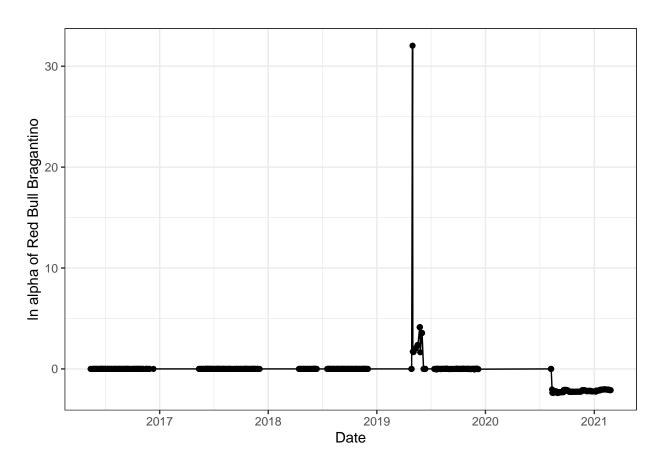
Red Bull Bragantino

```
library(dplyr)
library(ggplot2)
library(CVXR)
library(future.apply)
library(knitr)
source("~/GitHub/soccer-live-predictions/soccer-live-predictions/pred/pred_mod_8.R")
date = "2019-05-01"
csi = 0.0065/3.5
load("~/GitHub/soccer-live-predictions/soccer-live-predictions/weight/data/mod_8_dc.RData")
load("~/GitHub/soccer-live-predictions/soccer-live-predictions/scrape/data/results2.RData")
y = NULL
x = as.Date(names(mod_8_dc), format = "%Y-%m-%d")
for(i in 1:length(mod_8_dc)) {
 y[i] = mod_8_dc[[i]]$alpha["Red Bull Bragantino"]
tibble(x = x, y = y) \%
  ggplot(aes(x, y)) +
  geom_line() +
  theme_bw() +
  geom_point() +
  xlab("Date") +
  ylab("In alpha of Red Bull Bragantino")
```



results %>%
 filter(Home_Team == "Red Bull Bragantino" | Away_Team == "Red Bull Bragantino") %>%
 arrange(Date) %>%
 select(Season, Match, Date, Home_Team, Score_Home, Score_Away, Away_Team) %>%
 head(20) %>%
 kable()

Season	Match	Date	Home_Team	Score_Home	Score_Away	Away_Team
2020	4	2020-08-09	Santos	1	1	Red Bull Bragantino
2020	14	2020-08-12	Red Bull Bragantino	1	1	Botafogo
2020	27	2020-08-16	Bahia	2	1	Red Bull Bragantino
2020	34	2020-08-19	Red Bull Bragantino	2	1	Fluminense
2020	44	2020-08-23	Red Bull Bragantino	1	2	Coritiba
2020	59	2020-08-29	Fortaleza	3	0	Red Bull Bragantino
2020	68	2020-09-02	Athletico-PR	1	1	Red Bull Bragantino
2020	74	2020-09-06	Red Bull Bragantino	1	2	Palmeiras
2020	83	2020-09-09	São Paulo	1	1	Red Bull Bragantino
2020	95	2020-09-13	Atlético-MG	2	1	Red Bull Bragantino
2020	104	2020-09-19	Red Bull Bragantino	4	2	Ceará
2020	112	2020-09-27	Vasco da Gama	1	1	Red Bull Bragantino
2020	124	2020-10-03	Red Bull Bragantino	0	0	Corinthians
2020	134	2020-10-08	Red Bull Bragantino	0	2	Internacional
2020	150	2020-10-11	Atlético-GO	2	1	Red Bull Bragantino
2020	151	2020 - 10 - 15	Flamengo	1	1	Red Bull Bragantino
2020	164	2020-10-18	Red Bull Bragantino	2	0	Sport

Season	Match	Date	Home_Team	Score_Home	Score_Away	Away_Team
2020	174	2020-10-24	Red Bull Bragantino	2	0	Goiás
2020	186	2020-11-02	Grêmio	2	1	Red Bull Bragantino
2020	194	2020-11-08	Red Bull Bragantino	1	1	Santos

```
results %>%
  filter(Season == 2019) %>%
  arrange(Date) %>%
  select(Season, Match, Date, Home_Team, Score_Home, Score_Away, Away_Team) %>%
  head(20) %>%
  kable()
```

Season	Match	Date	${\rm Home_Team}$	Score_Home	Score_Away	Away_Team
2019	2	2019-04-27	Atlético-MG	2	1	Avaí
2019	5	2019-04-27	São Paulo	2	0	Botafogo
2019	6	2019-04-27	Flamengo	3	1	Cruzeiro
2019	8	2019-04-27	Chapecoense	2	0	Internacional
2019	1	2019-04-28	Grêmio	1	2	Santos
2019	3	2019-04-28	Ceará	4	0	Csa
2019	4	2019-04-28	Palmeiras	4	0	Fortaleza
2019	7	2019-04-28	Fluminense	0	1	Goiás
2019	9	2019-04-28	Bahia	3	2	Corinthians
2019	10	2019-04-28	Athletico-PR	4	1	Vasco da Gama
2019	11	2019-05-01	Internacional	2	1	Flamengo
2019	12	2019-05-01	Cruzeiro	1	0	Ceará
2019	13	2019-05-01	Fortaleza	2	1	Athletico-PR
2019	14	2019-05-01	Corinthians	1	0	Chapecoense
2019	16	2019-05-01	Vasco da Gama	1	2	Atlético-MG
2019	18	2019-05-01	Avaí	1	1	Grêmio
2019	19	2019-05-01	Goiás	1	2	São Paulo
2019	20	2019-05-01	Csa	1	1	Palmeiras
2019	15	2019-05-02	Santos	2	1	Fluminense
2019	17	2019-05-02	Botafogo	3	2	Bahia

```
load("~/GitHub/soccer-live-predictions/soccer-live-predictions/2015-2020/data/input.RData")
load("~/GitHub/soccer-live-predictions/soccer-live-predictions/2015-2020/data/input_mod_7.RData")
lines = match_dates %>%
    filter(Date < date)

lines1 = lines$Lines1 %>%
    unlist()

lines2 = lines$Lines2 %>%
    unlist()

lines1s = lines$Lines1s %>%
    unlist()
```

```
unlist()
M1_lambda = M1_lambda[lines1,]
M1_mu = M1_mu[lines1,]
M2_lambda = M2_lambda[lines2,]
M2_mu = M2_mu[lines2,]
delta1 = delta1[lines1]
delta2 = delta2[lines2]
H1r = H1r[lines1]
H2r = H2r[lines2]
A1r = A1r[lines1]
A2r = A2r[lines2]
delta1s = delta1s[lines1s]
delta2s = delta2s[lines2s]
int_reds_1 = int_reds_1[lines1s]
int_reds_2 = int_reds_2[lines2s]
H1s = H1s[lines1s]
H2s = H2s[lines2s]
A1s = A1s[lines1s]
A2s = A2s[lines2s]
ind = lines$Ind
U1 = U1[ind]
U2 = U2[ind]
r1 = r1[ind]
r2 = r2[ind]
c = c[ind]
dates_1 = dates_1[which(dates_1 < date)]</pre>
dates_2 = dates_2[which(dates_2 < date)]</pre>
dates_1s = dates_1s[which(dates_1s < date)]</pre>
dates_2s = dates_2s[which(dates_2s < date)]</pre>
dif_1 = as.integer(difftime(as.Date(date, "%Y-%m-%d"), as.Date(dates_1, "%Y-%m-%d"), units = "days"))
dif_2 = as.integer(difftime(as.Date(date, "%Y-%m-%d"), as.Date(dates_2, "%Y-%m-%d"), units = "days"))
dif_st = as.integer(difftime(as.Date(date, "%Y-%m-%d"), as.Date(lines$Date, "%Y-%m-%d"), units = "days"
w_1 = \exp(- csi * dif_1)
w_2 = \exp(- csi * dif_2)
w_1s = exp(-csi * dif_1s)
w_2s = exp(-csi * dif_2s)
w_st = exp(-csi * dif_st)
alpha = Variable(n)
beta = Variable(n)
gamma = Variable(1)
tau = Variable(1)
omega_xy = Variable(2)
omega = Variable(1)
```

```
theta = vstack(alpha, beta, gamma, tau, omega_xy[1], omega_xy[2], omega_xy[2], omega_xy[1], omega, omeg
eta = Variable(2)
rho = Variable(2)
kappa = Variable(1)
pi1 = eta[1] + rho[1] * r1
pi2 = eta[2] + rho[2] * r2 + c * kappa
a = Variable(2)
loglambda1 = log(delta1) + M1_lambda %*% theta
logmu1 = log(delta1) + M1_mu %*% theta
loglambda2 = log(delta2) + M2_lambda %*% theta
logmu2 = log(delta2) + M2_mu %*% theta
loglambda1s = log(int_reds_1) + a[1]
logmu1s = log(int_reds_1) + a[2]
loglambda2s = log(int_reds_2) + a[1]
logmu2s = log(int_reds_2) + a[2]
log_lik_goals = sum_entries((
  - exp(loglambda1) - exp(logmu1) +
   H1r*loglambda1 + A1r*logmu1) * w_1) +
  sum_entries((
    - exp(loglambda2) - exp(logmu2) +
      + H2r*loglambda2 + A2r*logmu2) * w_2)
log_lik_reds = sum_entries((
  - exp(loglambda1s) - exp(logmu1s) +
   H1s*loglambda1s + A1s*logmu1s) * w_1s) +
  sum_entries((
    - exp(loglambda2s) - exp(logmu2s) +
      + H2s*loglambda2s + A2s*logmu2s) * w_2s)
log_lik_st = sum_entries((U1 * log(pi1) + U2 * log(pi2) - pi1 - pi2) * w_st)
log_lik = log_lik_goals + log_lik_reds + log_lik_st
objective = Maximize(log_lik)
constraints = list(sum(alpha) - sum(beta) == 0)
problem = Problem(objective, constraints)
solution = solve(problem, solver = "MOSEK")
mod_8_cons = list(alpha = as.vector(c(solution$getValue(alpha))),
                  beta = as.vector(solution$getValue(beta)),
                  gamma = as.vector(solution$getValue(gamma)),
                  tau = as.vector(solution$getValue(tau)),
                  omega_xy = as.vector(solution$getValue(omega_xy)),
                  omega = as.vector(solution$getValue(omega)),
                  a = as.vector(solution$getValue(a)),
                  eta = as.vector(solution$getValue(eta)),
                  rho = as.vector(solution$getValue(rho)),
                  kappa = as.vector(solution$getValue(kappa)),
```

```
loglik = solution$value)
names(mod_8_cons$alpha) = times$Time
names(mod_8_cons$beta) = times$Time
names(mod_8_cons$omega_xy) = c("ahead", "behind")
names(mod_8_cons$omega) = "red"
names(mod_8_cons$a) = c("lambda", "mu")
mod_8_cons
   $alpha
##
##
             América-MG
                                Athletico-PR
                                                       Atlético-GO
                                                                            Atlético-MG
                                   -2.182798
                                                                              -2.103145
##
              -2.838196
                                                         -2.517537
##
                   Avaí
                                       Bahia
                                                         Botafogo
                                                                                  Ceará
##
              -2.678969
                                   -2.352878
                                                         -2.447604
                                                                              -2.661163
##
           Chapecoense
                                 Corinthians
                                                          Coritiba
                                                                               Cruzeiro
##
              -2.470348
                                   -2.377367
                                                         -2.465443
                                                                              -2.433229
##
                    Csa
                                 Figueirense
                                                                             Fluminense
                                                         Flamengo
             -17.410185
                                   -2.696496
##
                                                         -2.099090
                                                                              -2.524967
##
              Fortaleza
                                       Goiás
                                                            Grêmio
                                                                          Internacional
##
             -17.437101
                                   -2.449300
                                                         -2.270282
                                                                              -2.320728
##
              Joinville
                                   Palmeiras
                                                            Paraná
                                                                            Ponte Preta
              -2.866756
                                                         -3.263105
                                                                              -2.447408
##
                                   -1.961524
##
   Red Bull Bragantino
                                  Santa Cruz
                                                            Santos
                                                                              São Paulo
##
              32.037125
                                   -2.349861
                                                         -2.245080
                                                                              -2.279207
##
                  Sport
                               Vasco da Gama
                                                           Vitória
##
              -2.438185
                                   -2.472952
                                                         -2.414405
##
   $beta
##
##
             América-MG
                                Athletico-PR
                                                      Atlético-GO
                                                                            Atlético-MG
##
              -2.338389
                                   -2.608690
                                                         -2.239281
                                                                              -2.417258
##
                                       Bahia
                                                         Botafogo
                                                                                  Ceará
                   Avaí
##
              -2.329469
                                   -2.457922
                                                         -2.489460
                                                                              -2.650420
##
           Chapecoense
                                 Corinthians
                                                         Coritiba
                                                                               Cruzeiro
              -2.374987
                                   -2.665832
                                                         -2.403680
                                                                              -2.584921
##
##
                    Csa
                                 Figueirense
                                                         Flamengo
                                                                             Fluminense
##
              -1.149360
                                   -2.342272
                                                         -2.733107
                                                                              -2.377072
##
              Fortaleza
                                                                          Internacional
                                       Goiás
                                                            Grêmio
##
              -1.660983
                                   -2.616874
                                                         -2.741199
                                                                              -2.736669
##
              Joinville
                                   Palmeiras
                                                            Paraná
                                                                            Ponte Preta
                                                                              -2.341986
##
              -2.350373
                                   -2.751432
                                                         -2.154857
                                                                              São Paulo
##
   Red Bull Bragantino
                                  Santa Cruz
                                                            Santos
##
               0.000000
                                   -1.927020
                                                         -2.654380
                                                                              -2.608088
##
                  Sport
                               Vasco da Gama
                                                           Vitória
##
              -2.225726
                                   -2.366431
                                                         -2.140048
##
   $gamma
##
   [1] 0.5165079
##
##
   $tau
   [1] 0.254763
##
##
   $omega_xy
##
```

ahead

behind

```
## -0.2369025 0.1470653
##
## $omega
##
         red
## 0.2563516
##
## $a
##
      lambda
## -10.89324 -10.39585
##
## $eta
## [1] 2.265243 3.510628
## $rho
## [1] 0.8934947 0.2740488
##
## $kappa
## [1] 0.9272729
##
## $loglik
## [1] -2768.927
load("~/GitHub/soccer-live-predictions/soccer-live-predictions/2015-2020/data/input.RData")
load("~/GitHub/soccer-live-predictions/soccer-live-predictions/2015-2020/data/input_mod_7.RData")
lines = match_dates %>%
  filter(Date < date)</pre>
lines1 = lines$Lines1 %>%
  unlist()
lines2 = lines$Lines2 %>%
  unlist()
lines1s = lines$Lines1s %>%
  unlist()
lines2s = lines$Lines2s %>%
  unlist()
M1_lambda = M1_lambda[lines1,]
M1_mu = M1_mu[lines1,]
M2_lambda = M2_lambda[lines2,]
M2_mu = M2_mu[lines2,]
delta1 = delta1[lines1]
delta2 = delta2[lines2]
H1r = H1r[lines1]
H2r = H2r[lines2]
A1r = A1r[lines1]
A2r = A2r[lines2]
delta1s = delta1s[lines1s]
delta2s = delta2s[lines2s]
int_reds_1 = int_reds_1[lines1s]
```

```
int_reds_2 = int_reds_2[lines2s]
H1s = H1s[lines1s]
H2s = H2s[lines2s]
A1s = A1s[lines1s]
A2s = A2s[lines2s]
ind = lines$Ind
U1 = U1[ind]
U2 = U2[ind]
r1 = r1[ind]
r2 = r2[ind]
c = c[ind]
dates_1 = dates_1[which(dates_1 < date)]</pre>
dates_2 = dates_2[which(dates_2 < date)]</pre>
dates_1s = dates_1s[which(dates_1s < date)]</pre>
dates_2s = dates_2s[which(dates_2s < date)]</pre>
dif_1 = as.integer(difftime(as.Date(date, "%Y-%m-%d"), as.Date(dates_1, "%Y-%m-%d"), units = "days"))
dif_2s = as.integer(difftime(as.Date(date, "%Y-%m-%d"), as.Date(dates_2s, "%Y-%m-%d"), units = "days"))
dif_st = as.integer(difftime(as.Date(date, "%Y-%m-%d"), as.Date(lines$Date, "%Y-%m-%d"), units = "days"
w_1 = \exp(- csi * dif_1)
w_2 = \exp(- csi * dif_2)
w_1s = exp(-csi * dif_1s)
w_2s = exp(-csi * dif_2s)
w_st = exp(-csi * dif_st)
alpha = Variable(n)
beta = Variable(n)
gamma = Variable(1)
tau = Variable(1)
omega_xy = Variable(2)
omega = Variable(1)
theta = vstack(alpha, beta, gamma, tau, omega_xy[1], omega_xy[2], omega_xy[2], omega_xy[1], omega, omeg
eta = Variable(2)
rho = Variable(2)
kappa = Variable(1)
pi1 = eta[1] + rho[1] * r1
pi2 = eta[2] + rho[2] * r2 + c * kappa
a = Variable(2)
loglambda1 = log(delta1) + M1_lambda %*% theta
logmu1 = log(delta1) + M1_mu %*% theta
loglambda2 = log(delta2) + M2_lambda %*% theta
logmu2 = log(delta2) + M2_mu %*% theta
loglambda1s = log(int_reds_1) + a[1]
```

```
logmu1s = log(int_reds_1) + a[2]
loglambda2s = log(int_reds_2) + a[1]
logmu2s = log(int_reds_2) + a[2]
log_lik_goals = sum_entries((
  - exp(loglambda1) - exp(logmu1) +
   H1r*loglambda1 + A1r*logmu1) * w_1) +
  sum entries((
    - exp(loglambda2) - exp(logmu2) +
      + H2r*loglambda2 + A2r*logmu2) * w 2)
log_lik_reds = sum_entries((
  - exp(loglambda1s) - exp(logmu1s) +
    H1s*loglambda1s + A1s*logmu1s) * w_1s) +
  sum_entries((
    - exp(loglambda2s) - exp(logmu2s) +
      + H2s*loglambda2s + A2s*logmu2s) * w_2s)
log_lik_st = sum_entries((U1 * log(pi1) + U2 * log(pi2) - pi1 - pi2) * w_st)
log_lik = log_lik_goals + log_lik_reds + log_lik_st
objective = Maximize(log_lik)
problem = Problem(objective)
solution = solve(problem, solver = "MOSEK")
mod_8_no_cons = list(alpha = as.vector(c(solution$getValue(alpha))),
                     beta = as.vector(solution$getValue(beta)),
                     gamma = as.vector(solution$getValue(gamma)),
                     tau = as.vector(solution$getValue(tau)),
                     omega_xy = as.vector(solution$getValue(omega_xy)),
                     omega = as.vector(solution$getValue(omega)),
                     a = as.vector(solution$getValue(a)),
                     eta = as.vector(solution$getValue(eta)),
                     rho = as.vector(solution$getValue(rho)),
                     kappa = as.vector(solution$getValue(kappa)),
                     loglik = solution$value)
names(mod_8_no_cons$alpha) = times$Time
names(mod_8_no_cons$beta) = times$Time
names(mod_8_no_cons$omega_xy) = c("ahead", "behind")
names(mod_8_no_cons$omega) = "red"
names(mod_8_no_cons$a) = c("lambda", "mu")
mod_8_no_cons
## $alpha
##
            América-MG
                              Athletico-PR
                                                   Atlético-GO
                                                                        Atlético-MG
##
             -2.838196
                                 -2.182798
                                                     -2.517537
                                                                          -2.103145
##
                  Avaí
                                     Bahia
                                                                              Ceará
                                                      Botafogo
##
             -2.678969
                                 -2.352878
                                                     -2.447604
                                                                          -2.661163
##
           Chapecoense
                               Corinthians
                                                      Coritiba
                                                                           Cruzeiro
             -2.470348
                                                     -2.465443
                                                                          -2.433229
##
                                 -2.377367
##
                   Csa
                               Figueirense
                                                      Flamengo
                                                                         Fluminense
```

```
-2.696496
                                                                              -2.524967
##
            -17.410185
                                                        -2.099090
##
             Fortaleza
                                       Goiás
                                                            Grêmio
                                                                          Internacional
            -17.437101
                                   -2.449300
                                                                              -2.320728
##
                                                         -2.270282
##
              Joinville
                                   Palmeiras
                                                                            Ponte Preta
                                                            Paraná
              -2.866756
                                   -1.961524
                                                         -3.263105
                                                                              -2.447408
## Red Bull Bragantino
                                  Santa Cruz
                                                                              São Paulo
                                                            Santos
##
              0.000000
                                   -2.349861
                                                         -2.245080
                                                                              -2.279207
##
                               Vasco da Gama
                  Sport
                                                           Vitória
##
             -2.438185
                                   -2.472952
                                                         -2.414405
##
##
   $beta
##
                                Athletico-PR
                                                                            Atlético-MG
            América-MG
                                                      Atlético-GO
             -2.338389
                                   -2.608690
                                                        -2.239281
                                                                              -2.417258
##
##
                                       Bahia
                   Avaí
                                                         Botafogo
                                                                                  Ceará
##
             -2.329469
                                   -2.457922
                                                         -2.489460
                                                                              -2.650420
##
           Chapecoense
                                 Corinthians
                                                          Coritiba
                                                                               Cruzeiro
##
             -2.374987
                                   -2.665832
                                                         -2.403680
                                                                              -2.584921
##
                    Csa
                                 Figueirense
                                                         Flamengo
                                                                             Fluminense
##
             -1.149360
                                   -2.342272
                                                        -2.733107
                                                                              -2.377072
##
             Fortaleza
                                       Goiás
                                                            Grêmio
                                                                          Internacional
##
             -1.660983
                                   -2.616874
                                                        -2.741199
                                                                              -2.736669
##
             Joinville
                                   Palmeiras
                                                            Paraná
                                                                            Ponte Preta
             -2.350373
                                   -2.751432
                                                        -2.154857
                                                                              -2.341986
##
##
  Red Bull Bragantino
                                  Santa Cruz
                                                            Santos
                                                                              São Paulo
                                                                              -2.608088
##
              0.000000
                                   -1.927020
                                                        -2.654380
##
                  Sport
                               Vasco da Gama
                                                           Vitória
##
             -2.225726
                                   -2.366431
                                                        -2.140048
##
##
   $gamma
   [1] 0.5165079
##
## $tau
   [1] 0.254763
##
##
   $omega_xy
##
        ahead
                   behind
##
   -0.2369025 0.1470653
##
## $omega
##
         red
## 0.2563516
##
##
  $a
##
      lambda
                     mu
  -10.89324 -10.39585
##
   $eta
   [1] 2.265243 3.510628
##
## $rho
   [1] 0.8934947 0.2740488
##
## $kappa
## [1] 0.9272729
```

```
##
## $loglik
## [1] -2768.927
pred_mod_8(mod_8_cons, home_team = "Santos", away_team = "Fluminense", n = 10^6)
## $Result
##
       Santos
                     Draw Fluminense
##
     0.648044
                 0.243234
                            0.108722
##
## $Score
##
                                     2-1
                                               0-0
                                                        3-0
##
        1-0
                  2-0
                           1-1
  0.183577 0.138382 0.115608 0.109187 0.086956 0.068206 0.052887 0.050085
                                     3-2
                  1-2
                           4-0
                                               4-1
                                                        0 - 2
##
  0.035680 0.031146 0.025061 0.021270 0.019123 0.012136 0.007537 0.007397
        2-3
                  5-1
                           3-3
                                     1-3
                                               5-2
                                                        4-3
                                                                  0 - 3
## 0.006412 0.005679 0.004649 0.004640 0.002170 0.001984 0.001946 0.001816
        6-1
                  2-4
                           3 - 4
                                     1 - 4
                                               5-3
                                                        6-2
                                                                  7-0
## 0.001368 0.000725 0.000594 0.000549 0.000531 0.000517 0.000430 0.000329
##
        7-1
                  0 - 4
                           6-3
                                     5-4
                                               7-2
                                                        8-0
                                                                  3-5
## 0.000303 0.000235 0.000146 0.000124 0.000104 0.000072 0.000063 0.000061
                  1-5
                           4-5
                                     7-3
                                               6-4
                                                        0-5
                                                                  8-2
        8-1
## 0.000061 0.000055 0.000037 0.000036 0.000028 0.000021 0.000018 0.000011
        9-1
                  2 - 6
                           1 - 6
                                     9-0
                                              10-0
                                                        4-6
                                                                  9 - 2
                                                                           11 - 0
## 0.000008 0.000007 0.000006 0.000006 0.000004 0.000003 0.000003 0.000002
##
                  8-3
                          10-1
                                     3-6
                                               6-6
                                                        7-4
## 0.000002 0.000002 0.000001 0.000001 0.000001 0.000001 0.000001
pred_mod_8(mod_8_no_cons, home_team = "Santos", away_team = "Fluminense", n = 10^6)
## $Result
##
       Santos
                     Draw Fluminense
##
     0.647751
                 0.243881
                            0.108368
##
## $Score
##
##
                                               0 - 0
                                                        3-0
                  2 - 0
                           1 - 1
                                     2 - 1
## 0.183859 0.137753 0.116197 0.108897 0.087320 0.068503 0.053170 0.049768
                  1-2
                           4-0
                                     3-2
                                               4-1
                                                        0-2
                                                                  4-2
## 0.035392 0.031268 0.024877 0.020992 0.019287 0.011944 0.007710 0.007415
                  5-1
                           1-3
                                     3-3
                                               5-2
                                                        0-3
                                                                  4-3
## 0.006227 0.005545 0.004784 0.004610 0.002145 0.002002 0.001966 0.001815
        6-1
                  2-4
                           5-3
                                     3-4
                                               1 - 4
                                                        6-2
                                                                  7-0
## 0.001361 0.000685 0.000603 0.000599 0.000594 0.000523 0.000398 0.000343
        7-1
                  0 - 4
                           6-3
                                     7-2
                                               5-4
                                                        8-0
                                                                  2-5
## 0.000316 0.000254 0.000139 0.000107 0.000098 0.000072 0.000067 0.000063
##
                                     4-5
                                               7-3
                                                        9-0
                                                                  0-5
                  1 - 5
                           6 - 4
## 0.000051 0.000046 0.000036 0.000027 0.000027 0.000024 0.000022 0.000022
        5-5
                  9-1
                           1 - 6
                                     2-6
                                               3-6
                                                        7-4
                                                                  8-3
## 0.000019 0.000011 0.000008 0.000008 0.000006 0.000006 0.000004 0.000003
                                     7-5
        6-5
                  0 - 6
                           0 - 7
                                               6 - 7
                                                        9-2
                                                                  9 - 3
```

0.000003 0.000002 0.000002 0.000002 0.000001 0.000001 0.000001