

$$\begin{aligned} g_0 &= \alpha \omega_0 \\ g_1 &= \omega_0^2 \\ \omega_0 &= \frac{4\alpha}{1+\alpha^2} * noise\_bandwidth \end{aligned}$$

$$H(z) = g_0 + g_1 * \frac{T}{2} * (\frac{1+z^{-1}}{1-z^{-1}}) = \frac{g_0 + g_1 * \frac{T}{2} + (-g_0 + g_1 * \frac{T}{2})z^{-1}}{1-z^{-1}}$$

Because z-transfer function can always be represented as the ratio of two polynomials in z, we can write for  $1^{st}$  order filter:

$$H(z) = \frac{b_0 + b_1 z^{-1}}{1 + a_1 z^{-1}}$$

This give us following coefficients:

$$b_0 = g_0 + g_1 * \frac{T}{2}$$

$$b_1 = -g_0 + g_1 * \frac{T}{2}$$

$$a_1 = -1$$