

A decorative network diagram in the top-left corner of the slide. It features a complex web of interconnected nodes and edges. The nodes are represented by small circles, some of which are solid blue, some are solid grey, and some are hollow with a blue outline. The edges are thin grey lines connecting the nodes. The overall structure is a dense, interconnected graph.

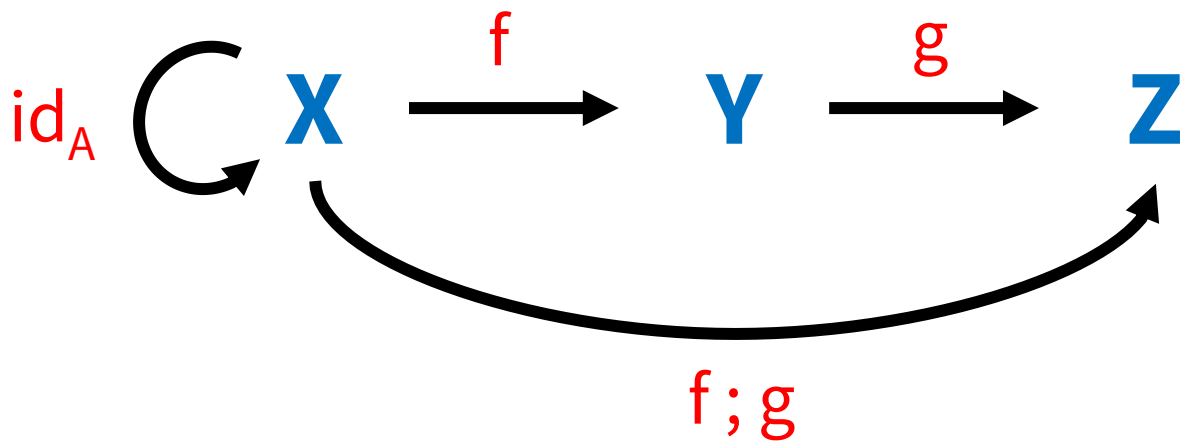
Lecture 2

# Categories

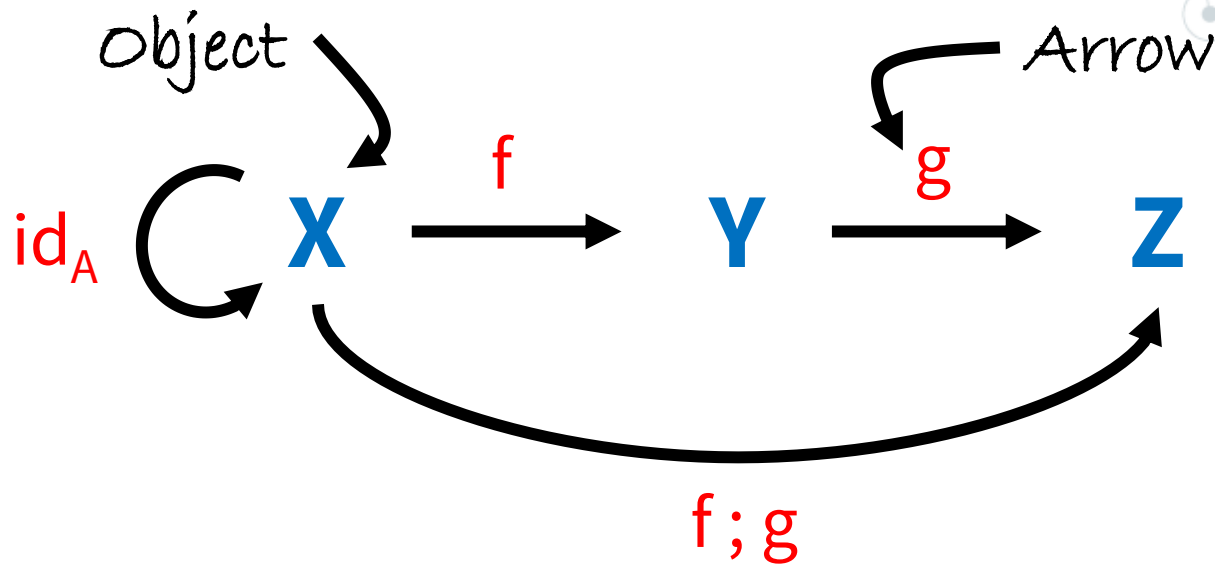
A decorative network diagram in the bottom-right corner of the slide. It features a complex web of interconnected nodes and edges. The nodes are represented by small circles, some of which are solid blue, some are solid grey, and some are hollow with a blue outline. The edges are thin grey lines connecting the nodes. The overall structure is a dense, interconnected graph.

# Category Theory

- You can use Categories to model Logic.
- You can use Categories to model Lambda calculus.
- Logic = Categories = Lambda calculus.
- Here is a category



# Category Theory



$$id_A ; f = f = f ; id_B$$

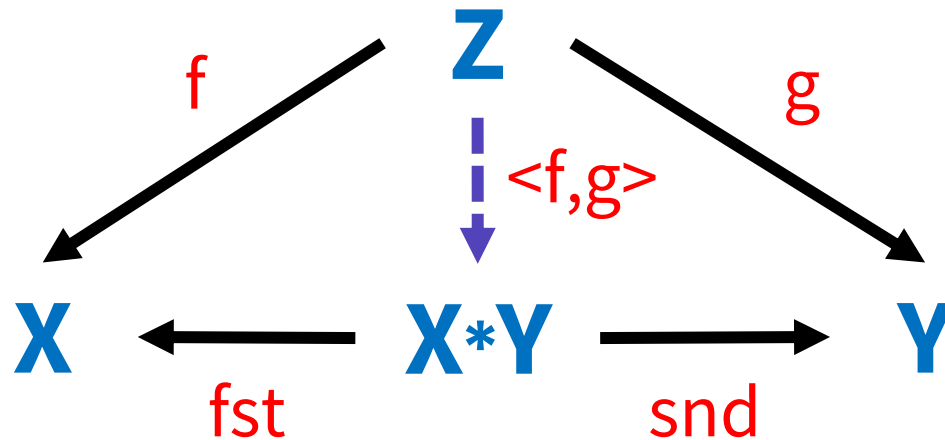
(Identity function)

$$(f ; g) ; h = f ; (g ; h)$$

(Composition)

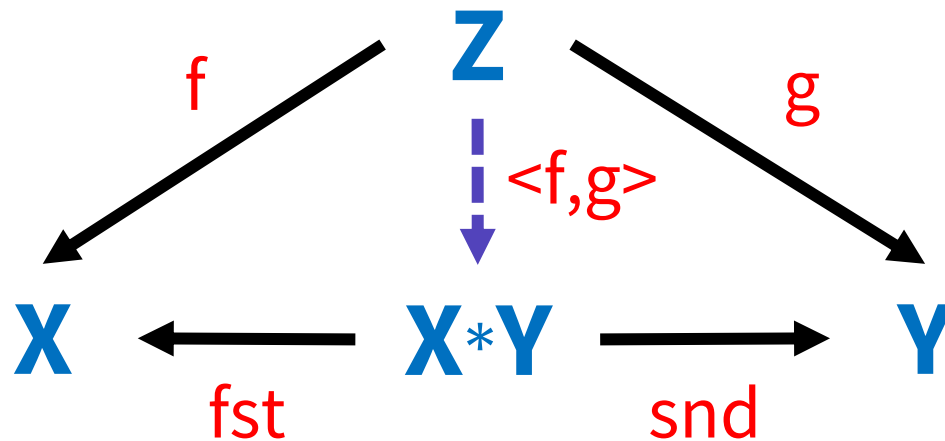
# Products

- The two most important structures in Programming Languages (Or the most two important logical connectives)



- For every object  $X$ , and every object  $Y$ , there is an object  $X$  times  $Y$  ( $X * Y$ )

# Products



$$\langle f, g \rangle ; \text{fst} = f$$

$$\langle f, g \rangle ; \text{snd} = g$$

- **In Computing:**  $X$  could be a data structure (Integer),  $Y$  is another type (String), and  $Z$  is a structure with two fields. ( **$X$  and  $Y$** )

# Products

If we have three different items of type X for example a string ["a", "b", "c"], and two different items of type Y [0,1]. How many different records can be created?

**3x2**

**("a",0)**

**("a",1)**

**("b",0)**

**("b",1)**

**("c",0)**

**("c",1)**



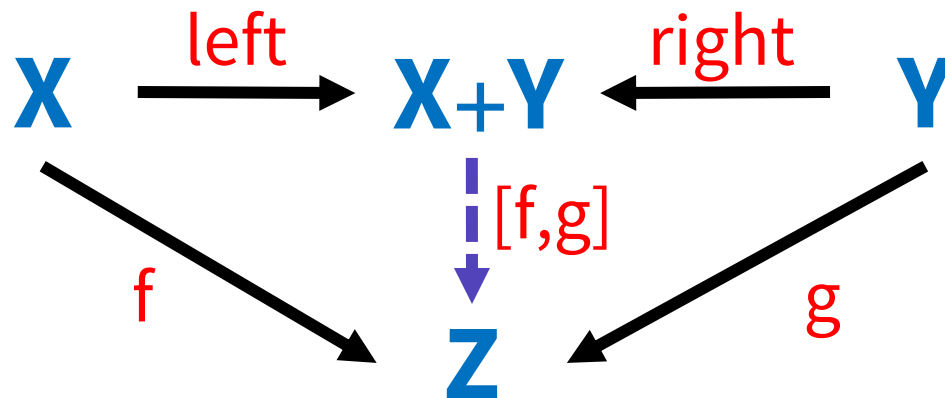
# Let's see Products in Java



```
public class Product<X,Y>{
    private X first;
    private Y second;
    public Product (X first,Y second){
        this.first=first; this.second=second;
    }
    public X getFst(){ return this.first;}
    public Y getSnd(){ return this.second;}
}

public class Test{
    public Product<Integer,String> pair= new
    Product(1,"two");
    public Integer one=pair.getFst();
    public String two=pair.getSnd();
}
```

# Sums



$$\text{left} ; [f,g] = f$$

$$\text{right} ; [f,g] = g$$

- If I know  $X$  or  $Y$ , I can conclude  $Z$ .
- In computing: for either a value of type  $X$  or a value of type  $Y$ , you can get to  $Z$ . ( **$X$  OR  $Y$** )



## Sums

If we have three different items of type X [a,b,c], and two different items of type Y [0,1]. How many different sums can be created?

**3+2**

**left “a”**

**right 0**

**left “b”**

**right 1**

**left “c”**



## Let's see Sums in Java

```
public interface Sum<X,Y>{
    private <Z> Z Selection(Function<X,Z> f, Function<Y,Z>
g);
}
public class Left<X,Y> implements Sum<X,Y>{
    private X x;
    public Left(X x) {this.x=x;}
    public <Z> Z Selection(Function<X,Z> f,
        Function<Y,Z> g){
        return f.apply(x);
    }
}
public class Right<X,Y> implements Sum<X,Y>{
    private Y y;
    public Right(Y y) {this.y=y;}
    public <Z> Z Selection(Function<X,Z> f, Function<Y,Z> g){
        return g.apply(y);
    }
}
```

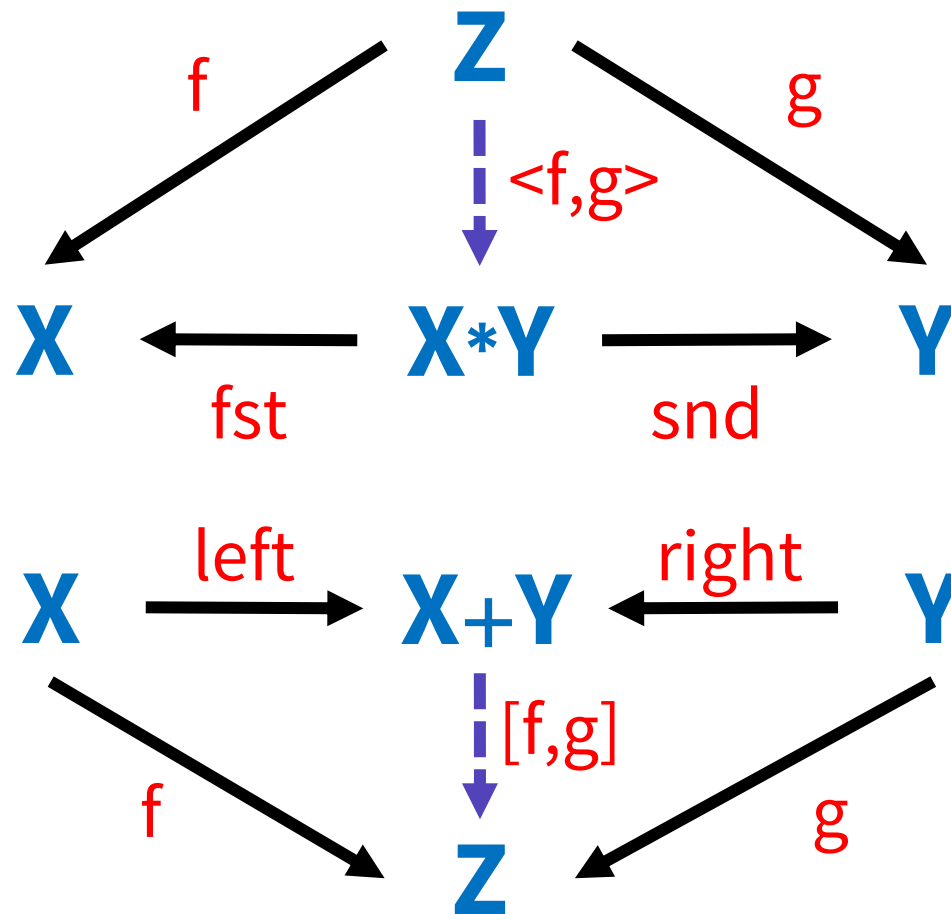
# Let's see Sums in Java



```
public class ErrInt extends Sum<Integer,String>{
    public ErrInt err= new Left("Error");
    public ErrInt one= new Right(1);
    public ErrInt add(ErrInt that){
        return this.Selection(
            e-> new Left(e),
            m-> that.Selection(
                e-> new Left(e),
                n-> new Right(m+n)
            )
        );
    }
    public ErrInt test=one.add(err);
}
```

You cannot add if an error exists

# Duals



- If you flip the arrows twice, you'll get back where you started. Sounds Familiar?

## De Morgan's laws

- The expression of conjunctions and disjunctions can be expressed in terms of each other via negation.

$$\overline{A \vee B} = \bar{A} \wedge \bar{B}$$

$$\overline{A \wedge B} = \bar{A} \vee \bar{B}$$

# Exponentials

How many different functions can be created from a type Y with two items  $[0,1]$  to a type X with three items  $[a,b,c]$ ?

$$2 \Rightarrow 3 = 3^2$$

$0 \rightarrow "a"$   
 $1 \rightarrow "a"$

$0 \rightarrow "b"$   
 $1 \rightarrow "a"$

$0 \rightarrow "c"$   
 $1 \rightarrow "a"$

$0 \rightarrow "a"$   
 $1 \rightarrow "b"$

$0 \rightarrow "b"$   
 $1 \rightarrow "b"$

$0 \rightarrow "c"$   
 $1 \rightarrow "b"$

$0 \rightarrow "a"$   
 $1 \rightarrow "c"$

$0 \rightarrow "b"$   
 $1 \rightarrow "c"$

$0 \rightarrow "c"$   
 $1 \rightarrow "c"$

# Isomorphisms

- Functions are Exponentials!

$$\begin{aligned}\mathcal{C}(Z, X * Y) &\cong \mathcal{C}(Z, X) * \mathcal{C}(Z, Y) \\ \mathcal{C}(X + Y, Z) &\cong \mathcal{C}(X, Z) * \mathcal{C}(Y, Z)\end{aligned}$$



$$\begin{aligned}(X * Y)^Z &= X^Z * Y^Z \\ Z^{(X+Y)} &= Z^X * Z^Y\end{aligned}$$



# Or-structure Example in Rust

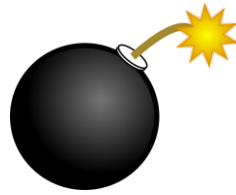


## std::result

- Result<T, E> is an enum with two variants:
  - Ok(T) → success and containing a value.
  - Err(E) → error and containing an error value.

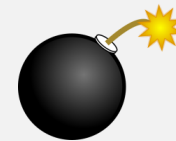
```
enum Result<T, E> {  
    Ok(T),  
    Err(E),  
}
```

# Attempt 1 =



```
use std::io::{stdin, stdout, Write}; //flush uses Write

fn main(){
    let mut my_string = String::new();
    print!("Enter a number: "); // prompt user
    stdout().flush().unwrap();
    stdin().read_line(&mut my_string)
        .expect("Did not enter a correct string");
    let my_number: f64 = my_string.trim().parse();
    println!("Yay! You entered a number. It was {:?}" ,
        my_num);
}
```



**because you need to handle a Result that has been returned by a function**

```
error[E0308]: mismatched types
    --> main.rs:20:26
       |
20   |         let my_number: f64 = my_string.trim().parse();
    // .unwrap();
                                     ^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^^
expected f64, found enum `std::result::Result`
    = note: expected type `f64`
           found type `std::result::Result<_, _>`
error: aborting due to previous error
```

has been returned by a function

```
pub fn parse<F>(&self) -> Result<F, <F as ... >::Err>
```

- So, how do we set the correct type?



# Fixing the Error with Expect()

- The expect() function looks at the Result type:
  - OK → returns the converted value.
  - Err → lets the program crash.

```
let my_number: f64 = my_string.trim().parse().expect("Parse failed");
```

- If the Result is Err, expect() will let the program crash and display the string that was passed to it.



# Fixing 1 Problem

```
use std::io::{stdin, stdout, Write}; //flush uses Write
fn main() {
    let mut my_string = String::new();
    print!("Enter a number: ");
    stdout().flush().unwrap(); //like expect(), ignore it
    let my_num = loop {
        my_string.clear(); //clearing any errors.
        stdin().read_line(&mut my_string)
            .expect("Did not enter a correct string");
        match my_string.trim().parse::<f64>() {
            Ok(okay) => break okay,
            Err(_) => println!("Try again. Enter a number.")
        }
    };
    println!("You entered {:?} ", my_num);
}
```

# Using Result in Your Own Functions

```
fn is_it_fifty(num: u32) -> Result<u32, &'static str> {
    let error = "It didn't work";
    if num == 50 {
        Ok(num)
    } else {
        Err(error)
    }
}

fn main() {
    let my_num = 50; //50 for example
    match is_it_fifty(my_num) {
        Ok(_) => println!("Good! my_num is 50"),
        Err(err) => println!("Error: {:?} ", err)
    }
}
```



# **Panic, panic – controlled chaos**

## **(C Style in Rust)**

# Can ...we try again?

```
fn open_config() -> Result<std::fs::File, std::io::Error> {  
  use std::fs::File;  
  match File::open("config.toml") {  
    Ok(f) => Ok(f),  
    // If not found, search in second location:  
    Err(e) => match File::open("data/config.toml") {  
      Ok(f) => Ok(f),  
      // Otherwise, bubble first error up to caller  
      _ => Err(e),  
    }  
  }  
}
```





## In main ...

```
fn main() {  
  let mut result = open_config();  
  if result.is_err() {  
    // If failed the first time  
    // Try again in about 5 seconds ...  
    std::thread::sleep(std::time::Duration::from_secs(5));  
    // Reattempt  
  
    result = open_config();  
  } match result {  
    // Proceed as usual ...  
    Ok(cfg) => println!("Opened the config file"),  
    // Print the cause to stderr, and DONT PANIC  
    Err(e) => {eprintln!("File could not be opened: {:?}", e.kind());  
    std::process::exit(1); // Exit with code 1 (fail)  
  }  
}
```



# Does it exist?

Choosing between existing  
OR non-existing things



### Example 3 -- Optional

An output can have either Some value or no value (None).

```
enum Option<T> { // T is a generic and it can  
                  contain any type of value.
```

```
    Some(T),
```

```
    None,
```


```
}
```



## Basic usages of Option

- ◎ if an argument of the function is optional,
- ◎ If the function is non-void and if the output it returns can be empty,
- ◎ If the value, of a property of the data type can be empty,
- ◎ We have to use their data type as an Option type





```
fn get_an_optional_value() -> Option<&str>
{    //if the optional value is not empty

    return Some("Some value");
    //else
        None
}
```



In a data structure

```
struct Name
```

```
{ first_name: String,
```

```
  middle_name: Option<String>, // middle_name  
                                can be empty
```

```
  last_name: String, }
```

## Pattern Matching

```
use std::env;
```

```
fn main()
```

```
{ let home_path = env::home_dir();
```

```
match home_path {
```

```
Some(p) => println!("{:?}", p), // prints "/root",
```

```
None => println!("Can not find the home directory!"),
```

```
}}
```

## Options and Results

```
fn main() {
```

```
    let o: Result<i8, &str> = Ok(8);
```

```
    let e: Result<i8, &str> = Err("message");
```

```
    assert_eq!(o.ok(), Some(8)); // Ok(v) ok = Some(v)
```

```
    assert_eq!(e.ok(), None); // Err(v) ok = None
```

```
    assert_eq!(o.err(), None); // Ok(v) err = None
```

```
    assert_eq!(e.err(), Some("message")); // Err(v) err = Some(v)
```

```
}
```