

$$Y = \hat{\beta}_0 + \hat{\beta}_1 \bar{X} \quad \text{plug in } \bar{X} \text{ for } X$$

$$= \bar{Y} - \hat{\beta}_1 \bar{X} + \hat{\beta}_1 \bar{X}$$

$$= \bar{Y} + \hat{\beta}_1 (\bar{X} - \bar{X})$$

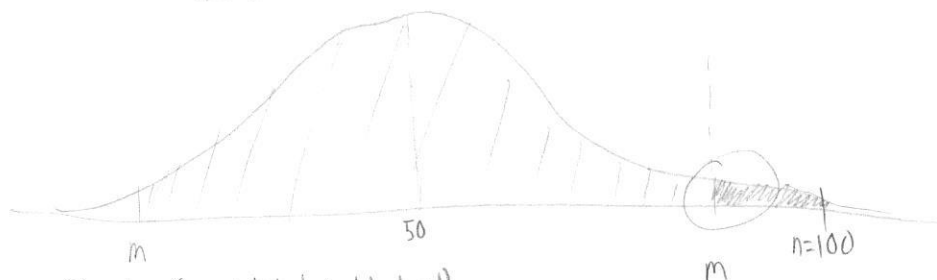
$$= \bar{Y}$$

$$Y = \bar{Y} \quad \checkmark$$

$$b(n, p, k) = \binom{n}{k} p^k (1-p)^{n-k} = \text{exact \# successes}$$

$$n=100$$

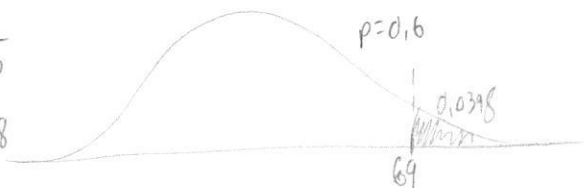
$$\alpha(p) = \sum_{m \leq k \leq n} b(n, p, k)$$



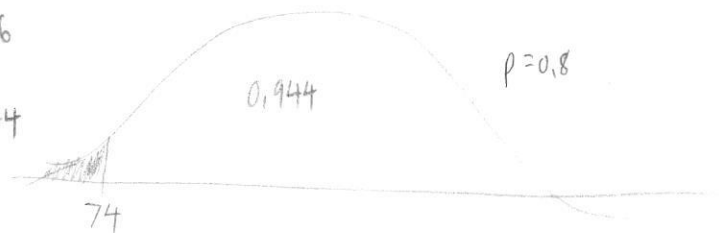
if m low, (equivalent to high alpha level)
harder for missed opportunity
 $\alpha(p)$ becomes higher
T2 error = $1 - \alpha(p)$
becomes lower

if m high, (equivalent to low alpha level)
harder for false alarm
T1 error goes down
 $\alpha(p)$ becomes lower

$$\begin{aligned} \text{T1 error} \quad & \sum_{68 \leq k \leq 100} b(100, 0.6, k) = 0.0615 \\ & \sum_{69 \leq k \leq 100} b(100, 0.6, k) = 0.0398 \end{aligned}$$



$$\begin{aligned} \text{T2 error} \quad & \sum_{73 \leq k \leq 100} b(100, 0.8, k) = 0.966 \\ & \sum_{74 \leq k \leq 100} b(100, 0.8, k) = 0.944 \end{aligned}$$



For T1 error, m at 69 gives us $< 5\%$ error rate. We would reject H_0 at this point.
Increasing m will only decrease this rate further.

For T2 error, m at 73 gives us $< 5\%$ error rate. The new H_0 is $p=0.8$. If the baseline is $p=0.6$, then getting $m=73$ or below would make us think $p=0.6$, hence causing Type 2 error.

Decreasing m will only decrease this rate further.

This is why $69 \leq m \leq 73$.