Small RNA dataset

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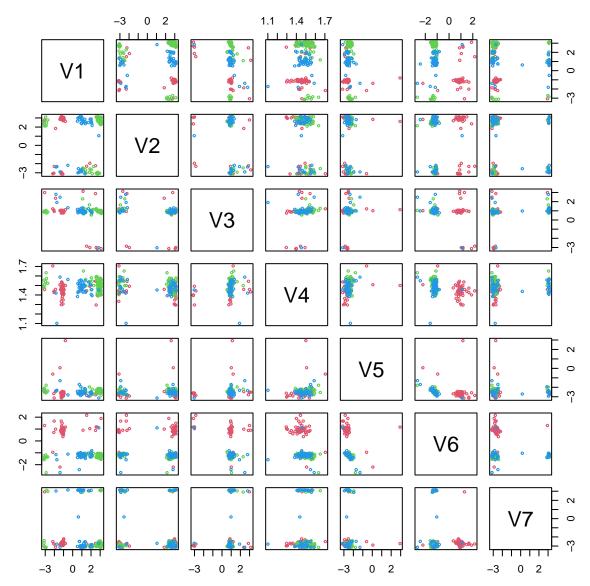
The objective in this case study is to recover clusters identified in smallrna\$clusters using only the information on smallrna\$angles, a 7-dimensional matrix of angles (i.e., data on $(\mathbb{S}^1)^7$)). The clusters have been constructed using the information in smallrna\$torsion. If a dimension-reduction technique is able to successfully identify clusters, then it will be doing a good job in terms of identifying the underlying structure of the data. Section 5.2 in Zoubouloglou et al. (2021) describes the history of the "Small RNA" dataset and its construction.

Let's begin by importing the data.

```
# Load package
library(pscsne)
stopifnot(packageVersion("pscsne") >= "0.0.1.900002")

# Load dataset
data("smallrna")

# Visualize original data
pairs(smallrna$angles, col = smallrna$clusters + 1, cex = 0.5)
```



We can now run psc-SNE. First, we transform the data and obtain the ρ 's giving the prescribed perplexity.

```
# Data to Cartesian coordinates
smallrna_X <- sphunif::Theta_to_X(Theta = smallrna$angles)

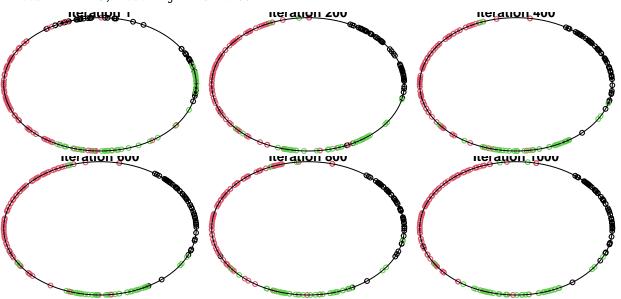
# Obtain rhos for given perplexity
rho_psc_list <- rho_optim_bst(x = smallrna_X, perp_fixed = 30)</pre>
```

Time difference of 10.1769 secs

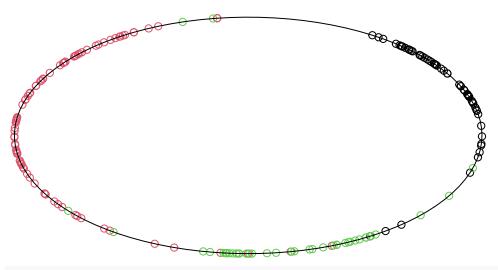
We run psc-SNE for d=1 with its default η .

```
## It: 1; obj: 1.196e+01; abs: 0.000e+00; rel: 0.000e+00; norm: 3.156e-01; mom: 0.000e+00;
## best it: 1; best obj: 1.196e+01
## It: 100; obj: 1.048e+01; abs: 1.892e+00; rel: 1.529e-01; norm: 2.554e-01; mom: 7.510e+00;
```

```
## best it: 14; best obj: 1.027e+01
## It: 200; obj: 1.150e+00; abs: 1.523e-02; rel: 1.342e-02; norm: 8.878e-02; mom: 4.454e+00;
## best it: 101; best obj: 1.078e+00
## It: 300; obj: 1.084e+00; abs: 3.854e-03; rel: 3.542e-03; norm: 8.592e-02; mom: 6.150e+00;
## best it: 248; best obj: 1.022e+00
## It: 400; obj: 1.088e+00; abs: 1.494e-03; rel: 1.371e-03; norm: 8.640e-02; mom: 6.108e+00;
## best it: 248; best obj: 1.022e+00
## It: 500; obj: 1.082e+00; abs: 1.050e-02; rel: 9.610e-03; norm: 8.634e-02; mom: 6.133e+00;
## best it: 248; best obj: 1.022e+00
## It: 600; obj: 1.083e+00; abs: 1.018e-02; rel: 9.309e-03; norm: 8.623e-02; mom: 6.173e+00;
## best it: 248; best obj: 1.022e+00
## It: 700; obj: 1.088e+00; abs: 5.319e-04; rel: 4.885e-04; norm: 8.626e-02; mom: 6.081e+00;
## best it: 248; best obj: 1.022e+00
## It: 800; obj: 1.085e+00; abs: 8.191e-03; rel: 7.495e-03; norm: 8.668e-02; mom: 6.122e+00;
## best it: 248; best obj: 1.022e+00
## It: 900; obj: 1.082e+00; abs: 7.312e-03; rel: 6.712e-03; norm: 8.591e-02; mom: 6.155e+00;
## best it: 248; best obj: 1.022e+00
## It: 1000; obj: 1.089e+00; abs: 2.103e-04; rel: 1.932e-04; norm: 8.629e-02; mom: 6.071e+00;
## best it: 248; best obj: 1.022e+00
```



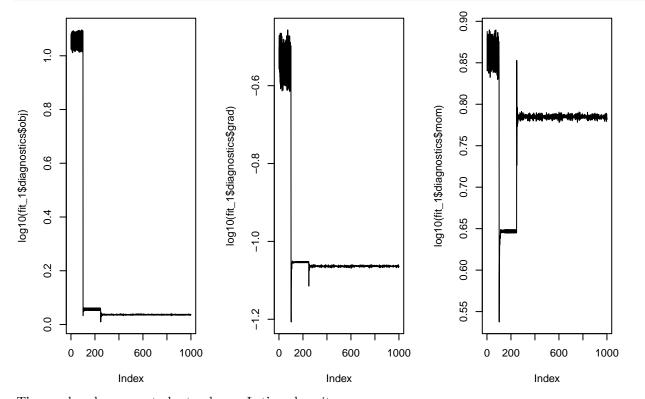
Iteration 248



Does not converge fit_1\$convergence

[1] FALSE

```
par(mfrow = c(1, 3))
plot(log10(fit_1$diagnostics$obj), type = "l")
plot(log10(fit_1$diagnostics$grad), type = "l")
plot(log10(fit_1$diagnostics$mom), type = "l")
```



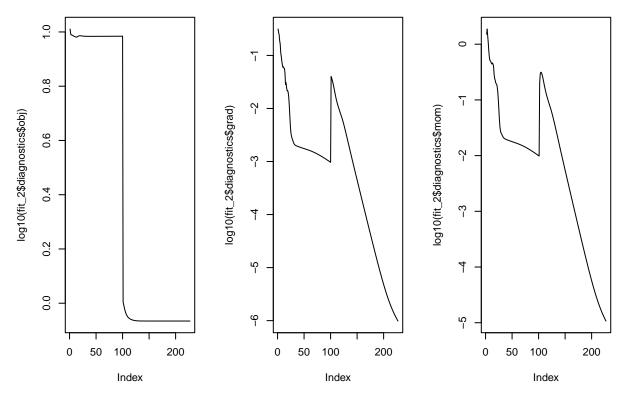
The employed η seems to be too large. Let's reduce it.

Converges

Iteration

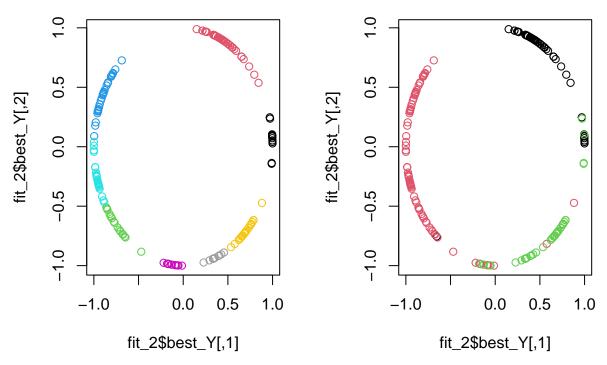
```
## [1] TRUE
par(mfrow = c(1, 3))
plot(log10(fit_2$diagnostics$obj), type = "l")
plot(log10(fit_2$diagnostics$grad), type = "l")
plot(log10(fit_2$diagnostics$mom), type = "l")
```

fit_2\$convergence

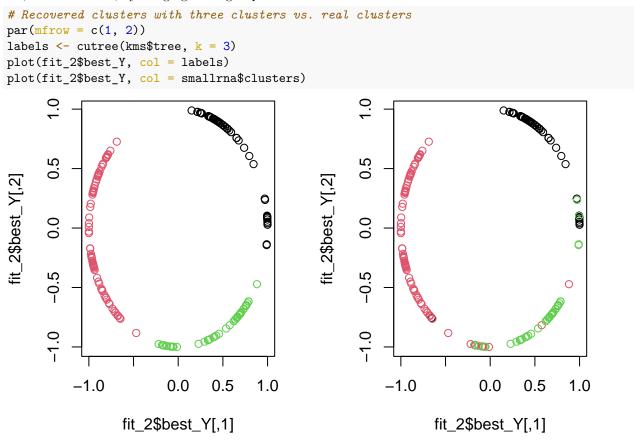


Convergence is attained in the second run, yet it is weird that the objective function takes exactly the zero value.

Let's see the recovery of the clusters.



The original clusters are not fully recovered, in the sense that more clusters are obtained. However, the three-cluster structure is present, as the new clusters appear dividing the three main ones. This can be checked by cutting the hierarchical clustering tree behind kernel mean shift clustering exactly at three groups. Or, in other words, by merging the 8 groups into 3.



```
# Correct classification rate: 90%
mean(labels == smallrna$clusters)
## [1] 0.9
```

```
# 19 incorrectly classified observations
sum(labels != smallrna$clusters)
```

[1] 19

The classification accuracy is on-par with Zoubouloglou et al. (2021), which misclassifies 16 points and has a classification rate of 0.916.