

The benefit of calling square during expmod is that every time that exp is even, you prevent a duplication of steps. This is because each $(\text{expmod base } (/ \text{ exp } 2) \text{ m})$ needs to only be evaluated once, and then the final value, which will just be a primitive number, can be squared. The result is a logarithmic procedure that requires an additional step (division in the even? case) as the input size doubles. Louis Reasoner's implementation would instead result in tree recursion every time that exp is even, duplicating the amount of work at each step. The more times exp is even, the more times that the remaining work will be duplicated, and thus the total number of steps will grow in proportion to the input size.

Specifically, what was before $\Theta(\log n)$ has been transformed into $\Theta(2^{\log_2 n})$, because the equivalent expmod calls in the even? case will result in two identical branches at each even? level, and the number of those levels is how many times n will be divided by 2 ($\log_2 n$). $\Theta(2^{\log_2 n})$ is equivalent to $\Theta(n)$ and thus a $\Theta(\log n)$ process has been transformed into a $\Theta(n)$ process.