A hybrid algorithm for a class of vehicle routing problems

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Abstract

In this work we propose a hybrid algorithm for a class of Vehicle Routing Problems with homogeneous fleet. A sequence of Set Partitioning (SP) models, with columns corresponding to routes found by a metaheuristic approach, are solved, not necessarily to optimality, using a Mixed Integer Programming (MIP) solver, that may interact with the metaheuristic during its execution. Moreover, we developed a reactive mechanism that dynamically controls the dimension of the SP models when dealing with large size instances. The algorithm was extensively tested on benchmark instances of the following Vechicle Routing Problem (VRP) variants: (i) Capacitated VRP; (ii) Asymmetric VRP; (iii) Open VRP; (iv) VRP with Simultaneous Pickup and Delivery; (v) VRP with Mixed Pickup and Delivery, (vi) Multi-depot VRP; (vii) Multi-depot VRP with Mixed Pickup and Delivery. The results obtained were quite competitive with those found by heuristics devoted to specific variants. A number of new best solutions were obtained.

Key words:

Vehicle Routing Problems, Matheuristic, Iterated Local Search, Set Partitioning

1. Introduction

The Vehicle Routing Problem (VRP) is a classical Combinatorial Optimization (CO) problem that was proposed in the late 1950's and it is still one of the most studied in the field of Operations Research (OR). The great interest in the VRP is due to its practical importance, as well as the difficulty of solving it.

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However, solving the VRP is far from a simple task since the problem is \mathcal{NP} -hard [1], which implies that no algorithm capable of finding optimal solutions in polynomial time is known. There has been lot of advances in the development of exact algorithms for dealing with the VRP, particularly those based on mathematical programming techniques. Unfortunately, to date, even the best exact algorithms can be very time consuming and seldom solve VRP instances with more than 150 customers. Combining (meta)heuristic and exact methods appears to be a very promising alternative in solving many CO problems. The interest in hybrid approaches has rapidly grown especially due to several encouraging results obtained by the fusion of these two methods (see [2]). The interaction between mathematical programming techniques and metaheuristics led to a new class of optimization algorithms called matheuristics. Nevertheless, the application of these kind of approaches have not received much attention yet from the VRP literature (see [3], [4] and [5]).

Most VRP heuristics usually focus on a particular type of problem. A relatively small number of works have suggested unified heuristic procedures for dealing with several variants (see, for example, [6], [7], [8], [9]). Seen from a practical point of view, these non-specific approaches are highly relevant. For instance, VRP commercial packages must be prepared to face real-life problems of different classes. Cordeau et al. [10] even state that when talking about attributes for good heuristics, one should take into account not only the solution quality (accuracy) and computational time (speed), but also the simplicity and flexibility factors.

Given the above, one of the interests of this work is to propose a general hybrid algorithm for solving different VRPs. However, because of the huge number of existing variations it becomes virtually impossible to tackle all of them here. Therefore, it was thought advisable to turn attention only to a subset of variants, namely the following ones: (i) Capacitated VRP (with or without route duration limits), (ii) Asymmetric CVRP, (iii) Open VRP, (iv) VRP with Simultaneous Pickup and Delivery, (v) VRP with Mixed Pickup and Delivery, (vi) Multi-depot VRP, (vii) Multi-depot VRP with Mixed Pickup and Delivery.

The developed hybrid algorithm combines an exact procedure based on the Set Partitioning (SP) formulation with an Iterated Local Search (ILS) based heuristic. This strategy is quite similar to the classical two-phase petal algorithm (see [11]). The idea is to store a pool of routes generated during the heuristic execution and then solve a SP problem in order to extract the best combination of routes. However, unlike traditional petal algorithms and other SP based approaches to VRPs [12, 13, 4], the proposed hybrid algorithm includes some enhanced strategies. The first one is the cooperation between a Mixed Integer Programming (MIP) solver and the ILS heuristic (while solving the SP problem). This scheme was successfully applied in a previous work [14] to solve the Heterogeneous Fleet VRP (HFVRP) but its efficiency in terms of scalability was limited to approximately 200 customers. To overcome this limitation we introduce a new second strategy, which includes a reactive mechanism that dynamically controls the dimension of the SP models when dealing with

large size instances, that still allows for taking advantage of the exact procedure. As a result, new improved solutions were found for instances with up to 480 customers.

The remainder of this paper is organized as follows. Section 2 briefly describes the VRPs considered in this work. Section 3 explains the proposed hybrid algorithm. Section 4 contains the results obtained and a comparison with those reported in the literature. Section 5 presents the concluding remarks of this work.

2. A brief description of the VRPs considered in the present work

In this section we present a formal description of the VRPs considered here and we also point the best known algorithms, to our knowledge, for each variant. A complete literature review regarding such variants can be found in [15].

2.1. Capacitated Vehicle Routing Problem (CVRP)

The CVRP is considered to be the classical version of the VRP. A formal definition of the problem is as follows. Let G = (V, E) be a complete graph with a set of vertices $V = \{0, ..., n\}$, where the vertex 0 represents the depot and the remaining ones the customers. Each edge $\{i,j\} \in E$ has a non-negative cost c_{ij} and each customer $i \in V' = V \setminus \{0\}$ has a demand d_i . Let $C = \{1, ..., m\}$ be the set of homogeneous vehicles with capacity Q. The CVRP consists in constructing a set of up to m routes in such a way that: (i) every route starts and ends at the depot; (ii) all demands are accomplished; (iii) the vehicle's capacity is not exceeded; (iv) a customer is visited by only a single vehicle; (v) the sum of costs is minimized. Some versions of this problem include route duration constraints. In such cases, there might be a travel time t_{ij} for each edge $\{i,j\} \in E$ and a service time s_i for each customer $i \in V'$. Among the best known heuristic algorithms are those Pisinger and Røpke [6], Mester and Bräysy [16], Nagata and Bräysy [17], Zachariadis and Kiranoudis [18] and Vidal et al. [9].

2.2. Asymmetric Capacitated Vehicle Routing Problem (ACVRP)

The ACVRP is a generalization of the CVRP where the cost between a pair of vertices is not necessarily symmetric, i.e., c_{ij} need not be equal to c_{ji} , $\forall i, j \in V$. Although this variant is more likely to be found in practice when compared to the CVRP (due to the existence of one-way streets in most urban zones), there are very few works that dealt with the ACVRP in the literature (see Fischetti et al. [19], De Franceschi et al. [3] and Pessoa et al. [20]).

2.3. Open Vehicle Routing Problem (OVRP)

The OVRP is a variant of the CVRP where the vehicles need not to return to the depot after visiting the last customer of a given route. Any OVRP instance can be converted to an ACVRP instance by simply setting $c_{i0} = 0, \forall i \in V$. Most authors also state that the primary objective is to minimize the number

of vehicles, while the secondary objective is to minimize the sum of the travel costs. The most competitive heuristics are those of Pisinger and Røpke [6], Fleszar et al. [21], Repoussis et al. [22] and Zachariadis and Kiranoudis [23].

2.4. Vehicle Routing Problem with Simultaneous Pickup and Delivery (VRP-SPD)

The VRPSPD is a generalization of the CVRP in which a customer $i \in V'$ have both a delivery demand d_i and also a pickup demand p_i . The heuristics of Subramanian et al. [24], Zachariadis and Kiranoudis [25] and Souza et al. [26] together produced the best known results.

2.5. Vehicle Routing Problem with Mixed Pickup and Delivery (VRPMPD)

The VRPMPD (a.k.a. the VRP with mixed backhauls) is a particular case of the VRPSPD, in which customers either have a pickup or a delivery demand but not both, i.e., if $d_i > 0$, then $p_i = 0$ and vice-versa. The best known heuristics are those of Røpke and Pisinger [7] and Gajpal and Abad [27].

2.6. Multi-depot Vehicle Routing Problem (MDVRP)

Let G be the set of depots. The MDVRP is a generalization of the CVRP where more than one depot may be considered, that is, $|G| \geq 1$. Also, the vehicle must start and end at the same depot. Typically, the number of vehicles per each depot is given as an input data. Pisinger and Røpke [6] and Vidal et al. [9] developed the best heuristic approaches for the MDVRP.

2.7. Multi-depot Vehicle Routing Problem with Mixed Pickup and Delivery (MD-VRPMPD)

The MDVRPMPD generalizes the VRPMPD by allowing $|G| \ge 1$ depot(s). The best known algorithm is the one of Røpke and Pisinger [7].

3. The hybrid algorithm

The proposed hybrid algorithm, called ILS-RVND-SP, essentially combines an ILS based heuristic, called ILS-RVND, and a SP approach. In this section we present a description of both the methods and how we merged them to efficiently tackle the seven variants considered in this work.

3.1. The ILS-RVND heuristic

In this section we briefly explain the general idea of the ILS-RVND heuristic. A highly detailed description of ILS-RVND can be found in [15, 28]. An earlier version of this heuristic was applied in a parallel fashion by Subramanian et al. [24] to solve the VRPSPD and it is still remains as one of the best heuristic approaches, in terms of solution quality, proposed for the problem. Modified versions of ILS-RVND were also successfully applied to solve single-vehicle routing problems such as the Minimum Latency Problem (a.k.a. the Delivery Man

Problem or the Cumulative Traveling Salesman Problem) [29] and the Traveling Salesman Problem with Mixed Pickup and Delivery [30].

The ILS-RVND heuristic is a multi-start procedure that uses insertion heuristics in the constructive phase, a Variable Neighborhood Descent with Random neighborhood ordering (RVND) in the local search phase and simple moves as perturbation mechanisms.

The insertion strategies are the Sequential Insertion Strategy (SIS) and the Parallel Insertion Strategy (PIS), while the insertion criteria are based on the Nearest Feasible Insertion Criterion (NFIC) and on a Modified Cheapest Feasible Insertion Criterion (MCFIC). At each iteration, the method randomly chooses a strategy and a criterion. In the case of NFIC, the cost of inserting a customer k after a customer i is simply given by c_{ik} . As for MCFIC, the cost of inserting a customer k between customers i and j is given by $(c_{ik} + c_{kj} - c_{ij}) + \gamma(c_{0k} + c_{k0})$. The parameter γ controls the level of incentive of inserting customers located far from the depot.

The RVND is composed of well-known VRP inter-route neighborhood structures, namely those based on λ -interchanges [31] and Cross-exchange [32]; and also by specific ones, namely ShiftDepot and SwapDepot. With respect to the λ -interchanges, we consider Shift $(\lambda,0)$, $\lambda \in \{1,2\}$, and Swap (λ_1,λ_2) , $\lambda_1,\lambda_2 \in$ {1,2}. As a result, five distinct neighborhood structures can be identified, i.e, Shift(1,0), Shift(2,0), Swap(1,1), Swap(1,2) and Swap(2,2). In Shift(λ , 0), λ consecutive customers are moved from a route r_1 to a route r_2 . In Swap (λ_1, λ_2) , λ_1 consecutive customers from a route r_1 are interchanged with λ_2 consecutive customers from a route r_2 . The Cross operator in our case consists of interchanging a segment from a route r_1 with a segment from a route r_2 . ShiftDepot and SwapDepot were incorporated in the present work and they consist, respectively, of moving and swapping routes from a depot to another one. The best improvement strategy was adopted and the neighborhoods are explored exhaustively. Every time a route is modified due to an inter-route move an intra-route local search is performed using classical Traveling Salesman Problem neighborhood structures, more precisely, Reinsertion, Or-opt2 [33], Or-opt3 [33], 2-opt [34] and Exchange. Reinsertion consists of transferring a customer from its current position to another one in the same route. Or-opt2 and Or-opt3 make use of the same rationale but involve two and three consecutive customers, respectively. In 2-opt, two nonadjacent arcs are removed and another two are added in such a way that a new route is generated. Exchange is the intra-route version of Swap(1,1).

The perturbation mechanisms consist of performing multiple Swap(1,1) or Shift(1,1) moves. The Shift (1,1) consists of moving a customer from a route r_1 to a route r_2 and vice-versa.

The ILS-RVND structure was slightly modified in order to store routes during its execution. Every time a local search is performed, the routes associated to the local optimal solution s may be added to a pool of routes (RoutePool). The method decides whether to add or not such routes based on the average number of customers per route (n/v) and on the deviation between the current best solution s^* and s (see Subsection 3.3). If this deviation, given by

 $(f(s) - f(s^*))/f(s^*)$, where f(.) is the cost function, is smaller than a threshold value (tolerance) then the routes of s are added to RoutePool. The input parameters of ILS-RVND are MaxIter, MaxIterILS, s_0 , RoutePool, v and tolerance. The first parameter indicates the number of iterations, the second one is the maximum number of consecutive perturbations without improvements and the third one is an initial solution. Of course, if s_0 is provided then the procedure that generates an initial solution is skipped.

3.2. A Set Partitioning approach

Let \mathcal{R} be the set of all possible routes of all vehicle types, $\mathcal{R}_i \subseteq \mathcal{R}$ be the subset of routes that contain customer $i \in V'$. Define y_j as the binary variable associated to a route $j \in \mathcal{R}$, and c_j as its cost. Consider the following basic SP formulation F1:

$$\operatorname{Min} \sum_{j \in \mathcal{R}} c_j y_j \tag{1}$$

subject to
$$\sum_{j \in \mathcal{R}_i} y_j = 1 \qquad \forall i \in V'$$
 (2)

$$y_j \in \{0, 1\} \qquad \forall j \in \mathcal{R}. \tag{3}$$

The objective function (1) minimizes the sum of the costs by choosing the best combination of routes. Constraints (2) state that a single route from the subset \mathcal{R}_i visits customer $i \in V'$. Since the enumeration of set \mathcal{R} is an impractical task, ILS-RVND-SP only considers a subset of this set, usually limited to a few thousand routes. Formulation F1 is mainly suitable for variants such as the Fleet Size and Mix VRP [14] because the number of vehicles of each type is not predefined. Let $\mathcal{R}_u \subseteq \mathcal{R}$ be the set of routes associated with vehicle type $u \in M$ or with depot $u \in G$ and let m_u be an upper bound on the number of vehicles of a given type or available at a given depot. In order to deal with MDVRPs one can add the following constraints:

$$\sum_{j \in \mathcal{R}_u} y_j \le m_u \qquad \forall u \in G. \tag{4}$$

Let v be the number of vehicles. For the remaining variants, one must include the constraint that ensure that the number of routes in the solution is equal to the number of vehicles available, i.e.,

$$\sum_{j \in \mathcal{R}} y_j = v. \tag{5}$$

It is important to mention that there are some instances of VRPs with homogeneous fleet that do not specify the number of vehicles, but ILS-RVND-SP fixes this value by using the number of vehicles of the current best solution. Although the solution space is reduced, this helps the problem to be solved more efficiently.

The pseudocode of the SP procedure is illustrated in Alg. 1. Input parameter MaxSPTime corresponds to the time limit imposed to the Mixed Integer Programming (MIP) solver. It is assumed that the MIP solver uses a branchand-bound or a branch-and-cut procedure. The algorithm starts by verifying if the number of vehicles should be minimized (e.g. OVRP) and if the number of vehicles of s^* is larger than the estimated lower bound on the number of vehicles $(v_{min} = \lceil (\sum_{i \in V'} d_i)/Q \rceil)$. If so, solution s^* is stored in s' and the number of vehicles is decreased by one unit (lines 2-3). Next, the SP_Model is created (line 4) according to the VRP variant and the Cutof f value is initialized (line 5). The SP problem is given to a MIP solver (line 6), which calls the ILS-RVND heuristic whenever an incumbent solution is found (Procedure IncumbentCallback). If the solution s^* is improved in the IncumbentCallback, the Cutoff value is updated, but s^* is not given back to the solver since it may contain a route that does not belong to the subset of routes \mathcal{R} of the SP model. The solver is interrupted if: (i) an optimal solution is found; (ii) LB > Cutoff (iii) MaxSPTime is exceeded. If the primary objective is to minimize the number of vehicles and the solution s^* is infeasible, then the number of vehicles is incremented by one unit, s^* is restored and the MIP solver is called again (lines 7-10).

Algorithm 1 SP

```
1: Procedure SP(s^*, RoutePool, MaxSPTime, v);
2: if v must be minimized and v > v_{min} then
3: v \leftarrow v - 1; s' \leftarrow s^*;
4: SP\_Model \leftarrow CreateSetPartitioningModel(RoutePool, <math>v);
5: Cutoff \leftarrow f(s^*); {Only if v = v_{min}. Otherwise, Cutoff \leftarrow \infty}
6: s^* \leftarrow MIPSolver(SP\_Model, s^*, Cutoff, MaxSPTime, IncumbentCallback(<math>s^*));
7: if v must be minimized and and s^* is infeasible then
8: s^* \leftarrow s'; v \leftarrow v + 1;
9: Update SP\_Model {Increasing one vehicle};
10: s^* \leftarrow MIPSolver(SP\_Model, s^*, Cutoff, MaxSPTime, IncumbentCallback(<math>s^*));
11: return s^*;
12: end SP.
```

3.3. The hybrid algorithm

One of the challenges of designing a unified hybrid solution approach is to ensure that the MIP model is computationally tractable, regardless of the instance. For example, a SP model that exceeds the time limit only to solve its linear relaxation (e.g. due to an excessive number of routes) is not a suitable improving mechanism. On the other hand, a SP model that contains relatively few routes, is easily solved, but seldom finds improved solutions. Hence, it is necessary that the SP models generated throughout the algorithm find a balance between computational tractability and improvement potential. Experiments carried out in many instances with distinct characteristics indicated that the following simple pieces of data are crucial for estimating the dimension (number of routes) of a properly balanced SP model: (i) number of customers and (ii) the average number of customers per route.

With respect to (i), we developed two strategies for ILS-RVND-SP. The first one, called ILS-RVND-SP-a, is executed when the number of customers is less than or equal to a parameter \mathcal{N} . The idea of ILS-RVND-SP-a is very straightforward: the SP procedure is run only once at the end of the algorithm, after the ILS-RVND heuristic, as performed in [14]. The second one, called ILS-RVND-SP-b, is executed when $n > \mathcal{N}$. In this case, the SP procedure is called after each iteration of the ILS-RVND heuristic. Both strategies are completely independent, as well as some of their parameters, namely: MaxIter-a, MaxIter-b, MaxIterILS-a, MaxIterILS-b, TDev-a, TDev-b. The parameter TDev is described next.

With respect to (ii), we do the following. Let \mathcal{A} be a parameter. It has been observed that when the ratio between the number of customers and the number of vehicles is smaller than $\mathcal{A}=11$, the SP models tend to become harder. In such cases, we only add the routes of a solution to the SP model if its deviation when compared to the incumbent solution is smaller than a given threshold TDev. However, this parameter is difficult to tune, especially in ILS-RVND-SP-b. To overcome this issue we implemented a reactive approach that dynamically adjusts its value throughout the execution of the algorithm, as will be further explained.

The pseudocode of ILS-RVND-SP and ILS-RVND-SP-a will be omitted since they are quite simple. Alg. 2 shows the pseudocode of ILS-RVND-SP-b. Firstly, tolerance (threshold deviation) is set to a given value according to the average number of customers per route (lines 2-5). In the main loop (lines 7-24), the ILS-RVND heuristic is executed with a single iteration (line 8) and the SP procedure is repeatedly called while there is any improvement over the best current solution (lines 10-21). When no improvement is observed, the nonpermanent routes (short-term memory), in this case those generated on that particular iteration, are removed from RoutePool (line 16). After each call to the SP procedure, the algorithm may update the value of tolerance, in case n/v < A, according to the following conditions. If the SP model is solved at the root node, meaning that the problem is easy, then tolerance is increased by one tenth of TDev-b (lines 17-18). If the time limit is exceeded then tolerance is decreased by one tenth of TDev-b (lines 19-20). If there is any improvement at the end of a given iteration, the incumbent solution s^* is updated and the associated routes are permanently added (long-term memory) to RoutePool (lines 22-24). Such routes are never removed from the pool.

Algorithm 2 ILS-RVND-SP-b

```
1: Procedure ILS-RVND-SP-b(MaxIter-b, MaxIterILS-b,
                                                                        RoutePool,
                                                                                             TDev-b,
    MaxSPTime);
   if n/v < A then
 3:
          tolerance \leftarrow TDev\text{-b};
 4: else
 5:
          tolerance \leftarrow 1;
 6: iter \leftarrow 0; s^* \leftarrow \emptyset;
                            s_0 \leftarrow NULL;
 7: while iter < MaxIter-b do
 8:
          s \leftarrow \text{ILS-RVND}(1, MaxIterILS-b, s_0, RoutePool, v, tolerance);
 9:
          improvement \leftarrow true;
           while improvement do
10:
                 s' \leftarrow SP(s, RoutePool, MaxSPTime, v);
11:
12:
                 if f(s') < f(s) then
                       s \leftarrow s';
13:
14:
                 else
15:
                       improvement \leftarrow false;
                       Remove non-permanent routes from RoutePool;
16:
17:
                 if n/v < A and Time > MaxSPTime then
18:
                       tolerance \leftarrow tolerance - 0.1 \times TDev-b;
19:
                 if n/v < A and Problem solved at the root node then
20:
                       tolerance \leftarrow tolerance + 0.1 \times TDev\text{-b};
21:
                 iter \leftarrow iter + 1;
22:
           if f(s) < f(s^*) or s^* is empty then
23:
24:
                 Add routes associated to s^* permanently to the pool;
25: return s^*;
```

4. Computational results

The algorithm ILS-RVND-SP was coded in C++ and the tests were executed on an Intel® $\rm Core^{TM}$ i7 with 2.93 GHz and 8 GB of RAM running under Ubuntu Linux 64 bits. CPLEX 12.2 was used as a MIP solver. The computational experiments were carried out using a single thread and the algorithm was executed 10 times for each instance.

Table 1 shows the values of the parameters used by ILS-RVND-SP, which were calibrated after preliminary experiments. The most crucial parameters are \mathcal{N} and \mathcal{A} . The values adopted for the remaining ones are not so critical, which is reflected in the round numbers chosen.

Table 1: Values of the parameters used by ILS-RVND-SP

Parameter	Value
\mathcal{N}	150
$\mathcal A$	11
MaxIter-a	50
MaxIter-b	100
MaxIterILS-a	$n+0, 5 \times v$
MaxIterILS-b	2000
Tdev-a	0.05
Tdev-b	0.005
γ	random value of the set $\{0.00, 0.05, 0.10, \dots, 1, 70\}$ [24]
MaxSPTime (s)	60

In the following tables, **Instance** denotes the test-problem, n is the number of customers, |G| is the number of depots, v is the number of vehicles available per depot, **BKS** represents the Best Known Solution (BKS) reported in the literature, **Best Sol.**, **Avg. Sol.** and **Time (s)** indicate, respectively, the best solution, the average solution and the average computational time in seconds associated to the corresponding work, **Gap** denotes the gap, given by $100 \times ((z_{\text{ILS-RVND-SP}} - z_{\text{BKS}})/z_{\text{BKS}})$, between the best solution found by ILS-RVND-SP and the BKS, **Avg. Gap** corresponds to the gap between the average solution found by ILS-RVND-SP and the best known solution, **Scaled time (s)** is the approximate average scaled time in seconds of each machine using the factors suggested by the benchmarks of Dongarra [35], when solving solving a system of equations of order 1000, with respect to our i7 2.93 GHz (5839 Mflop/s). The BKSs are highlighted in boldface and the improved solutions are underlined.

4.1. CVRP

The developed hybrid algorithm was tested on the instances of the A, B, E, M, P series and all known optimal solutions were easily determined. Table 2 only shows the results obtained on the three open instances of the M-series, namely: M-n151-k12, M-n200-k16 and M-n200-k17. The proposed algorithm was found capable of improving the result of the second one and to equal the BKSs of the first and third ones. Table 3 contains the results found on the instances suggested in [36] and a comparison with those reported in [13], [6] (ALNS 50K), [16], [17] and [9]. ILS-RVND-SP was successful to equal the BKS in 13 of the 14 instances and the average gap between the average solutions found by ILS-RVND-SP and the BKSs was 0.08%. Table 4 illustrates a comparison, in terms of average solution between the results obtained by ILS-RVND-SP and those found in [6] (ALNS 50K), [17] and [18] for the instances proposed in [37]. It can be seen that the ILS-RVND-SP outperformed the algorithm developed in [6], but it is not as effective as those presented in [17] and [9] in terms of average solution quality. Yet, the average gap between the average solutions found by ILS-RVND-SP and the BKSs was only 0.55%, a value smaller than the one obtained by the general heuristic proposed in [6]. On the other hand, in spite of obtaining slightly lower quality solutions, we believe that the proposed algorithm is simpler than those developed in [17], [9] and [18].

Table 2: Results found for the open instances of the M-series

			DILG		I	LS-RVNI	D-SP	
Instance	n	v	BKS	Best Sol.	Avg. Sol.	Gap (%)	Avg. Gap (%)	Time (s)
M-n151-k12	150	12	1015^a	1015	1015.5	0.00	0.05	37.12
M-n200-k16	199	16	1285^b	1278	1285.8	-0.54	0.06	772.01
M-n200-k17	199	17	1275^a	1275	1279.9	0.00	0.38	513.00
					Avg.	-0.18	0.17	440.71

a: Value presented in [38].

^b: Value obtained in [5].

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Table 3

		Time (s)	1.48	13.52	12.49	5.23	20.66	53.48	625.17	0.93	5.05	7.61	7.12	80.24	82.50	496.07	100.83
		Avg. Gap (%)	0.00	00.00	00.00	00.00	00.00	0.03	0.13	0.19	0.03	00.00	00.00	0.19	0.13	0.44	0.08
	D-SP	Gap (%)	0.00	0.00	0.00	0.00	0.00	0.00	< 0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	ILS-RVND-SP	Avg. Sol.	524.61	835.26	826.14	819.56	1042.11	1028.73	1293.18	556.49	910.00	865.94	866.37	1544.07	1164.11	1402.03	Avg.
		Best Sol.	524.61	835.26	826.14	819.56	1042.11	1028.42	1291.45	555.43	89.606	865.94	866.37	1541.14	1162.55	1395.85	
		Time ⁴ (s)	25.8	57.6	76.2	50.4	69.0	172.2	356.4	28.8	65.4	68.4	71.4	169.8	151.8	493.2	
[00]	Vidal et al.	Best. Sol.	524.61	835.26	826.14	819.56	1042.11	1028.42	1291.45	555.43	909.68	865.94	866.37	1541.14	1162.55	1395.85	
posea m	and sy	$Time^3$ (s)	4.3	22.3	17.1	8.1	21.0	75.2	302.1	5.1	38.9	23.5	13.2	106.9	135.6	390.6	
ances pro	Nagata and Bräysy	Best Sol.	524.61	835.26	826.14	819.56	1042.11	1028.42	1291.45	555.43	909.68	865.94	866.37	1541.14	1162.55	1395.85	
VRF IIIS	and sy	$Time^2$ (s)	0.2	5.5	1.0	0.2	1.1	10.2	2160.0	4.2	8.0	8.0	1.7	13.5	25.8	52.2	
ior the C	Mester and Bräysy	Best Sol.	524.61	835.26	826.14	819.56	1042.11	1028.42	1291.29	555.43	909.68	865.94	866.37	1541.14	1162.55	1401.12	
its iound	: and se	$Time^1$ (s)	21	36	78	73	113	160	219	21	36	78	73	113	160	219	
ne o: resuns tound for the CVRF instances proposed in [50	Pisinger and Røpke	Best Sol.	524.61	835.26	826.14	819.56	1042.11	1029.56	1297.12	555.43	909.68	865.94	866.37	1542.86	1163.68	1405.88	
Lat	and rd	Time	•	1	1	1	1	1	1		•	•	•	•	1	1	
	Rochat and Taillard	Best Sol.	524.61	835.26	826.14	819.56	1042.11	1028.42	1291.45	555.43	909.68	865.94	866.37	1541.14	1162.55	1395.85	
		BKS	a 524.61	835.26	826.14	819.56	1042.11	1028.42	1291.29	555.43	909.68	865.94	866.37	1541.14	1162.55	1395.85	
		v	5	10	œ	10	-1	12	17	9	11	6	11	11	14	18	
		u	50	22	100	100	120	150	199	20	22	100	100	120	150	199	
		Instance	C1	C_2	C3	C12	C11	C4	C2	Ce Ce	C7	C8	C14	C13	C3	C10	

Scaled Time (s)

100.83

72.24

49.62

80.89

54.48

a: Optimality proved.
1: Average of 10 runs on a Pentium IV 3.0 GHz (3181 Mflop/s).
2: Average of 10 runs on a Pentium IV 2.8 GHz (2444 Mflop/s).
3: Average of 10 runs on an Opteron 2.4 GHz (3485 Mflop/s).
4: Average of 10 runs on an Opteron 2.4 GHz scaled for a Pentium IV 3.0 GHz.

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Table 4:

				Pisinger and Røpke	and se	Nagata and Bräysy	and sy	Vidal et al.		Zachariadis and Kiranoudis	s and dis		ILS-I	ILS-RVND-SP	3P	
Instance	u	v	BKS	Avg. Sol.*	$Time^1$ (s)	Avg. Sol.*	$Time^2$ (s)	Avg. Sol.*	$Time^3$ (s)	Avg. Sol.*	Time ⁴ (s)	Best Sol.	Avg. Sol.	Gap (%)	Avg. Gap (%)	Time (s)
G17	240	22	a, b 707.76	710.59	304	707.78	582.4	708.09	423.6	708.94	962.3	707.76	707.81	0.00	0.01	937.59
G13	252	56	a,b 857.19	874.24	285	858.42	921.9	859.64	561.6	860.44	1189.3	857.19	860.00	0.00	0.33	910.35
G9	255	14	b 579.71	590.33	437	581.46	1043.3	581.79	973.2	584.66	929.4	583.24	585.21	0.61	0.95	1720.76
G18	300	27	a,b 995.13	1007.84	387	995.91	1465.9	998.44	993.6	997.74	1718.6	995.65	997.85	0.02	0.27	2297.62
G14	320	30	$^{a,b}1080.55$	1103.53	393	1080.84	1239.3	1082.41	847.2	1083.55	1187.4	1080.55	1082.15	0.00	0.15	1513.32
G10	323	16	a,b 736.26	751.36	616	739.56	1617.5	739.86	1551.6	739.86	1271.4	741.96	744.17	0.77	1.07	3229.35
G19	360	33	a,b 1365.60	1377.88	449	1366.70	2115.6	1367.83	1674.6	1370.77	1824.2	1366.29	1367.25	0.05	0.12	2917.31
G15	396	33 °	a,b 1337.92	1366.23	468	1344.32	1872.2	1343.52	2349.0	1344.41	1658.8	1347.13	1349.23	0.69	0.85	3265.68
G11	399	18	a,b 912.84	926.57	761	916.27	2337.5	916.44	2736.6	919.52	1392.2	921.46	922.93	0.94	1.11	5978.97
G20	420	38	a,b 1818.32	1834.70	488	1821.65	5 2824.7	1822.02	2293.8	1829.57	1199.3	1821.16	1823.52	0.16	0.29	4997.31
G16	480	37	a,b 1612.50	1645.67	549	1622.26	5 2616.2	1621.02	3496.2	1623.42	1848.5	1624.55	1627.76	0.75	0.95	4835.12
G12	483	19 °	$^{a,b}1102.69$	1125.22	911	1108.21	. 3561.9	1106.73	5740.2	1110.65	1282.3	1113.30	1116.52	96.0	1.25	10410.70
G5	200	ಸು	6460.98	6482.49	629	6460.98	164.7	6460.98	153.6	6460.98	986.6	6460.98	6460.98	00.00	0.00	978.69
G1	240	6	b 5623.47	5662.57	93	5632.05	3393	5627.00	700.8	5637.99	7.706	5657.74	5671.65	0.61	98.0	994.59
G6	280	-1	c 8412.88	8543.30	876	8413.41	830.3	8412.90	502.8	8412.90	1091.6	8412.90	8412.90	0.00	0.00	2455.56
G2	320	10	b 8404.61	8487.94	672	8440.25	1726.2	8446.65	1245.0	8457.92	1249.4	8447.92	8449.82	0.52	0.54	2659.68
G7	360	6	b 10102.70	10265.15	941	10186.93	\$ 2179.7	10157.63	1376.4	10192.47	1885.5	10195.58	10195.60	0.92	0.92	4410.84
G3	400	10	11036.22	11052.72	1015	11036.22	2606.8	11036.22	1679.4	11036.22	1164.0	11036.22	11036.22	0.00	0.00	6064.98
85	440	10	b 11635.30	11766.07	1011	11691.54	5776.7	11646.58	2440.2	11674.43	1657.4	11710.47	11774.40	0.65	1.20	7541.75
G4	480	10 6	$^{a}13592.88$	13748.50	1328	13618.55	3841.6	13624.52	2620.2	13632.59	1019.0	13624.53	13624.53	0.23	0.23	10644.50
			Avg.	$\mathrm{Gap}~(\%)$	1.34	Avg. Gap (%)	0.27	Avg. Gap (%)	0.26	Avg. Gap (%)	0.42		Avg.	0.40	0.55	3938.23
Scaled Time (s)	me (s)				343.57		1274.79		935.93		632.98					3938.23

2. Average of 10 runs on a T5500 1.66 GHz (2791 Mflop/s).

2. Average of 10 runs on an Opteron 2.4 GHz (3485 Mflop/s).

3. Average of 10 runs on an Opteron 2.4 GHz scaled for a Pentium IV 3.0 GHz.

4. Average of 10 runs

6. Found in [17]

b. Found in [9]

c. Found in [16]

4.2. ACVRP

ILS-RVND-SP was tested in the ACVRP instances suggested in [19]. The capacity of the vehicle is the same (Q=1000) and the number of customers varies between 33 and 70. Pessoa et al. [20] also considered the same data set of [19] but with different capacities (150, 250 and 500). The instances with Q=150 are not considered, since they can be easily solved using F1 (most feasible routes contain very few customers and it is practical to perform a complete enumeration), thus leading to a total of 24 instances. Table 5 shows the results found for the ACVRP instances. All the known optimal solutions were consistently found by ILS-RVND-SP. Regarding the two instances where the optimal solutions is not known, the proposed algorithm was capable of improving the BKS in one of them and to equal the best result in the other one.

Table 5:	Results	found	for	the	AC	VRP	instances	pro	posed	in	[19]	, 20	ĺ
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					ILS	S-RVND-	-SP	
Instance	n	v	$_{\rm BKS}$	Best	Avg.	Gap	Avg.	Time
				Sol.	Sol.	(%)	Gap (%)	(s)
							- ' '	
A034-02f	34	2	^a 1406	1406	1406.00	0.00	0.00	0.57
A034-04f	34	4	$^{a}1773$	1773	1773.00	0.00	0.00	0.47
A034-08f	34	8	a 2672	2672	2672.00	0.00	0.00	0.47
A036-03f	36	3	a 1644	1644	1644.00	0.00	0.00	0.64
A036-05f	36	5	a 2110	2110	2110.00	0.00	0.00	0.61
A036-10f	36	10	a 3338	3338	3338.00	0.00	0.00	5.67
A039-03f	39	3	a 1654	1654	1654.00	0.00	0.00	0.69
A039-06f	39	6	a 2289	2289	2289.00	0.00	0.00	0.60
A039-12f	39	12	a 3705	3705	3705.00	0.00	0.00	0.77
A045-03f	45	3	a 1740	1740	1740.00	0.00	0.00	1.06
A045-06f	45	6	a 2303	2303	2303.00	0.00	0.00	0.88
A045-11f	45	11	a 3544	3544	3544.00	0.00	0.00	2.46
A048-03f	48	3	a 1891	1891	1891.00	0.00	0.00	1.26
A048-05f	48	5	a 2283	2283	2289.50	0.00	0.28	1.79
A048-10f	48	10	a 3325	3325	3325.60	0.00	0.02	1.29
A056-03f	56	3	a 1739	1739	1740.00	0.00	0.06	2.09
A056-05f	56	5	a 2165	2165	2165.00	0.00	0.00	3.53
A056-10f	56	10	a 3263	3263	3264.50	0.00	0.05	2.26
A065-03f	65	3	a 1974	1974	1974.00	0.00	0.00	3.08
A065-06f	65	6	a 2567	2567	2571.70	0.00	0.18	3.30
A065-12f	65	12	a 3902	3902	3904.90	0.00	0.07	3.41
A071-03f	71	3	a 2054	2054	2054.00	0.00	0.00	4.46
A071-05f	71	5	$^{b}{f 2475}$	2457	2457.90	-0.73	-0.69	6.72
A071-10f	71	10	b 3486	3486	3492.90	0.00	0.20	5.61
			•	•	Avg.	-0.03	0.01	2.24

 $[^]a\colon$ Optimality proved. $^b\colon$ Value presented in [20].

4.3. OVRP

Table 6 presents the results found by ILS-RVND-SP in the set of instances proposed in [36, 39] and in the set of instances suggested in [40], as well as a comparison with those pointed out in [6] (ALNS 50K), [21], [22], and [23]. Regarding the set of instances introduced in [36, 39], ILS-RVND-SP was capable of obtaining the BKS in 12 cases and to improve another 3 solutions, but it failed to find 1 BKS. Furthermore, ILS-RVND-SP also failed to always obtain solutions with the minimum number of vehicles on instance C7 . The average

gap between the average solutions obtained by ILS-RVND-SP and the BKSs, disregarding instance C7, was 0.06%. As for the 8 instances suggested in [40], ILS-RVND-SP equaled the result of one instance and improved the results of the remaining ones. The average gap between the average solutions produced by ILS-RVND-SP and the BKSs was -0.08%.

It is worth mentioning that on the last set of instances, the ILS-RVND algorithm itself is sufficiently capable of obtaining, on average, competitive results, in terms of computational time and solution quality (see [15]), when compared to the best results reported in [25]. Nevertheless, the solutions obtained by ILS-RVND-SP are still much better than both of them, despite the larger computational time.

4.4. VRPSPD

Table 7 contains the results obtained in the set of instances suggested in [41] and a comparison with those reported in [27], [42] and [24]. It can be verified that the ILS-RVND-SP equaled 21 BKSs and improved another five. Table 8 presents the results found on the instances proposed in [43] and also those reported in [26], [25] and [24]. ILS-RVND-SP found 12 BKSs improved another six results. Furthermore, it is worth noting that the proposed algorithm had a satisfactory performance on the large size instances, always producing, on average, competitive results. The average gap between the average solutions produced by ILS-RVND-SP and the BKSs in the first and second group of instances was 0.12% and -0.07% respectively.

4.5. VRPMPD

Table 9 illustrates the results found by ILS-RVND-SP on the VRPMPD instances introduced in [41] and a comparison with those reported in [7] (6R - normal learning) and [27]. ILS-RVND-SP obtained the BKS in 25 instances and it managed to improve the result of another 12. The developed algorithm outperformed both the algorithms suggested in [7] and [27] in terms of solution quality. The average gap between the average solutions obtained by ILS-RVND-SP and the BKSs was -0.06%.

4.6. MDVRP

Tables 10 and 11 present a comparison, in terms of average solution, between the results found by ILS-RVND-SP and those determined in [6] (ALNS 50K) and [9] on the old and new set of instances presented in [44], respectively. The latter two clearly outperformed the first one in terms of solution quality. The average gap between the average solutions found by ILS-RVND-SP and the BKSs for the old and new benchmark sets was, respectively, 0.04% and 0.15%.

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				,	Pisi]	Pisinger and Røpke	r and ke		Fleszar et al.	ar		Repoussis et al.	oussis al.		Zachariadis and Kiranoudis	dis an oudis	pτ			ILS-RVND-SP	ND-SP		
Instance	u	v_{min}	BKS	vbest	Best Sol.	v	$Time^1$ (s)	Best Sol.	v	Time^2 (s)	e ²	Best Sol.	v Ti. ($\frac{\text{Time}^3}{\text{(s)}}$	Best Sol.	v T	Time ⁴ (s)	Best Sol.	v	Avg. Sol.	Gap (%) G	Avg. Gap (%)	Time (s)
	50	5	a 416.06	5	416.06	3 5	23	7	3 5		7 0.1	116.06	2	86	416.06	5	28	416.06	5	416.06	00.00	0.00	1.78
	71	4	a 177.00	4	177.00	4	104	178.66			3.2	177.00	4	264	177.00	4	132	177.00	4	177.21	0.00	0.12	4.41
C2	22	10	a 567.14	10	567.14	10	53	567.14	_		2.3	567.14 1	10	143	567.14	10	72	567.14	10	567.14	0.00	0.00	6.44
	100	œ	a 639.74	œ	641.76	.0	128	641.40		0,	_	639.74	∞	330	639.74	œ	26	639.74	œ	639.81	0.00	0.01	15.67
	100	10	a 534.24	10	534.24	10	118	534.40		_		534.24 1	0	363	534.24	01	47	534.24	10	534.24	0.00	0.00	5.74
	120	7	682.12	_	682.12	-1	141	9	7	1		682.12	7	318	682.12	~	92	682.12	_	682.12	0.00	0.00	23.54
	134	7	769.55	7	770.17	7	359	769.66		~	•		7	753	769.55	_	278	769.55	_	770.00	0.00	90.0	40.51
	150	12	733.13	12	733.13	3 12	279	737.82	2 12	4	5.4	733.13 1	12	613	733.13	12	204	733.13	12	733.13	0.00	0.00	27.77
	199	16	893.39	16	80.08	3 16	237	902.96	91 9	Ξ	17.1	894.11 1	9	1272	893.39	16	332	883.50	16	895.55	.1.11	0.24 1	1579.45
9C	50	ro	412.96	9	412.96	9	31	412.96	9	2	8.9	112.96	9	215	,	1	,	412.96	9	412.96	0.00	0.00	1.24
C2	22	10	583.19		583.19	10	33		_	23	22.3		10	367	1	,	,	583.19	10	582.07	0.00		7.29
	100	œ	644.63	6	645.16	3	114	٠	3	58,	Ī	344.63	6	510	1	,	,	644.63	6	644.95	0.00	0.02	9.21
C14	100	10	591.87	11	591.87	11	75	591.87	_	က		591.87	11	411	1	,	,	591.87	11	591.87	0.00	0.00	22.76
	120	7	904.04	11	909.80) 11	116	904.94	4 11	1820.1).1		11	890	1	,	ı	899.16	11	904.02	-0.54	0.00	37.35
	150	12	757.84	13	757.84		185	760.06	6 13	1094.1	1.1	764.56 1	13	933	1	,		757.91	13	759.38	0.01	0.20	38.93
	199	16	875.67	17	875.67	17	224	875.67	7 17	1252.4	2.4	888.46	7	1678	1	,		874.71	17	827.68	-0.11	0.23	472.91
																				Avg.	-0.11	90.0	143.44
Scaled Time	me (s)	<u></u>					75.59			100.75	75		7.4	25.68			61.38				,	$143.44 \ (189.48^b)$	(9.48^b)
01	200	ಬ	6018.52	5		<u>'</u>	'				9 -	6018.52	5 516	5161.55	6018.52	25	635	6018.52	5	6018.52	0.00	0.00	1270.81
02	240	6	4557.38	6			'		'		- 4	4583.70	9 521	$^{5}219.09$	4557.38	6	832	4544.46	9	4551.74	-0.28	-0.12 1	1247.37
	280	7	7731.00	7		'			'		- 7	7733.77	7 526	$^{5}263.05$	7731.00	_	921	7721.16	2	7728.77	-0.13	-0.03	2008.76
04	320	10	7253.20	10		'	'		'		- 7	7271.24 1	$^{5}2^{\circ}$	$^{5}297.71$	7253.20	01	1009	7215.48	$10\overline{2}$	7229.56	-0.52	-0.33	2663.24
	360	œ	9193.15	œ		1	'		'		0	9254.15	8 548	5487.85	9193.15	œ	1590	9180.93	œ	9205.01	-0.13		5702.38
	400	6	9793.72	6		1	1		'		0	9821.09	9 543		9793.72	6	1108	9773.83	6	9784.52	-0.20	-	5065.72
	440	10	10347.70	10		1	1		'		-	0363.4 1	$10^{-5}55$	_	10347.70	10		10326.57	10	10342.1	-0.20		6140.55
80	480	10 1	12415.36	10		'	'		'		- 1	2428.2 1	10 °55	⁵ 590.78 1	12415.36	10	1273 1	12389.43	10 1	12393.4	-0.21	-0.18	6653.41

Table 6: Results found for the OVRP instances proposed in [36, 39] and [45]

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Scaled Time (s)	a : Optimality proved.

-0.08 3844.033844.03

-0.21

Avg.

b: Average of 10 runs considering the following instances: C1, F11, C2, C3, C12, C11, F12, C4 and C5.

1: Average of 10 runs on a Pentium IV 3.0 GHz (3181 Mflop/s).

2: Best run on a Pentium M 2.0 GHz (1738 Mflop/s).

3: Best run on a Scaled to a Pentium II 400 MHz (262 Mflop/s).

4: Average of 10 runs on a T5500 1.66 GHz (2791 Mflop/s).

5: Best run on a Pentium IV 2.8 GHz.

			Table 7: I	Results i	found for	the VF	PSPD in	stances	Table 7: Results found for the VRPSPD instances proposed in [41]	in [41]			
			Gajpal and Abad	and	Zachariadis et al.	ariadis al.	Subramanian et al.	anian J.		ILS-I	ILS-RVND-SP	-SP	
Instance	u	BKS	Best Sol.	$Time^1$ (s)	Best Sol.	$Time^2$ (s)	Best Sol.	$Time^3$ (s)	Best Sol.	Avg. Sol.	Gap (%)	Avg. Gap (%)	Time (s)
CMT1X	50 3	3 466.77	7 466.77	5.00	469.80	2.1	466.77	2.3	466.77	466.77	0.00	0.00	2.08
CMT1Y	50	3 466.77	7.466.77	5.00	469.80	3.8	466.77	2.3	466.77	466.77	0.00	0.00	1.97
CMT2X	75 6	684.21	684.21	41.25	684.21	5.4	684.21	6.4	684.21	684.78	0.00	0.08	12.79
CMT2Y	75 (684.21	. 684.94	22.25	684.21	8.9	684.21	6.4	684.21	684.59	0.00	0.06	10.83
CMT3X 1	2 001	5 4721.27	721.40	377.50	721.27	11.9	721.27	12.1	721.27	721.46	0.00	0.03	17.69
	100	5 4721.27		43.75	721.27	11	721.27	12.3	721.27	721.50	0.00	0.03	17.61
	100	662.22		36.25	662.22	9.3	662.22	10.3	662.22	663.44	0.00	0.18	9.07
CMT12Y 1	100	662.22		39.25	662.22	4.8	662.22	10.8	662.22	663.12	0.00	0.14	9.34
CMT11X 1	120 4	833.92	839.66	57.25	833.92	21.2	833.92	18.9	846.23	848.65	1.48	1.77	51.82
CMT11Y 1	120 4	833.92	840.19	52.75	833.92	14.4	833.92	19.0	846.23	848.74	1.48	1.78	48.63
CMT4X 1	150 7	852.46	854.12	131.75	852.46	29.6	852.46	30.9	852.46	853.02	0.00	0.07	98.03
CMT4Y 1	150 7	852.46	855.76	140.25	852.46	27.4	852.46	31.6	852.46	852.73	0.00	0.03	80.63
CMT5X 1	199 10	1029.25	1034.87	377.50	1030.55	62.8	1029.25	71.5	1029.25	1029.52	0.00	0.03	1786.74
CMT5Y 1	199 10	1029.25	1037.34	393.50	1030.55	47.7	1029.25	9.69	1029.25	1029.25	0.00	0.00	1726.18
CMT6X	50 7	7 555.43	555.43	14.00	1	1	'	1	555.43	557.35	0.00	0.35	1.04
$_{ m CMT6Y}$	50 7	7 555.43	555.43	13.75	1	1	1	1	555.43	557.10	0.00	0.30	1.08
CMT7X	75 13	3 900.12	900.12	47.75	1	1	1	1	900.12	901.02	0.00	0.10	4.55
CMT7Y	75 13	3 900.54	900.54	46.25	1	1	1	1	900.12	901.08	-0.05	0.06	4.87
	100 10			80.75	1	•	1	•	865.50	865.50	0.00	0.00	7.36
	100 10			77.75	1	1	1	1	865.50	865.50	0.00	0.00	7.74
	100 11			78.50	1	1	1	1	821.75	821.75	0.00	0.00	5.42
	100 11			74.75	1	1	1	1	821.75	821.75	0.00	0.00	5.48
CMT13X 1	120 12	2 1542.86	1542.86	160.25	1	•	1	•	1542.86	1543.54	-0.03	0.04	68.72
· ·	120 12	٠.		160.25	1	•	1	•	1542.86		0.00	0.10	73.49
				300.00	1	1	1	1	1160.68		-0.07	0.02	64.43
CMT9Y 1	150 16	1161.54	1161.54	291.75	1	1	1	•	1160.68		-0.07	0.09	80.86
CMT10X 1	199 20	1386.29	_	773.50	1	•	1	•	1373.40	1379.19	-0.93	-0.51	552.81
CMT10Y 1	19920	1395.04	1395.04	757.50	1	1	1	1	1373.40	1377.03	-1.55	-1.29	547.39
										Avg.	0.01	0.12	189.24
Scaled Time (s)	e (s)			55.65		8.83		İ				$189.24 \ (276.67^b)$	(76.67^{b})

<sup>a: Optimality proved.
b: Average of 10 runs considering the following instances: CMT1X, CMT1Y, CMT2X, CMT2Y, CMT3X, CMT13Y, CMT112X, CMT112X, CMT111X. CMT111X. CMT4X, CMT4Y, CMT5X and CMT5Y.
cMT112X, CMT112Y, CMT111X. CMT111Y, CMT4X, CMT4Y, CMT5X and CMT5Y.
dest run on a Xeon 2.4 GHz (1978 Mflop/s).
Average of 50 runs on a cluster with 32 SMP nodes, where each node consists of two Intel Xeon 2.66 GHz (wall clock).</sup>

			Souza et al.	ø .	Zachariadis et al.	iadis 1.	Subramanian et al.	anian 1.		ILS-R	ILS-RVND-SP	Ь	
Instance	n	BKS	Best Sol.	$Time^1$ (s)	Best Sol.	$Time^2$ (s)	Best Sol.	$Time^3$ (s)	Best Sol.	Avg. Sol.	Gap (%) G	Avg. Gap (%)	Time (s)
r101	100 12	a 1009.95	1009.95	35.7	1009.95	28.7	1009.95	15.8	1009.95	1010.08	0.00	0.01	65.42
r201	100 3		666.20	39.6	666.20	31.4	666.20	16.0	666.20	666.20	0.00	0.00	15.71
c101	100 16	1220.18	1220.18	18.3	1220.18	18.5	1220.18	10.4	1220.18	1220.43	0.00	0.02	12.93
c201	100 5	4662.07	662.07	16.6	662.07	23.5	662.07	8.8	662.07	662.07	0.00	0.00	9.77
rc101	100 10	a1059.32	1059.32	12.8	1059.32	23.8	1059.32	11.1	1059.32	1059.32	0.00	0.00	16.89
rc201	100 3	a672.92	672.92	24.0	672.92	21.2	672.92	7.3	672.92	672.92	0.00	0.00	11.42
r_{1-2-1}	200 23	3357.64	3357.64	175.8	3375.19	84.6	3360.02	66.2	3353.80	3355.04	-0.11	-0.08	1142.05
r_{2-2-1}	200 5	a1665.58	1665.58	103.4	1665.58	72.7	1665.58	45.3	1665.58	1665.58	0.00	0.00	1425.88
c_{1-2-1}	200 28	3629.89	3636.74	117.6	3641.89	57.0	3629.89	87.4	3628.51	3636.53 -0.04	-0.04	0.18	2874.50
$c2_{-}2_{-}1$	200	1726.59	1726.59	127.8	1726.73	67.3	1726.59	65.0	1726.59	1726.59	0.00	0.00	1365.93
$rc1_{-2_{-1}}$	200 23	3306.00	3312.92	299.3	3316.94	83.4	3306.00	71.7	3303.70	3306.73 -0.07	-0.07	0.02	1293.53
rc2.2.1	200 5	a1560.00	1560.00	77.5	1560.00	74.4	1560.00	44.7	1560.00	1560.00	0.00	0.00	1361.87
r_{1-4-1}	40054	$^{b}9605.75$	9627.43	2928.3	9668.18	421.5	9618.97	481.6	9519.45	9239.56 -0.90	-0.90	-0.69	9177.90
$r2_{-4_{-1}}$	400 10	3551.38	3582.08	9.892	3560.73	352.0	3551.38	459.2	3546.49	3549.49	-0.14	-0.05	9086.79
c_{1-4-1}	400 63	11098.21	11098.21	1510.4	11125.14	384.6	11099.54	546.2	11047.19	11075.60 - 0.46	-0.46	-0.20	8016.83
$c2_{-4-1}$	400 15	3546.10	3596.37	569.0	3549.20	341.1	3546.10	488.6	3539.50	3543.65	-0.19	-0.07	10691.30
$rc1_{-4_{-1}}$	40052	9520.06	9535.46	2244.2	9520.06	412.7	9536.77	513.4	9447.53	9478.12	-0.76	-0.44	10867.10
$rc2_{-4.1}$	400 11	3403.70	3422.11	3306.8	3414.90	264.7	3403.70	422.6	3403.70	3403.70	0.00	0.00	8326.18
										Avg.	Avg0.15	-0.07	3653.44
Scaled Time (s)	ime (s)			329.35		73.53		'					3653.44

e: Optimality proved. ¹: Best run on an Intel Core 2 Duo 1.66 GHz (2791 Mflop/s).
²: Average of 10 runs T5500 1.66 GHz ((2791 Mflop/s)).
³: Average of 50 runs on a cluster with 32 SMP nodes, where each node consists of two Intel Xeon 2.66 GHz (wall clock).
^b: Found in [24].

Table 9: Results found for the VRPMPD instances proposed in [41]

Instance	Table 9: Results	iouna ic	or the vn.	FMFD	mstances	propose	ս ու լ	[41]	
CMT1H 50 4° 465.02 465 51 465.02 5.6 465.02 465.03 0.00 0						ILS-I	RVND)-SP	
CMT1H 50 4° 465.02 465 51 465.02 5.6 465.02 465.03 0.00 0	Instance n v BKS Bes	t Time ¹	Best	Time ²	Best	Ave	Gan	Ave	Time
CMT1H 50 4 °465.02 465 51 465.02 5.6 465.02 465.03 0.0 0.00 2.07 CMT1Q 50 6 °489.74 490 41 489.74 6.0 489.74 489.74 0.00 0.00 1.52 CMT1T 50 7 °520.06 520.06 520.34 520.06 7.0 520.06 520.06 520.06 0.00 0.00 1.62 CMT2H 75 5 662.63 663 78 662.63 22.0 662.63 662.63 0.00 0.00 5.16 CMT2Q 75 7 732.76 733 65 732.76 26.2 731.26 731.40 -0.20 -0.19 8.03 CMT2T 75 9 °782.77 783 57 782.77 26.0 782.77 782.77 0.00 0.00 7.56 CMT3H 100 3 °700.94 701 186 701.31 35.6 700.94 700.94 0.00 0.00 17.65 CMT3H 100 3 °700.94 701 186 701.31 35.6 700.94 700.94 0.00 0.00 7.56 CMT3H 100 6 °629.37 629 150 629.37 32.9 747.15 747.15 0.00 0.00 9.70 CMT3T 100 5 °798.07 798 109 798.07 42.6 789.07 798.07 0.00 0.00 28.76 CMT12H 100 6 °629.37 629 150 629.37 32.8 629.37 629.37 0.00 0.00 13.93 CMT12Q 100 8 °729.25 729 108 729.46 42.0 729.25 729.25 -0.03 -0.03 17.37 CMT11T 120 4 818 818 303 820.35 45.8 818.05 818.06 0.01 0.01 6.79 CMT1H 150 6 °893.36 939 196 939.36 66.2 939.36 939.36 0.00 0.00 20.35 CMT11Q 120 6 °939.36 939 196 939.36 66.2 939.36 939.36 0.00 0.00 20.35 CMT11T 100 7 998.80 1000 164 998.80 700.9 998.81 0.00 0.00 19.51 CMT1H 150 11 990.39 1000 212 999.39 166.8 990.39 90.39 0.00 0.00 19.51 CMT4H 150 6 829 829 345 831.39 125.4 828.12 831.59 -0.11 0.31 80.24 CMT4H 150 11 990.39 1000 212 990.39 166.8 990.39 90.39 0.00 0.00 50.42 CMT5H 200 15 1227 1227 333 1232.08 460.8 1218.77 1220.24 -0.67 -0.55 1802.81 CMT6H 50 7 555.43 555 31 555.43 15.5 55.43 557.35 0.00 0.35 1.08 CMT6H 50 7 555.43 555 31 555.43 1.8 555.43 557.35 0.00 0.01 7.8 CMT6H 50 7 555.43 555 31 555.43 1.8 555.43 557.35 0.00 0.01 7.8 CMT6H 50 7 555.48 555 31 555.43 1.8 555.43 557.35 0.00 0.01 7.76 CMT3H 100 10 865.50 866 95 865.50 865.50 865.50 0.00 0.00 7.78 CMT6H 50 7 555.48 555 31 555.43 1.8 555.43 557.35 0.00 0.01 7.79 CMT8H 100 10 865.50 866 95 865.50 865.50 865.50 0.00 0.00 7.78 CMT1H 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.01 7.70 CMT8H 100 11 821.75 822 85 861.50 66.8 865.50 865.50 0.00 0.00 7.78 CMT114 100 11 821.75 822 88 821.75 77.44 821.75 821.75 0.00 0.00 5.4									
CMTIQ 50 6 \$^488,74 490 41 488,74 6.0 488,74 489,74 0.00 0.00 1.52 CMTIT 50 7 \$^520,06 520, 66 2.3 34 520,06 7.0 520,06 520,06 0.00 0.00 1.60 CMT2H 75 5 662.63 663 78 662.63 22.0 662.63 662.63 0.00 0.00 5.16 CMT2Q 75 7 732,76 733 65 732.76 26.2 731.26 731.40 -0.20 -0.19 8.03 CMT2T 75 9 \$^82,77 783.76 55 732.77 26.0 782,77 782.77 780.0 0.00 7.65 CMT3H 100 3 \$^970.94 701 186 701.31 35.6 700.94 700.94 0.00 0.00 17.65 CMT3H 100 3 \$^970.94 701 186 701.31 35.6 700.94 700.94 0.00 0.00 17.65 CMT3H 100 5 \$^8798.07 798 109 798.07 42.6 798.07 798.07 0.00 0.00 28.76 CMT12H 100 6 \$^829.37 629 150 629.37 32.8 629.37 629.37 0.00 0.00 28.76 CMT12H 100 6 \$^829.37 629 150 629.37 32.8 629.37 629.37 0.00 0.00 31.33 CMT12Q 100 8 \$^8729.25 729 108 729.46 42.0 729.25 729.25 -0.00 0.00 6.79 CMT11H 102 4 818 818 303 820.35 45.8 818.05 818.06 0.01 0.01 63.18 CMT11Q 120 6 \$^939.36 939 166 939.36 66.2 939.36 939.36 0.00 0.00 20.35 CMT11Q 120 6 \$^939.36 939 166 939.36 66.2 998.80 999.81 0.00 0.00 19.91 CMT4H 150 6 829 829 345 831.39 125.4 828.12 831.59 -0.11 0.31 80.24 CMT4Q 150 9 913.93 918 244 913.93 153.0 915.27 915.27 0.15 0.15 58.92 CMT4T 150 11 990.39 1000 212 999.39 166.8 990.39 90.39 0.00 0.00 19.91 CMT5H 200 9 992.37 983 514 992.37 351.4 978.74 1.37 -1.37 1531.73 CMT5T 200 15 1227 1227 333 123.08 460.8 1218.77 1220.24 -0.67 -0.55 1802.81 CMT6H 50 7 555.43 555 31 555.43 15.5 54.3 15.5 56.40 0.00 0.01 6.78 CMT6H 50 7 555.43 555 31 555.43 12.8 555.43 557.35 0.00 0.03 51.08 CMT6H 50 7 555.43 555 31 555.43 12.8 555.43 557.35 0.00 0.01 5.47 CMT5H 100 11 821.75 822 88 881.55 865.50 865.50 865.50 866 93 865.50 46.8 805.50 865.50 0.00 0.00 7.78 CMT5H 100 10 865.50 866 93 865.50 46.8 805.50 865.50 0.00 0.00 7.78 CMT6H 100 11 821.75 822 88 821.75 72.4 821.75 821.75 0.00 0.00 5.47 CMT14H 100 11 821.75 822 88 821.75 72.4 821.75 821.75 0.00 0.00 7.78 CMT9H 150 16 16161.51 1166 177 1161.63 306.4 1160.68 1162.17 0.00 0.00 7.78 CMT9H 150 16 1162.86 1164 171 1161.61 171 1161.63 206.1 1161.64 1141 1161.69 0.02 0.08 821.75 86.64 100.00 0.00 7.78 CMT9	CMT1H 50 4 465 02 46		465.02			465.03		* \ /	
CMT1T 50 7 *520.06 520 34 520.06 7.0 520.06 520.06 0.00 0.00 1.60 CMT2H 75 5 662.63 663 378 662.63 22.0 662.63 662.63 0.00 0.00 5.16 CMT2Q 75 7 732.76 733 65 732.76 26.2 731.26 731.40 -0.20 -0.19 8.03 CMT2T 75 9 *782.77 783 57 782.77 26.0 782.77 782.77 0.00 0.00 7.56 CMT3Q 100 4 *747.15 747 128 747.15 39.8 747.15 747.15 0.00 0.00 17.65 CMT3Q 100 5 *798.07 798 109 798.07 42.6 798.07 0.00 0.00 9.70 CMT3T 100 5 *798.07 798 109 798.07 42.6 798.07 0.00 0.00 9.70 CMT3T 100 6 *629.37 629 150 629.37 32.8 629.37 629.37 0.00 0.00 13.93 CMT12Q 100 8 *729.25 729 108 729.46 42.0 729.25 729.25 -0.03 -0.03 17.37 CMT12T 100 9 *787.52 788 96 787.52 785 20 787.52 787.52 0.00 0.00 6.79 CMT11H 120 4 818 818 303 820.35 45.8 818.05 818.06 0.01 0.01 63.18 CMT11Q 120 6 *939.36 939 196 939.36 66.2 939.36 939.60 0.00 0.00 20.35 CMT11T 120 7 998.80 1000 164 998.80 70.2 998.80 998.81 0.00 0.00 19.91 CMT4H 150 6 829 829 345 831.39 125.4 828.12 831.59 -0.11 0.31 80.24 CMT4Q 150 9 992.37 983 514 992.37 351.4 978.74 -1.37 -1.37 1531.73 CMT5Q 200 12 *b1118 1119 381 1134.72 451.8 1104.87 1105.79 -1.17 -1.09 1627.78 CMT5T 200 15 1227 1227 333 1232.08 460.8 1218.77 1220.24 -0.67 -0.55 1802.81 CMT6H 50 7 555.43 555 31 555.43 12.8 555.43 557.35 0.00 0.00 0.02 1.35 CMT1T 75 14 900.69 901 53 900.09 600 90.05 4 900.84 0.06 0.09 4.47 CMT7Q 75 14 900.69 901 53 900.09 600 90.09 63.5 56.54 556.43 557.15 0.00 0.00 0.00 CMT5T 75 14 900.69 901 53 900.09 900.09 900.09 000.09 000 000 000	_								
CMT2H 75 5 682.63 663 78 662.63 22.0 662.63 662.63 0.00 0.00 5.16 CMT2Q 75 7 732.76 733 65 732.76 26.2 731.26 731.40 -0.20 -0.19 8.03 CMT2T 75 9 "782.77 783 57 782.77 26.0 782.77 782.77 0.00 0.00 7.56 CMT3H 100 3 "700.94 701 186 701.31 35.6 700.94 700.94 0.00 0.00 17.65 CMT3G 100 4 "747.15 747 128 747.15 39.8 747.15 747.15 0.00 0.00 9.70 CMT3T 100 5 "798.07 798 109 798.07 42.6 798.07 798.07 0.00 0.00 9.70 CMT3T 100 6 "629.37 629 150 629.37 32.8 629.37 629.37 0.00 0.00 13.93 CMT12Q 100 8 "729.25 729 108 729.46 42.0 729.25 729.5 -0.03 -0.03 17.37 CMT12T 100 9 "787.52 788 96 787.52 52.0 787.52 789.50 -0.00 0.00 6.79 CMT11H 120 4 818 818 303 820.35 45.8 818.05 818.06 0.01 0.01 63.18 CMT11Q 120 6 "939.36 939 196 939.36 66.2 939.36 939.36 0.00 0.00 6.79 CMT11H 120 7 998.80 1000 164 998.80 70.2 998.80 998.81 0.00 0.00 19.91 CMT4H 150 6 829 829 345 831.39 1254 828.12 831.59 -0.11 0.31 80.24 CMT4Q 150 9 913.93 918 244 913.93 153.0 915.27 0.15 0.15 58.92 CMT5H 200 9 992.37 983 514 992.37 351.4 978.74 978.74 -1.37 -1.37 1531.73 CMT5Q 200 12 "1118 1119 381 1134.72 451.8 1104.87 1105.79 -1.17 -1.09 1627.78 CMT6H 50 7 555.43 555 30 555.43 12.8 555.43 557.15 0.00 0.31 1.08 CMT6H 50 7 555.43 555 30 555.43 12.8 555.43 557.15 0.00 0.31 1.08 CMT6H 50 7 555.43 555 30 555.43 12.8 555.43 557.15 0.00 0.31 1.08 CMT6T 50 7 555.43 555 30 555.43 11.6 555.43 557.35 0.00 0.02 1.15 CMT7H 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.21 4.90 CMT5T 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.21 4.90 CMT5T 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.21 4.90 CMT5T 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.01 1.08 CMT6T 100 10 865.50 866 95 865.50 865.50 865.50 865.50 0.00 0.00 7.78 CMT8H 100 10 865.50 866 95 865.50 865.50 865.50 0.00 0.00 7.78 CMT9H 100 11 821.75 822 88 821.75 72.4 821.75 821.75 0.00 0.00 7.78 CMT9H 100 11 821.75 822 88 821.75 72.4 821.75 821.75 0.00 0.00 7.78 CMT9H 100 11 821.75 822 86 865.50 865.50 865.50 0.00 0.00 7.78 CMT9H 100 10 865.50 866 93 865.50 865.50 865.50 0.00 0.00 7.78 CMT9H 15									
CMT2Q 75 7 732.76 733 65 732.76 26.2 731.26 731.40 -0.20 -0.19 8.03 CMT2T 75 9 °782.77 783 57 782.77 26.0 782.77 782.77 782.77 0.00 -0.00 7.56 CMT3H 100 3 °700.94 701 186 701.31 35.6 700.94 700.94 0.00 0.00 17.65 CMT3Q 100 4 °747.15 747 128 747.15 39.8 747.15 747.15 0.00 0.00 9.70 CMT3T 100 5 °789.07 798.07 798.07 798.07 798.07 70.00 0.00 28.76 CMT12H 100 6 °629.37 629 150 629.37 32.8 629.37 629.37 0.00 0.00 13.93 CMT12Q 100 8 °729.25 729 108 729.46 42.0 729.25 729.25 -0.03 -0.03 17.33 CMT12T 100 9 °787.52 788 96 787.52 52.0 787.52 787.52 0.00 0.00 6.79 CMT11H 120 4 818 818 303 820.35 45.8 818.05 818.06 0.01 0.01 63.18 CMT11Q 120 6 °393.69 393 916 939.36 66.2 939.36 939.36 0.00 0.00 20.35 CMT11T 120 7 998.80 1000 164 998.80 70.2 998.80 998.81 0.00 0.00 19.91 CMT4H 150 6 829 829 345 831.39 125.4 828.12 831.59 0.11 0.31 80.24 CMT4Q 150 9 913.93 918 244 913.93 153.0 915.27 915.27 0.15 0.15 88.92 CMT5H 200 9 992.37 983 514 992.37 381 134.72 451.8 1104.87 1105.79 -1.17 -1.09 1627.78 CMT5T 200 15 1227 1227 333 1232.08 460.8 1218.77 1220.24 -0.67 -0.55 1802.81 CMT6H 50 7 555.43 555 30 555.43 13.0 555.43 557.35 0.00 0.03 5.108 CMT6H 50 7 555.43 555 30 555.43 11.6 555.43 557.35 0.00 0.02 1.2 15 CMT7H 75 14 900.69 901 53 900.69 46.8 900.84 0.06 0.09 4.47 CMT7T 75 14 900.69 901 53 900.69 46.8 900.89 902.80 0.00 0.02 1.15 CMT7T 75 14 903.05 903 86.50 93 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT8T 100 10 865.50 866 93 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT8T 100 10 865.50 866 93 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT3H 100 10 865.50 866 93 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT3H 100 11 821.75 822 88 821.75 81.6 821.75 81.6 821.75 0.00 0.00 7.78 CMT3H 100 10 865.50 866 93 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT3H 100 10 865.50 866 95 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT3H 100 10 865.50 866 95 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT3H 100 10 865.50 866 95 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT3H 100 10 865.50 866 95 865.50 74.4 865.50 865.50 0.00 0.00 7.78 CMT3H 100 10 865.50 866									
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CMT5T 200 15 1227 1227 333 1232.08 460.8 1218.77 1220.24 -0.67 -0.55 1802.81 CMT6H 50 7 555.43 555 31 555.43 13.0 555.43 557.35 0.00 0.35 1.08 CMT6Q 50 7 555.43 555 30 555.43 11.6 555.43 556.64 0.00 0.22 1.15 CMT7H 75 13 900 900 54 900.84 50.0 900.54 900.84 0.06 0.09 4.47 CMT7Q 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.21 4.90 CMT7T 75 14 903.05 903 52 903.05 39.0 903.05 903.00 0.00 0.01 4.77 CMT8H 100 10 865.50 866 95 865.50 865.50 865.50 0.00 0.00 7.78 CMT8TW 100 11	CMT5H 200 9 992.37 98	3 514	992.37	351.4	978.74	978.74	-1.37	-1.37	1531.73
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CMT6H 50 7 555.43 555 31 555.43 13.0 555.43 557.35 0.00 0.35 1.08 CMT6Q 50 7 555.43 555 30 555.43 12.8 555.43 557.15 0.00 0.31 1.08 CMT6T 50 7 555.43 555 31 555.43 11.6 555.43 556.64 0.00 0.22 1.15 CMT7T 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.21 4.90 CMT7T 75 14 903.05 903 52 903.05 39.0 903.05 90.00 0.00 0.21 4.90 CMT8H 100 10 865.50 866 95 865.50 856 865.50 0.00 0.00 7.78 CMT8T 100 10 865.54 866 95 865.54 65.6 865.54 865.50 <td>CMT5T 200 15 1227 122</td> <td>7 333</td> <td>1232.08</td> <td>460.8</td> <td>$\overline{1218.77}$</td> <td>$\overline{1220.24}$</td> <td>-0.67</td> <td>-0.55</td> <td>1802.81</td>	CMT5T 200 15 1227 122	7 333	1232.08	460.8	$\overline{1218.77}$	$\overline{1220.24}$	-0.67	-0.55	1802.81
CMT6Q 50 7 555.43 555 30 555.43 12.8 555.43 557.15 0.00 0.31 1.08 CMT6T 50 7 555.43 555 31 555.43 11.6 555.43 556.64 0.00 0.22 1.15 CMT7H 75 14 900.69 90.84 50.0 900.54 900.84 0.06 0.09 4.47 CMT7Q 75 14 903.05 903 52 903.05 39.0 903.05 903.05 0.00 0.00 4.77 CMT8H 100 10 865.50 866 95 865.50 85.6 865.50 865.50 0.00 0.00 7.78 CMT8H 100 10 865.50 866 95 865.50 85.6 865.50 865.50 0.00 0.00 7.78 CMT8T 100 10 865.54 866 95 865.54 65.5 865.50 0.00 0.									
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CMT7H 75 13 900 900 54 900.84 50.0 900.54 900.84 0.06 0.09 4.47 CMT7Q 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.21 4.90 CMT7T 75 14 903.05 903 52 903.05 39.0 903.05 903.05 0.00 0.00 4.77 CMT8H 100 10 865.50 866 95 865.50 85.6 865.50 0.00 0.00 7.78 CMT8T 100 10 865.54 866 95 865.54 65.6 865.54 865.50 0.00 0.00 7.50 CMT14H 100 11 821.75 822 89 821.75 81.6 821.75 0.00 0.00 5.37 CMT14Q 100 11 821.75 822 85 821.75 72.4 821.75 821.75 0.00 0.00 5.37 CMT14Q 100 11	CMT6Q 50 7 555.43 55	5 30	555.43	12.8	555.43	557.15	0.00	0.31	1.08
CMT7Q 75 14 900.69 901 53 900.69 46.8 900.69 902.62 0.00 0.21 4.90 CMT7T 75 14 903.05 903 52 903.05 39.0 903.05 903.05 0.00 0.00 4.77 CMT8H 100 10 865.50 866 95 865.50 865.50 865.50 0.00 0.00 7.78 CMT8T 100 10 865.54 866 95 865.54 65.6 865.54 0.00 0.00 7.58 CMT14H 100 11 821.75 822 89 821.75 81.6 821.75 821.75 0.00 0.00 5.37 CMT14Q 100 11 821.75 822 85 821.75 72.4 821.75 821.75 0.00 0.00 5.47 CMT14T 100 11 826.77 82 826.77 72.4 821.75 821.75 0.00 0.00 5.47 CMT14T 100 11 824.	CMT6T 50 7 555.43 55	5 31	555.43	11.6	555.43	556.64	0.00	0.22	1.15
CMT7T 75 14 903.05 903 52 903.05 39.0 903.05 903.05 0.00 0.00 4.77 CMT8H 100 10 865.50 866 95 865.50 85.6 865.50 865.50 0.00 0.00 7.78 CMT8Q 100 10 865.54 866 95 865.50 74.4 865.50 865.50 0.00 0.00 7.50 CMT8T 100 10 865.54 866 95 865.54 865.54 865.50 0.00 0.00 7.50 CMT14H 100 11 821.75 822 89 821.75 81.6 821.75 821.75 0.00 0.00 5.37 CMT14Q 100 11 821.75 822 85 821.75 72.4 821.75 821.75 0.00 0.00 5.47 CMT14T 100 11 826.77 827 86 826.77 72.4 821.75 821.75 0.00 0.00 5.47 CMT13T	CMT7H 75 13 900 90	0 54	900.84	50.0	900.54	900.84	0.06	0.09	4.47
CMT8H 100 10 865.50 866 95 865.50 85.6 865.50 865.50 0.00 7.78 CMT8Q 100 10 865.50 866 93 865.50 74.4 865.50 865.50 0.00 0.00 7.50 CMT8T 100 10 865.54 866 95 865.54 65.6 865.54 80.00 0.00 7.18 CMT14H 100 11 821.75 822 89 821.75 81.6 821.75 821.75 0.00 0.00 5.37 CMT14T 100 11 826.77 827 86 826.77 64.6 826.77 826.77 0.00 0.00 5.37 CMT13H 120 12 1542.86 1543 125 1542.86 164.2 1542.86 1544.54 0.00 0.11 73.82 CMT13Q 120 12 1542.97 1543 120 1542.97 157.8 1542.86 1544.54 0.00 0.11 73.82 CMT13T 120 12 1542.97 1544 1	CMT7Q 75 14 900.69 90	1 53	900.69	46.8	900.69	902.62	0.00	0.21	4.90
CMT8H 100 10 865.50 866 95 865.50 85.6 865.50 865.50 0.00 7.78 CMT8Q 100 10 865.50 866 93 865.50 74.4 865.50 865.50 0.00 0.00 7.50 CMT8T 100 10 865.54 866 95 865.54 65.6 865.54 80.00 0.00 7.18 CMT14H 100 11 821.75 822 89 821.75 81.6 821.75 821.75 0.00 0.00 5.37 CMT14T 100 11 826.77 827 86 826.77 64.6 826.77 826.77 0.00 0.00 5.37 CMT13H 120 12 1542.86 1543 125 1542.86 164.2 1542.86 1544.54 0.00 0.11 73.82 CMT13Q 120 12 1542.97 1543 120 1542.97 157.8 1542.86 1544.54 0.00 0.11 73.82 CMT13T 120 12 1542.97 1544 1	CMT7T 75 14 903.05 90	3 52	903.05	39.0	903.05	903.05	0.00	0.00	4.77
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	CMT8H 100 10 865.50 86	6 95	865.50		865.50	865.50	0.00	0.00	7.78
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	CMT8Q 100 10 865.50 86	6 93	865.50	74.4	865.50	865.50	0.00	0.00	7.50
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	CMT8T 100 10 865.54 86	6 95	865.54	65.6	865.54	865.54	0.00	0.00	7.18
CMT14Q 100 11 821.75 822 85 821.75 72.4 821.75 821.75 0.00 0.00 5.47 CMT14T 100 11 826.77 827 86 826.77 64.6 826.77 826.77 0.00 0.00 6.30 CMT13H 120 12 1542.86 1543 125 1542.86 164.2 1542.86 1544.54 0.00 0.11 73.82 CMT13Q 120 12 1542.97 1543 120 1542.97 157.8 1542.86 1544.05 -0.01 0.07 69.87 CMT13T 120 12 1542.97 1543 120 1542.97 152.8 1542.86 1544.05 -0.01 0.07 69.87 CMT19H 150 16 16161 1166 177 1161.63 306.4 1160.68 1162.17 -0.03 0.10 77.95 CMT9Q 150 16 1161.51 1162 171 1161.51 289.6 1161.24 1161.69 -0.02 0.02 80.64 CMT10H 199 20 1383.78 1		2 89	821.75		821.75		0.00	0.00	5.37
CMT14T 100 11 826.77 827 86 826.77 64.6 826.77 826.77 0.00 0.00 6.30 CMT13H 120 1542.86 1543 125 1542.86 164.2 1542.86 1544.54 0.00 0.11 73.82 CMT13Q 120 1542.97 1543 120 1542.97 152.8 1542.86 1544.05 -0.01 0.07 69.87 CMT13T 120 12 1542.97 1544 127 1542.97 152.8 1542.86 1544.05 -0.01 0.07 69.87 CMT9H 150 16 1161 1166 177 1161.63 306.4 1160.68 1162.17 -0.03 0.10 77.95 CMT9Q 150 16 1161.51 1162 171 1161.51 289.6 1161.24 1161.69 -0.02 0.02 80.64 CMT9T 150 16 1162.68 1164 178 1162.68 261.0 1162.55									
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		3 125							
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CMT10T 199 20 b1395 1402 291 1400.22 658.6 1381.04 1388.17 -1.00 -0.49 501.65 Avg0.15 -0.06 178.13									
Avg0.15 -0.06 178.13									
	CM1101 199 20 1395 140	291	1400.22	0.860	1381.04				
Scaled Time (s) 51.31 51.28 178.13						Avg.	-0.15	-0.06	178.13
	Scaled Time (s)	51.31		51.28					178.13

<sup>a: Optimality proved. ^b: Found in [7] using another version of their algorithm.
1: Average of 10 runs on a Pentium IV 1.5 GHz (1311 Mflop/s).
2: Best run on a Xeon 2.4 GHz (1978 Mflop/s).</sup>

					Pisinger and	r and		Pisinger and Vidal					Į.	
			i		Røpke	ke		et al.			ILS	LS-RVND-SP	-SP	
Instance	u	v	$ \mathcal{C} $	BKS	$\frac{\text{Avg.}^*}{\text{Sol.}}$	I	Γ ime ¹ (s)	Avg.* Sol.	$Time^2$ (s)	Best Sol.	Avg. Sol.	$_{(\%)}^{\rm Gap}$	Avg. Gap (%)	Time (s)
	50	4	4	a 576.87	576.87	87	29	576.87	13.8	576.87	576.87	00.0	0.00	2.80
	20	2	4	a 473.53	473.53	53	28	473.53	12.6	473.53	473.53		00.00	2.27
	22	က	7	c 641.19	641.19	19	64	641.19	-	641.19	641.19	0.00	00.00	7.25
	80	2	7	b 1318.95	1319.13	.13	75	1318.95	31.2	1318.95	1318.95	0.00	0.00	6.14
	100	_∞	2	d 1001.04	1006.09	60.	88	1001.23	116.4	1001.04	1001.04	0.00	00.00	51.76
	100	വ	2	c 750.03	752.34	.34	120	750.03	63.6	750.03	750.21	0.00	0.02	31.54
	100	9	3	b 876.50	883.01	.01	93	876.50	68.4	876.50	876.50	0.00	00.00	25.70
	100	4	4	d 881.97	889.36	.36	88	884.43	93.0	881.97	881.97	0.00	00.00	21.88
	160	20	4	$^{c}2505.42$	2519.64	.64	253	2505.42	115.2	2505.42	2505.42	0.00	00.00	48.59
- '	240	ro	9	$^{\circ}3702.85$	3736.53	.53	419	3702.85	271.2	3702.85	3702.85	0.00	00.00	1019.76
	360	20	6	c 5474.84	5501.58	.58	582	5476.41	0.009	5474.84	5474.84	0.00	0.00	2544.57
	80	2	2	b 1318.95	1318.95	95	09	1318.95	34.2	1318.95	1318.95	0.00	0.00	3.06
	80	ಬ	7	$^{c}1360.12$	1360.12	12	28	1360.12	33.0	1360.12	1360.12	0.00	00.00	19.11
	160	20	4	b 2572.23	2573.95	.95	188	2572.23	118.2	2572.23	2572.23	0.00	00.00	247.77
	160	2	4	$^{c}2709.09$	2709.09	60	179	2709.09	128.4	2709.09	2710.21	0.00	0.04	1448.47
.,	240	ro	9	b 3827.06	3838.76	92.	315	3827.06	252.0	3827.06	3827.55	0.00	0.01	1214.57
- '	240	വ	9	$^{c}4058.07$	4064.76	92.	300	4058.07	-	4058.07	4058.07		00.00	544.80
	249	14	7	$^{e}4372.78$	4421.03	.03	333	4397.42	0.009	4379.46	4393.70	0.15	0.48	1244.57
	249	12	33	$^{e}3858.66$	3892.50	.50	361	3868.59	570.0	3859.54	3864.22	0.02	0.14	1431.88
	249	∞	4	$^{e}3631.11$	3666.85	.85	363	3636.08	589.2	3631.37	3634.72	0.01	0.10	1422.66
	249	9	ಬ	d 3546.06	3573.23	.23	357	3548.25	428.4	3546.06	3546.15	0.00	< 0.01	1217.35
	360	2	6	$^{c}5702.16$	5722.19	.19	462	5702.16	0.009	5702.15	5705.84	0.00	90.0	846.01
	360	2	6	d 6078.75	6092.66	99.	443	6078.75	0.009	6078.75	6078.75	0.00	0.00	1019.15
				A	Avg. Gap (%)	%) 0.	0.40 Av	Avg. Gap (%) 0.07	0.07		Avg.	0.01	0.04	627.03
Scaled Time (s)	ne (s						77.44		82.87					627.03
		١												

Scaled Time (s)

<sup>a: Optimality proved. ¹: Average of 10 runs on a Pentium IV 3.0 GHz (3181 Mflop/s).
²: Average of 10 runs on an Opteron 2.4 GHz scaled for a Pentium IV 3.0 GHz. *: Average of 10 runs.
^b: First found in [46]. ^c: First found in [44].
^d: First found in [6]. ^e: First found in [9].</sup>

Table 11: Results found for the new MDVRP instances proposed in [44]

					$ ext{Pising} ext{R}_{oldsymbol{arkappa}}$	Pisinger and Røpke	pı	Vidal et al.	_		ILS-	ILS-RVND-SP	-SP	
Instance	u	v	$ \mathcal{C} $	BKS	Avg.* Sol.		$\frac{\text{Time}^1}{\text{(s)}}$	${ m Avg.}^*$ Sol.	$Time^2$ (s)	Best Sol.	Avg. Sol.	Gap (%)	Avg. Gap (%)	Time (s)
pr01	48	2	4	b 861.32	8	361.32	30	861.32	10.2	861.32	861.32	0.00	0.00	1.24
pr07	72	3	9	b 1089.56	1	089.56	58	1089.56	20.4	1089.56	1089.56	0.00	0.00	3.87
pr02	96	4	4	$^{c}1307.34$	130	308.17	103	1307.34	45.6	1307.34	1308.53	0.00	0.09	12.39
pr03	144	9	4	d 1803.80		810.66	214	1803.80	114.6	1803.81	1804.09	0.00	0.02	55.04
pr08	144	9	9	$^{c}1664.85$		1675.74	207	1665.05	123.0	1664.85	1665.08	0.00	0.01	393.98
pr04	192	_∞	4	d 2058.31	207	073.16	296	2059.36	313.2	2058.31	2060.93	0.00	0.13	779.30
pr09	216	6	9	d 2133.20	214	2144.84	350	2134.17	366.0	2133.20	2135.37	0.00	0.10	1070.41
pr05	240	10	4	d 2331.20	235	350.31	372	2340.29	573.6	2331.20	2338.12	0.00	0.30	1337.10
pr06	288	12	4	d 2676.30	269	3695.74	465	2681.93	0.009	2680.77	2685.23	0.17	0.33	2297.66
pr10	288	12	9	d 2868.26	,	2905.43	455	2886.59	0.009	2874.28	2882.41	0.21	0.49	3009.53
					Avg. Gap (%) 0.52	(%)		Avg. Gap (%) 0.13	0.13		Avg.	Avg. 0.04	0.15	896.05
Scaled Time (s)	me (s	(s					86.38		93.72					896.05

 $^1.$ Average of 10 runs on a Pentium IV 3.0 GHz (3181 Mflop/s). $^2.$ Average of 10 runs on an Opteron 2.4 GHz scaled for a Pentium IV 3.0 GHz. $^*:$ Average of 10 runs. $^b:$ First found in [6]. $^d:$ First found in [6]. $^d:$ First found in [9].

4.7. MDVRPMPD

Table 12 presents the results found by ILS-RVND-SP and those pointed out in [7] (6R - no learning) on the set of instances proposed in [41]. With respect to the solution quality, the developed algorithm clearly had a better performance, equaling 17 BKSs and improving the result of another 16. The average gap between the average solutions and the BKSs was -0.10%.

Table 12: Results found for the MDVRPMPD instances proposed in [41]

]	Røpke an Pisinger			ILS-	RVND	-SP	
Instance	n	v	G	BKS	Best Sol.	Avg. Sol.*	Time ¹ (s)	Best Sol.	Avg. Sol.	Gap (%)	Avg. Gap (%)	Time (s)
GJ01Q	50	4	4	528	528	528	36	528.30	528.30	0.06	0.06	3.12
GJ01T	50	4	4	569	569	569	34	569.43	569.43	0.08	0.08	2.98
GJ02H	75	4	2	440	440	440	51	440.00	440.00	0.00	0.00	2.95
GJ02Q	75	4	2	450	450	451	43	449.72	449.72	-0.06	-0.06	2.60
GJ02T	75	4	2	464	464	464	37	464.13	464.13	0.03	0.03	2.50
GJ03H	100	5	3	581	581	583	81	579.45	579.45	-0.27	-0.27	9.54
GJ03Q	100	5	3	605	605	608	71	605.25	605.25	0.04	0.04	8.95
GJ03T	100	5	3	624	$\bf 624$	626	65	624.44	624.44	0.07	0.07	10.94
GJ04H	100	2	8	790	790	797	112	789.19	789.30	-0.10	-0.09	31.69
GJ04Q	100	2	8	875	$\bf 875$	876	94	874.78	874.79	-0.03	-0.02	41.89
GJ04T	100	2	8	962	$\bf 962$	969	85	962.25	962.65	0.03	0.07	37.95
GJ05H	100	2	5	678	678	680	168	676.81	676.91	-0.18	-0.16	22.24
GJ05Q	100	2	5	700	702	705	133	700.15	700.15	0.02	0.02	19.55
GJ05T	100	2	5	733	733	738	118	733.17	733.18	0.02	0.02	39.31
GJ06H	100	3	6	745	747	751	116	742.18	742.18		-0.38	32.28
GJ06Q	100	3	6	794	794	800	100	793.85	793.87	-0.02	-0.02	25.00
GJ06T	100	3	6	851	851	853	90	$\bf 850.82$	850.82	-0.02	-0.02	27.19
GJ07H	100	4	4	733	733	734	117	732.73	732.73	-0.04	-0.04	24.66
GJ07Q	100	4	4	802	803	807	94	801.91	801.94	-0.01	-0.01	38.58
GJ07T	100	4	4	$\bf 854$	855	862	88	853.54	853.54	-0.05	-0.05	20.64
GJ08H	249	2	14	3327	3327	3373	581	3320.39	3342.91	-0.20	0.48	1435.21
GJ08Q	249	2	14	3762	3774	3810	479	3745.18	3769.01		0.19	1288.57
GJ08T	249	2		4134	4134	4170	431		4120.27		-0.33	1272.63
GJ09H	249	3	12	3005	3006	3028	646	2990.92	3005.52	-0.47	0.02	1478.35
GJ09Q	249	3	12	3355	3355	3393	535	3351.18	3361.23	-0.11	0.19	1362.18
GJ09T	249	3	12	3677	3677	3718	492	3656.03	3661.62	-0.57	-0.42	1316.84
GJ010H	249	4	8	2927	2930	2963	644	2894.71	2905.23	-1.10	-0.74	1452.52
GJ010Q	249	4	8	3242	3245	3267	513	3220.79	3226.79			1315.68
GJ010T	249	4	8	3485	3485	3524	472	3470.70	3477.99		-0.20	1281.92
GJ011H	249	5	6	2855	2880	2905	609	2842.79	2845.71	-0.43	-0.33	1357.58
GJ011Q	249	5	6	3155	3165	3192	511	3138.64	3143.33	-0.52	-0.37	1267.12
GJ011T	249	5	6	3390	3390	3421	469	3360.48	3367.63	-0.87	-0.66	1181.56
					Avg.	Gap (%)	0.66		Avg.	-0.22	-0.10	497.54
Scaled T	ime ($(\mathbf{s})^{-}$				55.48						497.54

^{*:} Average of 10 runs.

5. Concluding Remarks

This work presented an algorithm that hybridizes an Iterated Local Search based heuristic and a Set Partitioning formulation. Its design favored the flexibility, allowing its application in the solution of several VRP variants. Moreover,

b: Found in [7] using another version of their algorithm.
 1: Average of 10 runs on a Pentium IV 1.5 GHz (1311 Mflop/s).

we believe that the developed hybrid approach is relatively simple and easy to implement. The key aspects of the proposed methodology are the interaction between a solver and a metaheuristic approach while solving a given MIP model and an efficient scheme of dynamically controlling the size of the SP models when solving large size instances. These ideas can be employed to efficiently solve a large class of combinatorial optimization problems.

The ILS-RVND-SP algorithm was evaluated in hundreds of well-known instances of the variants considered in this work, with up to 480 customers. The same parameter tuning was adopted and the results obtained were quite competitive with those found by heuristics devoted to specific variants. Table 13 shows the summary of the results found by ILS-RNVD-SP. In this table **Avg. Gap** corresponds to the average gap between the average solutions and the BKSs, **#Instances** is the number of instances of a particular benchmark, **#Improv** denotes the number of solutions improved and **#Ties** represents the number of ties. It can be seen that 52 new best solutions were found and that the Avg. Gap was always smaller than 0.55%.

Table 13: Summary of ILS-RVND-SP results

			,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		
Variant	#Instances	#Improv	#Ties	Avg. Gap (%)	Avg. Time (s)
CVRP ¹ ACVRP ¹ OVRP ¹ VRPSPD ¹ VRPMPD ¹ MDVRP ¹	^a 3, ^b 14, ^c 20 ^d 24 ^e 16, ^f 8 ^g 28, ^h 18 ^g 42 ⁱ 23, ^j 10 ^g 33	a1, b0, c0 $d1$ $e3, f7$ $g5, h7$ $g12$ $i0, j0$ $g16$	$a^{a}2, b^{b}13, c^{c}5$ $a^{d}23$ $a^{e}12, f^{f}1$ $a^{g}21, b^{h}11$ $a^{g}29$ $a^{i}20, f^{g}8$ $a^{g}17$	$^{a}0.17, ^{b}0.08, ^{c}0.55$ $^{d}0.01$ $^{e}0.06, ^{f}-0.08$ $^{g}0.12, ^{h}-0.07$ $^{g}-0.06$ $^{i}0.04, ^{j}0.15$ $^{g}-0.10$	$^a17.41$ $^b100.83$, $^c3938.23$ $^d2.24$ $^e143.44$, $^f3844.03$ $^g189.24$, $^h3653.44$ $^g178.13$ $^i627.03$, $^j896.05$ $^g497.54$
Total	239	52	162		

^a: M series open instances; ^b: Christofides et al. [36]; ^c: Golden et al. [37].

As for future work, we intend to extend the range of application of ILS-RVND-SP by tackling variants with additional constraints such as time windows, backhauls and site/time dependence.

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^d: Fischetti et al. [19] and Pessoa et al. [20].

^e: Christofides et al. [36] and Fisher [39]; ^f: Li et al. [40].

 $[^]g\colon$ Salhi and Nagy [41]; $^h\colon$ Montané and Galvão [43];

i: Cordeau et al. (old) [44]; j: Cordeau et al. (new) [44].

 $^{^{1}\}colon$ Core i7 2.93 GHz (single thread).

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