#     print("Data saved successfully")
```

Processing points: 15%| | 413/2807 [19:17<1:14:54, 1.88s/it]

Error processing point 416: ('Connection aborted.', RemoteDisconnected('Remote end closed connection'))

Processing points: 18%| | 493/2807 [23:15<2:07:44, 3.31s/it]

Error processing point 497: ('Connection aborted.', RemoteDisconnected('Remote end closed connection'))

Processing points: 18%| | 511/2807 [24:02<1:18:04, 2.04s/it]

No items found for point 513 (88.888888, 88.888888)

Processing points: 33%| | 933/2807 [43:10<1:02:52, 2.01s/it]

No items found for point 935 (88.888888, 88.888888)

Processing points: 59%| | 1668/2807 [1:16:21<36:45, 1.94s/it]

Error processing point 1671: ('Connection aborted.', RemoteDisconnected('Remote end closed connection'))

Processing points: 78%| | 2201/2807 [1:40:42<22:58, 2.27s/it]

Error processing point 2204: ('Connection aborted.', RemoteDisconnected('Remote end closed connection'))

Processing points: 86%| | 2406/2807 [1:50:21<18:09, 2.72s/it]

Error processing point 2410: ('Connection aborted.', RemoteDisconnected('Remote end closed connection'))

Processing points: 92%| | 2582/2807 [1:58:41<14:03, 3.75s/it]

Error processing point 2586: ('Connection aborted.', RemoteDisconnected('Remote end closed connection'))

Processing points: 100%| | 2807/2807 [2:08:47<00:00, 2.75s/it]

Data saved successfully

## 7.1 Update missing data

```
def update_missing_dlr_data(
    target_raw_path='data/France_lab.csv',
    input_parquet="data/auxiliary_data_results_full.parquet",
    output_parquet="data/auxiliary_data_results_updated.parquet",
    cache_dir="data/stac_data_cache_full",
    max_workers=4,
    max_retries=3
):
    """
    Find and update missing DLR data points

    Args:
        target_raw_path: Path to the CSV containing all target points (with GPS_LONG, GPS_
        input_parquet: Path to the existing parquet file containing the processed results
        output_parquet: Path to save the updated parquet file (if None, overwrites input_p
        cache_dir: Directory containing cached point data
        max_workers: Maximum number of parallel workers
        max_retries: Maximum number of retry attempts for each point

    Returns:
        Updated GeoDataFrame with all available points
    """
    import pandas as pd
    import geopandas as gpd
    import os
    import time
    import random
    from shapely.geometry import Point
    from concurrent.futures import ThreadPoolExecutor, as_completed
    from tqdm import tqdm
    import pystac_client

    if output_parquet is None:
        output_parquet = input_parquet

    # Load original target points
    print(f"Loading original target points from {target_raw_path}")
    target_raw = pd.read_csv(target_raw_path)
    original_points = target_raw[['GPS_LONG', 'GPS_LAT']]
```

```

# Try to load existing results
if os.path.exists(input_parquet):
    try:
        print(f"Loading existing results from {input_parquet}")
        existing_data = gpd.read_parquet(input_parquet)
        print(f"Loaded {len(existing_data)} points from existing data")

        # Extract unique source coordinates from the existing data
        processed_coords = set(zip(existing_data['source_lon'], existing_data['source_lat']))
        print(f"Found {len(processed_coords)} unique processed coordinates")
    except Exception as e:
        print(f"Error loading existing results: {e}")
        existing_data = None
        processed_coords = set()
else:
    print(f"No existing results found at {input_parquet}")
    existing_data = None
    processed_coords = set()

# Identify missing points
missing_points = []
for idx, row in original_points.iterrows():
    point_coord = (row['GPS_LONG'], row['GPS_LAT'])
    if point_coord not in processed_coords:
        missing_points.append((idx, point_coord[0], point_coord[1]))

print(f"Found {len(missing_points)} missing points out of {len(original_points)} total")

if not missing_points:
    print("No missing points to process!")
    return existing_data

# Initialize STAC catalog
dlr_catalog = pystac_client.Client.open("https://geoservice.dlr.de/eoc/ogc/stac/v1")

# Define collection
dlr_collection = ["S2-soilsuite-europe-2018-2022-P5Y"]

# Define measurements
dlr_measurements = [
    "MREF_B02", "MREF_B03", "MREF_B04", "MREF_B05", "MREF_B06", "MREF_B07", "MREF_B08"
]

```



```

        print(f"Error processing point {idx} ({lon}, {lat}) - Attempt {retry+1}/{max_retries}")

        if retry < max_retries - 1:
            sleep_time = 5 + random.random() * 10
            print(f"Waiting {sleep_time:.1f} seconds before retry...")
            time.sleep(sleep_time)

    print(f"Failed to process point {idx} ({lon}, {lat}) after {max_retries} attempts")
    return None

# Process missing points in parallel
new_results = []
with ThreadPoolExecutor(max_workers=max_workers) as executor:
    # Submit all tasks and track with progress bar
    futures = [executor.submit(process_point_with_retries, point) for point in missing_points]

    for future in tqdm(as_completed(futures), total=len(missing_points), desc="Processing missing points"):
        result = future.result()
        if result is not None:
            new_results.append(result)

print(f"Successfully processed {len(new_results)} out of {len(missing_points)} missing points")

# Combine with existing results
if new_results:
    # Combine all new results
    new_points_df = pd.concat(new_results, ignore_index=True)

    # Create geometry points for GeoDataFrame
    geometry_points = [Point(x, y) for x, y in zip(new_points_df['x'], new_points_df['y'])]

    # Convert to GeoDataFrame
    new_points_gdf = gpd.GeoDataFrame(new_points_df, geometry=geometry_points, crs=3003)

    # Combine with existing data if available
    if existing_data is not None:
        combined_gdf = pd.concat([existing_data, new_points_gdf], ignore_index=True)
    else:
        combined_gdf = new_points_gdf

# Save the updated results

```

```

        combined_gdf.to_parquet(output_parquet)
        print(f"Updated data saved to {output_parquet} ({len(combined_gdf)} total points)")

        return combined_gdf
    else:
        print("No new data to add")
        return existing_data

# Load your original data points
target_raw = pd.read_csv('data/France_lab.csv')
long_lat = target_raw[['GPS_LONG', 'GPS_LAT']]

# Update missing points
updated_results = update_missing_dlr_data(
    target_raw_path='data/France_lab.csv',
    input_parquet="data/auxiliary_data_results_full.parquet",
    output_parquet="data/auxiliary_data_results_full_updated.parquet", # Optional: set to
    cache_dir="data/stac_data_cache_full",
    max_workers=4,
    max_retries=3
)

```

Loading original target points from data/France\_lab.csv  
 Loading existing results from data/auxiliary\_data\_results\_full.parquet  
 Loaded 2799 points from existing data  
 Found 2797 unique processed coordinates  
 Found 8 missing points out of 2807 total points

Processing missing points: 0%| | 0/8 [00:00<?, ?it/s]

Successfully processed point 497 (0.57576, 46.423743)Successfully processed point 416 (-1.278

Successfully processed point 1671 (-2.833854, 48.198354)  
 Successfully processed point 2204 (3.056281, 46.46886)  
 Successfully processed point 2410 (-2.852118, 47.522143)  
 Successfully processed point 2586 (-0.317878, 48.826356)  
 No items found for point 513 (88.888888, 88.888888)  
 No data found for point 513 (88.888888, 88.888888) - Attempt 1/3  
 Waiting 13.7 seconds before retry...  
 No items found for point 935 (88.888888, 88.888888)  
 No data found for point 935 (88.888888, 88.888888) - Attempt 1/3



Waiting 13.2 seconds before retry...

No items found for point 935 (88.888888, 88.888888)

No data found for point 935 (88.888888, 88.888888) - Attempt 2/3

Waiting 7.1 seconds before retry...

No items found for point 513 (88.888888, 88.888888)

No data found for point 513 (88.888888, 88.888888) - Attempt 2/3

Waiting 8.5 seconds before retry...

Processing missing points: 88%| | 7/8 [00:21<00:03, 3.01s/it]

No items found for point 935 (88.888888, 88.888888)

No data found for point 935 (88.888888, 88.888888) - Attempt 3/3

Failed to process point 935 (88.888888, 88.888888) after 3 attempts

Processing missing points: 100%| | 8/8 [00:22<00:00, 2.84s/it]

No items found for point 513 (88.888888, 88.888888)

No data found for point 513 (88.888888, 88.888888) - Attempt 3/3

Failed to process point 513 (88.888888, 88.888888) after 3 attempts

Successfully processed 6 out of 8 missing points

Updated data saved to data/auxiliary\_data\_results\_full\_updated.parquet (2805 total points)

## 8 Getting Soil Grid Data

```
import pandas as pd
import requests
import json
import time
import random
import os
import concurrent.futures
from tqdm import tqdm
import threading

# Add a lock to prevent race conditions when saving data
save_lock = threading.Lock()

def get_soilgrids_point(lon, lat, point_idx, properties=None, max_retries=3):
    """Get SoilGrids data for a single point with correct field mapping"""
    if properties is None:
        properties = ['soc', 'clay', 'sand', 'silt', 'bdod', 'phh2o']

    url = "https://rest.isric.org/soilgrids/v2.0/properties/query"
    params = {
        'lon': lon,
        'lat': lat,
        'property': properties,
        'depth': ['0-5cm', '5-15cm', '15-30cm'],
        'value': ['mean']
    }

    for retry in range(max_retries):
        try:
            response = requests.get(url, params=params)

            # Handle rate limiting
            if response.status_code == 429:
                wait_time = 15 + random.random() * 15
```

```

        #print(f"Rate limited for point {point_idx}, waiting {wait_time:.1f} seconds")
        time.sleep(wait_time)
        continue

    if response.status_code == 200:
        data = response.json()

        # Start with basic info
        result = {'point_index': point_idx, 'lon': lon, 'lat': lat}

        # Extract data using the correct field structure
        if 'properties' in data and 'layers' in data['properties']:
            for layer in data['properties']['layers']:
                # Get property name
                prop_name = layer.get('name', 'unknown')

                for depth in layer.get('depths', []):
                    # Get depth label (which is the string format we need)
                    depth_label = depth.get('label', 'unknown')

                    # Clean the depth label for column naming
                    clean_depth = depth_label.replace('-', '_to_')

                    # Extract values
                    for value_type, value in depth.get('values', {}).items():
                        column_name = f"{prop_name}_{clean_depth}_{value_type}"
                        result[column_name] = value

        # Debug print to verify data is being captured correctly
        #print(f"Retrieved data for point {point_idx}: {lon}, {lat}")
        return result
    else:
        #print(f"Error for point {point_idx}: Status code {response.status_code}")
        if retry < max_retries - 1:
            wait_time = 10 * (retry + 1)
            #print(f"Retrying in {wait_time} seconds...")
            time.sleep(wait_time)
        else:
            return {'point_index': point_idx, 'lon': lon, 'lat': lat,
                    'error': f"Status {response.status_code}"}

```

```

    except Exception as e:
        #print(f"Exception for point {point_idx}: {str(e)}")
        if retry < max_retries - 1:
            wait_time = 10 * (retry + 1)
            #print(f"Retrying in {wait_time} seconds...")
            time.sleep(wait_time)
        else:
            return {'point_index': point_idx, 'lon': lon, 'lat': lat,
                    'error': f"Exception: {str(e)}"}

    return {'point_index': point_idx, 'lon': lon, 'lat': lat,
            'error': "Max retries reached"}

def process_point(args):
    """Wrapper function for concurrent processing"""
    lon, lat, idx, properties = args
    # Add jitter to avoid all workers hitting the API simultaneously
    time.sleep(random.random() * 2)
    return get_soilgrids_point(lon, lat, idx, properties)

def save_checkpoint(results, filename, verbose=False):
    """Save results to a checkpoint file using a lock to prevent race conditions"""
    with save_lock:
        try:
            df_results = pd.DataFrame(results)
            # First write to a temporary file, then rename to avoid partial writes
            temp_file = f"{filename}.temp"
            df_results.to_csv(temp_file, index=False)
            os.replace(temp_file, filename)
            if verbose:
                print(f"Saved checkpoint with {len(results)} points to {filename}")
        except Exception as e:
            print(f"Error saving checkpoint: {str(e)}")

def get_soilgrids_parallel(coordinates_df, num_workers=4, lon_col='GPS_LONG', lat_col='GPS_LAT',
                           properties=None, cache_file='soilgrids_parallel.csv',
                           checkpoint_interval=10, debug=False):
    """
    Retrieve soil data for multiple points in parallel using multiple workers

    Args:
    """

```

```

coordinates_df: DataFrame with coordinates
num_workers: Number of parallel workers (default: 4)
lon_col: Column name for longitude
lat_col: Column name for latitude
properties: List of SoilGrids properties to retrieve
cache_file: Output file name
checkpoint_interval: Save intermediate results every N points
debug: Enable additional debug output
"""
if properties is None:
    properties = ['soc', 'clay', 'sand', 'silt', 'bdod', 'phh2o']

# Print the input data to verify it's correct
if debug:
    print("Input coordinate data sample:")
    print(coordinates_df.head())
    print(f"Longitude column: {lon_col}, Latitude column: {lat_col}")

# Check for existing cache to resume from
results = []

if os.path.exists(cache_file):
    try:
        existing_df = pd.read_csv(cache_file)
        if len(existing_df) > 0:
            results = existing_df.to_dict('records')
            processed_indices = set(existing_df['point_index'].unique())
            print(f"Found {len(processed_indices)} already processed points in {cache_file}")
            coordinates_df = coordinates_df[~coordinates_df.index.isin(processed_indices)]
            print(f"Remaining points to process: {len(coordinates_df)}")
        except Exception as e:
            print(f"Error reading existing cache: {str(e)}. Starting from scratch.")

if len(coordinates_df) == 0:
    print("All points already processed!")
    return pd.DataFrame(results)

# Prepare arguments for parallel processing
args_list = []
for idx, row in coordinates_df.iterrows():
    # Verify and clean coordinate values

```

```

    try:
        lon = float(row[lon_col])
        lat = float(row[lat_col])
        args_list.append((lon, lat, idx, properties))
        if debug and len(args_list) <= 5:
            print(f"Prepared point {idx}: lon={lon}, lat={lat}")
    except (ValueError, TypeError) as e:
        print(f"Error with coordinates at index {idx}: {e}")
        print(f"Row data: {row}")

print(f"Processing {len(args_list)} points with {num_workers} workers")

completed_count = 0

# Use ThreadPoolExecutor for parallel HTTP requests
with concurrent.futures.ThreadPoolExecutor(max_workers=num_workers) as executor:
    # Submit all tasks
    future_to_args = {executor.submit(process_point, args): args for args in args_list}

    # Use tqdm for a progress bar
    for future in tqdm(concurrent.futures.as_completed(future_to_args), total=len(args_list)):
        args = future_to_args[future]
        point_idx = args[2]

        try:
            result = future.result()
            if result:
                results.append(result)
                completed_count += 1

            # Save intermediate results periodically
            if completed_count % checkpoint_interval == 0:
                save_checkpoint(results, cache_file)

        except Exception as e:
            print(f"\nError processing point {point_idx}: {str(e)}")

# Save final results
save_checkpoint(results, cache_file, verbose=False)

# Verify the final output

```

```

try:
    final_df = pd.read_csv(cache_file)
    print(f"Final output has {len(final_df)} rows and {len(final_df.columns)} columns")
    print("Column names:", final_df.columns.tolist())
    print("First few rows:")
    print(final_df.head())
except Exception as e:
    print(f"Error verifying final output: {str(e)}")

return pd.DataFrame(results)

# Example usage:
# df = pd.read_csv('coordinates.csv', index_col=0) # Set the first column as index if tha
# results = get_soilgrids_parallel(df, num_workers=4)

# Load your data
target_raw = pd.read_csv('data/France_lab.csv')
long_lat = target_raw[['GPS_LONG', 'GPS_LAT']]
get_soilgrids_parallel(long_lat, num_workers=4, properties=['soc', 'clay', 'sand', 'silt',

```

Found 670 already processed points in soilgrids\_parallel.csv  
 Remaining points to process: 2137  
 Processing 2137 points with 4 workers

100%| | 2137/2137 [1:41:01<00:00, 2.84s/it]

Final output has 2807 rows and 22 columns  
 Column names: ['point\_index', 'lon', 'lat', 'bdod\_0\_to\_5cm\_mean', 'bdod\_5\_to\_15cm\_mean', 'bdod\_15\_to\_30cm\_mean', 'clay\_0\_to\_5cm\_mean', 'clay\_5\_to\_15cm\_mean', 'sand\_0\_to\_5cm\_mean', 'sand\_5\_to\_15cm\_mean', 'silt\_0\_to\_5cm\_mean', 'silt\_5\_to\_15cm\_mean']  
 First few rows:

	point_index	lon	lat	bdod_0_to_5cm_mean	bdod_5_to_15cm_mean	\
0	1	4.584692	45.816720	125.0	134.0	
1	0	4.680379	45.893933	128.0	138.0	
2	3	4.601575	45.908022	133.0	140.0	
3	2	4.671533	45.983716	129.0	139.0	
4	6	4.439863	46.224665	102.0	116.0	

	bdod_15_to_30cm_mean	clay_0_to_5cm_mean	clay_5_to_15cm_mean	\
0	141.0	250.0	270.0	
1	141.0	303.0	319.0	
2	144.0	247.0	268.0	
3	143.0	249.0	254.0	

4	121.0	188.0	172.0
	clay_15_to_30cm_mean	phh2o_0_to_5cm_mean	... sand_0_to_5cm_mean \
0	302.0	58.0	... 375.0
1	338.0	62.0	... 263.0
2	288.0	60.0	... 334.0
3	300.0	63.0	... 305.0
4	205.0	52.0	... 505.0
	sand_5_to_15cm_mean	sand_15_to_30cm_mean	silt_0_to_5cm_mean \
0	366.0	366.0	375.0
1	243.0	275.0	434.0
2	320.0	329.0	418.0
3	295.0	313.0	446.0
4	514.0	494.0	306.0
	silt_5_to_15cm_mean	silt_15_to_30cm_mean	soc_0_to_5cm_mean \
0	364.0	332.0	489.0
1	438.0	387.0	467.0
2	412.0	383.0	401.0
3	451.0	387.0	422.0
4	314.0	301.0	786.0
	soc_5_to_15cm_mean	soc_15_to_30cm_mean	error
0	249.0	246.0	NaN
1	254.0	182.0	NaN
2	289.0	153.0	NaN
3	271.0	154.0	NaN
4	620.0	239.0	NaN

[5 rows x 22 columns]

	point_index	lon	lat	bdod_0_to_5cm_mean	bdod_5_to_15cm_mean	bdod_15_to_20cm_mean
0	1	4.584692	45.816720	125.0	134.0	141.0
1	0	4.680379	45.893933	128.0	138.0	141.0
2	3	4.601575	45.908022	133.0	140.0	144.0
3	2	4.671533	45.983716	129.0	139.0	143.0
4	6	4.439863	46.224665	102.0	116.0	121.0
...	...	...	...	...	...	...
2802	2803	5.058028	45.713629	131.0	147.0	150.0
2803	2806	4.784826	45.881063	128.0	137.0	141.0



	point_index	lon	lat	bdod_0_to_5cm_mean	bdod_5_to_15cm_mean	bdod_15_
2804	2805	4.381513	45.788303	124.0	135.0	137.0
2805	2800	4.718750	45.498638	119.0	129.0	135.0
2806	2799	4.578846	45.617959	NaN	NaN	NaN

## 8.1 Update

```
def update_missing_soilgrids_data(csv_file, output_file=None, max_retries=5, delay_between
    """
    Update missing data in a SoilGrids CSV file

    Args:
        csv_file: Path to the CSV file with missing data
        output_file: Path to save the updated CSV (default: overwrite input file)
        max_retries: Maximum number of retries for failed API calls
        delay_between_retries: Delay in seconds between retries

    Returns:
        DataFrame with the updated data
    """
    import pandas as pd
    import time
    import random
    import numpy as np

    if output_file is None:
        output_file = csv_file

    # Load the CSV file and force column types
    print(f"Loading data from {csv_file}...")
    df = pd.read_csv(csv_file, header=None)

    # Determine data types for all columns
    dtypes = df.dtypes
    print(f"Column data types: {dtypes}")

    # Identify rows with missing data (rows with mostly empty values)
    # Consider both NaN values and empty strings as missing
    missing_mask = ((df.iloc[:, 3:].isna()) | (df.iloc[:, 3:] == "")).sum(axis=1) > (df.sh
```

```

missing_indices = df[missing_mask].index

print(f"Found {len(missing_indices)} rows with missing data")

if len(missing_indices) == 0:
    print("No missing data to update!")
    return df

# Prepare a results list to store updated rows
updated_rows = []

# Process each row with missing data
for idx in missing_indices:
    row = df.iloc[idx]
    point_idx = row[0]
    lon = row[1]
    lat = row[2]

    print(f"Processing missing data for point {point_idx} at coordinates {lon}, {lat}")

    # Make API call with retries
    for retry in range(max_retries):
        try:
            result = get_soilgrids_point(lon, lat, point_idx)

            if 'error' in result:
                print(f"Attempt {retry+1}/{max_retries} failed: {result.get('error')}")

                # If we've reached the max retries, save what we have
                if retry == max_retries - 1:
                    print(f"Failed to update point {point_idx} after {max_retries} attempts")
                    break

                # Wait before retrying
                sleep_time = delay_between_retries + random.random() * 10
                print(f"Retrying in {sleep_time:.1f} seconds...")
                time.sleep(sleep_time)
                continue

        except Exception as e:
            print(f"Error: {e}")

    # Create a new row with the correct data types
    updated_row = row.copy()

```

```

# Set the basic fields (point_idx, lon, lat)
# Convert to the same type as the original DataFrame to avoid warnings
updated_row[0] = point_idx # This should already be the correct type
updated_row[1] = lon        # This should already be the correct type
updated_row[2] = lat        # This should already be the correct type

# Map the result fields to the appropriate columns in the dataframe
soil_properties = ['soc', 'clay', 'sand', 'silt', 'bdod', 'phh2o']
depths = ['0_to_5cm', '5_to_15cm', '15_to_30cm']

# Assuming the columns in the original DataFrame follow this order:
column_idx = 3 # Start after point_idx, lon, lat
for prop in soil_properties:
    for depth in depths:
        column_name = f"{prop}_{depth}_mean"
        if column_name in result and column_idx < len(df.columns):
            # Try to match the data type
            value = result[column_name]
            if pd.api.types.is_float_dtype(dtypes[column_idx]):
                value = float(value) if value is not None else np.nan
            elif pd.api.types.is_integer_dtype(dtypes[column_idx]):
                value = int(value) if value is not None else np.nan
            updated_row[column_idx] = value
            column_idx += 1

# Update the DataFrame
df.iloc[idx] = updated_row
print(f"Successfully updated point {point_idx}")

# Add a small delay to avoid rate limiting
time.sleep(2 + random.random() * 3)
break

except Exception as e:
    print(f"Error updating point {point_idx}: {str(e)}")

    if retry < max_retries - 1:
        sleep_time = delay_between_retries + random.random() * 10
        print(f"Retrying in {sleep_time:.1f} seconds...")
        time.sleep(sleep_time)
    else:

```

```

        print(f"Failed to update point {point_idx} after {max_retries} attempts")

    # Save the updated DataFrame
    print(f"Saving updated data to {output_file}...")
    df.to_csv(output_file, index=False, header=False)

    return df

# Update the missing data
updated_df = update_missing_soilgrids_data(
    csv_file='data/soilgrids_parallel.csv',
    output_file='data/soilgrids_updated.csv',
    max_retries=5,
    delay_between_retries=20
)

```

Loading data from data/soilgrids\_parallel.csv...

Column data types: 0      object

```

1      object
2      object
3      object
4      object
5      object
6      object
7      object
8      object
9      object
10     object
11     object
12     object
13     object
14     object
15     object
16     object
17     object
18     object
19     object
20     object
21     object

```

dtype: object

Found 103 rows with missing data

Processing missing data for point 155 at coordinates 0.669178, 49.855175

Successfully updated point 155  
Processing missing data for point 191 at coordinates 2.743706, 48.544291  
Successfully updated point 191  
Processing missing data for point 190 at coordinates 2.557593, 48.513858  
Successfully updated point 190  
Processing missing data for point 216 at coordinates 3.131174, 48.695394  
Successfully updated point 216  
Processing missing data for point 250 at coordinates -0.054073, 46.837853  
Successfully updated point 250  
Processing missing data for point 297 at coordinates 2.737896, 49.699723  
Successfully updated point 297  
Processing missing data for point 338 at coordinates 5.884201, 48.020614  
Successfully updated point 338  
Processing missing data for point 365 at coordinates 4.987468, 44.229435  
Successfully updated point 365  
Processing missing data for point 398 at coordinates 1.13659, 43.97067  
Successfully updated point 398  
Processing missing data for point 397 at coordinates 1.33483, 44.15072  
Successfully updated point 397  
Processing missing data for point 396 at coordinates 1.4312, 44.17679  
Successfully updated point 396  
Processing missing data for point 451 at coordinates -4.271489, 47.855326  
Successfully updated point 451  
Processing missing data for point 466 at coordinates 0.381898, 46.769025  
Successfully updated point 466  
Processing missing data for point 491 at coordinates 0.237318, 46.266361  
Successfully updated point 491  
Processing missing data for point 513 at coordinates 88.888888, 88.888888  
Successfully updated point 513  
Processing missing data for point 511 at coordinates 3.00959, 48.2002  
Successfully updated point 511  
Processing missing data for point 512 at coordinates 3.18728, 48.08494  
Successfully updated point 512  
Processing missing data for point 555 at coordinates 2.046038, 48.134749  
Successfully updated point 555  
Processing missing data for point 574 at coordinates 6.0446, 49.39529  
Successfully updated point 574  
Processing missing data for point 605 at coordinates 1.121382, 45.981392  
Successfully updated point 605  
Processing missing data for point 622 at coordinates 1.139869, 43.299735  
Successfully updated point 622  
Processing missing data for point 627 at coordinates 2.207169, 46.193274  
Successfully updated point 627

Processing missing data for point 668 at coordinates -1.359804, 47.234471  
Successfully updated point 668  
Processing missing data for point 695 at coordinates -0.3349, 45.15926  
Successfully updated point 695  
Processing missing data for point 722 at coordinates 1.347223, 43.571493  
Successfully updated point 722  
Processing missing data for point 759 at coordinates 4.11086, 43.98437  
Successfully updated point 759  
Processing missing data for point 762 at coordinates 4.80933, 43.98572  
Successfully updated point 762  
Processing missing data for point 788 at coordinates 0.089928, 43.929543  
Successfully updated point 788  
Processing missing data for point 787 at coordinates 0.870324, 43.911071  
Successfully updated point 787  
Processing missing data for point 838 at coordinates 3.1851, 43.36619  
Successfully updated point 838  
Processing missing data for point 856 at coordinates 5.092115, 47.879903  
Successfully updated point 856  
Processing missing data for point 904 at coordinates -1.875838, 48.306003  
Successfully updated point 904  
Processing missing data for point 935 at coordinates 88.888888, 88.888888  
Successfully updated point 935  
Processing missing data for point 923 at coordinates 6.510341, 48.672605  
Successfully updated point 923  
Processing missing data for point 1012 at coordinates 5.384717, 47.009183  
Successfully updated point 1012  
Processing missing data for point 1031 at coordinates 0.98026, 47.88937  
Successfully updated point 1031  
Processing missing data for point 1057 at coordinates 1.77986, 47.60863  
Successfully updated point 1057  
Processing missing data for point 1056 at coordinates 1.106791, 47.62817  
Successfully updated point 1056  
Processing missing data for point 1081 at coordinates 4.05244, 45.73408  
Successfully updated point 1081  
Processing missing data for point 1110 at coordinates 4.31513, 45.188658  
Successfully updated point 1110  
Processing missing data for point 1244 at coordinates 5.967521, 48.996453  
Successfully updated point 1244  
Processing missing data for point 1246 at coordinates 5.634411, 45.251803  
Successfully updated point 1246  
Processing missing data for point 1269 at coordinates 1.48663, 46.78984  
Successfully updated point 1269  
Processing missing data for point 1280 at coordinates 1.17236, 46.6196

Successfully updated point 1280  
Processing missing data for point 1272 at coordinates 1.35562, 47.10523  
Successfully updated point 1272  
Processing missing data for point 1333 at coordinates -0.95724, 43.623243  
Successfully updated point 1333  
Processing missing data for point 1351 at coordinates -0.239878, 43.806771  
Successfully updated point 1351  
Processing missing data for point 1361 at coordinates 2.819498, 44.916088  
Successfully updated point 1361  
Processing missing data for point 1399 at coordinates 4.054361, 48.730593  
Successfully updated point 1399  
Processing missing data for point 1396 at coordinates 4.300754, 48.959924  
Successfully updated point 1396  
Processing missing data for point 1418 at coordinates -0.757008, 48.058626  
Successfully updated point 1418  
Processing missing data for point 1465 at coordinates -1.305934, 48.566394  
Successfully updated point 1465  
Processing missing data for point 1493 at coordinates 1.564248, 48.749983  
Successfully updated point 1493  
Processing missing data for point 1515 at coordinates 0.879868, 48.297504  
Successfully updated point 1515  
Processing missing data for point 1513 at coordinates 1.966878, 48.291714  
Successfully updated point 1513  
Processing missing data for point 1507 at coordinates 1.600771, 48.047341  
Successfully updated point 1507  
Processing missing data for point 1546 at coordinates 5.05454, 44.32302  
Successfully updated point 1546  
Processing missing data for point 1549 at coordinates 5.13098, 44.30854  
Successfully updated point 1549  
Processing missing data for point 1575 at coordinates 6.666943, 47.128374  
Successfully updated point 1575  
Processing missing data for point 1576 at coordinates 6.559288, 47.161011  
Successfully updated point 1576  
Processing missing data for point 1645 at coordinates -3.255429, 48.239248  
Successfully updated point 1645  
Processing missing data for point 1648 at coordinates -2.951216, 48.439631  
Successfully updated point 1648  
Processing missing data for point 1751 at coordinates -0.345346, 46.0298  
Successfully updated point 1751  
Processing missing data for point 1773 at coordinates -0.514265, 45.559151  
Successfully updated point 1773  
Processing missing data for point 1851 at coordinates 0.21301, 45.683683  
Successfully updated point 1851

Processing missing data for point 1829 at coordinates 0.554783, 45.950545  
Successfully updated point 1829  
Processing missing data for point 1898 at coordinates -0.246134, 49.141341  
Successfully updated point 1898  
Processing missing data for point 1902 at coordinates 0.091428, 49.117383  
Successfully updated point 1902  
Processing missing data for point 1930 at coordinates 4.792664, 43.894531  
Successfully updated point 1930  
Processing missing data for point 1938 at coordinates 4.664076, 43.399791  
Successfully updated point 1938  
Processing missing data for point 1944 at coordinates 4.764023, 43.386851  
Successfully updated point 1944  
Processing missing data for point 1957 at coordinates 3.11161, 44.19392  
Successfully updated point 1957  
Processing missing data for point 2079 at coordinates 1.59067, 49.07755  
Successfully updated point 2079  
Processing missing data for point 2083 at coordinates 4.7675, 49.721748  
Successfully updated point 2083  
Processing missing data for point 2134 at coordinates 7.164566, 43.716186  
Successfully updated point 2134  
Processing missing data for point 2204 at coordinates 3.056281, 46.46886  
Successfully updated point 2204  
Processing missing data for point 2239 at coordinates 3.509173, 49.764728  
Successfully updated point 2239  
Processing missing data for point 2241 at coordinates 3.408321, 49.686713  
Successfully updated point 2241  
Processing missing data for point 2274 at coordinates 5.658703, 46.280918  
Successfully updated point 2274  
Processing missing data for point 2287 at coordinates 5.371121, 45.962301  
Successfully updated point 2287  
Processing missing data for point 2284 at coordinates 5.670066, 45.776498  
Successfully updated point 2284  
Processing missing data for point 2310 at coordinates -4.464553, 48.524331  
Successfully updated point 2310  
Processing missing data for point 2339 at coordinates -3.909861, 48.322179  
Successfully updated point 2339  
Processing missing data for point 2362 at coordinates 5.971293, 48.652804  
Successfully updated point 2362  
Processing missing data for point 2366 at coordinates 1.69355, 48.95858  
Successfully updated point 2366  
Processing missing data for point 2415 at coordinates -3.147249, 47.723656  
Successfully updated point 2415  
Processing missing data for point 2414 at coordinates -3.286465, 47.943738



Successfully updated point 2414  
Processing missing data for point 2526 at coordinates 3.153084, 50.518051  
Successfully updated point 2526  
Processing missing data for point 2532 at coordinates 3.137133, 50.609016  
Successfully updated point 2532  
Processing missing data for point 2522 at coordinates 3.191674, 50.233321  
Successfully updated point 2522  
Processing missing data for point 2548 at coordinates 2.643136, 49.224024  
Successfully updated point 2548  
Processing missing data for point 2560 at coordinates 2.155684, 49.335503  
Successfully updated point 2560  
Processing missing data for point 2607 at coordinates 0.703044, 48.518116  
Successfully updated point 2607  
Processing missing data for point 2661 at coordinates 1.688209, 50.603511  
Successfully updated point 2661  
Processing missing data for point 2685 at coordinates 3.534318, 45.758041  
Successfully updated point 2685  
Processing missing data for point 2667 at coordinates 3.862523, 45.361973  
Successfully updated point 2667  
Processing missing data for point 2671 at coordinates 3.47058, 45.428731  
Successfully updated point 2671  
Processing missing data for point 2689 at coordinates 3.689698, 45.532144  
Successfully updated point 2689  
Processing missing data for point 2731 at coordinates 2.16721, 44.30777  
Successfully updated point 2731  
Processing missing data for point 2737 at coordinates 0.099172, 43.294687  
Successfully updated point 2737  
Processing missing data for point 2778 at coordinates 7.667896, 48.900893  
Successfully updated point 2778  
Processing missing data for point 2791 at coordinates 7.443721, 47.962394  
Successfully updated point 2791  
Processing missing data for point 2799 at coordinates 4.578846, 45.617959  
Successfully updated point 2799  
Saving updated data to data/soilgrids\_updated.csv...