Parameters Série A 2020 model r2

Rates for the home and away goals

$$\begin{split} \lambda_k(t) &= \alpha_i \beta_j \gamma_h \tau^{\mathbb{I}\{\text{half} = 2\}} e^{(x-y)\omega_{\lambda(x-y)}} e^{(y^*-x^*)\omega_{\lambda(y^*-x^*)}} \\ \mu_k(t) &= \alpha_j \beta_i \tau^{\mathbb{I}\{\text{half} = 2\}} e^{(y-x)\omega_{\mu(y-x)}} e^{(x^*-y^*)\omega_{\mu(x^*-y^*)}} \end{split}$$

- *i*: home team index;
- j: away team index;
- α : attack strength parameter;
- $1/\beta$: defense strength parameter;
- γ_h : home advantage parameter;
- τ : second half parameter;
- x: the number of goals of the home team until minute t;
- y: the number of goals of the away team until minute t;
- x^* : the number of red cards of the home team until minute t;
- y^* : the number of red cards of the away team until minute t;
- $\omega_{\lambda(x-y)}$ and $\omega_{\mu(y-x)}$: parameters that measure the impact of leading the score in goals;
- $\omega_{\lambda(y^*-x^*)}$ and $\omega_{\mu(x^*-y^*)}$: parameters that measure the impact of having extra players on the field.

Rates for the home and away red cards

$$\lambda_k^*(t) = A_\lambda \log(t + 1 + 45^{\mathbb{I}\{\text{half} = 2\}})$$
$$\mu_k^*(t) = A_\mu \log(t + 1 + 45^{\mathbb{I}\{\text{half} = 2\}})$$

Stoppage time

The stoppage time for the first half, U^1 , and the second half, U^2 , are modeled as:

$$U^1 \sim \text{Poisson}(\eta_1 + \phi_1 g^1 + \rho_1 r^1)$$

 $U^2 \sim \text{Poisson}(\eta_2 + \phi_2 g^2 + \rho_2 r^2 + \kappa c)$

- g^t is the amount of goals scored in half t until minute 45;
- r^t is the amount of red cards received in half t until minute 45;
- $c = \begin{cases} 1, & \text{if } |x-y| \le 1 \text{ at minute } 45 \text{ of the second half;} \\ 0, & \text{otherwise.} \end{cases}$

Constraint

The constraint for identificability is

$$\sum_{i=1}^{n} \log(\alpha_i) = \sum_{i=1}^{n} \log(\beta_i).$$

Table 1: Alphas and betas

Team	α	β
Athletico-PR	0.0794	0.0750
Athletico-GO	0.0848	0.0942
Atlético-MG	0.1412	0.0930
Bahia	0.0984	0.1301
Botafogo	0.0650	0.1325
Ceará	0.1142	0.1066
Corinthians	0.0951	0.0913
Coritiba	0.0637	0.1153
Flamengo	0.1480	0.0991
Fluminense	0.1176	0.0876
Fortaleza	0.0721	0.0917
Goiás	0.0823	0.1333
Grêmio	0.1146	0.0827
Internacional	0.1352	0.0682
Palmeiras	0.1111	0.0762
Red Bull Bragantino	0.1096	0.0818
Santos	0.1097	0.1062
São Paulo	0.1253	0.0857
Sport	0.0623	0.1076
Vasco da Gama	0.0788	0.1190

Table 2: Goal rate parameters

Parameter	Estimative
$\overline{\gamma_h}$	1.3797
au	1.1396
$\omega_{\lambda(x-y)}$	-0.1459
$\omega_{\mu(y-x)}$	-0.0991
$\omega_{\lambda(y^*-x^*)}$	0.3456
$\omega_{\mu(x^*-y^*)}$	0.4402

```
Parameter = c("$A_\\lambda$", "$A_\\mu$")
reds = tibble(Parameter, Estimative = exp(c(mod_r2$a)))
kable(reds, digits = 8, caption = "Red card rate parameters")
```

Table 3: Red card rate parameters

Parameter	Estimative
$\overline{A_{\lambda}}$	0.00036059
A_{μ}	0.00039003

Table 4: Stoppage time parameters

Parameter	Estimative
$\overline{\eta_1}$	2.8909
η_2	4.6762
ϕ_1	0.0305
ϕ_2	0.0372
$ ho_1$	1.8638
$ ho_2$	0.1383
κ	1.2101

```
mod_r2$loglik
```

[1] 1729.566