

```
((double (double double)) inc) 5)
```

This will apply `inc` $2^4 = 16$ times to 5, yielding 21. This is because `double` is applied **four successive** times, since the outer `double` will have an outer pair of doubles, and an inner pair, which will happen again, resulting in 4 nested doubles.

This is **different** to a procedure with three initial nested doubles:

```
((double (double (double inc)))) 5)
```

 which would instead produce $5 + 2^3 = 13$.

Here is how applying `double` to `(double double)` yields four nested double calls instead of the three above.

```
((double (double double)) inc) 5)  
(((double double) ((double double) x)) inc) 5)  
(((double (double *x*)) ((double (double x)) x)) inc) 5)
```

Now substitute the highlighted `x`.

```
(((double (double ((double (double x)) x))) inc) 5))
```

We now have four nested doubles, so the innermost `double` will produce 2 `inc` calls. The next `double` will turn that into 4, since it will do the procedure that is its argument (which in this case is a procedure to do `inc` twice) twice. The next `double` will thus yield 8 `inc` calls, and the final one will apply 16 `inc` calls, thus resulting in $5 + 16 = 21$.

We can generalize this to say that each outer `double` from this point will result in a doubling of the number of nested doubles. This is because the outermost `double` will result in `(# of prev doubles (# of prev doubles x))`, which doubles the number of doubles. Due to the nature of `double` all the `doubles` will eventually be nested, with all the `doubles` inside that initial nested parenthesis being nested within the outer `doubles`, and both groups themselves splitting into an outer and inner group however many times necessary to get to the final nesting where each successive `double` call is nested.

Thus, if we added another outer `double` to the original problem, then those four nested `doubles` would become 8 nested `doubles`. This means that

```
((double (double (double double))) inc) 5)
```

will return $5 + 2^8 = 261$ because the outer `double` will apply the inner `double` (which itself is 4 `doubles`) twice, resulting in 8 nested `double` calls.

We would then predict

```
((double (double (double (double double))))) inc) 5)
```

to have 16 nested `doubles` and return $5 + 2^{16} = 65541$ which it does.