$$f(t) = \log(t+1)$$

```
options(scipen = 999)

library(dplyr)
library(ggplot2)
library(CVXR)

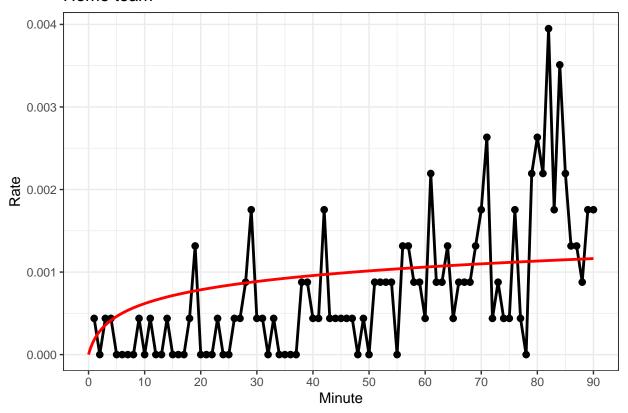
load("scrape/data/reds.RData")
load("2015-2020/data/input.RData")
```

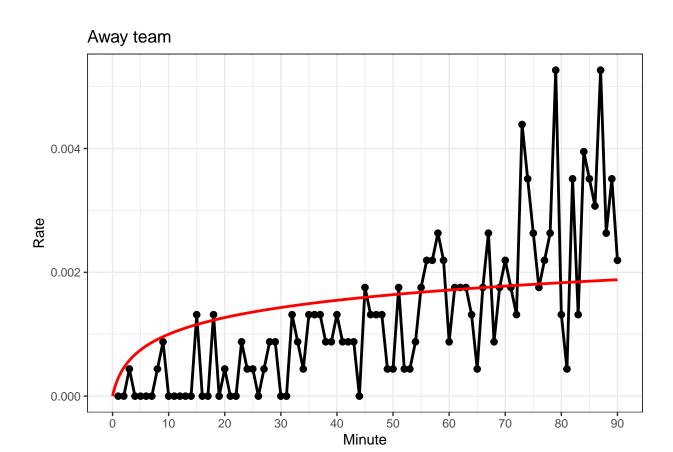
$$\lambda_k^*(t) = A_\lambda \log(t+1)$$
$$\mu_k^*(t) = A_\mu \log(t+1)$$

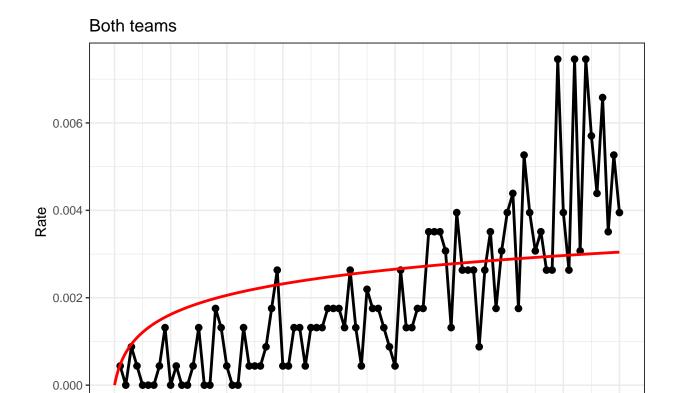
```
reds$Stoppage_Time[which(is.na(reds$Stoppage_Time))] = 0
reds = reds %>%
  mutate(Minute = Minute + Stoppage_Time) %>%
  filter(Minute <= 45)</pre>
reds$Minute[which(reds$Half == 2)] = reds$Minute[which(reds$Half == 2)] + 45
tib_zeros = tibble(Minute = 1:90, n = 0L)
complete_zeros <- function(tib_count) {</pre>
  tib_count %>%
    full_join(tib_zeros, by = c("Minute", "n")) %>%
    group_by(Minute) %>%
    summarise(n = sum(n))
}
home = reds %>%
  filter(Team == 1) %>%
  count(Minute) %>%
  complete_zeros() %>%
  mutate(Rate = n/N)
both = reds %>%
  count(Minute) %>%
  complete_zeros() %>%
  mutate(Rate = n/N)
away = reds %>%
  filter(Team == 2) %>%
  count(Minute) %>%
  complete_zeros() %>%
  mutate(Rate = n/N)
```

```
for(k in 1:N) {
  I2s[[k]] = I2s[[k]] + 45
}
int_reds_1 = list(); int_reds_2 = list();
for(k in 1:N) {
  tmp_int_reds_1 = NULL
  for(l in 1:(length(I1s[[k]])-1)) {
   t1 = I1s[[k]][1]
   t2 = I1s[[k]][1+1]
    tmp_int_reds_1[1] = (t2+1) * (log(t2+1)-1) - (t1+1) * (log(t1+1)-1) # <---
  int_reds_1[[k]] = tmp_int_reds_1
for(k in 1:N) {
  tmp_int_reds_2 = NULL
  for(l in 1:(length(I2s[[k]])-1)) {
   t1 = I2s[[k]][1]
    t2 = I2s[[k]][1+1]
    tmp_int_reds_2[1] = (t2+1) * (log(t2+1)-1) - (t1+1) * (log(t1+1)-1) # <---
  int_reds_2[[k]] = tmp_int_reds_2
int_reds_1 = unlist(int_reds_1)
int_reds_2 = unlist(int_reds_2)
a = Variable(2)
loglambda1s = log(int_reds_1) + a[1]
logmu1s = log(int_reds_1) + a[2]
loglambda2s = log(int_reds_2) + a[1]
logmu2s = log(int_reds_2) + a[2]
log_lik_reds = sum_entries(
  - exp(loglambda1s) - exp(logmu1s) +
    H1s*loglambda1s + A1s*logmu1s) +
  sum_entries(
    - exp(loglambda2s) - exp(logmu2s) +
      + H2s*loglambda2s + A2s*logmu2s)
objective = Maximize(log_lik_reds)
problem = Problem(objective)
solution = solve(problem, solver = "MOSEK")
A = exp(as.vector(solution$getValue(a)))
names(A) = c("A_lambda", "A_mu")
##
       A lambda
## 0.0002579376 0.0004169571
t = seq(0, 90, by = 0.01)
rate home = A[1] * log(t+1) # <---
rate_away = A[2] * log(t+1) # <---
```

Home team







Minute

solution\$value

[1] -2398.135