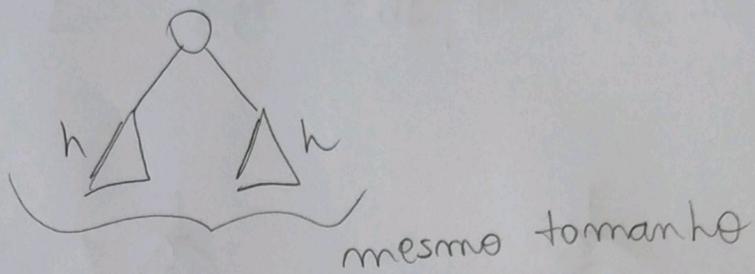
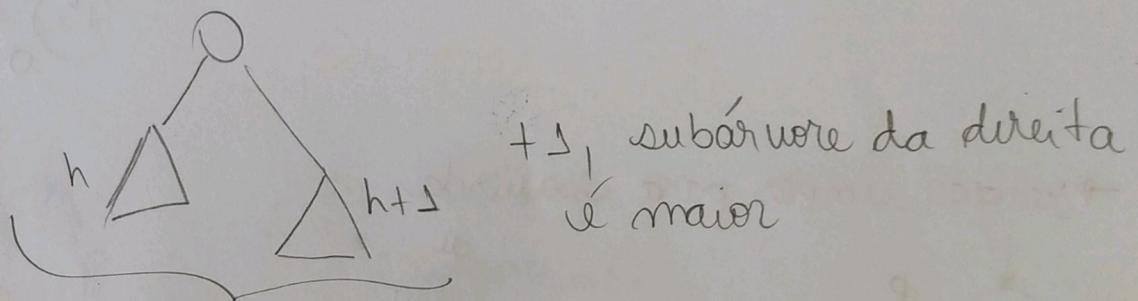


- direita - esquerda = h

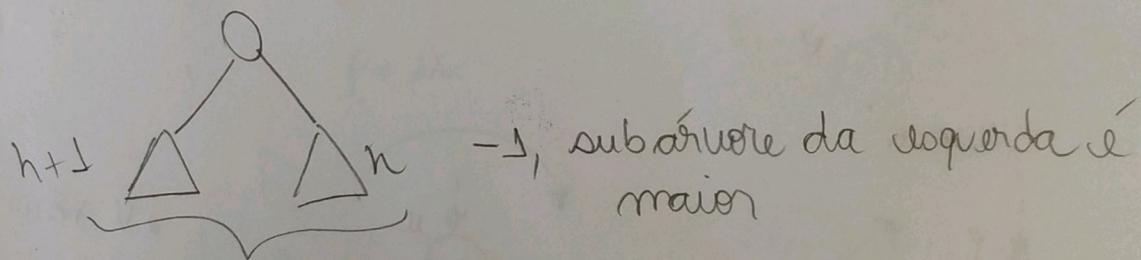
- se $h = 0$



- se $h = +1$



- se $h = -1$



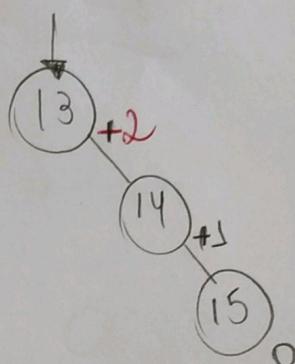
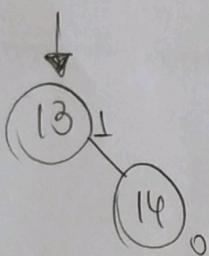
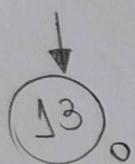
AVL Tree

AVL = Adelson-Velsky and Landis } 2 casos

→ Sequência de inserções

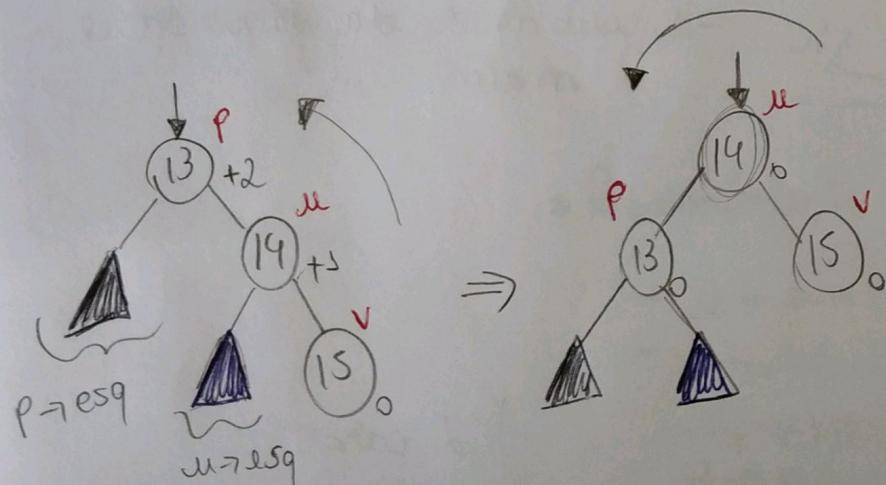
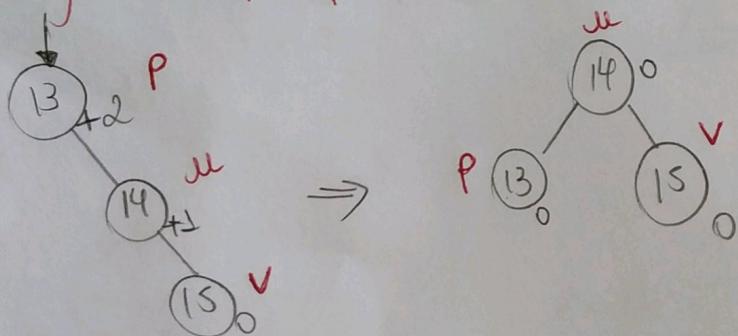
M N O L k Q P H J A

→ 13, 14, 15, 12, 11, 17, 16, 89, 1



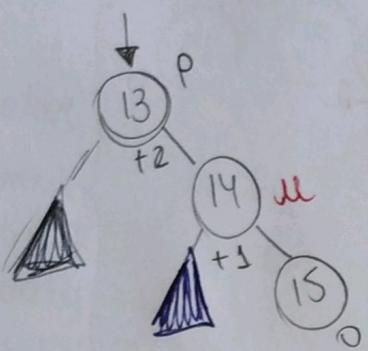
} rotação simples para esquerda

→ rotações simples para esquerda

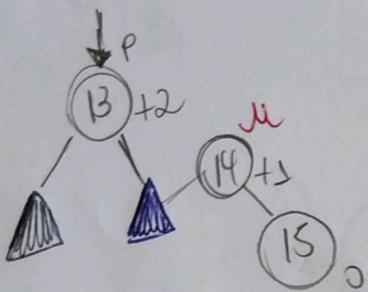


} V não é alterado
• $p = \rho \rightarrow$ direita
 $\rho \rightarrow \text{dir} = \mu \rightarrow \text{log}$
 $\mu \rightarrow \text{esq} = \rho$
 $\rho \rightarrow \text{balance} = \emptyset$
 $\rho = \mu$

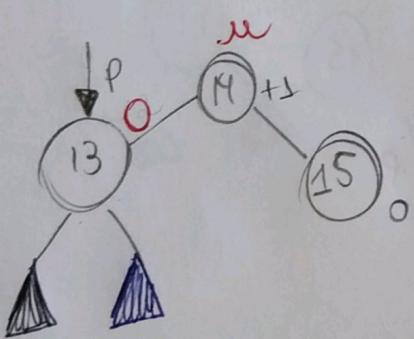
→ rotogar passo a passo



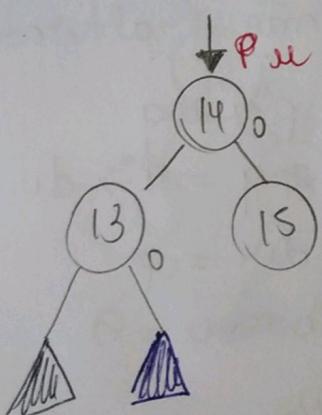
$$\mu = p \rightarrow \text{direita}$$



$$p \rightarrow \text{dir} = \mu \rightarrow \text{esq}$$



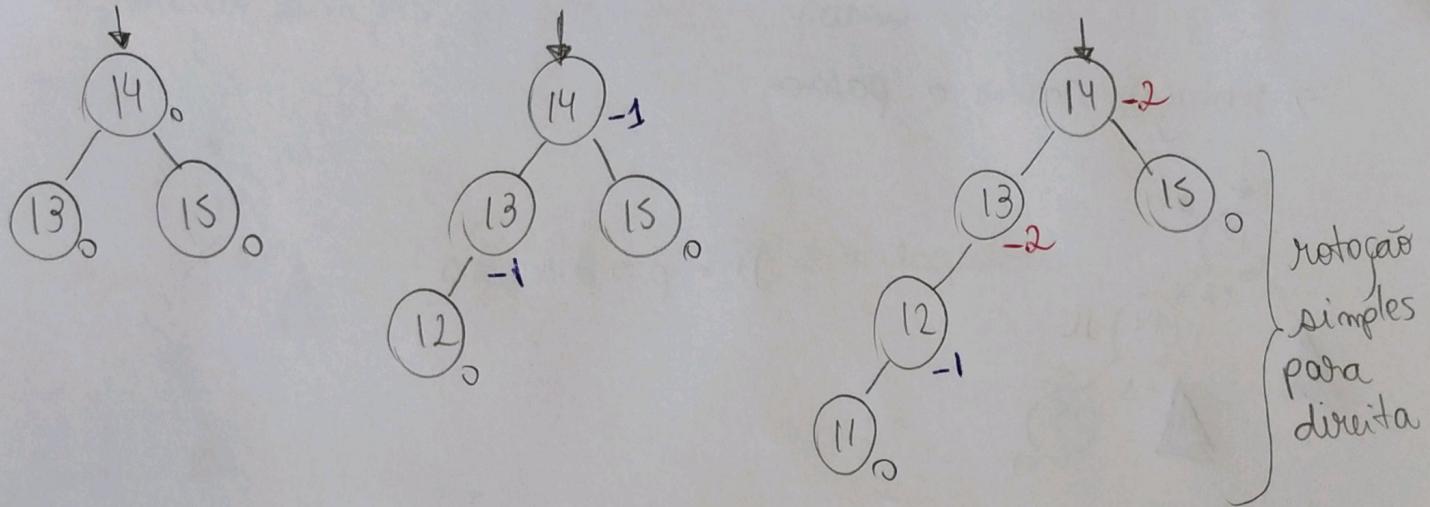
$$\mu \rightarrow \text{esq} = p$$
$$p \rightarrow \text{balance} = 0$$



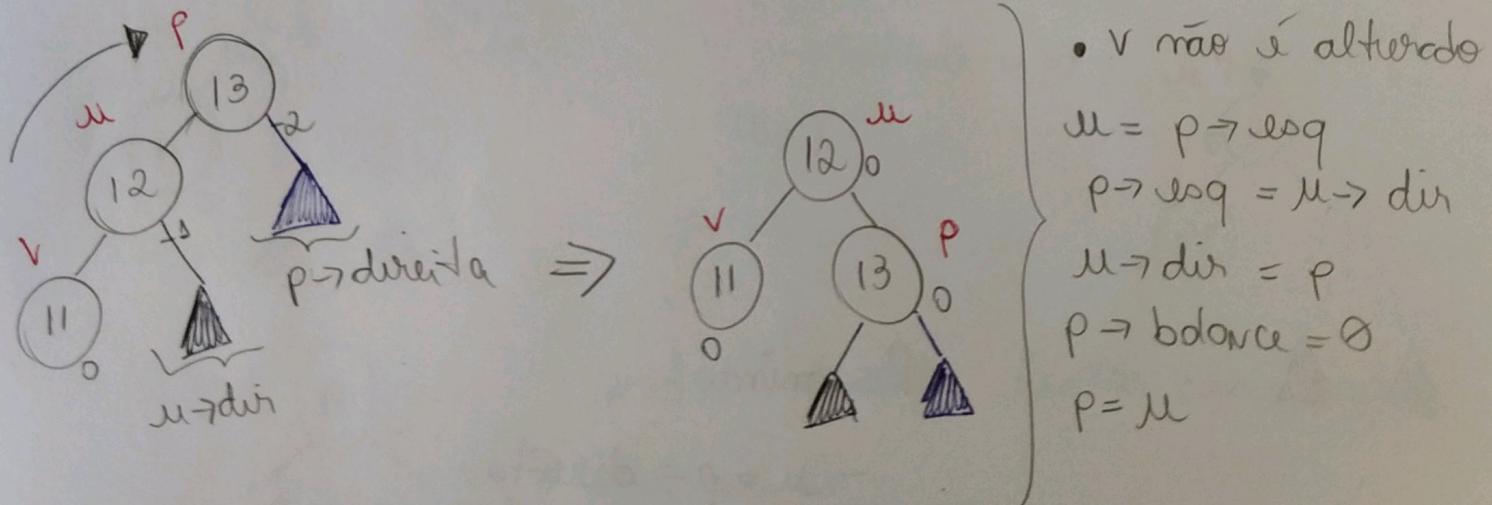
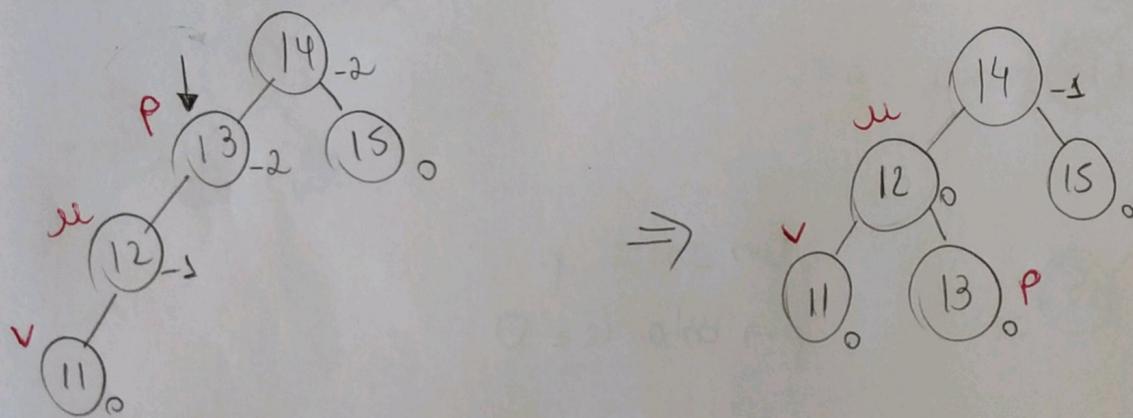
$$p = \mu$$

• Resumindo:

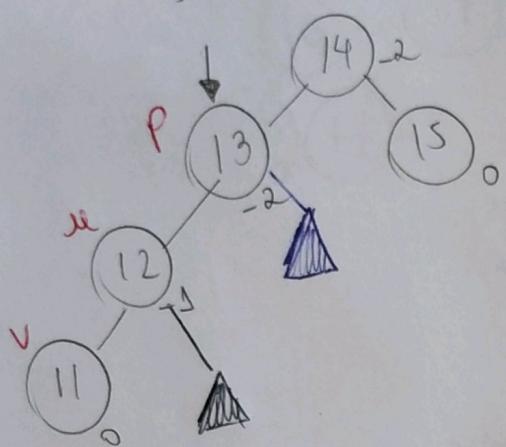
- $\mu = p \rightarrow \text{direita}$
- $p \rightarrow \text{dir} = \mu \rightarrow \text{esq}$
- $\mu \rightarrow \text{esq} = p$
- $p \rightarrow \text{balance} = 0$
- $p = \mu$



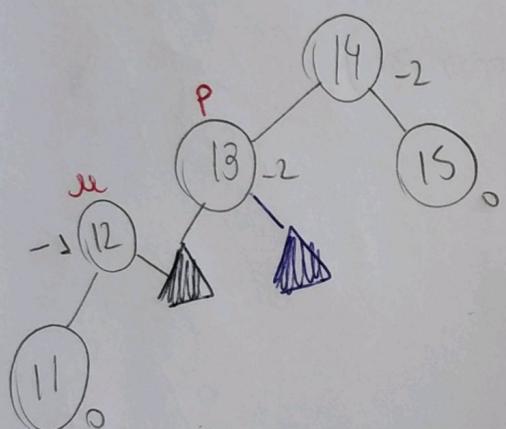
→ rotações simples para direita



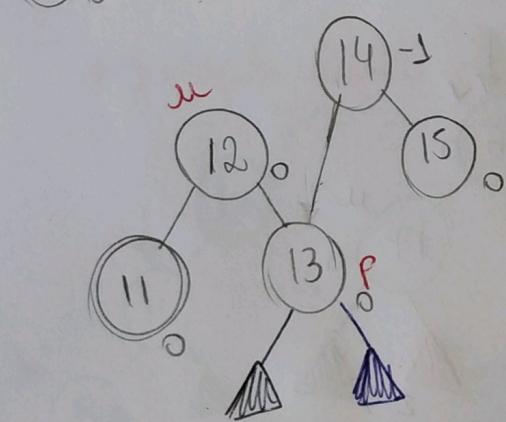
→ rotação simples p/ direita, passo a passo:



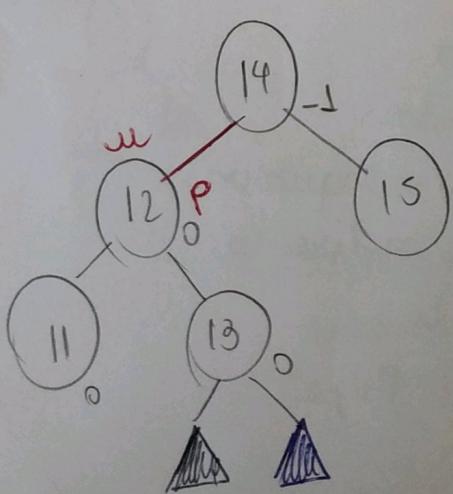
$\mu = p \rightarrow \text{esquerda};$



$p \rightarrow \text{esq} = \mu \rightarrow \text{direita};$

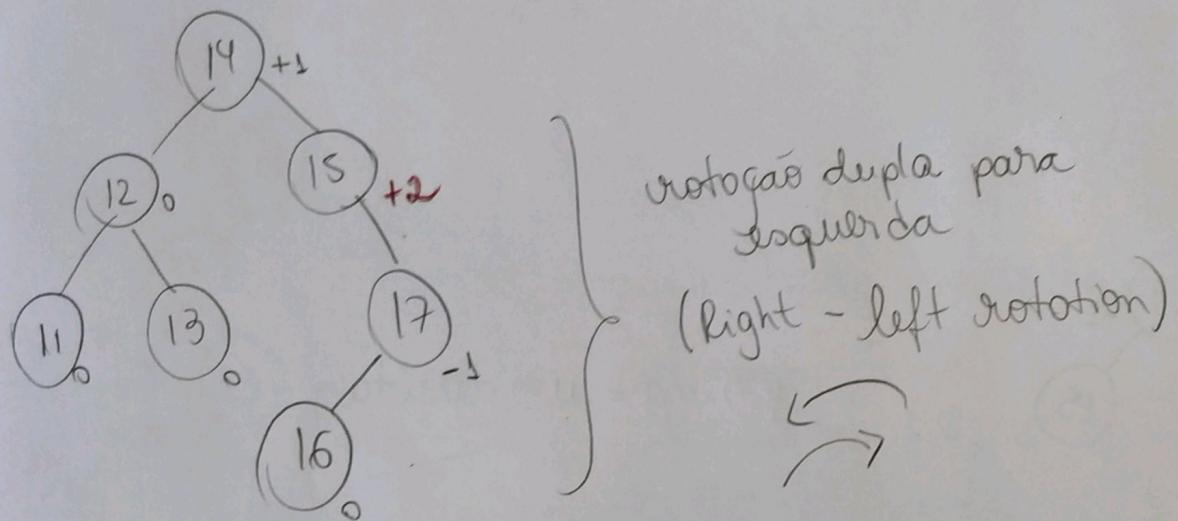
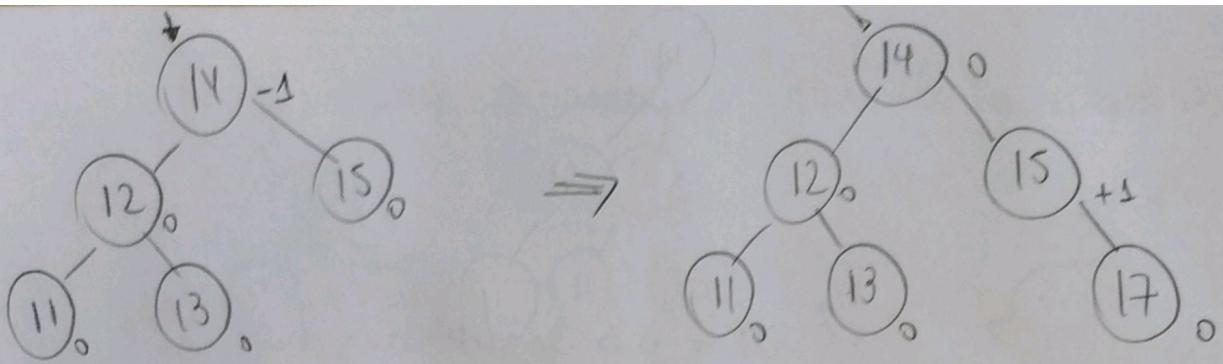


$\mu \rightarrow \text{direita} = p;$
 $p \rightarrow \text{balance} = \emptyset;$

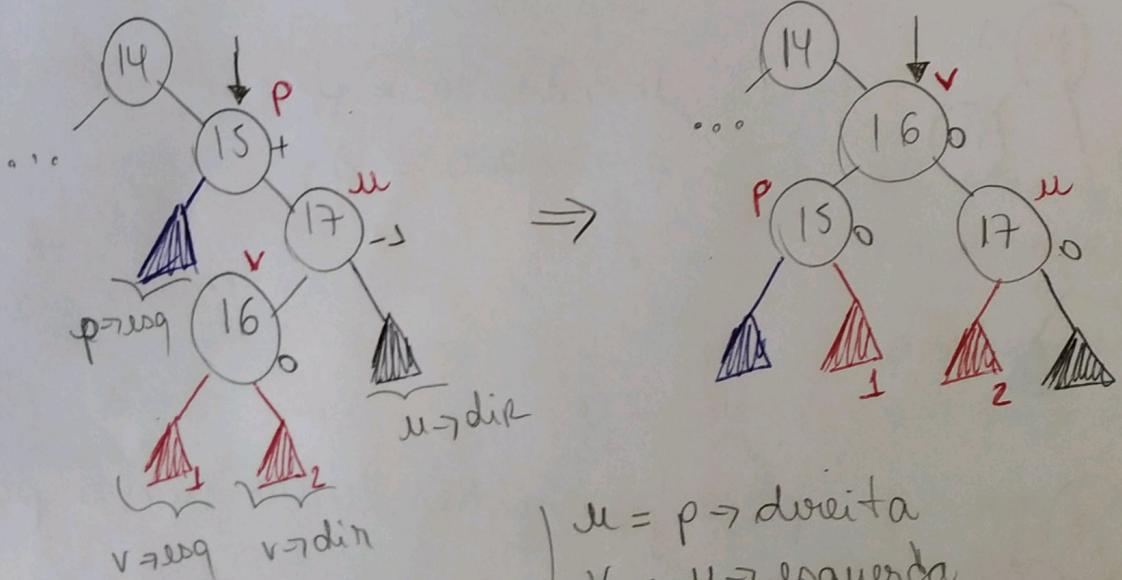


$p = \mu \} \text{ permite linkar com o pai}$
: Resumindo

- $\mu = p \rightarrow \text{esquerda}$
- $p \rightarrow \text{esquerda} = \mu \rightarrow \text{direita}$
- $\mu \rightarrow \text{direita} = p;$
- $p \rightarrow \text{balance} = \emptyset;$
- $p = \mu$



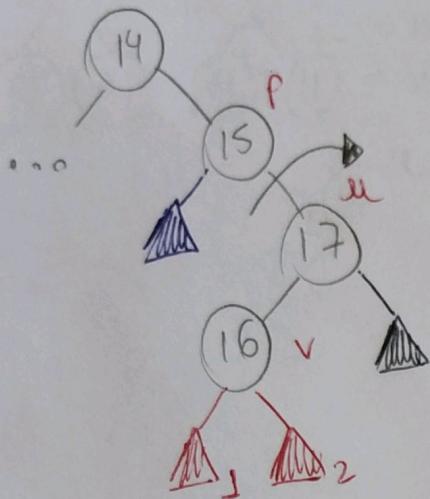
* rotogāo dupla para esquerda



atualizar:
- $p \rightarrow \text{balance}$
 $v \rightarrow \text{balance}$
 $u \rightarrow \text{balance}$

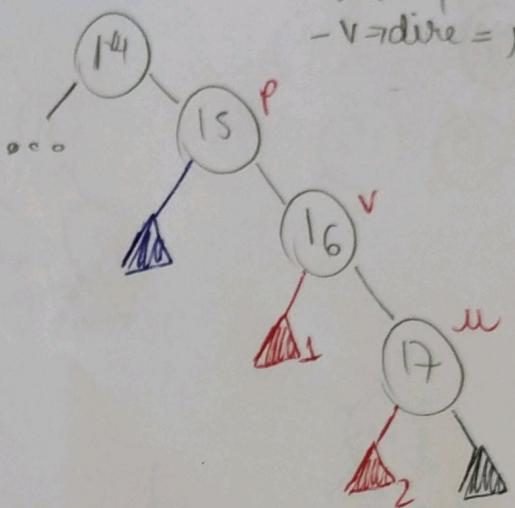
$$\left. \begin{array}{l} u = p \rightarrow \text{direita} \\ v = u \rightarrow \text{esquerda} \\ p \rightarrow \text{direita} = v \rightarrow \text{esquerda} \\ u \rightarrow \text{esquerda} = v \rightarrow \text{direita} \\ v \rightarrow \text{direita} = u \\ v \rightarrow \text{esquerda} = p \\ p = v \end{array} \right\}$$

Passo a passo:

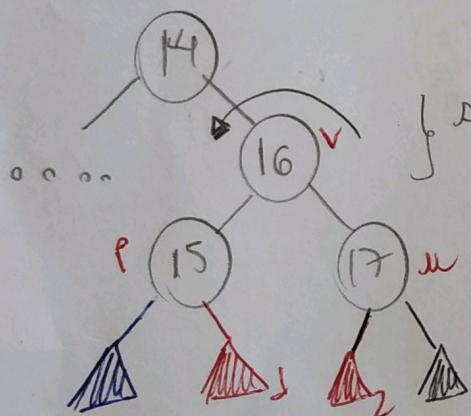


} primeira
rotogāo para
direita

$$\begin{aligned}-u &= p \rightarrow \text{dire} \\ -v &= u \rightarrow \text{esq}\end{aligned}$$



$$\begin{aligned}-u \rightarrow \text{esq} &= v \rightarrow \text{direit} \\ -v \rightarrow \text{dire} &= u\end{aligned}$$



} segunda rotogāo
para esquerda

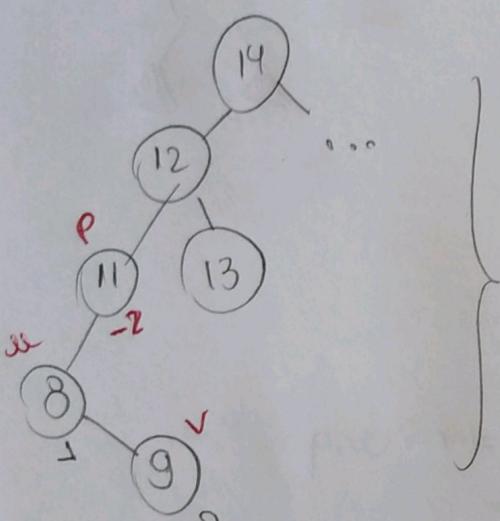
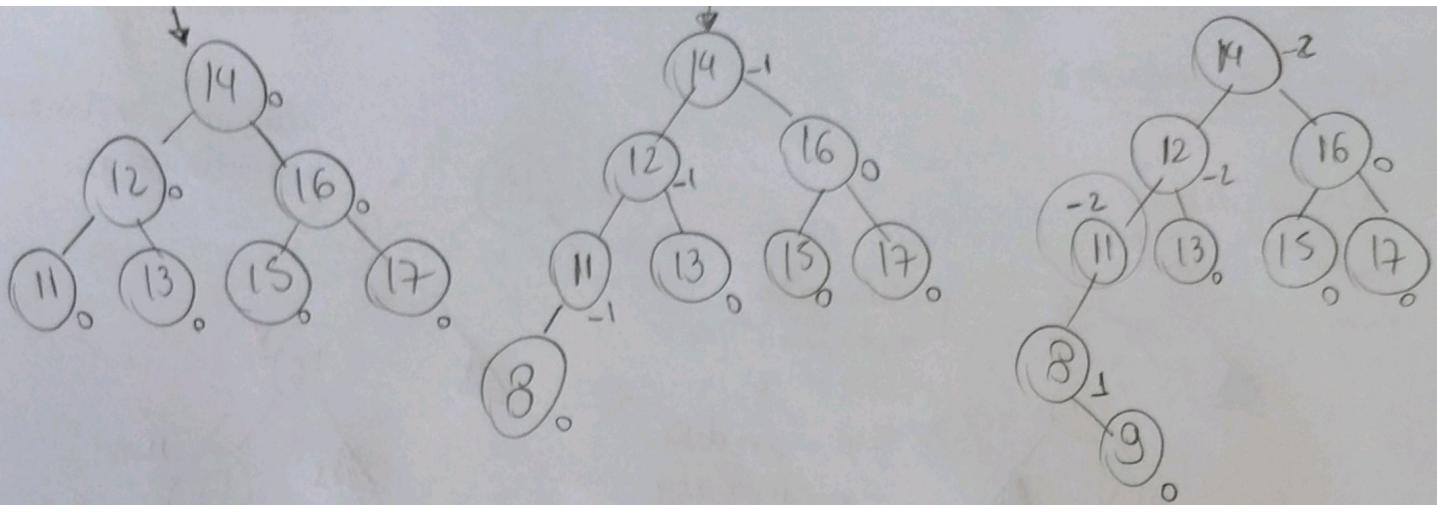
$$\begin{aligned}-p \rightarrow \text{dir} &\Rightarrow v \rightarrow \text{esq} \\ -v \rightarrow \text{esq} &= p\end{aligned}$$

atualiza desbalanceamento:

$$\begin{aligned}-p \\ -v \\ -u\end{aligned}$$

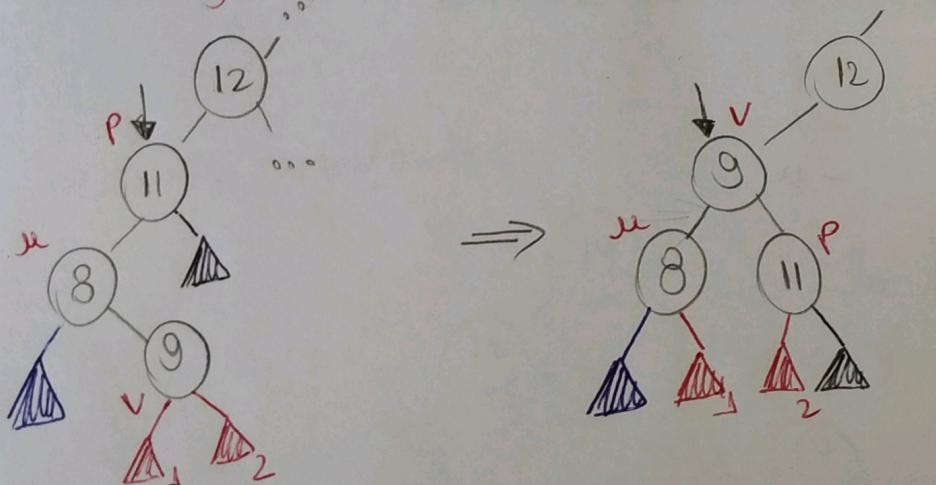
final:

$$p = v$$



} rotação dupla à direita
 → esquerda (8)
 → direita (9)

* rotação dupla para direita



$$u = p \rightarrow \text{esq}$$

$$v = u \rightarrow \text{dir}$$

$$u \rightarrow \text{dir} = v \rightarrow \text{esq}$$

$$v \rightarrow \text{esq} = u$$

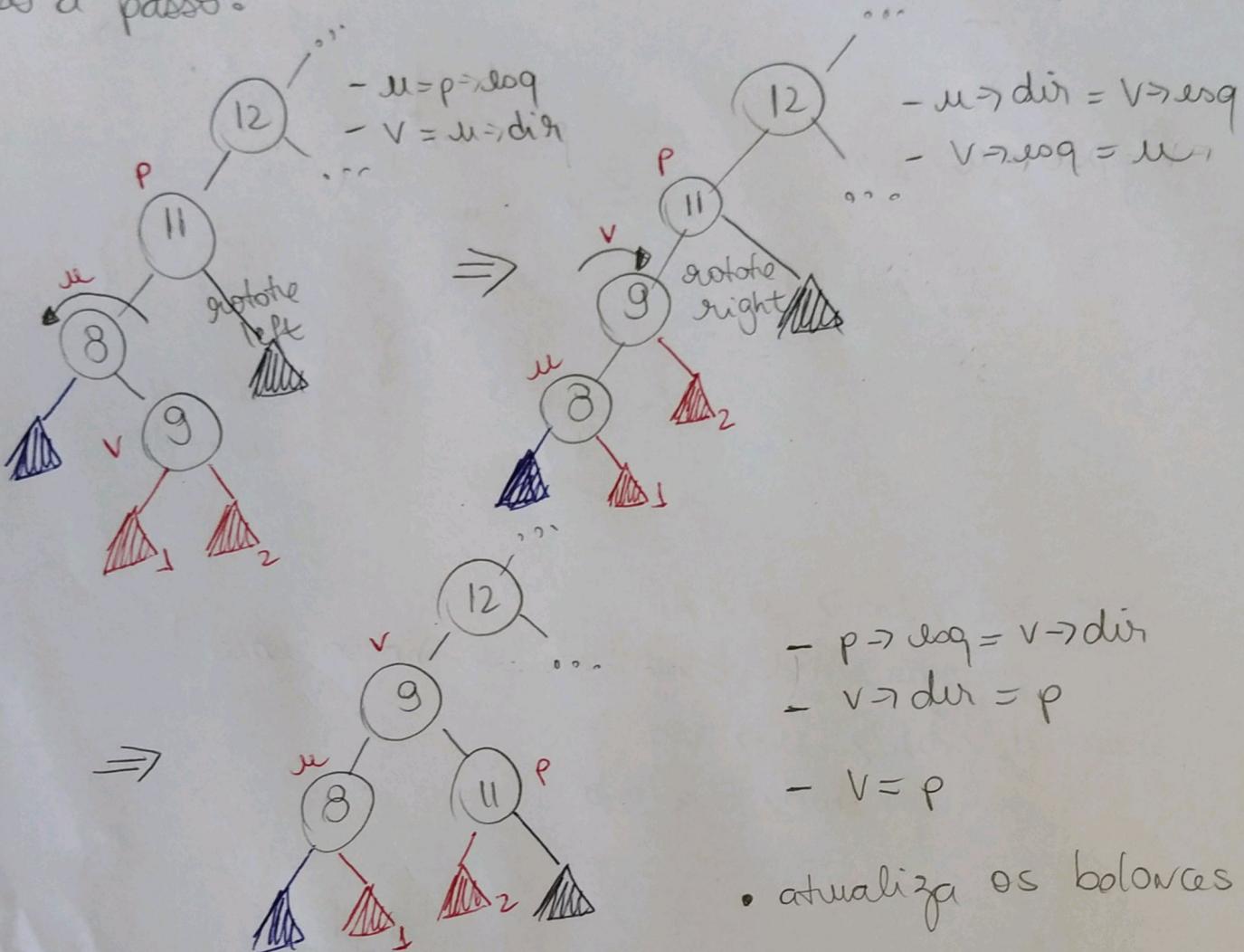
$$p \rightarrow \text{esq} = v \rightarrow \text{dir}$$

$$v \rightarrow \text{dir} = p$$

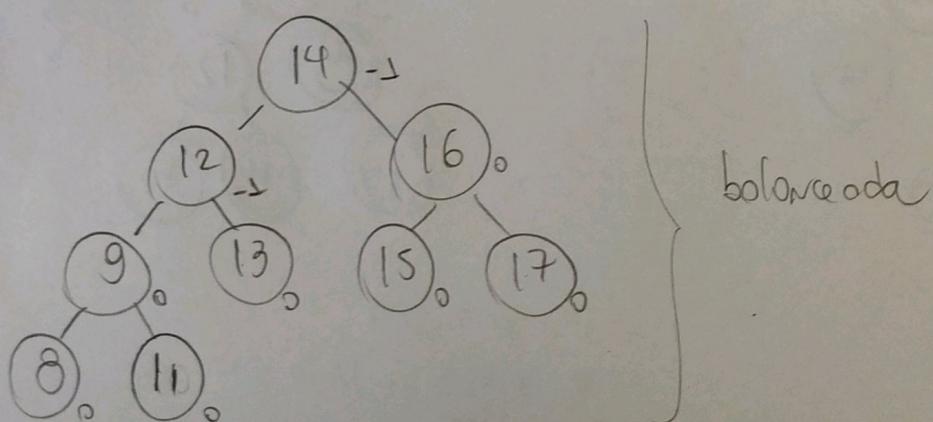
$p = v$] retornar a
 ref correta
 na recursão

* atualizar os
 balanços de (p, u, v)
 depois das rotações

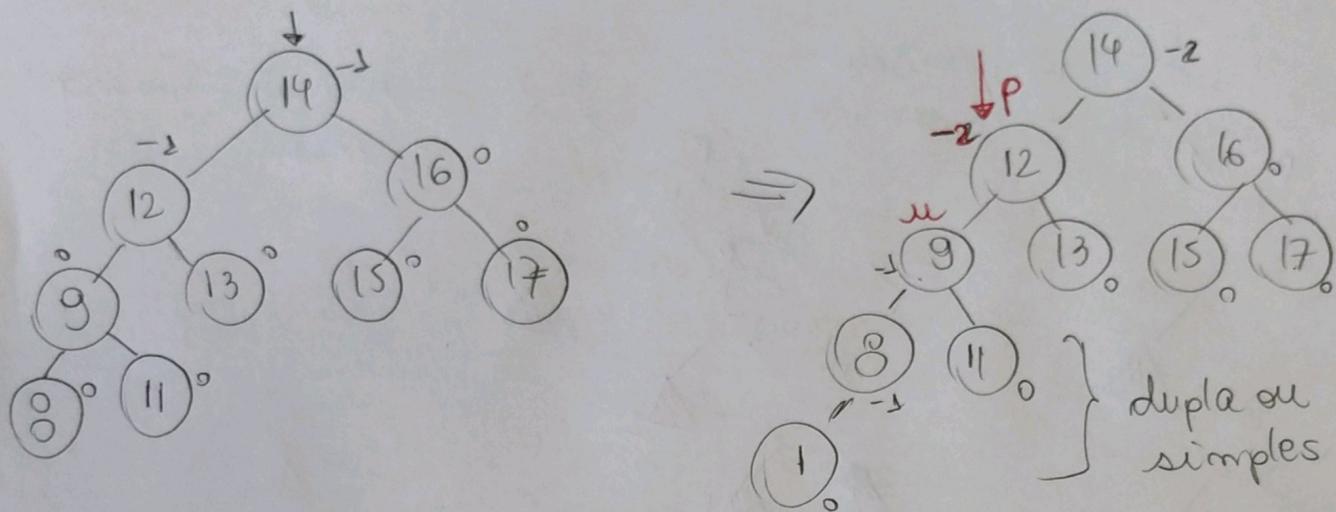
Passo a passo:



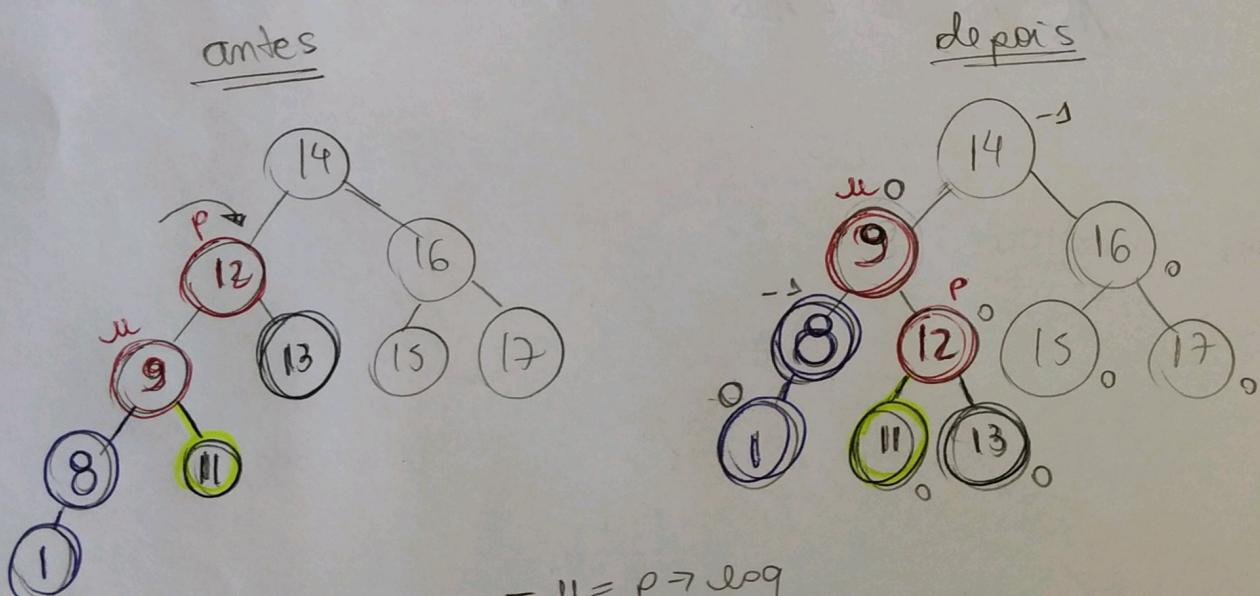
→ árvore resultante:



→ inserindo ↓:



- se $u \rightarrow \text{esq} > u \rightarrow \text{dir}$
rotogāo simples Esquerda * *nossa case!*
- se $u \rightarrow \text{dir} > u \rightarrow \text{esq}$
rotogāo dupla Esquerda



$$\begin{aligned}
 - u &= p \rightarrow \text{esq} \\
 - p \rightarrow \text{esq} &= u \rightarrow \text{dir} \\
 - u \rightarrow \text{dir} &= p \\
 - p &= u
 \end{aligned}$$