

Circuits for Benchmarking

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Summary

This document describes the classes of quantum circuits and respective data, available at https://github.com/luisps/QCircuits_BenchTest.git.

Each circuit class is identified by a number (usually an exact thousand, hundred or dozen. Particular circuits are then identified by the lower digits.

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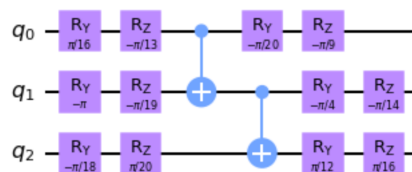
Class 19 – variational EfficientSU2

This class of circuits corresponds to the so-called “hardware efficient” ansatz for variational circuits. It is obtained with the Qiskit method:

```
EfficientSU2(num_qubits, entanglement='linear', reps=reps)
```

The number of qubits and the number of layer repetitions is varied for the different circuit instances below.

Circuit 19- variational EfficientSU2: 3 qubits, 1 rep



6 layers

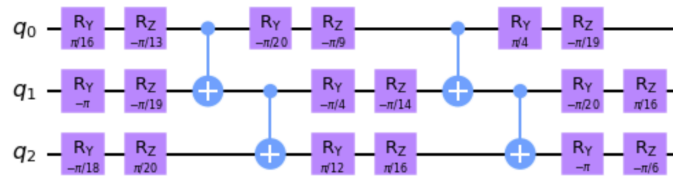
$$32768 \text{ paths} = 2^{(3 \cdot (6-1))} = 2^{15}$$

Non zero paths for $\langle 0|U|0 \rangle = 4$

$$\langle 0|U|0 \rangle = 0.07304992 + 0.01779798i$$

Available Files	
circuit_19.data	The circuit definition
circuit_19.csv	Exact amplitudes for different transitions
circuit_19-raw-values.csv	Non zero paths for $\langle 0 U 0 \rangle$
circuit_19.data_stats_IS_0_0.csv	Amplitudes and variances as a function of the number of samples for Importance Sampling and $\langle 0 U 0 \rangle$
circuit_19.data_stats_BD_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling and $\langle 0 U 0 \rangle$
circuit_19.data_stats_BD_MIS_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling with MIS and $\langle 0 U 0 \rangle$

Circuit 191- variational EfficientSU2: 3 qubits, 2 rep



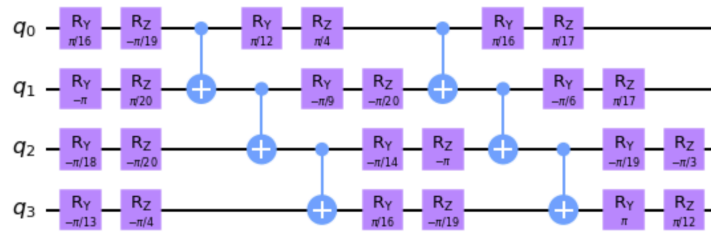
10 layers

$$1.342 * 10^8 \text{ paths} = 2^{(3*(9-1))} = 2^{24}$$

$$\langle 0|U|0\rangle = -0.29465061 - 0.18699787j$$

Available Files	
circuit_191.data	The circuit definition
circuit_191.csv	Exact amplitudes for different transitions
circuit_191.data_stats_IS_0_0.csv	Amplitudes and variances as a function of the number of samples for Importance Sampling and $\langle 0 U 0\rangle$
circuit_191.data_stats_BD_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling and $\langle 0 U 0\rangle$
circuit_191.data_stats_BD_MIS_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling with MIS and $\langle 0 U 0\rangle$

Circuit 192- variational EfficientSU2: 4 qubits, 2 layers



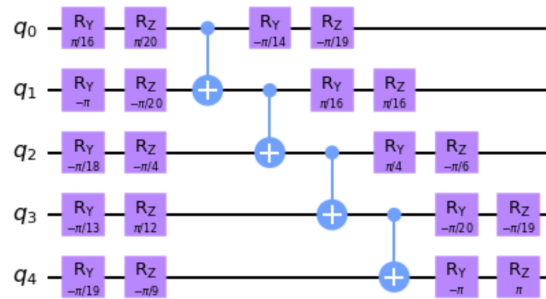
11 layers

$$1.1 * 10^{12} \text{ paths} = 2^{(4*(10-1))} = 2^{36}$$

$$\langle 0|U|0\rangle = 0.06600214 - 0.21540996j$$

Available Files	
circuit_192.data	The circuit definition
circuit_192.csv	Exact amplitudes for different transitions
circuit_192.data_stats_IS_0_0.csv	Amplitudes and variances as a function of the number of samples for Importance Sampling and $\langle 0 U 0 \rangle$
circuit_192.data_stats_BD_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling and $\langle 0 U 0 \rangle$
circuit_192.data_stats_BD_MIS_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling with MIS and $\langle 0 U 0 \rangle$

Circuit 193- variational EfficientSU2: 5 qubits, 1 rep



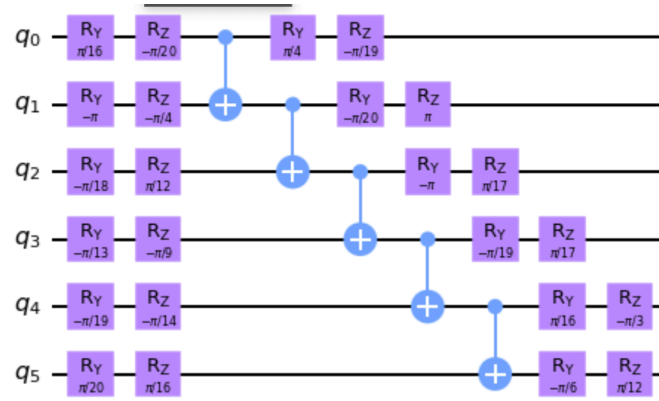
8 layers

$$3.436\text{e}+10 \text{ paths} = 2^{(5 \cdot (8-1))} = 2^{35}$$

$$\langle 0|U|0 \rangle = -0.00172150 + 0.00127863j$$

Available Files	
circuit_193.data	The circuit definition
circuit_193.csv	Exact amplitudes for different transitions
circuit_193.data_stats_IS_0_0.csv	Amplitudes and variances as a function of the number of samples for Importance Sampling and $\langle 0 U 0 \rangle$
circuit_193.data_stats_BD_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling and $\langle 0 U 0 \rangle$
circuit_193.data_stats_BD_MIS_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling with MIS and $\langle 0 U 0 \rangle$

Circuit 194- variational EfficientSU2: 6 qubits, 1 rep



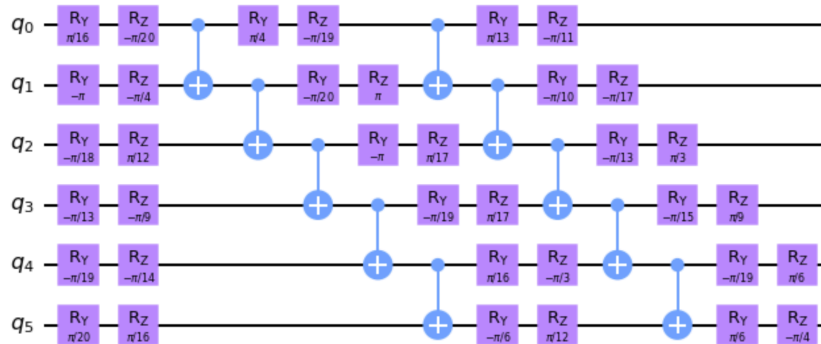
9 layers

$$2.815e+14 \text{ paths} = 2^{(6 \cdot (9-1))} = 2^{48}$$

$$\langle 0|U|0 \rangle = -0.00273768 - 0.00909492j$$

Available Files	
circuit_194.data	The circuit definition
circuit_194.csv	Exact amplitudes for different transitions

Circuit 195- variational EfficientSU2: 6 qubits, 2 rep



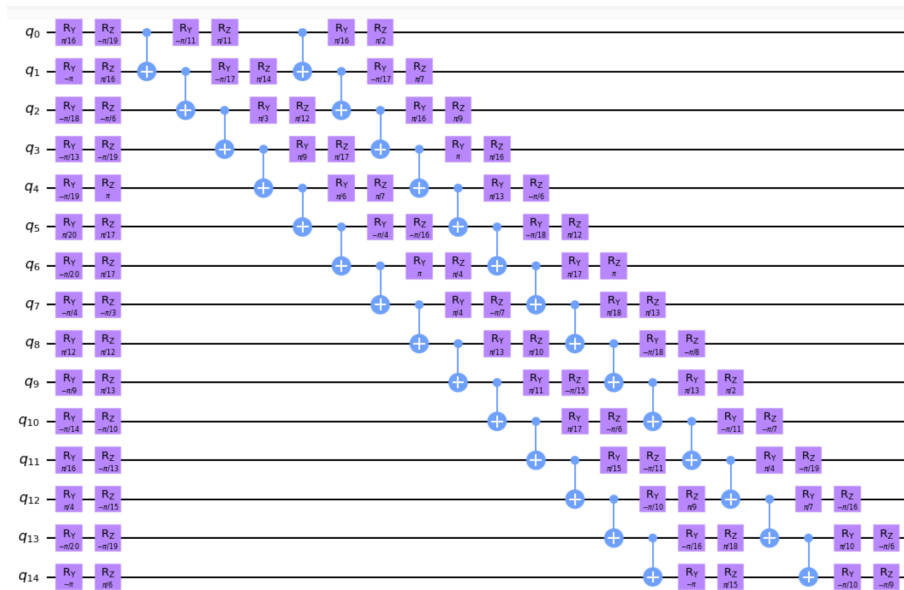
13 layers

$$4.722e+21 \text{ paths} = 2^{(6 \cdot (13-1))} = 2^{72}$$

$$\langle 0|U|0 \rangle = -0.00514611 - 0.02104634j$$

Available Files	
circuit_195.data	The circuit definition
circuit_195.csv	Exact amplitudes for different transitions

Circuit 196- variational EfficientSU2: 15 qubits, 2 rep



22 layers

$$6.675e+94 \text{ paths} = 2^{(15 \cdot (22-1))} = 2^{315}$$

$$\langle 0|U|0 \rangle = 0.00364578 + 0.00060584j$$

Available Files	
circuit_196.data	The circuit definition
circuit_196.jpg	Circuit diagram
circuit_196.csv	Exact amplitudes for different transitions
circuit_196.data_stats_IS_0_0.csv	Amplitudes and variances as a function of the number of samples for Importance Sampling and $\langle 0 U 0 \rangle$
circuit_196.data_stats_BD_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling and $\langle 0 U 0 \rangle$
circuit_196.data_stats_BD_MIS_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling with MIS and $\langle 0 U 0 \rangle$

Class 4100 – Hidden Shift Circuits

Deterministic circuits, in the sense that only one basis state in the output has an amplitude different from 0 (= 1.0).

These are based on the algorithm (and code) presented in Peres, Filipa 2023 (sec 4.1)

<https://arxiv.org/pdf/2203.01789.pdf>

Circuit 4100- Hidden shift: 100 qubits, hidden string = 1023

43 layers

$$\text{paths} = 2^{(100 \cdot (43-1))} = 2^{4200}$$

$$\langle 1023|U|0 \rangle = 1.0 + 0.0j$$

Available Files	
circuit_4100.data	The circuit definition
circuit_4100.jpg	Circuit diagram

Circuit 4101- Hidden shift: 8 qubits, hidden string = 7

53 layers

$$1.692\text{e}+125 \text{ paths} = 2^{(8*(53-1))} = 2^{416}$$

$$\langle 7|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4101.data	The circuit definition
circuit_4101.jpg	Circuit diagram
circuit_4101.csv	Exact amplitudes for different transitions

Circuit 4110- Hidden shift: 10 qubits, hidden string = 1023

56 layers

$$2^{(10*(56-1))} = 2^{560}$$

$$\langle 1023|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4110.data	The circuit definition
circuit_4110.jpg	Circuit diagram

Circuit 4120- Hidden shift: 20 qubits, hidden string = 1023

46 layers

$$2^{(20*(46-1))} = 2^{900}$$

$$\langle 1023|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4120.data	The circuit definition
circuit_4120.jpg	Circuit diagram

Circuit 4130- Hidden shift: 30 qubits, hidden string = 1023

43 layers

$$2^{(30*(43-1))} = 2^{1260}$$

$$\langle 1023|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4130.data	The circuit definition
circuit_4130.jpg	Circuit diagram

Circuit 4140- Hidden shift: 40 qubits, hidden string = 1023

43 layers

$$2^{(40*(43-1))} = 2^{1680}$$

$$\langle 1023|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4140.data	The circuit definition
circuit_4140.jpg	Circuit diagram

Circuit 4150- Hidden shift: 50 qubits, hidden string = 1023

43 layers

$$2^{(50*(43-1))} = 2^{2100}$$

$$\langle 1023|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4150.data	The circuit definition
circuit_4150.jpg	Circuit diagram

Circuit 4160- Hidden shift: 60 qubits, hidden string = 1023

43 layers

$$\text{paths} = 2^{(60*(43-1))} = 2^{2520}$$

$$\langle 1023|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4160.data	The circuit definition
circuit_4160.jpg	Circuit diagram

Circuit 4170- Hidden shift: 70 qubits, hidden string = 1023

43 layers

$$\text{paths} = 2^{(70*(43-1))} = 2^{2940}$$

$$\langle 1023|U|0\rangle = 1.0 + 0.0j$$

Available Files	
circuit_4170.data	The circuit definition
circuit_4170.jpg	Circuit diagram

Circuit 4180- Hidden shift: 80 qubits, hidden string = 1023

43 layers

$$\text{paths} = 2^{(80 \times (43-1))} = 2^{3360}$$

$$\langle 1023|U|0 \rangle = 1.0 + 0.0j$$

Available Files	
circuit_4180.data	The circuit definition
circuit_4180.jpg	Circuit diagram

Circuit 4190- Hidden shift: 90 qubits, hidden string = 1023

43 layers

$$\text{paths} = 2^{(90 \times (43-1))} = 2^{3780}$$

$$\langle 1023|U|0 \rangle = 1.0 + 0.0j$$

Available Files	
circuit_4190.data	The circuit definition
circuit_4190.jpg	Circuit diagram

Class 300 – IQP Inversion test

Inversion test of two random states encoded using IQP.

The probability of $P(|0\rangle^n)$ is the overlap between the states.

Circuit 305- IQP: 5 qubits

17 layers

$$1.209\text{e}+24 \text{ paths} = 2^{(5 \times (17-1))} = 2^{80}$$

$$\langle 0|U|0 \rangle = -0.104462+0.106694j$$

Available Files	
circuit_305.data	The circuit definition
circuit_305.jpg	Circuit diagram
circuit_305.csv	Exact amplitudes for different transitions

Circuit 315- IQP: 15 qubits

55 layers

$$6.828\text{e}+243 \text{ paths} = 2^{(15 \times (55-1))} = 2^{810}$$

$$\langle 0|U|0 \rangle = -0.00128171-0.00008649j$$

Available Files	
circuit_315.data	The circuit definition
circuit_315.jpg	Circuit diagram
circuit_315.csv	Exact amplitudes for different transitions

Circuit 325- IQP: 25 qubits

97 layers

$$\text{paths} = 2^{(25 \times (97-1))} = 2^{2400}$$

$$\langle 0|U|0\rangle = -0.00013443-0.00022139j$$

Available Files	
circuit_325.data	The circuit definition
circuit_325.jpg	Circuit diagram
circuit_325.csv	Exact amplitudes for different transitions

Class 500 – Random Circuits

Randomly generated circuits. The output state should follow a quasi-uniform distribution.

These are based on the algorithm (and code) presented in Peres, Filipa 2023 (sec 4.2)
<https://arxiv.org/pdf/2203.01789.pdf>

Circuit 508- Random: 8 qubits, nCycles = 6

9 layers

$$1.845e+19 \text{ paths} = 2^{(8 \times (9-1))} = 2^{64}$$

$$\langle 0|U|0\rangle = -0.04419417+0.10669417j$$

Available Files	
circuit_508.data	The circuit definition
circuit_508.jpg	Circuit diagram
circuit_508.csv	Exact amplitudes for different transitions
circuit_508.data_stats_BD_MIS_0_0.csv	Amplitudes and variances as a function of the number of samples for Bidirectional Sampling with MIS and $\langle 0 U 0\rangle$

Circuit 510- Random: 10 qubits, nCycles = 7

13 layers

$$\text{paths} = 2^{(10 \times (13-1))} = 2^{120}$$

$$\langle 0|U|0\rangle = -0.02209709+0.05334709j$$

Available Files	
circuit_510.data	The circuit definition
circuit_510.jpg	Circuit diagram
circuit_510.csv	Exact amplitudes for different transitions

Circuit 512- Random: 12 qubits, nCycles = 8

15 layers

$$\text{paths} = 2^{(12 \cdot (15-1))} = 2^{168}$$

$$\langle 16|U|0 \rangle = 0.009153 - 0.022097j$$

Available Files	
circuit_512.data	The circuit definition
circuit_512.jpg	Circuit diagram
circuit_512.csv	Exact amplitudes for different transitions

Circuit 516- Random: 16 qubits, nCycles = 12

22 layers

$$1.400e+101 \text{ paths} = 2^{(16 \cdot (22-1))} = 2^{336}$$

$$\langle 0|U|0 \rangle = -0.00040451 - 0.00138107j$$

Available Files	
circuit_516.data	The circuit definition
circuit_516.jpg	Circuit diagram
circuit_516.csv	Exact amplitudes for different transitions

Circuit 525 - Random: 25 qubits, nCycles = 18

31 layers

$$5.922e+225 \text{ paths} = 2^{(25 \cdot (31-1))} = 2^{750}$$

$$\langle 0|U|0 \rangle = 0.00035204 + 0.00038255j$$

Available Files	
circuit_525.data	The circuit definition
circuit_525.jpg	Circuit diagram
circuit_525.csv	Exact amplitudes for different transitions