

# Prova P1

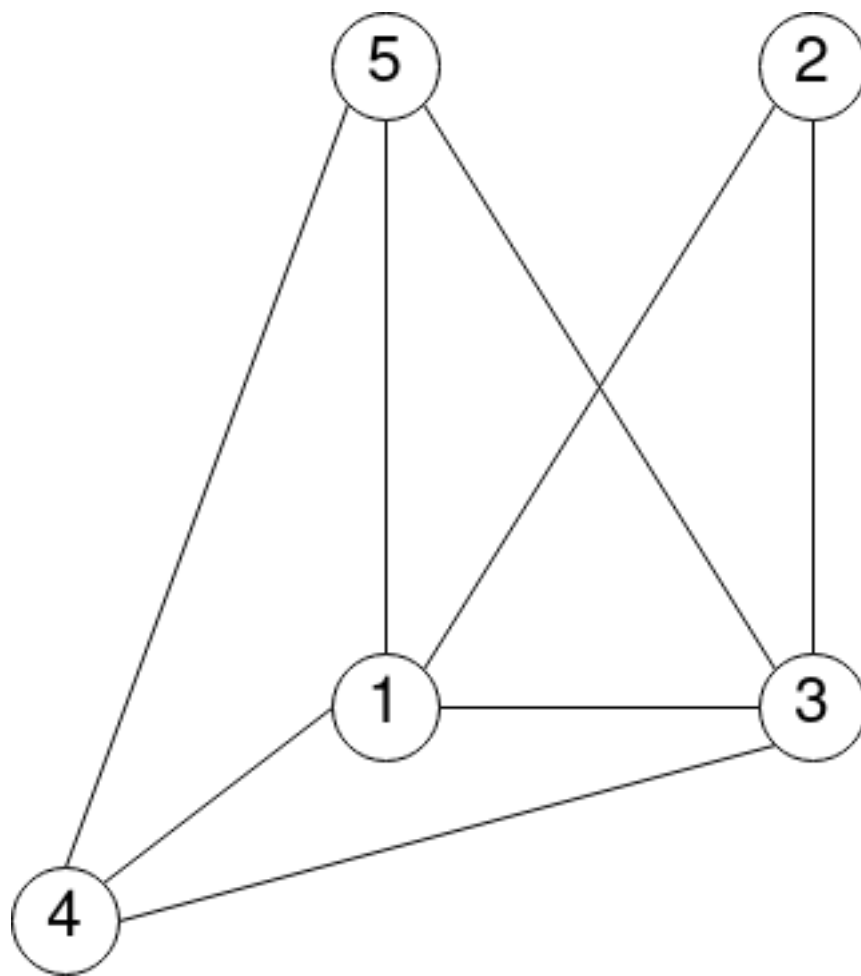
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1)

```
boolean is_regular(){  
    return grauMinimo() == grauMaximo();  
}
```

2)

a)



b)

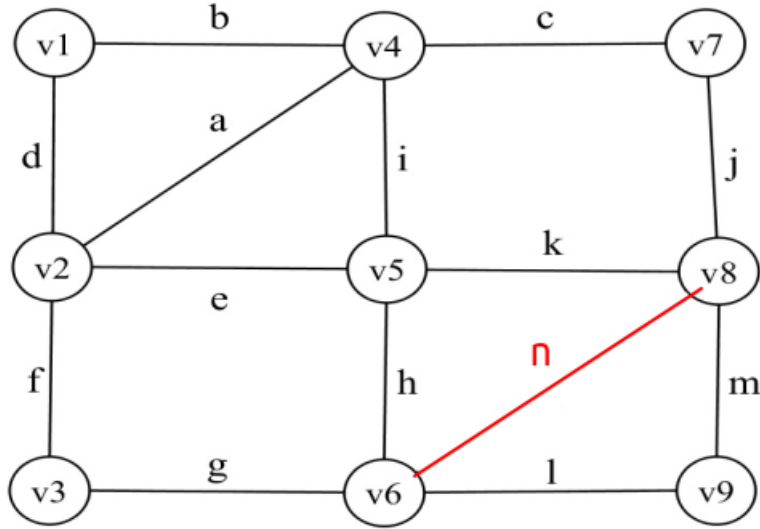
	1	2	3	4	5
1	0	1	1	1	1
2	1	0	1	0	0
3	1	1	0	1	1
4	1	0	1	0	1
5	1	0	1	1	0

3)

Nao, pois possui vertices de grau impar( $v_6$  e  $v_8$ )

b)

Para que  $G$  seja um grafo euleriano, é necessario adicionar apenas **uma aresta**, obtendo  $G'$  abaixo:



$$T_0 = v_1$$

$$T_1 = v_1, b, v_4$$

$$T_2 = v_1, b, v_4, c, v_7$$

$$T_3 = v_1, b, v_4, c, v_7, j, v_8$$

$$T_4 = v_1, b, v_4, c, v_7, j, v_8, m, v_9$$

$$T_5 = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6$$

$$T_6 = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8$$

$$T_7 = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5$$

$$T_8 = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5, h, v_6$$

$$T_9 = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5, h, v_6, g, v_3$$

$$T_{10} = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5, h, v_6, g, v_3, f, v_2$$

$$T_{11} = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5, h, v_6, g, v_3, f, v_2, c, v_5$$

$$T_{12} = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5, h, v_6, g, v_3, f, v_2, c, v_5, i, v_4$$

$T_{13} = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5, h, v_6, g, v_3, f, v_2, c, v_5, i, v_4, a, v_2$

$T_{14} = v_1, b, v_4, c, v_7, j, v_8, m, v_9, l, v_6, n, v_8, k, v_5, h, v_6, g, v_3, f, v_2, c, v_5, i, v_4, a, v_2, d, v_1$

4)

Sim, pois possui o seguinte circuito hamiltoniano

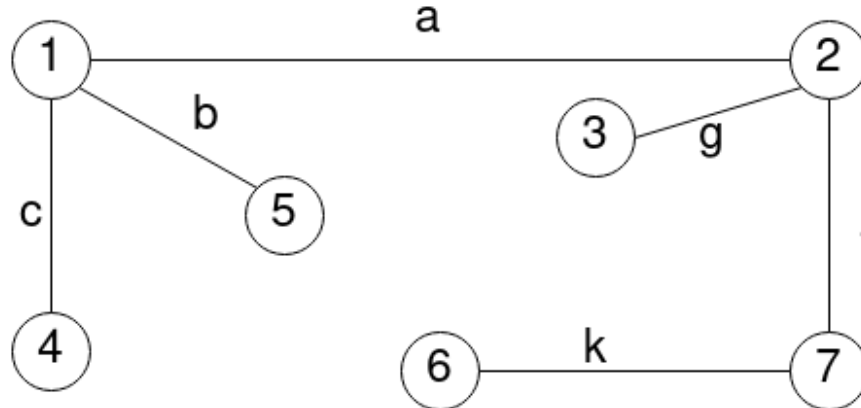
$C = v_1, a, v_5, i, v_4, c, v_7, j, v_8, m, v_9, l, v_6, g, v_3, f, v_2, d, v_1$

5)

Arestas	a	c	k	b	j	d	g	e	i	l	k
Custos	1	4	4	5	5	6	6	7	8	8	9

Somando os custos:

$$a + b + c + g + k + l = 25$$



6)

a)

$$E = \{k, a, h, b\}$$

b)

$$C = \{v_0, v_2, v_6, v_4\}$$

**c)**

Sendo  $H$  um grafo bipartido, o número de arestas em um emparelhamento máximo é igual ao número de vértices em uma cobertura mínima.