

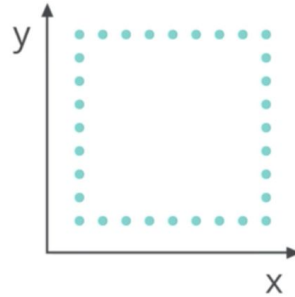
An exploration and implementation of implementing the **Hough Transform** to Identify Straight Lines

Hough transform is a robust tool for **detecting straight lines** in images, making it essential for computer vision tasks involving structure recognition. They involve the steps seen:

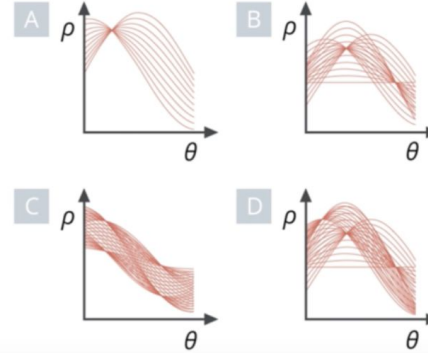
- 1) Load the input image
- 2) Initialize the accumulator array for Hough Transform parameters.
- 3) For each pixel :
 - if white: skip.
 - if black:
 - for each θ :
 - $\rho = x \cdot \cos(\theta) + y \cdot \sin(\theta)$.
 - normalise ρ to image space.
 - update the Hough matrix at (θ, ρ) .
- 4) Identifying the maxima of the Hough Transform (isolate spots, enlarge spots, locate centroid of the spots)
- 5) Draw straight lines in the original image

What will this image look like in Hough Space? Choose the correct plot.

Image Space



Hough Space



Click to write the which

☐ A)

☐ B)

☒ C)

☐ D)

☐ E) I dont' know

What is a common issue faced when using the Hough Transform for shape detection in images?

- ☐ A) Overfitting to specific shapes
- ☒ B) High computational cost compared to edge detection
- ☐ C) Inability to detect colors to comparison to black and white
- ☐ D) Loss of image quality during the transform processing
- ☐ E) I don't know

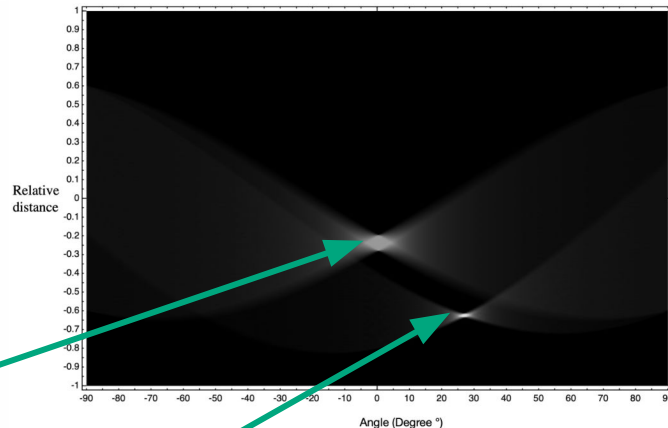
What happens when you increase the r_dim and $theta_dim$ in the Hough space matrix?

- ☐ A) The computational time decreases but the accuracy increases.
- ☒ B) The computational time increases and the resolution of detected lines improves.
- ☐ C) The image size increases proportionally.
- ☐ D) It decreases the sensitivity to lines in the original image.
- ☐ E) I don't know

Creating the hough transform matrix step by step

1. We start by creating a numpy array of arbitrary dimensions.

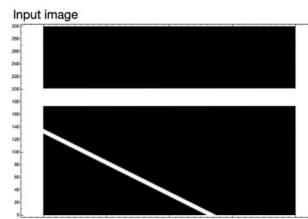
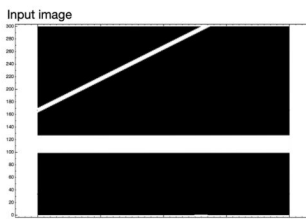
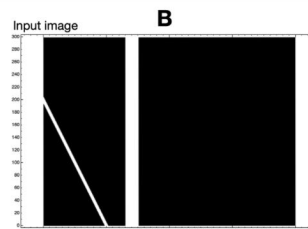
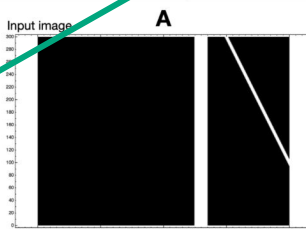
```
# We choose to have a final matrix of the following  
# dimensions. This is an arbitrary decision  
  
r_dim = 200  
theta_dim = 300
```



The larger gray spot corresponds to a thicker vertical line, with a relative distance 0.2 of the half image from the center, in a vertical direction.

The bright, small spot at $\varphi = 28^\circ$ corresponds to a thin bright line perpendicular to the projection line at $\varphi = 28^\circ$, i.e. with an angle of 62° , with a relative distance of 0.6 from the center of the image.


Which one corresponds to the sketch?



C

D

Why was it necessary to shift and scale the computed ρ ($=r$) values before indexing into the Hough accumulator array (with $\theta \in [0, \pi)$) ?

- ☐ A) To normalize by image size for scale invariance.
- ☐ B) To increase the numerical accuracy of the accumulator.
-  ☒ C) To map ρ into non-negative values for the array indices
- ☐ D) To convert ρ to $[0,1]$
- ☐ E) I don't know

$$[r = x \cdot \cos(\theta) + y \cdot \sin(\theta)]$$

1. Scaling ρ to the Hough Space Index:

- The computed r value from the equation $r = x \cdot \cos(\theta) + y \cdot \sin(\theta)$ can range from $-r_{\max}$ to r_{\max} .
- However, array indices must be non-negative integers.
- To map r to a valid index (`ir`) in the Hough space array (`hough_space`), we scale and shift r accordingly.

Suppose you are using a Hough transform to do line fitting, but we notice that **our system is detecting 2 lines** where **there is actually 1** line in the image. Which of the following is most likely to alleviate this problem?



☒ A) Increase the size of the bins in the Hough transform .

☐ B) Decrease the size of the bins in the Hough transform.

☐ C) Sharpen the image.

☐ D) Make the image larger (e.g., through interpolation).

☐ E) I don't know