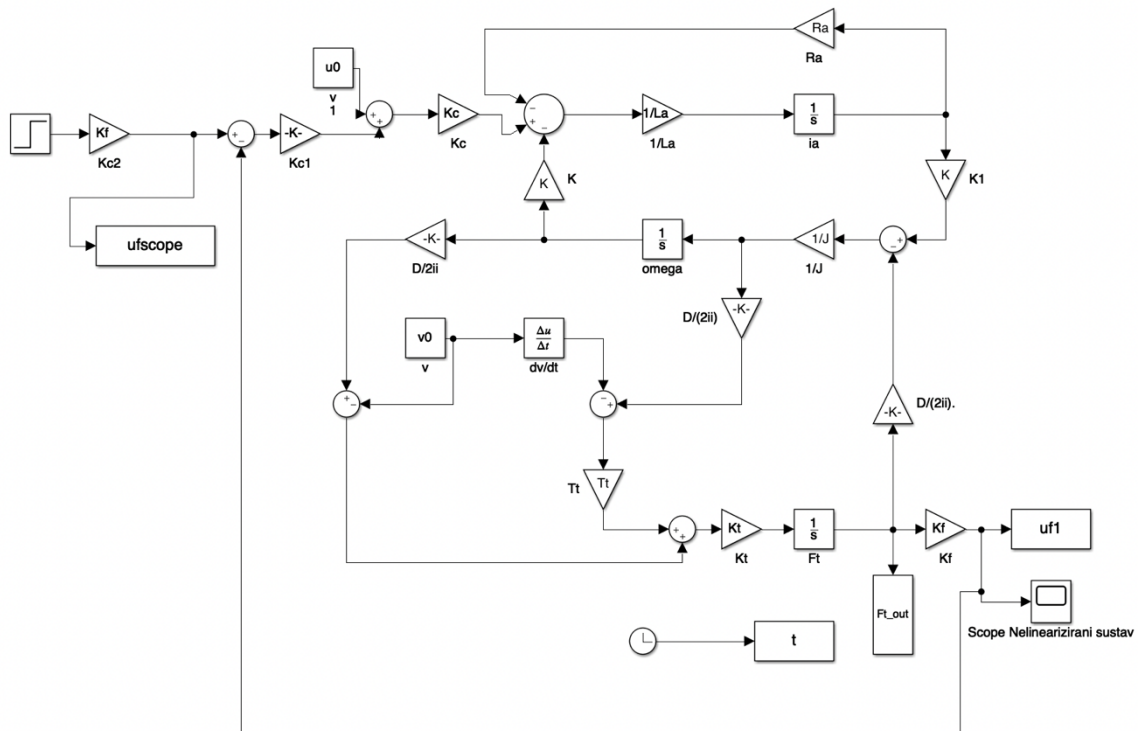


## II. Priprema za vježbu:

a) Nacrtati blokovsku shemu dinamičkog matematičkog modela razmatranog procesa upravljanog P-regulatorom te izraditi simulacijski model razmatranog procesa u Simulinku. Model donijeti na vježbu.



b) Nacrtati polove i nule prijenosne funkcije procesa u  $s$ -ravnini.

**Polovi i nule:**

```
44 - P = pole(G)
45 - Z = zero(G)
```

#### Command Window

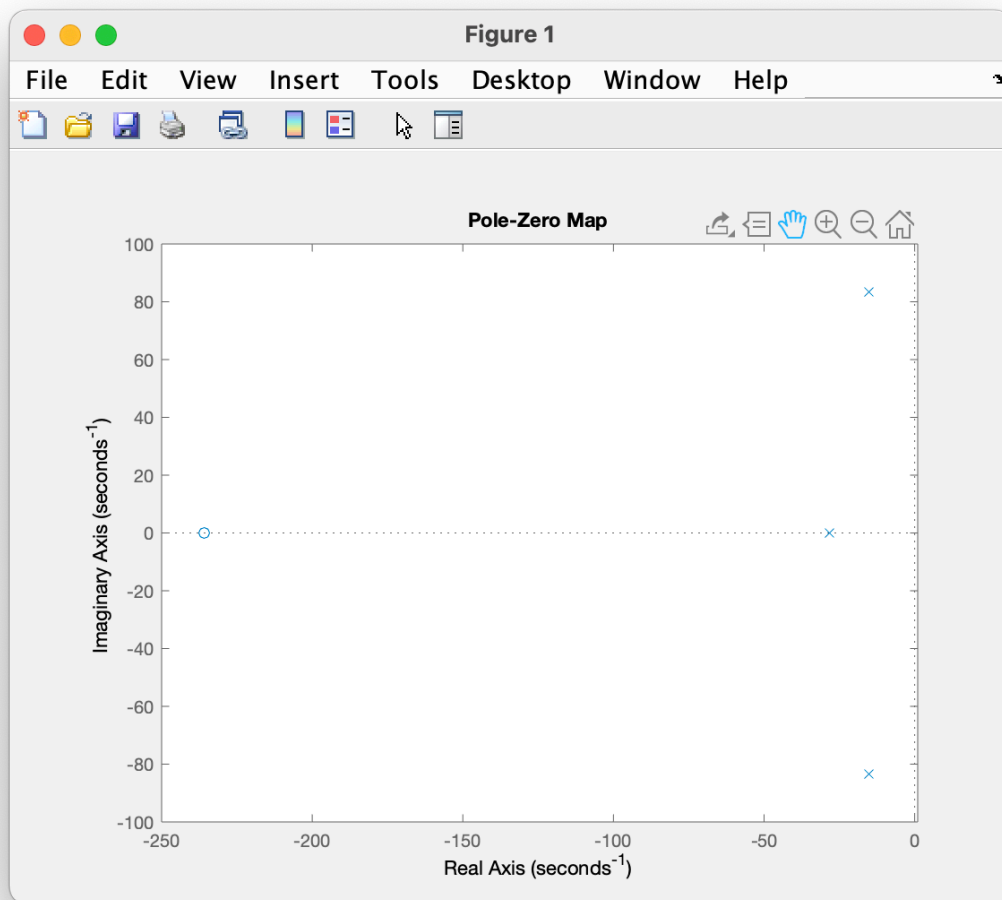
P =

-15.2452 +83.4635i  
-15.2452 -83.4635i  
-28.2184 + 0.0000i

Z =

-235.8491

**Naredba pzplot(G) ih crta:**



c) Pomoću Hurwitzovog kriterija stabilnosti odrediti područje vrijednosti pojačanja P-regulatora za koje je regulacijski krug stabilan. Prikažite izračun.

STANDARDNI COLIK

$$c) \quad G_0 = \left( 0,22907 \cdot 5 + 0,17857 \right) \cdot 10^6$$

$$G_{SE} = \frac{G_0}{1 + G_0} \Rightarrow \frac{(239075 + (6.14 \times 10^5)K)}{1 + 241 \cdot 10^{-6} s^{-1} + 23907 \cdot 10^{-7} s^{-2} + 6059625 s^{-3}}$$

$$1 + \frac{(0.0003 - 0.0003 + 0.0003)K}{4.926 \cdot 10^{-6} s^2 + 2.9907 \cdot 10^{-5} s + 0.039635 + s + 1}$$

$$= (C28905 + 68 \text{ A337}) u$$

$$4,9242 \cdot 10^3 s^{-6} + 2,3907 \cdot 10^2 s^{-4} + 0,0996857 s^{-2} + 1 + (0,28907 s + 63,17852143) v$$

$$4,9242 \cdot 10^{-6} \text{ s}^3 + 2,335 \cdot 10^{-4} \text{ s}^2 + 0,0396805 \text{ s} +$$

$$= (0,239075 + 62,1737) \text{ h}$$

$$4.9242 \cdot 10^{-6} s^2 + 2.8507 \cdot 10^{-5} s + 0.0396857 s + 1 + 10,28907 s + 1.62178714 s$$

$$a_2 \Rightarrow 4,244 \cdot 10^{-4}$$

$$a_2 \Rightarrow 2,8507 \cdot 10^{-4}$$

$$a_1 \Rightarrow 0,0396857 + k - 0,28907 > 0$$

$$a_0 \Rightarrow 1 + 68,1785k > 0$$

$$k - 0,28907 > -0,0396857$$

$$k > -0,1373$$

$$k > -0,1373$$

$$1 + 68,1785k > 0$$

$$68,1785k > -1$$

$$k > -0,0146$$

$$k \in \langle -0,1373, \infty \rangle$$



Dr:

$$D_1 = |a_1| > 0 = 0,0396877 + 0,2807u > 0$$

$$0,2807u > -0,0396877$$

$$u > -0,137$$

$$D_2 = \begin{vmatrix} a_1 & a_2 \\ a_3 & a_4 \end{vmatrix} = \begin{vmatrix} 0,0396877 + 0,2807u & 1,04145u \\ 1,914 \cdot 10^{-6} & 2,357 \cdot 10^{-4} \end{vmatrix}$$

$$= (0,0396877 + 0,2807u)(2,357 \cdot 10^{-4}) - ((1,04145u) \cdot (1,914 \cdot 10^{-6})) > 0$$

$$1,147 \cdot 10^{-5} + 8,36 \cdot 10^{-5} u - [1,914 \cdot 10^{-6} + 3,357 \cdot 10^{-4} u] > 0$$

$$6,5458 \cdot 10^{-6} - 2,521 \cdot 10^{-4} u > 0 \quad | : (-1)$$

$$-2,521 \cdot 10^{-4} u > -6,5458 \cdot 10^{-6} \quad | : (-1)$$

$$u < 0,02596$$

Ukupno:

$$u < 0,02596,$$

$$u > -0,137$$

$$u \in \langle -0,137, 0,02596 \rangle$$

$$= \langle 0,02596 \rangle$$

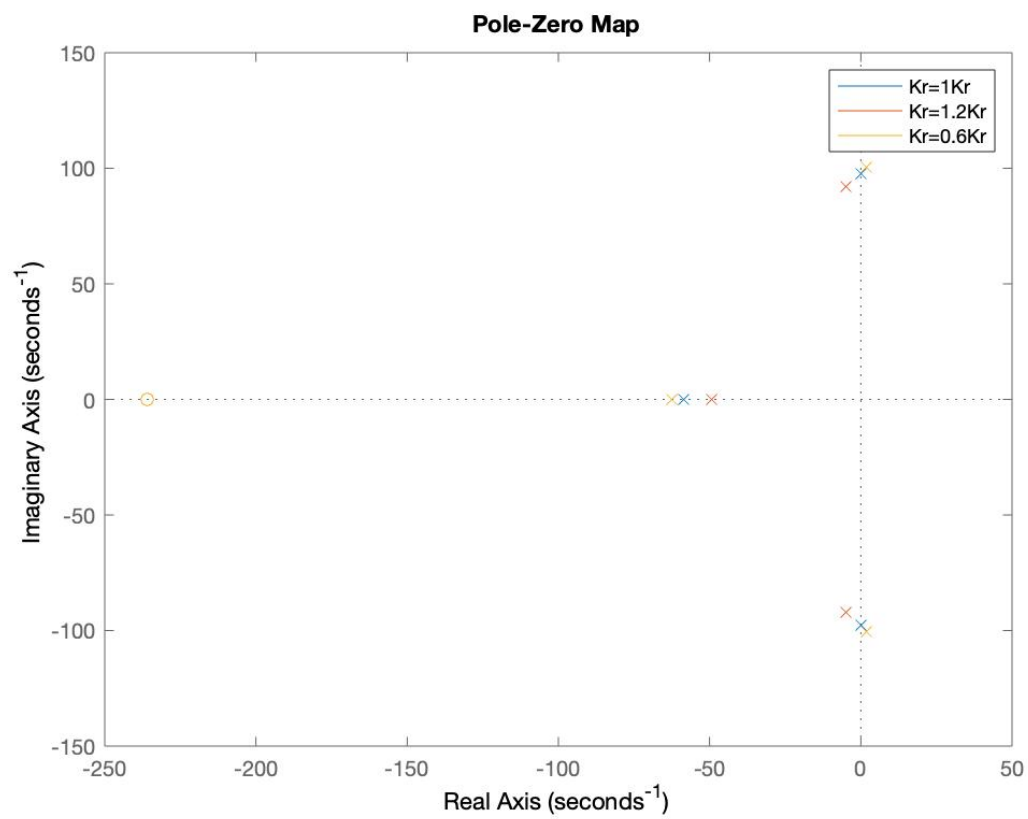
$$u_{\text{min}} = 0,02596$$

III. Rad na vježbi:

Za tri različite vrijednosti pojačanja regulatora  $K_R = 0.6 K_{R,kr}$ ,  $K_R = K_{R,kr}$  i  $K_R = 1.2 K_{R,kr}$  uradite sljedeće:

1. a) Simulacijom odredite odziv regulacijskog kruga na skokovitu promjenu referentne veličine sile napetosti  $F_r$  s  $F_{T0}$  na  $1.1 \cdot F_{T0}$ .
2. b) Naredbama Matlaba nacrtati polove i nule regulacijskog kruga u  $s$ -ravnini.

```
59 %pokusavam nesto
60 %obicniKr
61 - num1 = [0.28907*0.02596 68.17857*0.02596]
62 - den1 = [4.9242*10^-6 2.8907*10^-4 0.0396857+0.02596*0.28907 1+68.1785*0.02596]
63 - fja1 = tf(num, den)
64
65
66 %kr je 0.6Kr
67 - numv = [0.28907*0.015576 68.17857*0.015576]
68 - denv = [4.9242*10^-6 2.8907*10^-4 0.0396857+0.015576*0.28907 1+68.1785*0.015576]
69 - fjav = tf(numv, denv)
70
71
72 %kr je 1.2Kr
73 - numm = [0.28907*0.031152 68.17857*0.031152]
74 - denm = [4.9242*10^-6 2.8907*10^-4 0.0396857+0.031152*0.28907 1+68.1785*0.031152]
75 - fjam = tf(numm, denm)
76
77
78 - pzmap(fja1, fjav, fjam)
79 - legend('Kr=1Kr', 'Kr=1.6Kr', 'Kr=0.2Kr')
80
81
```



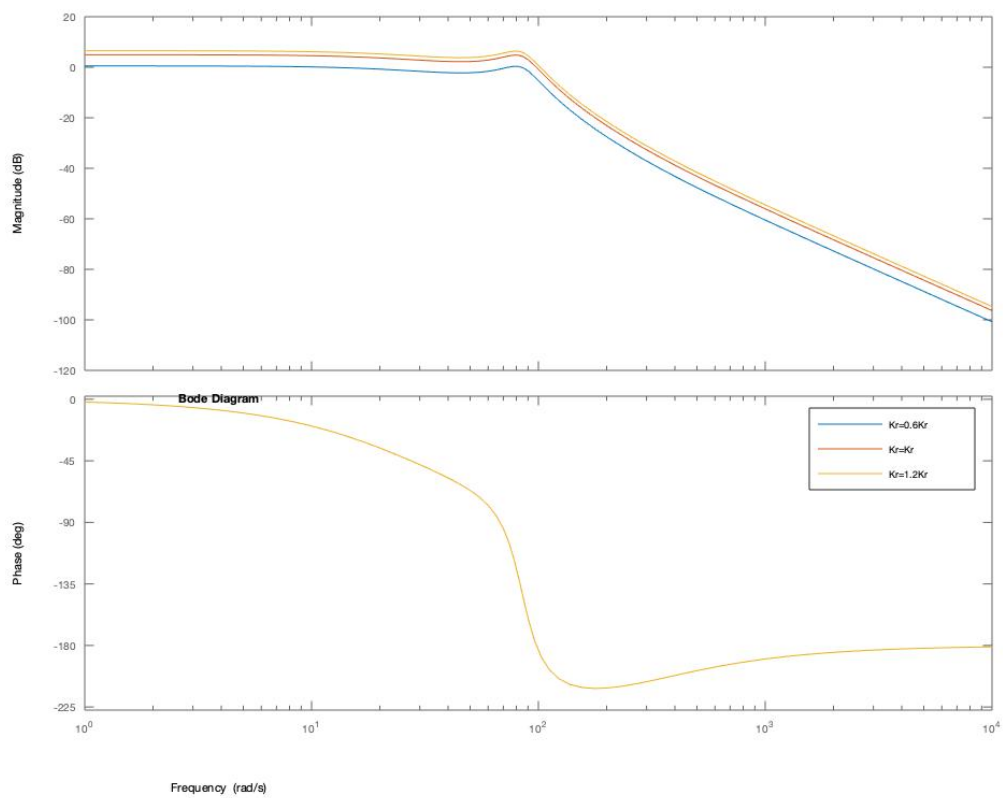
3. c) Naredbama Matlaba nacrtati Bodeov dijagram i odrediti fazno osiguranje, amplitudno osiguranje i presječnu frekvenciju.



```

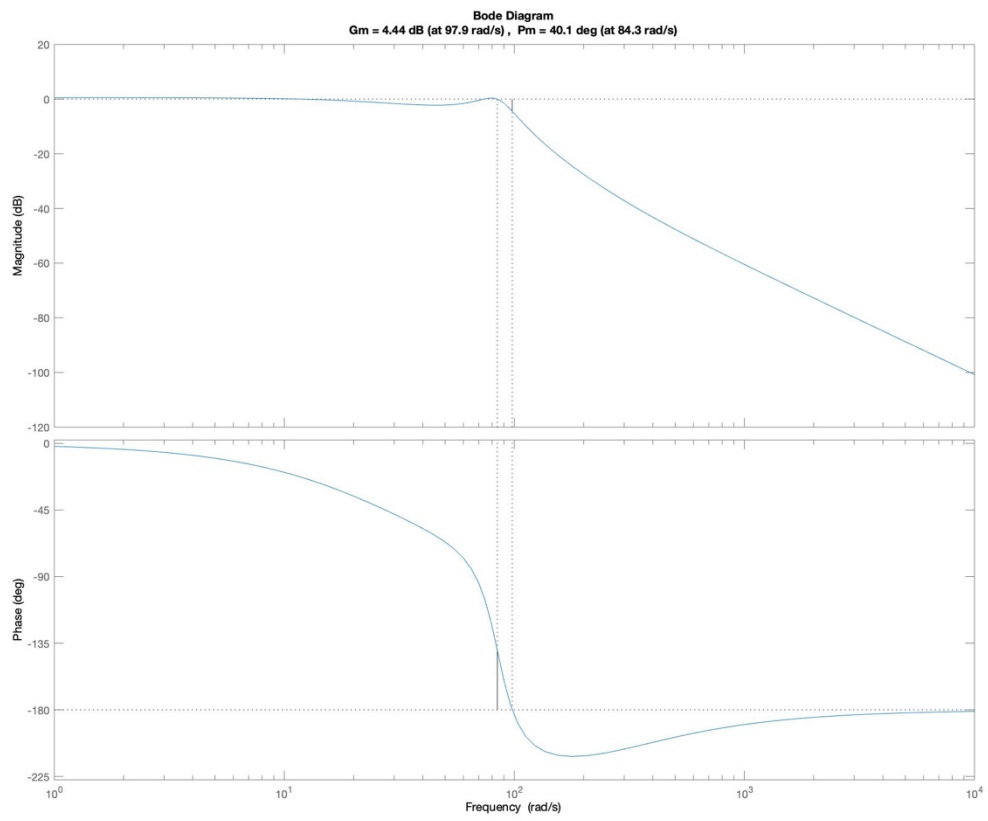
87
88 %pokusaj bodea
89
90 - numb == [0.28907*0.02596 68.17857*0.02596]
91 - denb == [4.9242*10^-6 2.8907*10^-4 0.039685 1]
92
93 - numb12 == [0.28907*0.031152 68.17857*0.031152]
94 - denb12 == [4.9242*10^-6 2.8907*10^-4 0.039685 1]
95
96
97 - numb06 == [0.28907*0.015576 68.17857*0.015576]
98 - denb06 == [4.9242*10^-6 2.8907*10^-4 0.039685 1]
99
100
101
102
103 - funkcijabode == tf(numb, denb)
104 - funkcijabode12 == tf(numb12, denb12)
105 - funkcijabode06 == tf(numb06, denb06)
106
107 - bode(funkcijabode06, funkcijabode, funkcijabode12)
108 - title('funkcijabode bode');
109 - legend('Kr=0.6Kr', 'Kr=Kr', 'Kr=1.2Kr')
110

```



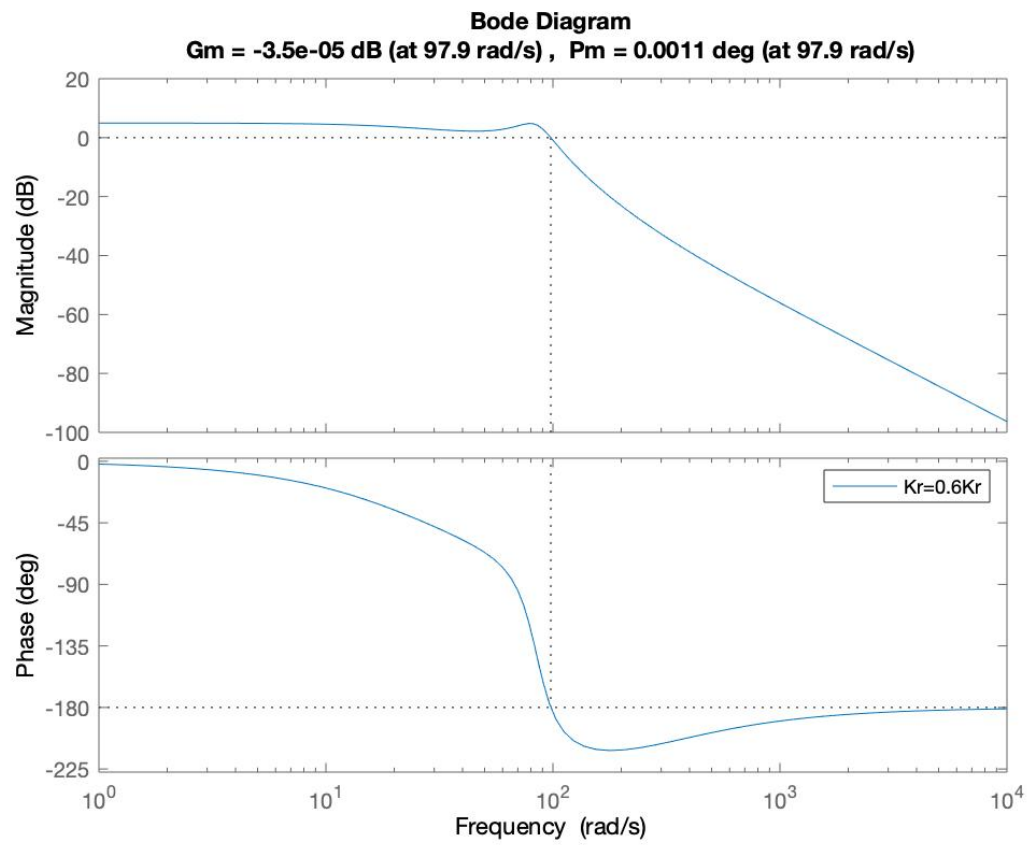
**Za  $Kr = 0.6Kr$**

$A_r=4.44$ (ispod osi)dB  $\omega_n=97.9$ rad/s  $\omega_c=84.3$ rad/s  $\gamma=40.1$ deg



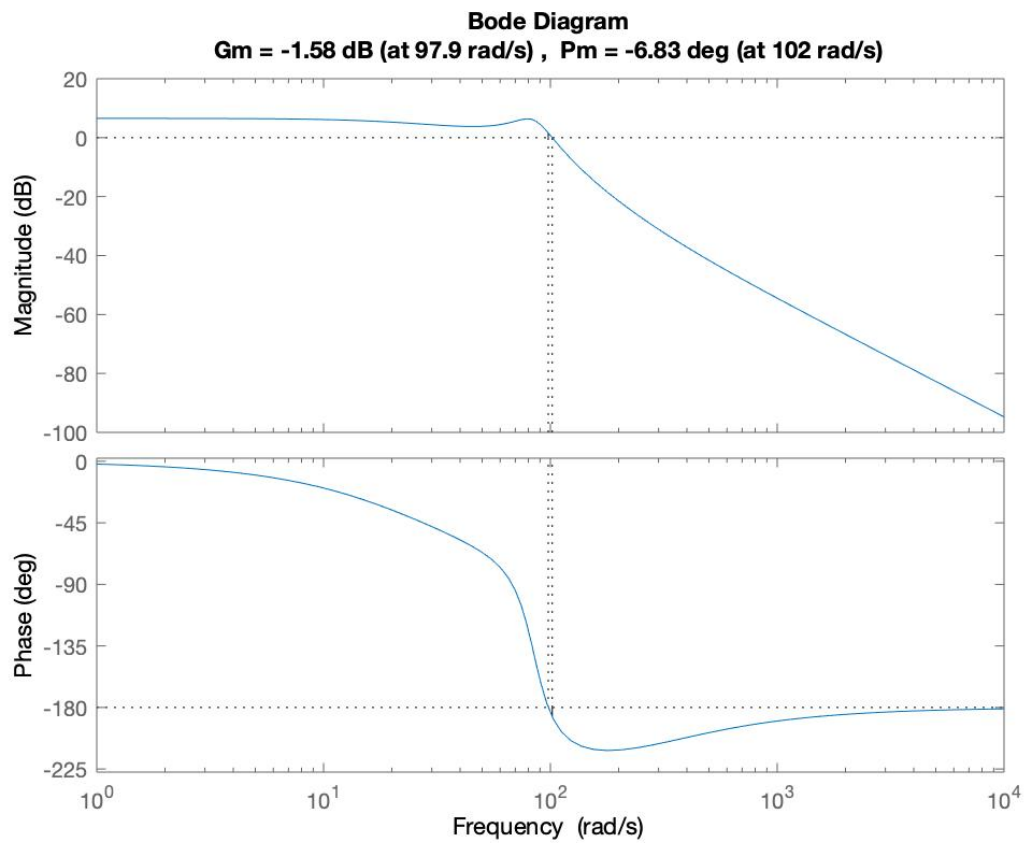
**Za Kr=Kr**

$A_r = -0.000035 \text{ dB}$   $\omega_r = 97.9 \text{ rad/s}$   $\omega_c = 97.9 \text{ rad/s}$   $\gamma = 0.0011 \text{ deg}$



**Za  $Kr=1.2 Kr$**

$A_i = -1.58 \text{ dB}$  (iznad x osi)  $\omega_n = 97.9 \text{ rad/s}$   $\omega_c = 102 \text{ rad/s}$   $\gamma = -6.83 \text{ deg}$



4. d) Naredbama Matlabu nacrtati Nyquistov dijagram. Usporediti dijagrame za zadana pojačanja.

```
denb06 = [4.9242*10^-6 2.8907*10^-4 0.039685 1]
```

```
%
```

```
funkcijabode = tf(numb, denb)
```

```
funkcijabode12 = tf(numb12, denb12)
```

```
funkcijabode06 = tf(numb06, denb06)
```

```
% bode(funkcijabode06, funkcijabode, funkcijabode12);
```

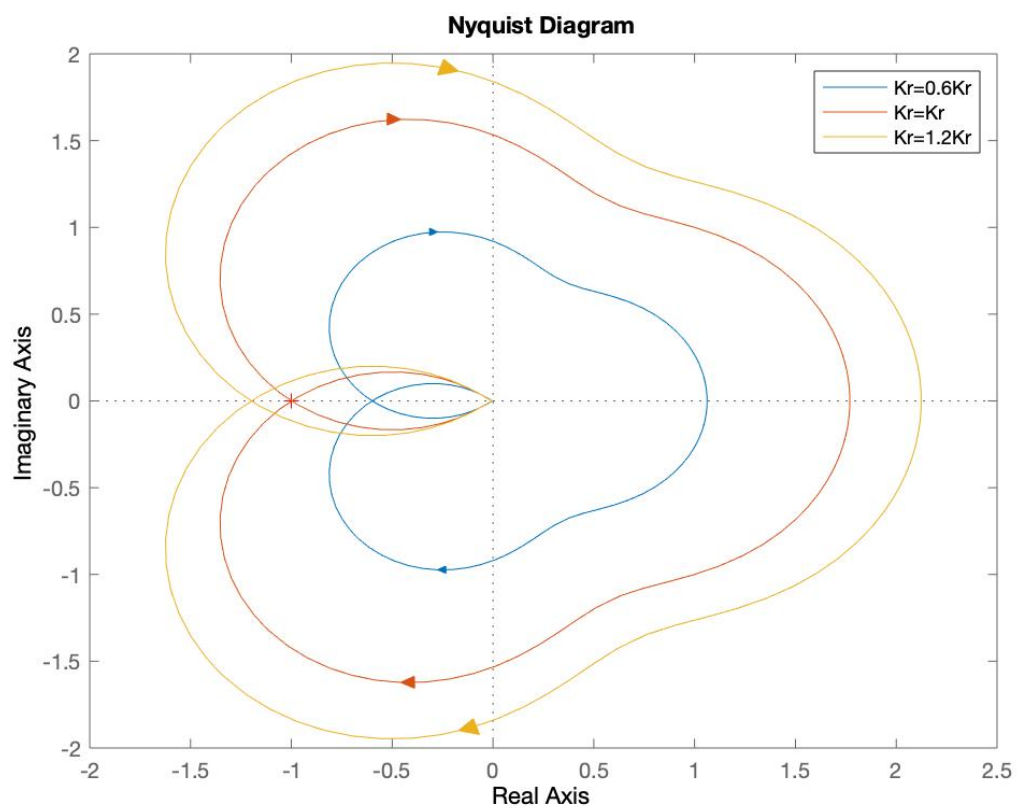
```
% title('funkcijabode bode');
```

```
% legend('Kr=0.6Kr', 'Kr=Kr', 'Kr=1.2Kr');
```

```
nyquist(funkcijabode06, funkcijabode, funkcijabode12)
```

```
legend('Kr=0.6Kr', 'Kr=Kr', 'Kr=1.2Kr')
```

5. `zPol = poles/(Kr)*f(s)`



6.



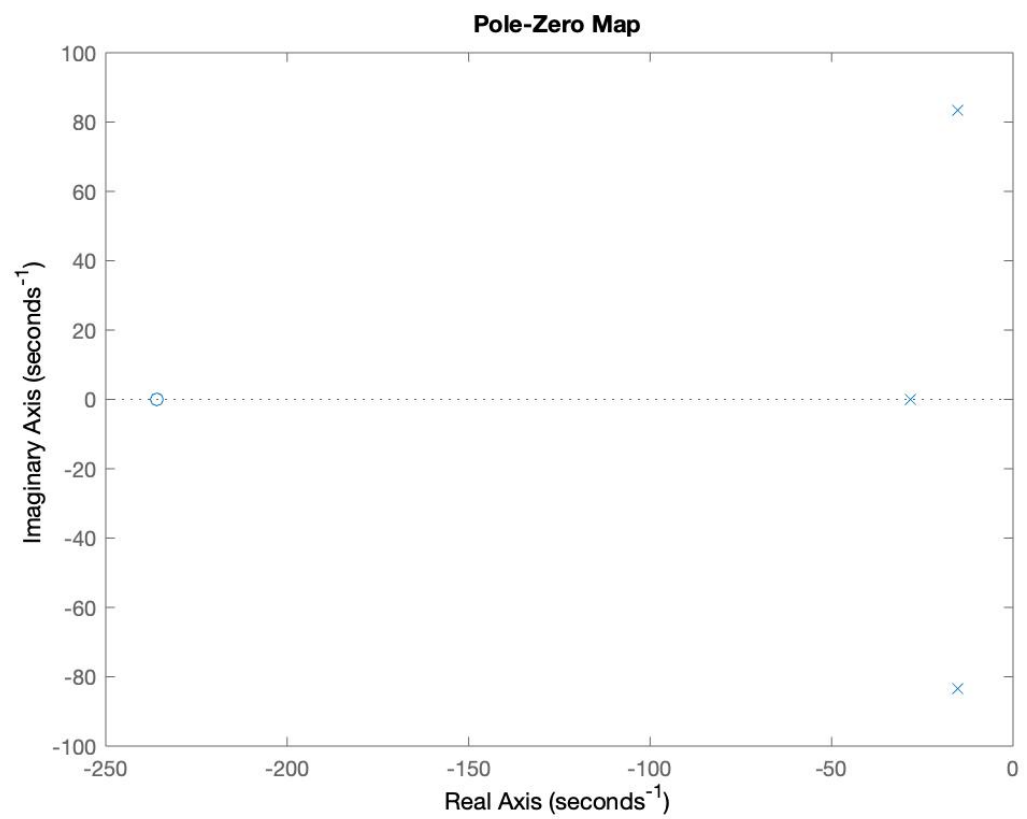
**Neke od naredbi Matlaba korisne za rad na vježbi:**

*margin, bode, nyquist, zoom, pzmap, feedback*

### ***IZVJEŠTAJ***

Odgovorite na sljedeća pitanja.

1. a) Prikažite polove i nule prijenosne funkcije procesa u  $s$ -ravnini.



b) Koliko iznosi najveće pojačanje regulatora za koje je regulacijski krug stabilan, tj. vrijednost [1]  $K_{R,kr}$  dobivena u točki c) pripreme za vježbu? [1]

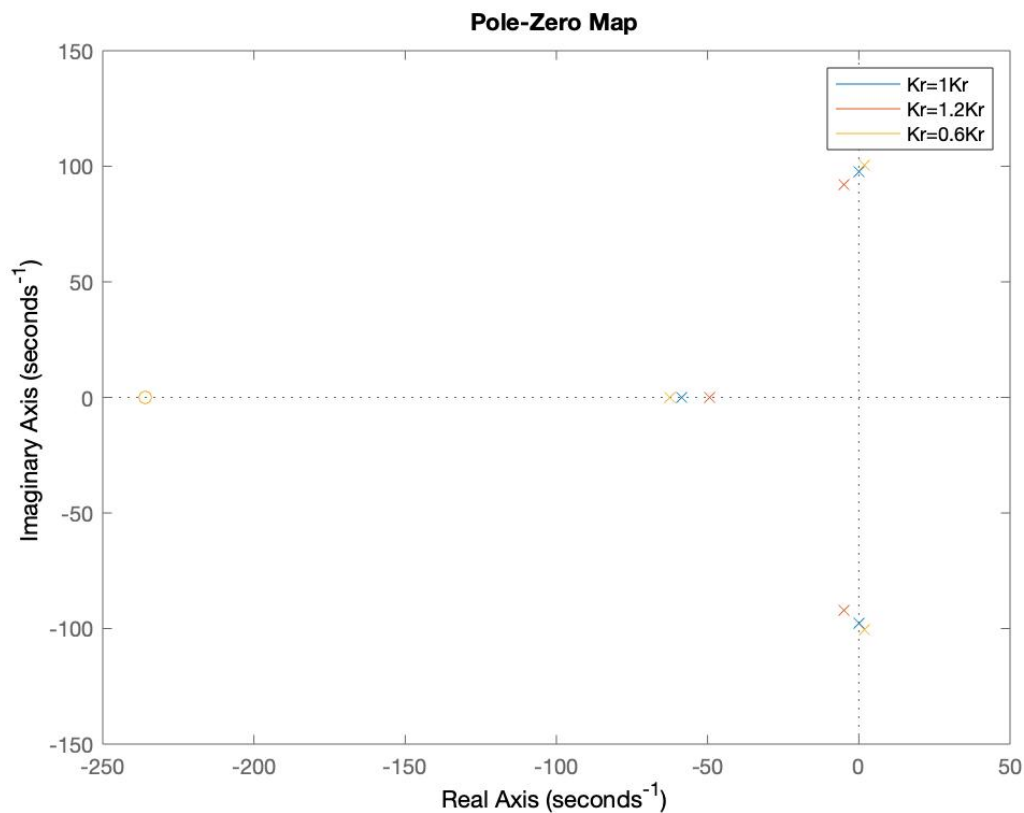
**Odgovor:  $K_r = 0.02596$**

c) Napišite karakteristični polinom prijenosne funkcije zatvorenog kruga u standardnom obliku.

[1]

$$4.9242 \cdot 10^{-6} s^3 + 2.8908 \cdot 10^{-4} s^2 + 0.0396857s + 1 + K_r \cdot 0.28907s + K_r \cdot 68.1785 = 0$$

4. d) Na istom grafu prikažite polove i nule zatvorenog regulacijskog kruga za  $K_R = 0.6 K_{R,kr}$ ,  $K_R = K_{R,kr}$  te  $K_R = 1.2 K_{R,kr}$ . Dodajte legendu [2]



5. e) Odrediti amplitudno osiguranje  $A_r$ , frekvenciju  $\omega_\pi$ , fazno osiguranje  $\gamma$  i presječnu frekvenciju  $\omega_c$  regulacijskog kruga ako se koristi  $P$  regulator:
- $K_R = 0.6 K_{R,kr}$ ; [2]
  - $K_R = K_{R,kr}$ ; [2]
  - $K_R = 1.2 K_{R,kr}$ ; [2]

**Za  $K_r = 0.6K_r$**

$$A_i = 4.44 (\text{ispod osi}) \text{ dB} \quad \omega_n = 97.9 \text{ rad/s} \quad \omega_c = 84.3 \text{ rad/s} \quad \gamma = 40.1 \text{ deg}$$

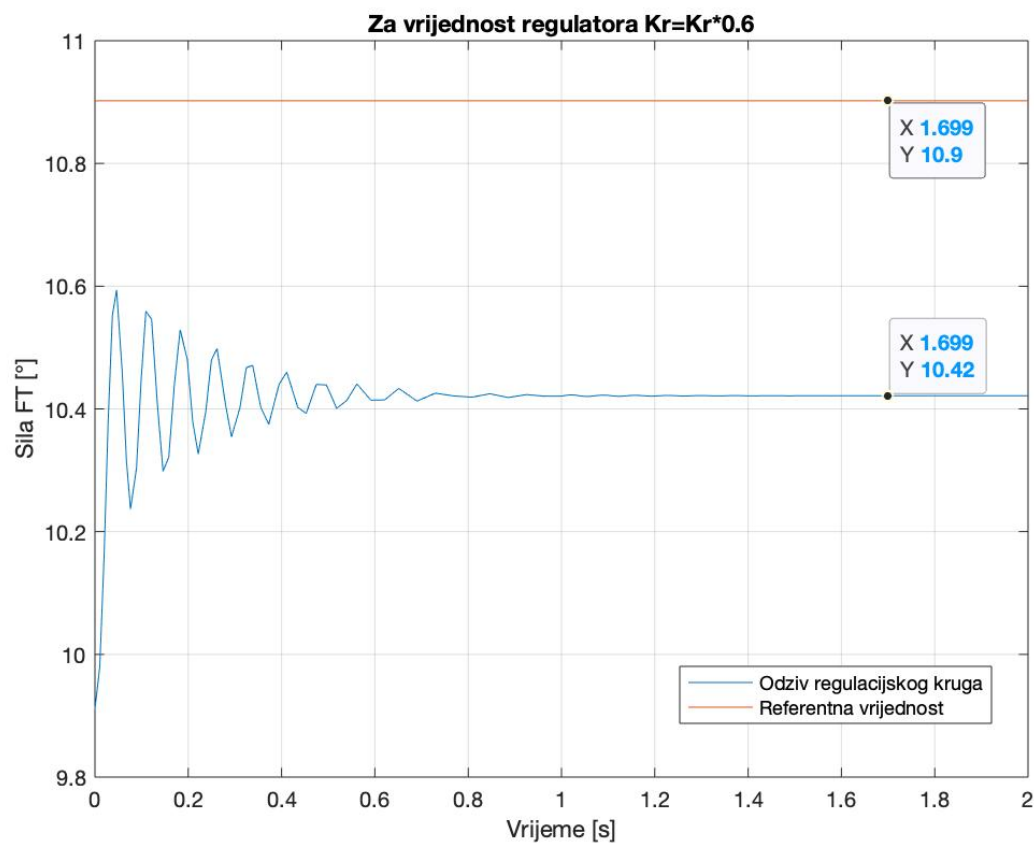
$$\mathbf{Za \quad Kr = Kr}$$

$$A_i = -0.000035 \text{ dB} \quad \omega_n = 97.9 \text{ rad/s} \quad \omega_c = 97.9 \text{ rad/s} \quad \gamma = 0.0011 \text{ deg}$$

$$\mathbf{Za \quad Kr = 1.2 \quad Kr}$$

$$A_i = -1.58 \text{ dB} \quad (\text{iznad x osi}) \quad \omega_n = 97.9 \text{ rad/s} \quad \omega_c = 102 \text{ rad/s} \quad \gamma = -6.83 \text{ deg}$$

6. f) Za vrijednosti pojačanja regulatora  $K_R = 0.6 K_{R,kr}$  i skokovitu promjenu referentne veličine sile napetosti  $F_r$  s  $F_{T0}$  na  $1.1 \cdot F_{T0}$ ,
- i. prikažite odziv regulacijskog kruga. [1]



- ii. koliko iznosi pogreška u stacionarnom stanju  $\varepsilon_\infty$ ? [1]  
 7.  $\varepsilon_\infty = 0.48V$  referenca – izlaz sustava sve kroz referencu puta 100%

- i. koliko iznosi maksimalno nadvišenje  $\sigma_m$ ? [1]

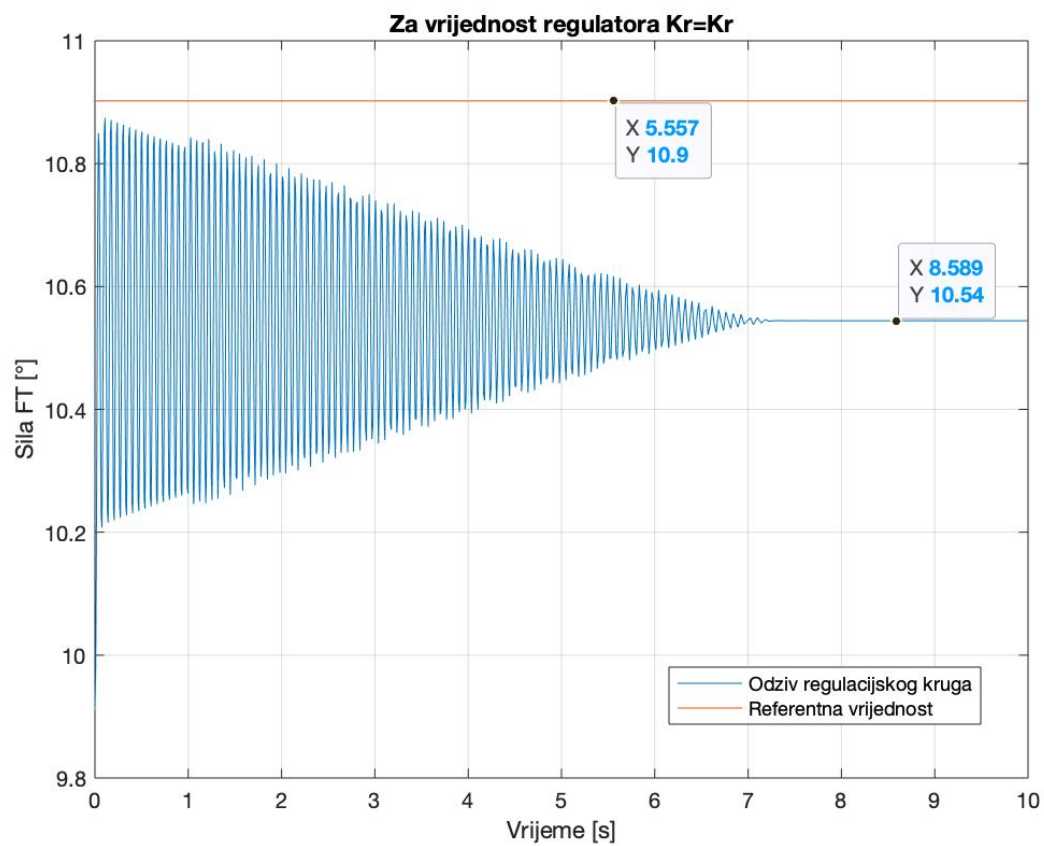
$(y_{\max} - y_s) / (y_s - y_{\min})$  sve puta 100%

$y_{\max} = 10.59, y_s = 10.42 \dots y_{\min} = 10.23$

**10.42 do 10.59**

8. g) Za vrijednosti pojačanja regulatora  $K_R = K_{R,kr}$  i skokovitu promjenu referentne veličine sile napetosti  $F_r$  s  $F_{T0}$  na  $1.1 \cdot F_{T0}$ ,

- i. prikažite odziv regulacijskog kruga. [1]

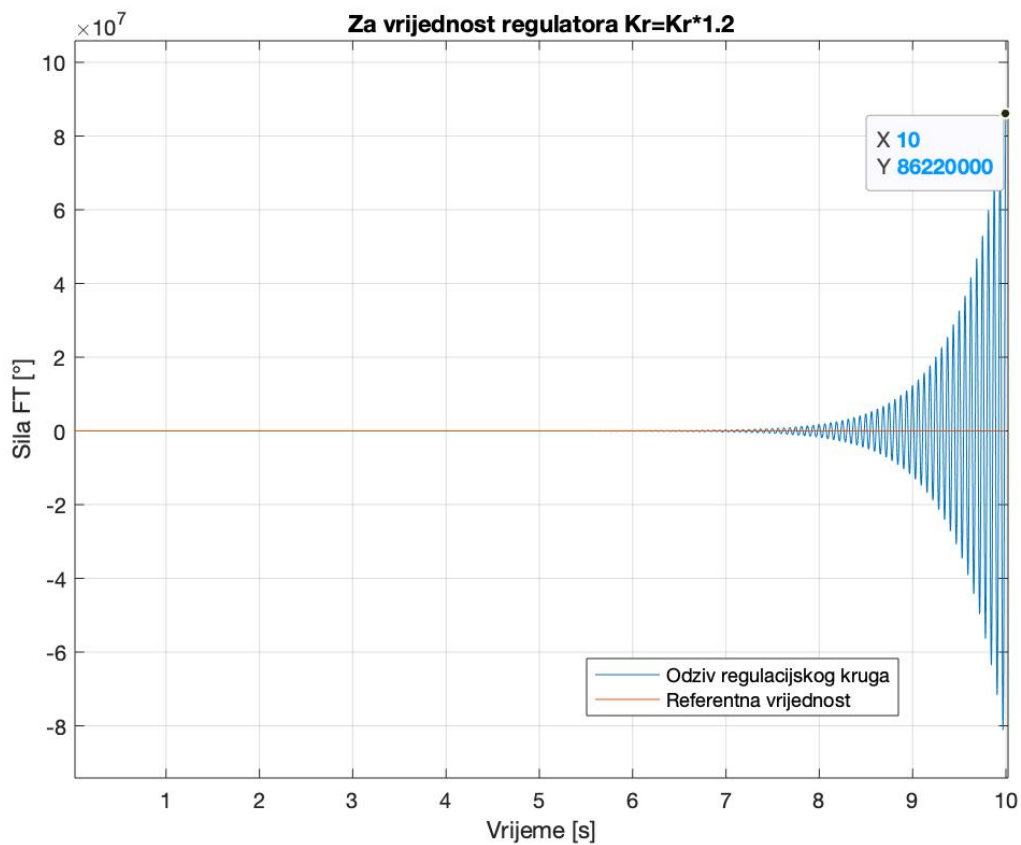


- ii. koliko iznosi pogreška u stacionarnom stanju  $\varepsilon_\infty$ ? [1]

$$\varepsilon_\infty = 0.36V$$



9. h) Za vrijednosti pojačanja regulatora  $K_R = 1.2 K_{R,kr}$  i skokovitu promjenu referentne veličine sile napetosti  $F_r$  s  $F_{T0}$  na  $1.1 \cdot F_{T0}$ ,  
 i. prikazite odziv regulacijskog kruga. [1]



- ii. koliko iznosi pogreška u stacionarnom stanju  $\varepsilon_\infty$ ?

$$\varepsilon_\infty = 8.622e+07$$