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Interferometry

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1. Motivation

In this experiment we aim at determining the refraction index of air and glass by using the principles of interferometry. A Sagnac interferometer is used to achieve effects of interference.

2. Theory

When two wavefronts meet, interference phenomena can occur under certain conditions. Interference means that the waves add up according to the superposition principle. This can result in intensity maxima and minima. In the following, the physics behind interference and the connection to other physical properties like the refraction index is examined based on the example of the Sagnac interferometer.

2.1. Coherence

Two waves can interfere with other when they are coherent, meaning a constant phase relation is given. It is differentiated between temporal and spacial coherence. For the temporal coherence, the phase relation stays the same for an infinite time. Spacial coherence describes the constant phase relation regarding the spacial direction of propagation. In reality, there will be hardly any waves that are perfectly coherent. Nevertheless, a coherence length can be identified as the distance between waves under which the waves are sufficiently coherent. The degree of coherence γ_{12} is given by

$$\gamma_{12}(\tau) = \frac{\langle E_1(t + \tau)E_2^*(t) \rangle}{\sqrt{\langle |E_1|^2 \rangle \langle |E_2|^2 \rangle}}. \text{CHECK FORMULA}$$

It becomes clear that the lower $|\gamma_{12}|$ the less the light is coherent with $0 \leq |\gamma_{12}| \leq 1$.

2.2. Polarization

Another important property of light is its polarization. The polarization of a light beam describes the direction in which the electric or magnetic field oscillates. Normal sunlight is unpolarized and thus has no distinguished oscillation direction of the electric or magnetic field. There are several ways to polarise light beams, for example polarization filters that only let light pass that is linearly polarized under a certain angle.

2.3. Sagnac Interferometer

3. Experimental setup and measurement process

4. Analysis

4.1. Dependence of the contrast on the polarisation angle

At first the dependence of the contrast on the polarisation angle ϕ is analysed. The measurements listed in Table 1 show the minimum and maximum intensity of the lasers interference for different polarisation angles ϕ .

Table 1: Measurements for the polarisation angle dependence of the contrast K .

$\phi / ^\circ$	$I_{\min 1} / \text{V}$	$I_{\max 1} / \text{V}$	$I_{\min 2} / \text{V}$	$I_{\max 2} / \text{V}$	$I_{\min 3} / \text{V}$	$I_{\max 3} / \text{V}$
0	1.60	1.75	1.57	1.77	1.63	1.78
15	0.97	1.57	0.94	1.49	0.95	1.54
30	0.51	1.28	0.52	1.27	0.53	1.30
45	0.39	1.31	0.40	1.34	0.40	1.36
60	0.53	1.74	0.54	1.78	0.53	1.76
75	0.96	2.23	0.97	2.13	0.98	2.21
90	1.87	2.05	1.97	2.41	2.01	2.24
105	1.81	3.10	1.78	3.22	1.84	3.53
120	1.31	4.30	1.35	4.23	1.41	4.47
135	1.15	5.06	1.23	4.78	1.21	5.05
150	1.39	4.44	1.44	4.32	1.47	4.54
165	1.65	3.16	1.69	3.19	1.73	3.33
180	1.66	1.87	1.64	1.82	1.80	2.01

In order to compute the contrast K , **?? EQREF HERE** is applied for each measurement series. After that, the average values and the standard deviations of the three measurements are calculated. The corresponding datapoints are shown in Figure 1. The theory law of the angle dependence is given by **?? EQREF HERE**. Here, a function of the form

$$K = 2K_0 \cdot |\sin(\phi - \delta)\cos(\phi - \delta)|$$

is fitted to the data points. The offset δ is used to compensate for deviations in the experimental setup. The fitparameters follow as

$$K_0 = 0.57 \pm 0.01 \qquad \delta = (3.23 \pm 0.58)^\circ$$

using the *python* extension *scipy* [2]. The resulting fit function is also displayed in Figure 1. For the following measurements the polarisation angle is set to 45° .

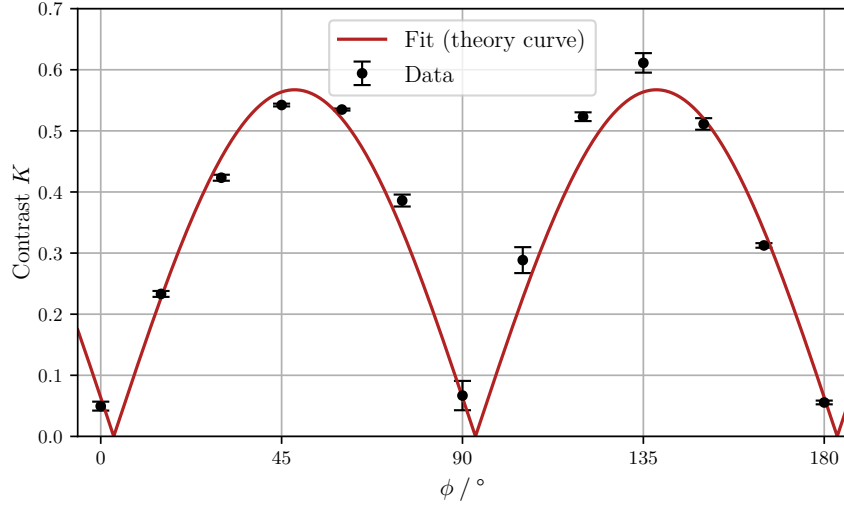


Figure 1: Averaged measurements of the contrast K against the polarisation angle ϕ and fit using *scipy* [2].

4.2. refractive index of glass

For the determination of the refractive index of glass the double glass holder is placed in the two beams. The two glass panes are already tilted by an angle $\Theta_0 = \pm 10^\circ$. Using ?? **EQREF HERE** the number of maxima passing the center of the interference spectrum is given by

$$M = \frac{\Delta\phi_+ + \Delta\phi_-}{2\pi}$$

where $\Delta\phi_{\pm}$ is the phase shift induced by the glass panes tilted by $\pm 10^\circ$. This expression can be simplified to

$$M = \frac{2T}{\lambda} \cdot \frac{n-1}{n} \cdot \Theta_0 \theta \quad (1)$$

where $\lambda = 632.99 \text{ nm}$ is the wavelength of the laser and $T = 1 \text{ mm}$ is the thickness of the glass panes. The number of measured maxima is again averaged over the ten measurement series. The values are shown in Table 2. The experimental value of the

Table 2: Measurements of the maxima M passing the center of the interference spectrum and tilt angle θ .

θ	M_1	M_2	M_3	M_4	M_5	M_6	M_7	M_8	M_9	M_{10}	\overline{M}
2	6	6	6	6	5	6	6	6	7	6	6.00 ± 0.45
4	12	13	12	13	12	12	12	12	13	12	12.30 ± 0.46
6	19	20	19	20	18	19	18	20	20	19	19.20 ± 0.75
8	25	26	25	26	24	25	25	26	26	25	25.30 ± 0.64

refractive index of glass follows from a linear fit of Equation 1 to the datapoints. The datapoints and the fit are shown in Figure 2. The resulting value is $n_{\text{glass}} = 1.484 \pm 0.008$.

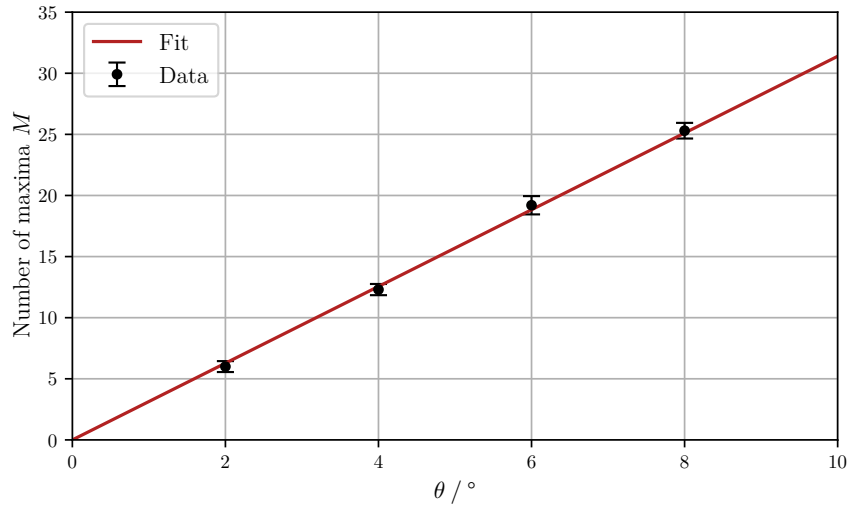


Figure 2: Averaged measurements of the number of maxima \overline{M} against the tilt angle θ and fit using *scipy* [2].

4.3. refractive index of air

To determine the refractive index of air, the measurements listed in Table 3 are used. Again the average over the five measurement series is calculated. Using **EQREF HERE** and the length $L = (100.0 \pm 0.1)$ mm of the air chamber the corresponding refractive indices of air can be calculated at each pressure value. The resulting refractive indices are also listed in Table 3 and are shown against the pressure in Figure 3. From these values, the refractive index of air at standard atmosphere ($T = 15^\circ\text{C}$, $p = 1013$ hPa) can be obtained. The Lorentz-Lorenz law (??) can be approximated for $n \approx 1$ as

$$n = \frac{3}{2} \frac{Ap}{RT} + 1.$$

Using this approach, the experimentally determined values of the refractive index in Figure 3 are fitted with a linear function

$$n(p, T = T_0) = \frac{3}{2} \frac{p}{RT_0} \cdot a + b$$

where a and b are the free parameters of the fit and $T_0 = 22.2^\circ\text{C} = 295.35$ K is the measured room temperature. The fit parameters determined using *scipy* [2] follow as

$$a = (4.38 \pm 0.02) \times 10^{-4} \quad b = 1 + (3 \pm 66) \times 10^{-8}.$$

The experimental value of the refractive index of air at standard atmosphere then reads $n_{\text{exp}} = 1 + (27.05 \pm 0.13) \times 10^{-5}$.

Table 3: Measurements of the maxima M passing the center of the interference spectrum and pressure p in the air chamber. The refractive indices are displayed for the averaged value for each pressure.

p / mbar	M_1	M_2	M_3	M_4	M_5	$(\bar{n} - 1) / 10^{-5}$
8	0	0	0	0	0	0
50	2	2	2	2	2	1.27
100	4	4	4	4	4	2.53
150	6	6	6	7	6	3.92 ± 0.25
200	8	9	9	9	9	5.57 ± 0.25
250	10	11	11	11	11	6.84 ± 0.25
300	13	13	13	13	13	8.23 ± 0.01
350	15	15	15	15	15	9.49 ± 0.01
400	17	17	17	17	17	10.76 ± 0.01
450	19	19	19	19	19	12.03 ± 0.01
500	21	21	21	21	21	13.29 ± 0.01
550	23	23	23	23	23	14.56 ± 0.01
600	25	25	25	25	25	15.82 ± 0.02
650	27	28	28	27	27	17.34 ± 0.31
700	29	30	30	30	30	18.86 ± 0.25
750	32	32	32	32	32	20.26 ± 0.02
800	34	34	34	34	34	21.52 ± 0.02
850	36	36	36	36	36	22.79 ± 0.02
900	38	38	38	38	38	24.05 ± 0.02
950	40	40	40	40	40	25.32 ± 0.03
981	41	41	41	41	41	25.95 ± 0.03

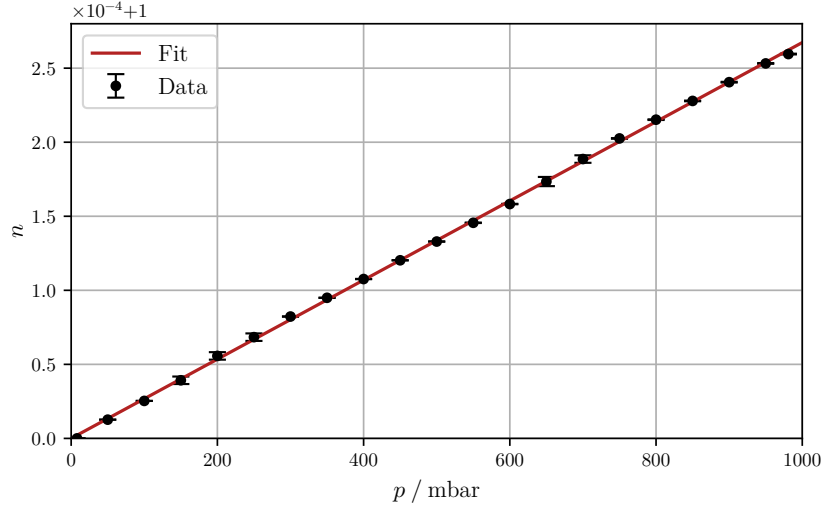


Figure 3: Calculated refractive index of air against measured pressure and linear fit using *scipy* [2].

5. Discussion

The dependence of the contrast on the polarisation angle showed good agreement between the expected theory curve and the observed data. An angle offset of $\delta = (3.23 \pm 0.58)^\circ$ was observed compared to the theory which could possibly be explained by a constant offset on the scale of the polariser or other deviations in the experimental setup. The maximum contrast reaches a value of $K_0 = 0.57 \pm 0.01$ where the ideal contrast would be $K = 1$. This could hint to a suboptimal alignment.

The refractive index of glass was determined to be $n_{\text{glass, exp}} = 1.484 \pm 0.008$. In the literature the value is given by $n_{\text{glass, theory}} \approx 1.515$ [1], but many different glass types exist with different refractive indices. The relative deviation of the experimental value is $\Delta_{\text{rel}}(n_{\text{glass}}) = 2\%$. Considering the general experimental uncertainties and the fact, that the exact composition of the glass panes used in the experiment is unknown, the refractive index of glass was determined with a sufficient precision.

Lastly, the refractive index of air at standard atmosphere (15°C , 1013 hPa) was determined as $n_{\text{air, exp}} = 1.000\,270\,5 \pm 0.000\,001\,3$. The literature value is $n_{\text{air, theory}} = 1.00027653$ [1] which implies a deviation of $\Delta_{\text{rel}}(n_{\text{air}}) < 0.001\%$. The small deviation could e.g. be caused by humidity in the air which was neglected for the theory value. Therefore, the refractive index of air was determined precisely. All in all the refractive indices were determined successfully, but a more careful alignment of the Sagnac-interferometer could lead to a higher contrast which may increase precision.

References

- [1] Mikhail Polyanskiy. *Refractive Index Database*. URL: <https://refractiveindex.info/?shelf=glass&book=BK7&page=SCHOTT> (visited on 15/11/2023).
- [2] Pauli Virtanen et al. ‘SciPy 1.0: Fundamental Algorithms for Scientific Computing in Python’. In: *Nature Methods* 17 (2020), pp. 261–272. DOI: 10.1038/s41592-019-0686-2.

A. Anhang

A.1. Originaldaten

