

The way `partial-tree` works is that it will divide the given $n - 1$ in two (`left-size`), and then it makes a recursive call to form a balanced tree for the left branch (`left-result`). The root node will be the first leftover element of the recursive left branch call (`this-entry`). The right branch recursive call will be the remaining half (`right-size`) of $n - 1$. The rest of the leftovers from the first recursive call (`left-result`), are the elements for the second one (`right-result`). Whatever is left over from that second call will be the list elements not included in the tree (`remaining-elts`). The car of the result will be the balanced binary tree with a root node of `this-entry` and left and right branches taken as the car of the recursive calls.

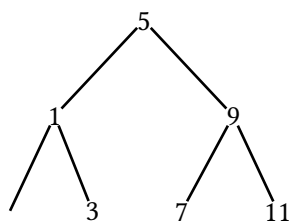
For the list (1 3 5 7 9 11), `list->tree` will form the below tree. The first call to `partial-tree` is (`partial-tree` '(1 3 5 7 9 11) 6).

The left recursive call will be (`partial-tree` '(1 3 5 7 9 11) 2). This itself spawns a `left-result` of `(() (1 3 5 7 9 11))` because `left-size` is 0. The entry node will be 1 and the right branch will be the recursive call (`partial-tree` '(3 5 7 9 11) 1). This itself yields a `left-result` of `(() (3 5 7 9 11))`, an entry of 3, and a `right-result` of `(() (5 7 9 11))`. The remaining elements are thus (5 7 9 11). The entire left recursive call referenced at the beginning of this paragraph thus yields `((1 () (3 () ())) 5 7 9 11)`.

The root node will be thus be 5, the car of `non-left-elts` which are (5 7 9 11).

The right recursive call will thus be (`partial-tree` '(7 9 11) 3). The `left-result` will be the result of the recursive call (`partial-tree` '(7 9 11) 1) which itself has a `left-result` of `(() (7 9 11))`, entry node of 7, and `right-result` of `(() (9 11))`. Therefore, the entry node of the previous recursive call will be 9, and its `right-result` will be the recursive call (`partial-tree` '(11) 1). This itself has a `left-result` of `(() (11))`, an entry node of 11, and a `right-result` of `(() ())`. Therefore, there are no remaining elements and the entire right branch (first recursive call mentioned in this paragraph) will yield the pair `((9 (7 () ()) (11 () ())) ())`.

Thus the original call to `partial-tree` will return the pair `((5 (1 () (3 () ())) (9 (7 () ()) (11 () ())) ())) ())`, and `list->tree` will return the tree (5 (1 () (3 () ())) (9 (7 () ()) (11 () ()))), which is visualized below.



The order of growth in the number of steps required by `list->tree` to convert a list of n elements is $\Theta(n)$ because each node is traversed only once. Either a node is a leaf and its further recursive `partial-tree` calls immediately return the remaining elements, or it will spawn one or two recursive calls depending on how whether it has a left or right branch or both. This results in the number of meaningful (to our analysis) `partial-tree` calls being equal to n . Doubling the size of n might require only one more `partial-tree` call to be kept track of (when thinking of space), but still there will be twice as many `partial-tree` calls made, as there is one for each n .