

RESPONSE TO REFEREE

ON SOFIC GROUPOIDS AND THEIR FULL GROUPS

SUR LES GROUPOÏDES SOFIQUES ET LEUR GROUPE PLEINS

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I agree with all of the comments made by the referee, and they have all been addressed. Below are the changes I made:

- (1) Stated instead that they are "injections and thus Borel isomorphisms onto their images", with appropriate reference.
- (2) Added the definition of strong limit of measures as a footnote.
- (3) Added a small paragraph after Definition 3.1, as an example (G sofic implies $[G]$ metrically sofic). Added a paragraph at the beginning of the proof of 3.5 referring to it.
- (4) Added "sofic approximation" to Definition 3.1.
- (5) substituted by "the distance between $\phi_k(r(\alpha A))$ and $\theta_k(\alpha)(\phi(A))$ converges to zero". Also restated that (θ, ϕ) is "asymptotically covariant" (instead of "invariant").
- (6) Corrected.

I was not aware of [2], and I thank the referee for pointing this out. A remark was added after Definition 2.2, and the abstract was modified accordingly (removed the parts stating we introduce this notion).

I also corrected the name in reference [3], and re-referenced the Lusin-Novikov theorem to Kechris' book [1]), since the proof from Srivastava's book ([4]) comes from Kechris'.

Finally, I added a paragraph with "Acknowledgements" at the end, and moved the reference of my supervisors there instead of the footnote in the first page.

Below is the list of comments sent by the referee, for simplicity:

- (1) p. 1, line 50: in the definition of the Borel full semigroup, it would be more clear to say that $s|_A$ and $r|_A$ are both injections (as opposed to bijections), since only the domains of these functions are specified, but not the codomains.
- (2) p. 3, line 15: It would be helpful if the definition of "strong limit" of measures was given.
- (3) p. 7, Theorem 3.5: Only one of the implications in the statement of Theorem 3.5 is acknowledged in the proof sketch.
- (4) p. 7, line 14: "sofic approximation for $[G]$ " was never defined. Presumably this means "a sequence of maps as in Definition 3.1," but this should be made explicit
- (5) p. 7, lines 18-19: "as close as necessary" is an awkward phrase to use here and should be rephrased.
- (6) p. 7, line 20: "sofic approximation of $[[G]]$ " should be "sofic approximation of G "

REFERENCES

- [1] A. S. Kechris. *Classical descriptive set theory*, volume 156 of *Graduate Texts in Mathematics*. Springer-Verlag, New York, 1995.
- [2] Y. Kida. Invariants of orbit equivalence relations and Baumslag-Solitar groups. *Tohoku Math. J. (2)*, 66(2):205–258, 2014.
- [3] L. Păunescu. On sofic actions and equivalence relations. *J. Funct. Anal.*, 261(9):2461–2485, 2011.

- [4] S. M. Srivastava. *A course on Borel sets*, volume 180 of *Graduate Texts in Mathematics*. Springer-Verlag, New York, 1998.
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