

20/ Junio / 2024

Práctica: Regresión Lineal con el Dataset Pressure

Fórmula:  $y = \beta_0 + \beta_1 x + \epsilon$

Fórmulas:

$$\beta_1 = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^n (x_i - \bar{x})^2}$$

$$\beta_0 = \bar{y} - \beta_1 \bar{x}$$

Variables

x (Temperature) Independiente

y (Pressure) Dependiente

① Cálculo de las Medias

Temperature	$\sum x = 3420 / 19 = 180$
Pressure	$\sum y = 2,362.3974 / 19 = 124.3367053$

② Cálculo de la Varianza y Covarianza

Varianza Temperature

$$\begin{aligned} \sum_{x=1}^{19} (x - 180)^2 &= (0 - 180)^2 + (20 - 180)^2 + (40 - 180)^2 \\ &+ (60 - 180)^2 + (80 - 180)^2 + (100 - 180)^2 \\ &+ (120 - 180)^2 + (140 - 180)^2 + (160 - 180)^2 \\ &+ (180 - 180)^2 + (200 - 180)^2 + (220 - 180)^2 \\ &+ (240 - 180)^2 + (260 - 180)^2 + (280 - 180)^2 \\ &+ (300 - 180)^2 + (320 - 180)^2 + (340 - 180)^2 \\ &+ (360 - 180)^2 = 228,000 \end{aligned}$$

$$\begin{aligned} s^2 &= 228,000 / 19 \\ &= 12000 \end{aligned}$$



Covarianza Temperature y Pressure

$$\begin{aligned} \sum_{i=1}^{19} &= ((0-180) * (0.0002 - 124.3367)) + \\ &+ ((20-180) * (0.0012 - 124.3367)) + \\ &+ ((40-180) * (0.0060 - 124.3367)) + \\ &+ ((60-180) * (0.0300 - 124.3367)) + \\ &+ ((80-180) * (0.0900 - 124.3367)) + \\ &+ ((100-180) * (0.2300 - 124.3367)) + \\ &+ ((120-180) * (0.7500 - 124.3367)) + \\ &+ ((140-180) * (1.8300 - 124.3367)) + \\ &+ ((160-180) * (4.9000 - 124.3367)) + \\ &+ ((180-180) * (8.8000 - 124.3367)) + \\ &+ ((200-180) * (17.3000 - 124.3367)) + \\ &+ ((220-180) * (22.1000 - 124.3367)) + \\ &+ ((240-180) * (37.0000 - 124.3367)) + \\ &+ ((260-180) * (46.0000 - 124.3367)) + \\ &+ ((280-180) * (157.0000 - 124.3367)) + \\ &+ ((300-180) * (247.0000 - 124.3367)) + \\ &+ ((320-180) * (376.0000 - 124.3367)) + \\ &+ ((340-180) * (558.0000 - 124.3367)) + \\ &+ ((360-180) * (806.0000 - 124.3367)) \\ &= 344834.732 \end{aligned}$$

Calcular Coeficientes de Regresión

$$B_0 = \bar{y} - B_1 \bar{x} = 124.3367 - 1.512419877 * 180 = -147.8988779$$

$$B_1 = \frac{\text{Cov } x y}{\text{Var } x} = \frac{344834.732}{228,000} = 1.512419877$$



Predicción

$$\text{pred} = B_0 + B_1 * X$$

$$\begin{aligned} -147.8988779 + 1.512479877 * 90 \\ = -11.78108697 \end{aligned}$$

~~Robert Costa~~