Parameters Série A 2019

Rates for the home and away teams

Model 0

$$\lambda_k = \alpha_i \beta_j \gamma_h$$
$$\mu_k = \alpha_i \beta_i$$

- *i*: home team index;
- j: away team index;
- α : attack strength parameter;
- $1/\beta$: defense strength parameter;
- γ_h : home advantage parameter.

Model 1

$$\lambda_k(t) = \alpha_i \beta_j \gamma_h$$
$$\mu_k(t) = \alpha_j \beta_i$$

Model 2

$$\lambda_k(t) = \alpha_i \beta_j \gamma_h \tau^{\mathbb{I}\{\text{half} = 2\}}$$
$$\mu_k(t) = \alpha_j \beta_i \tau^{\mathbb{I}\{\text{half} = 2\}}$$

• τ : second half parameter.

Model 3

$$\begin{split} \lambda_k(t) &= \alpha_i \beta_j \gamma_h \tau^{\mathbb{I}\{\text{half} = 2\}} \lambda_{xy} \\ \mu_k(t) &= \alpha_j \beta_i \tau^{\mathbb{I}\{\text{half} = 2\}} \mu_{xy} \end{split}$$

•
$$\lambda_{xy} = \begin{cases} 1, & \text{if } x = y; \\ \lambda_{10}, & \text{if } x > y; \\ \lambda_{01}, & \text{if } x < y; \end{cases}$$

•
$$\mu_{xy} = \begin{cases} 1, & \text{if } x = y; \\ \mu_{10}, & \text{if } x > y; \\ \mu_{01}, & \text{if } x < y. \end{cases}$$

Stoppage time

For all models except model 0, the stoppage time for the first half, U^1 , and the second half, U^2 , are modeled as:

$$U^1 \sim \text{Poisson}(\eta_1 + \phi_1 g^1)$$

 $U^2 \sim \text{Poisson}(\eta_2 + \phi_2 g^2 + \kappa c)$

- g^t is the amount of goals scored in half t until minute 45;
- $c = \begin{cases} 1, & \text{if } |x y| \le 1 \text{ at minute 45 of the second half;} \\ 0, & \text{otherwise.} \end{cases}$

Constraint

The constraint for identificability in all models is

kable(alphas, digits = 4, caption = "Alphas")

$$\sum_{i}^{n} \log(\alpha_i) = \sum_{i}^{n} \log(\beta_i)$$

Table 1: Alphas

Time	mod_0	mod_1	mod_2	mod_3
Athletico-PR	1.1254	0.1134	0.1074	0.1057
Atlético-MG	1.0132	0.1014	0.0960	0.0920
Avaí	0.4108	0.0417	0.0395	0.0362
Bahia	0.9835	0.0991	0.0938	0.0897
Botafogo	0.6940	0.0703	0.0665	0.0638
Ceará	0.8023	0.0805	0.0761	0.0718
Chapecoense	0.6998	0.0709	0.0670	0.0644
Corinthians	0.9286	0.0939	0.0888	0.0867
Cruzeiro	0.6050	0.0615	0.0582	0.0542
CSA	0.5454	0.0554	0.0524	0.0485

Time	mod_0	mod_1	mod_2	mod_3
Flamengo	1.9129	0.1935	0.1833	0.1919
Fluminense	0.8521	0.0857	0.0811	0.0771
Fortaleza	1.1262	0.1139	0.1078	0.1073
Goiás	1.0551	0.1058	0.1002	0.0956
Grêmio	1.4253	0.1448	0.1371	0.1364
Internacional	0.9787	0.0980	0.0928	0.0906
Palmeiras	1.3467	0.1360	0.1287	0.1304
Santos	1.3261	0.1348	0.1276	0.1314
São Paulo	0.8581	0.0861	0.0814	0.0807
Vasco da Gama	0.8735	0.0876	0.0829	0.0810

Table 2: Betas

Time	mod_0	mod_1	mod_2	mod_3		
Athletico-PR	0.6954	0.0698	0.0660	0.0623		
Atlético-MG	1.0584	0.1061	0.1005	0.0977		
Avaí	1.2971	0.1322	0.1252	0.1299		
Bahia	0.9273	0.0933	0.0883	0.0854		
Botafogo	0.9556	0.0968	0.0916	0.0911		
Ceará	0.8757	0.0882	0.0834	0.0823		
Chapecoense	1.1046	0.1115	0.1055	0.1051		
Corinthians	0.7311	0.0738	0.0698	0.0656		
Cruzeiro	0.9722	0.0990	0.0937	0.0930		
CSA	1.2220	0.1243	0.1177	0.1212		
Flamengo	0.8400	0.0847	0.0802	0.0734		
Fluminense	0.9851	0.0994	0.0940	0.0919		
Fortaleza	1.0649	0.1075	0.1017	0.0977		
Goiás	1.3856	0.1391	0.1317	0.1311		
Grêmio	0.8616	0.0869	0.0823	0.0796		
Internacional	0.8409	0.0847	0.0802	0.0770		
Palmeiras	0.7039	0.0712	0.0674	0.0642		
Santos	0.7251	0.0736	0.0697	0.0649		
São Paulo	0.6426	0.0645	0.0610	0.0578		
Vasco da Gama	0.9648	0.0966	0.0914	0.0886		

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mu_01 = c(NA, NA, NA, exp(mod_3$mu_xy["01"])),
    eta_1 = c(NA, mod_1$eta[1], mod_2$eta[1], mod_3$eta[1]),
    eta_2 = c(NA, mod_1$eta[2], mod_2$eta[2], mod_3$eta[2]),
    phi_1 = c(NA, mod_1$phi[1], mod_2$phi[1], mod_3$phi[1]),
    phi_2 = c(NA, mod_1$phi[2], mod_2$phi[2], mod_3$phi[2]),
        kappa = c(NA, mod_1$kappa, mod_2$kappa, mod_3$kappa))

kable(param, digits = 4, caption = "Other parameters",
    col.names = c("Model", "$\\gamma_h$", "$\\tau$", "$\\lambda_{10}$",
        "$\\lambda_{10}$", "$\\mu_{10}$", "$\\mu_{10}$", "$\\mu_{10}$", "$\\end{tappa}"))
```

Table 3: Other parameters

Mod	lel	γ_h	au	λ_{10}	λ_{01}	μ_{10}	μ_{01}	η_1	η_2	ϕ_1	ϕ_2	κ
0	1.4	957	-	-	-	-	-	-	-	-	-	
1	1.49	990	-		-	-	-	2.8341	3.6016	0.2261	0.2075	1.5566
2	1.49	994	1.2284	-	-	-	-	2.8341	3.6017	0.2261	0.2075	1.5566
3	1.6'	761	1.2707	0.7697	1.0283	1.2564	0.7582	2.8341	3.6016	0.2261	0.2075	1.5566