

# Bayesian statistics approach to interferometry

*RESOLVE meets ALMA*

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# Observational astrophysics 101



Image credit: NASA, ESA, CSA, and STScI

# Observational astrophysics 101

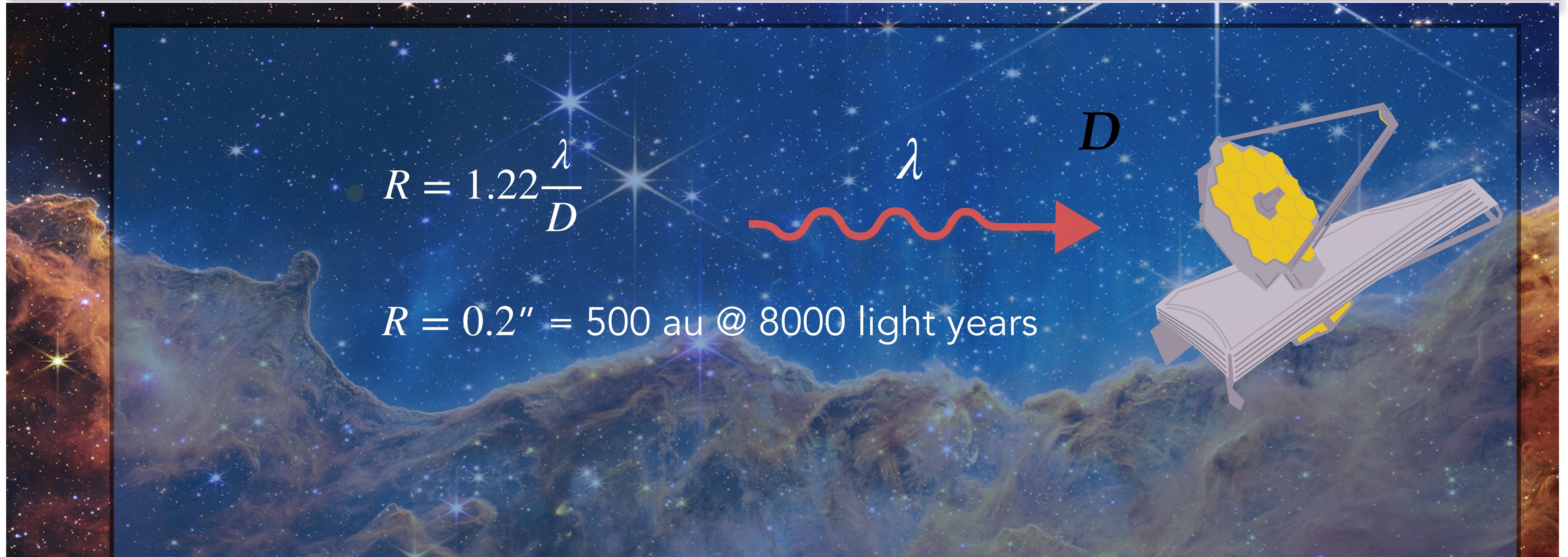


Image credit: NASA, ESA, CSA, and STScI

# Longer wavelengths: peering into the cooler universe



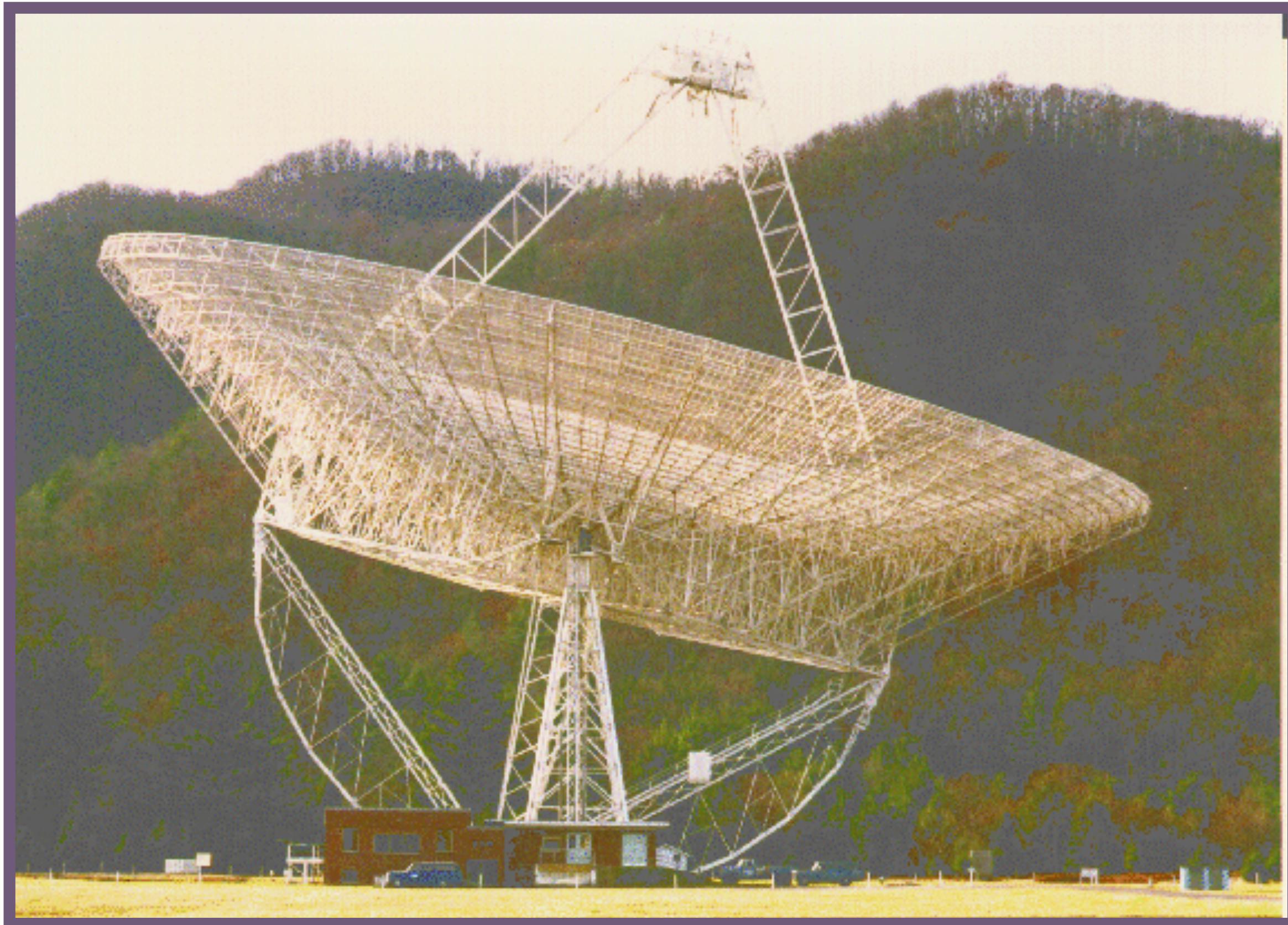
Image credit: NASA, ESA, CSA, and STScI

# Longer wavelengths: peering into the cooler universe



# For longer wavelengths we need bigger telescopes...

Old Green Bank Telescope (90 m)



$$R = 1.22 \frac{\lambda}{D}$$

$$R = 30'' = 80\,000 \text{ au} @ 8000 \text{ light years}$$

Image credit: Richard Porcas/NRAO

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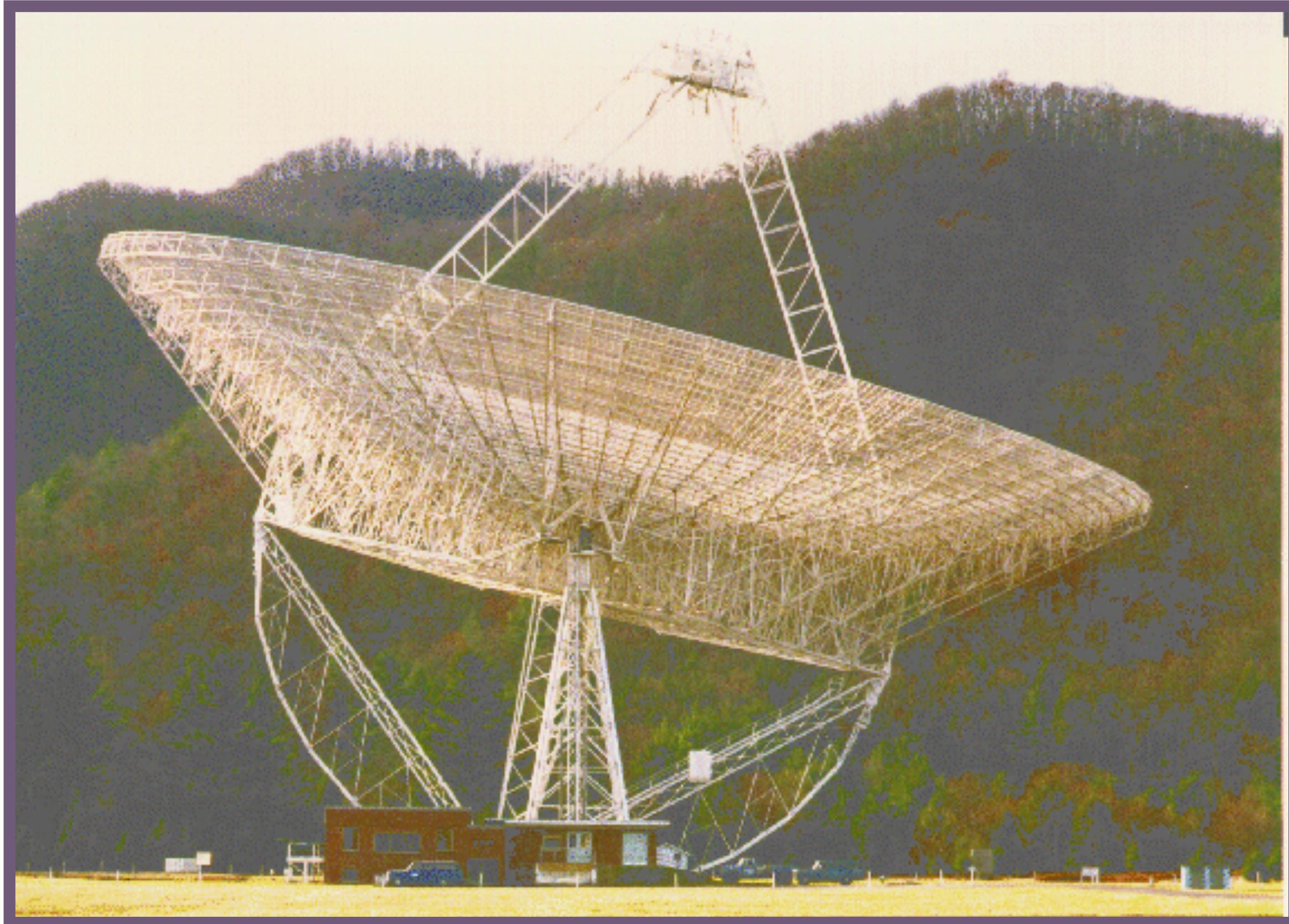
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Image credit: Richard Porcas/NRAO

# ...and building big telescopes is hard!

Old Green Bank Telescope (0 m)



Image credit: Richard Porcas/NRAO

# ...and building big telescopes is hard!

Old Green Bank Telescope (0 m)



Image credit: Richard Porcas/NRAO

Very Large Array (25 m)

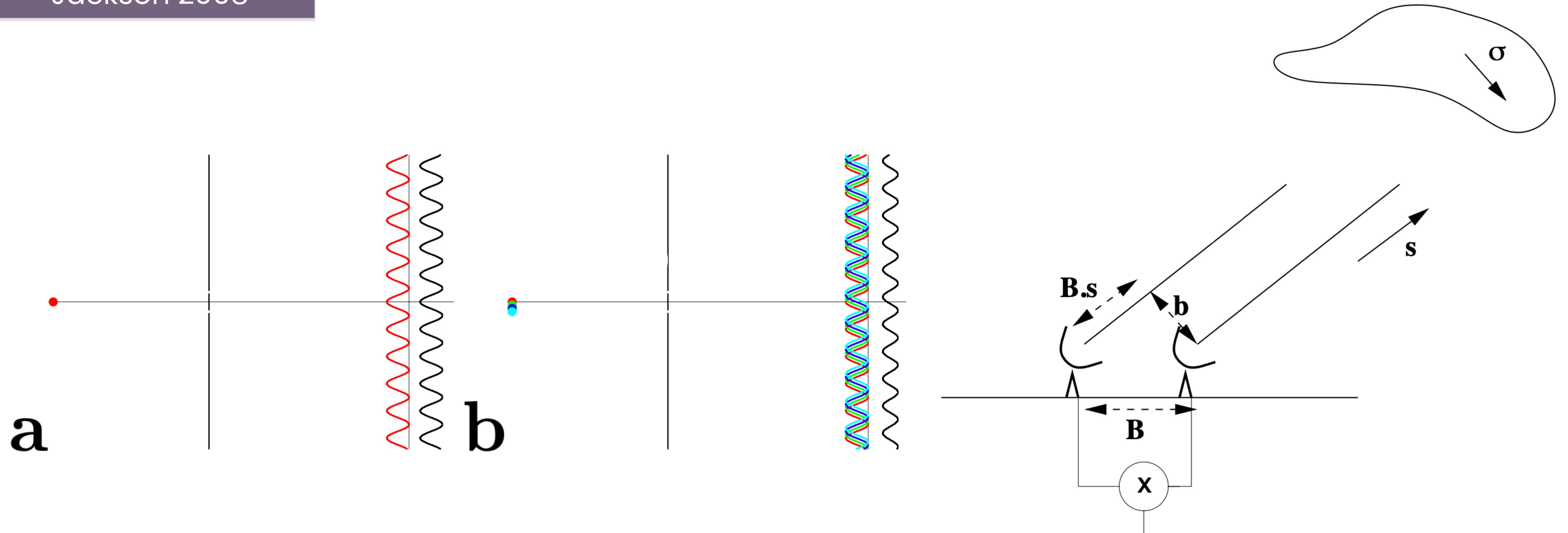


Image credit: NRAO

We can use many small telescopes as one big array!

# Young experiment - principle of interferometry

Jackson 2008



Interferometry - using wave properties of light to overcome technical limitations

# Atacama Large Millimeter/submillimeter Array (ALMA)

5000 m.a.s.l at Atacama Plateau - one of the driest places on Earth

66 antennas (12 and 7 metres diameter)

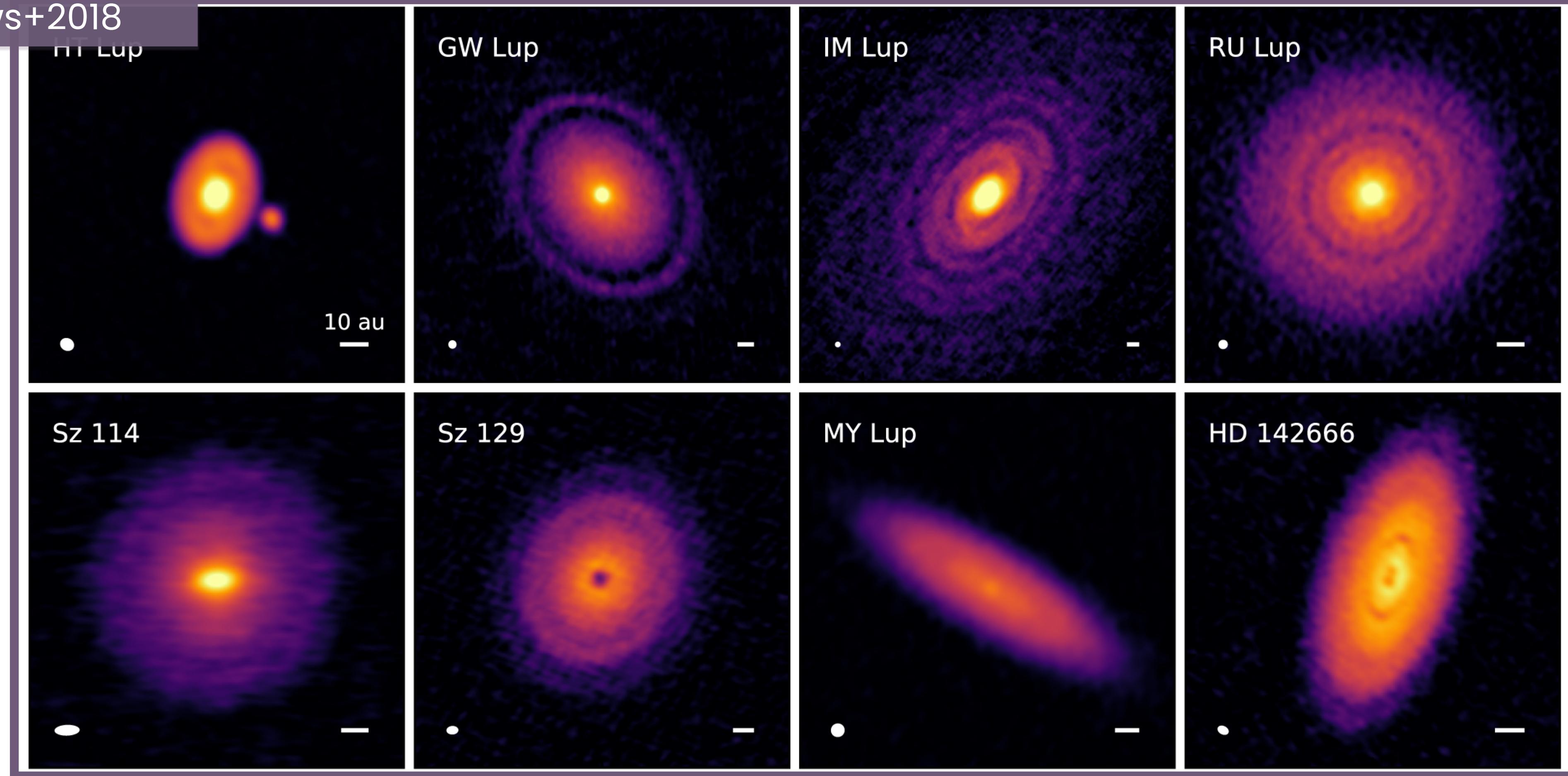
Configurations from 160 m to 16 km max. baseline



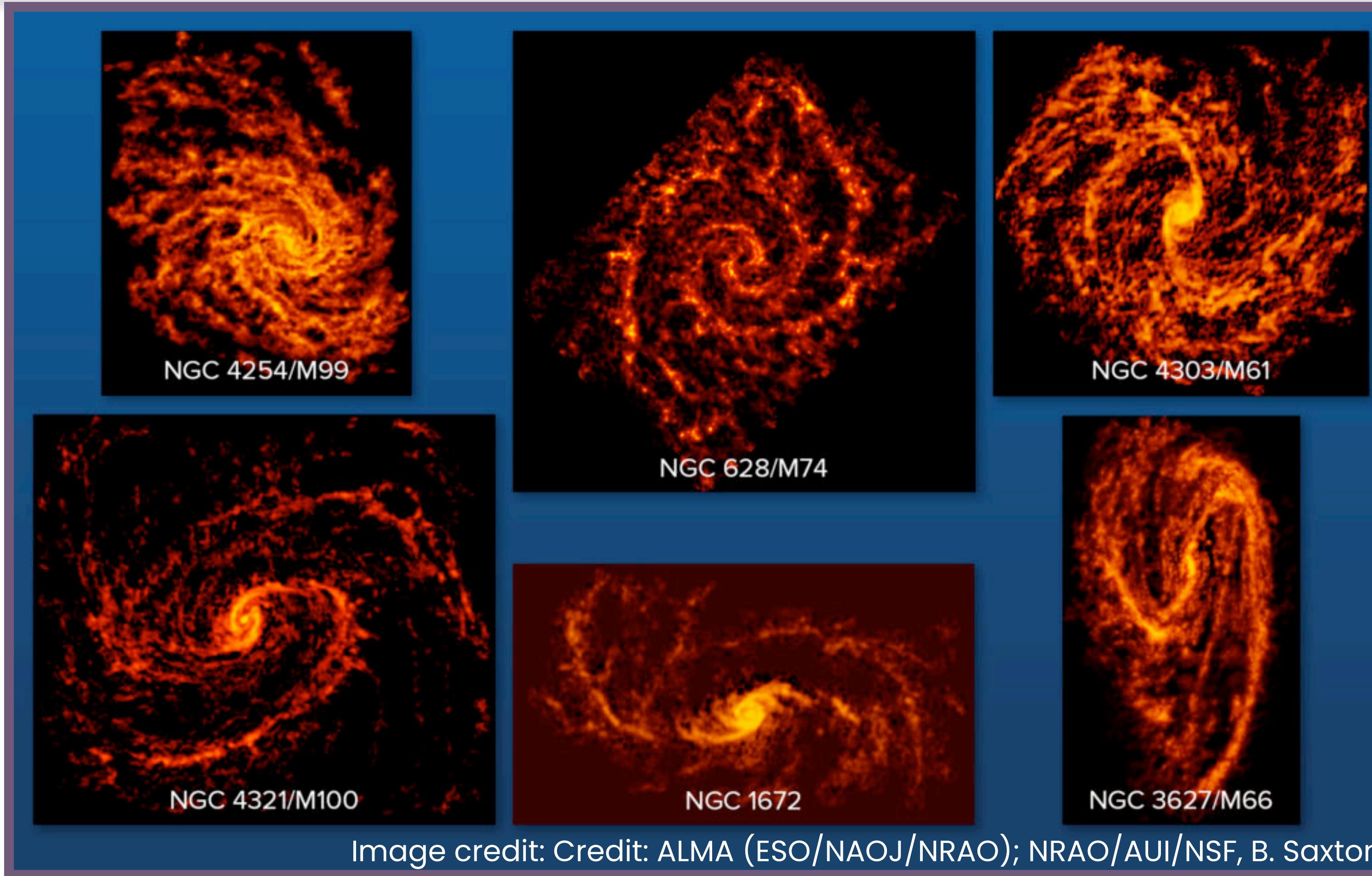
Image credit: ALMA

# Revolution of interferometry – ALMA

Andrews+2018



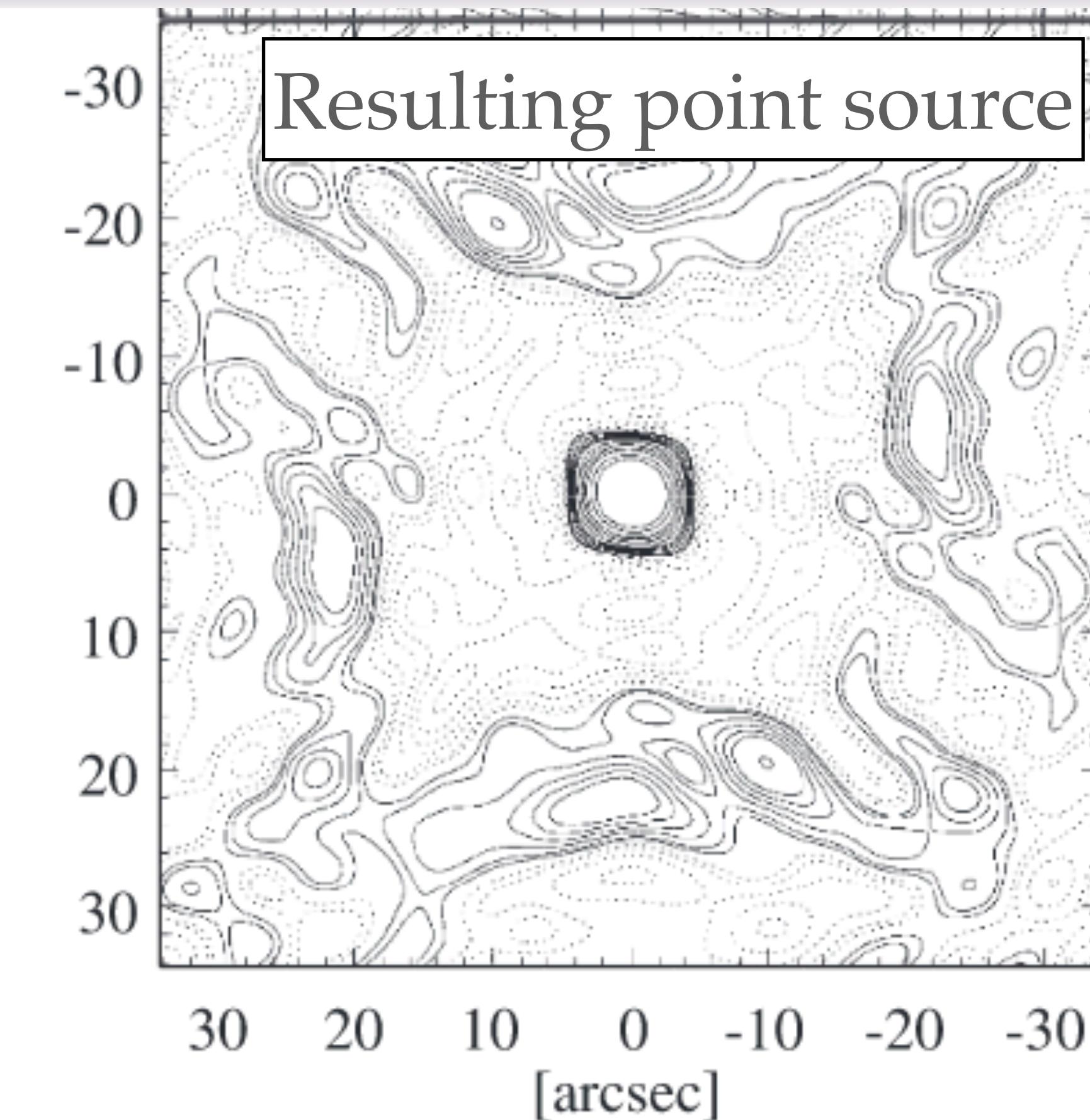
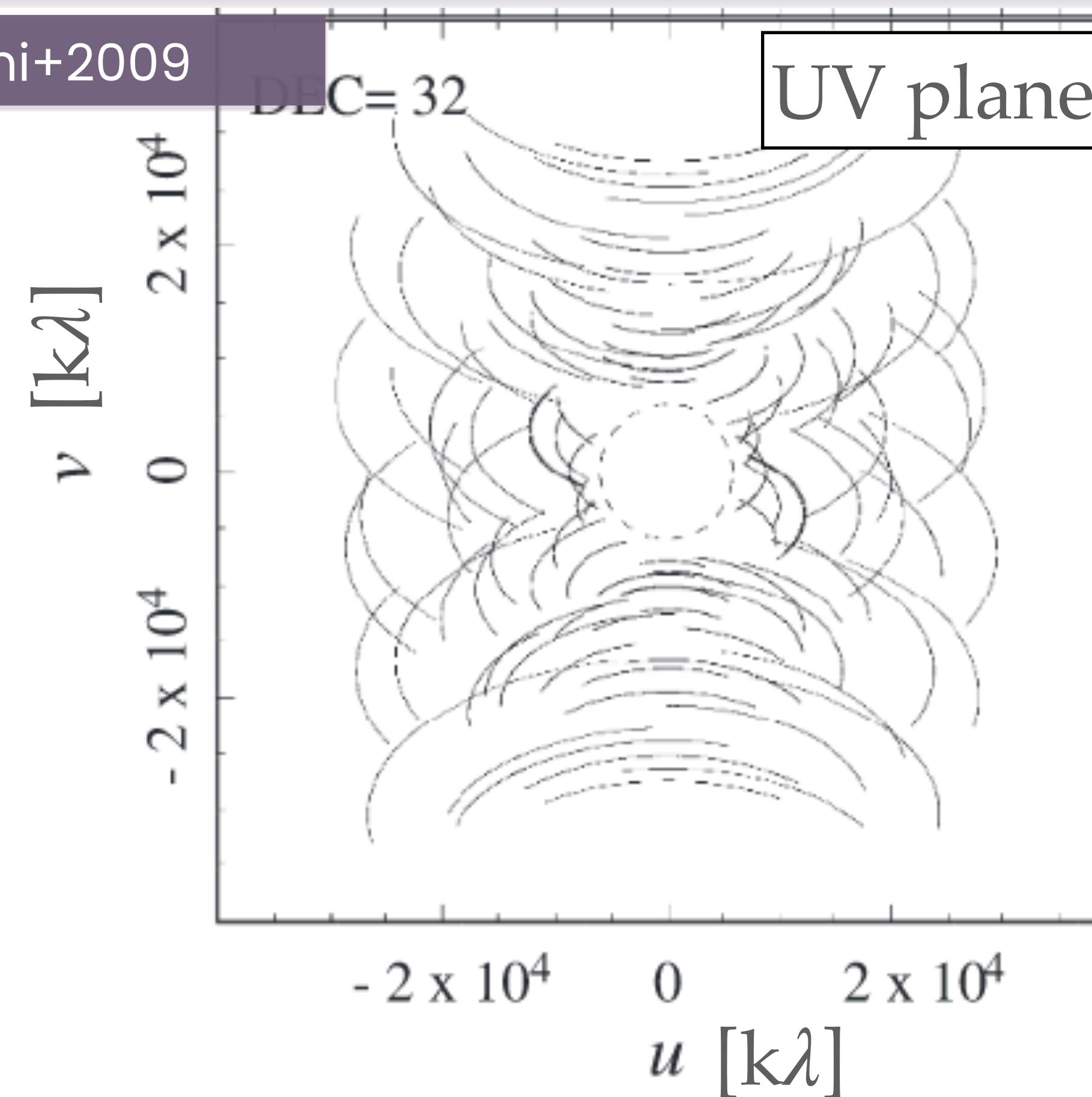
# Revolution of interferometry – ALMA



ALMA delivered stunning images at various cosmic scales

# Missing information problem in interferometry

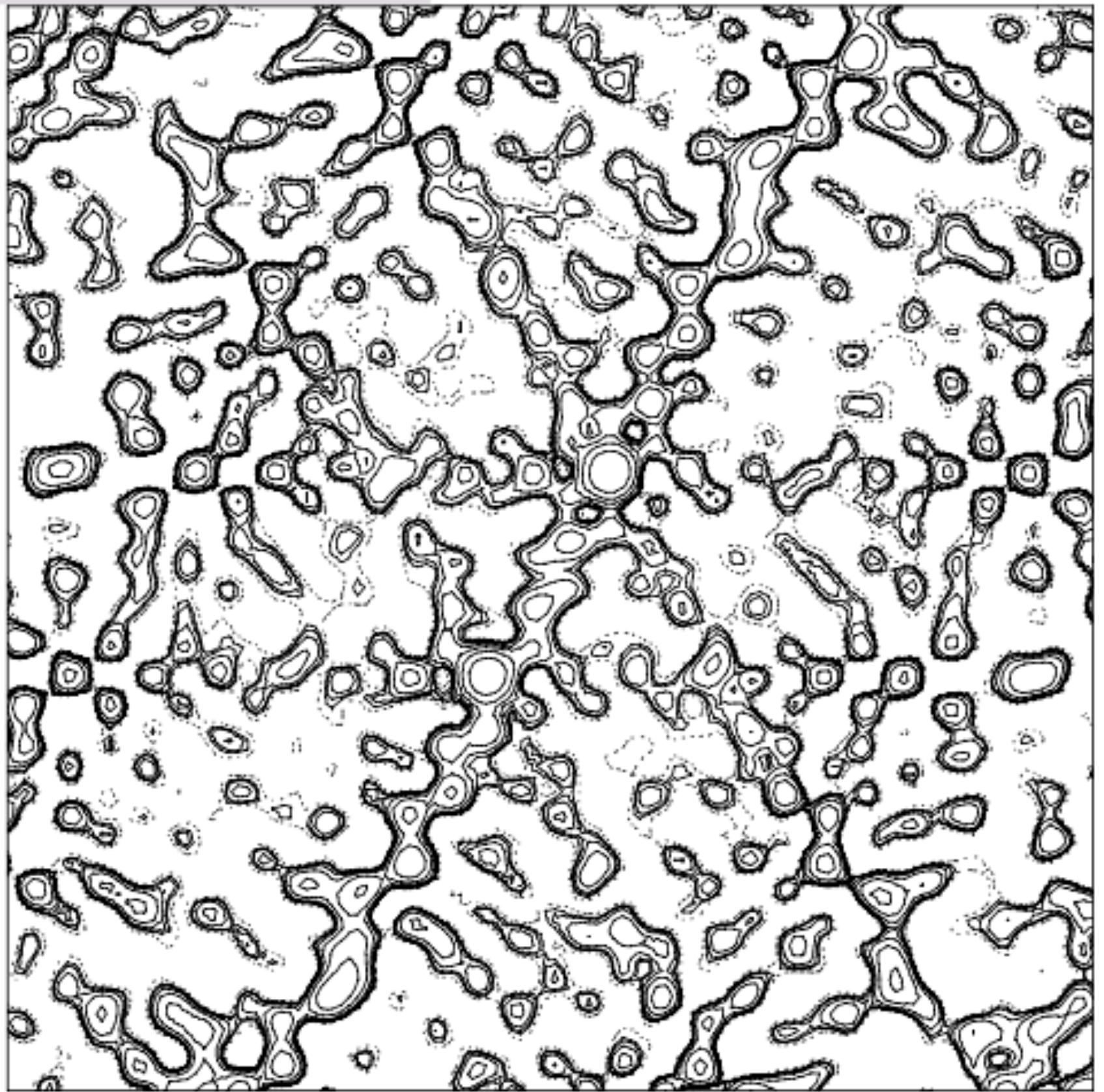
Iguchi+2009



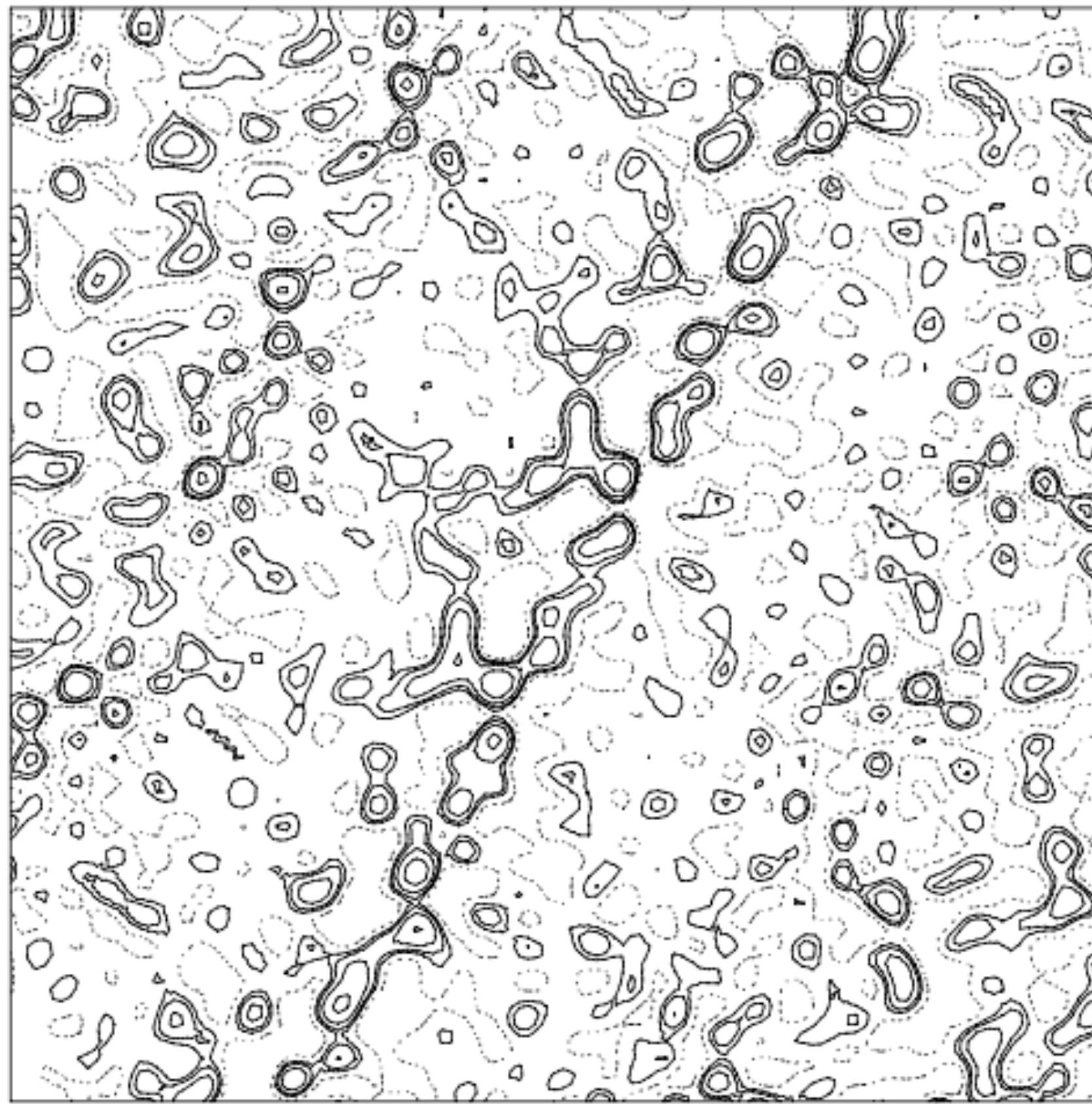
Superior resolution comes with a cost - we cannot sample all scales equally

# CLEAN fundamentals

Jackson 2008

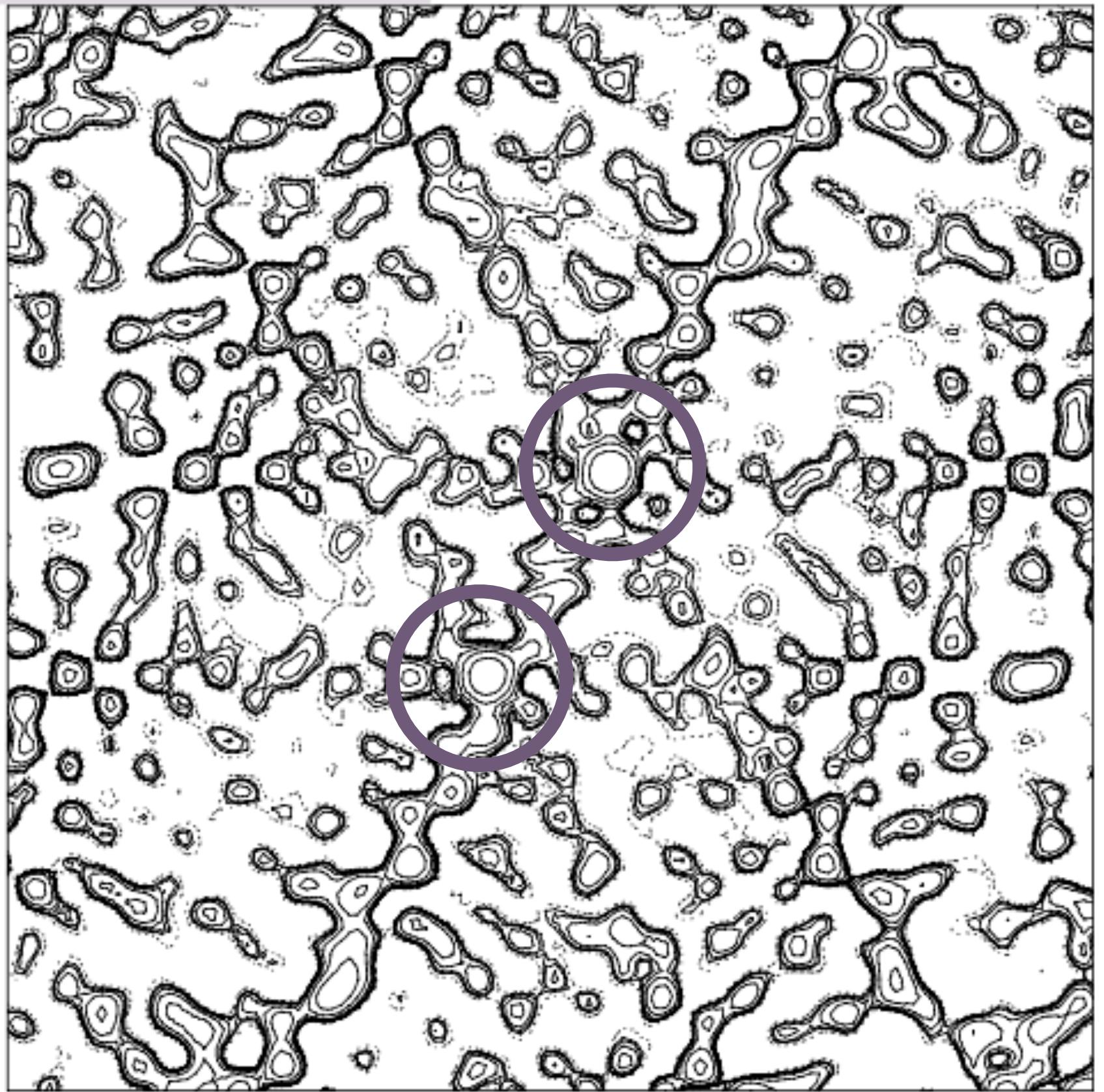


*remove  
PSF*

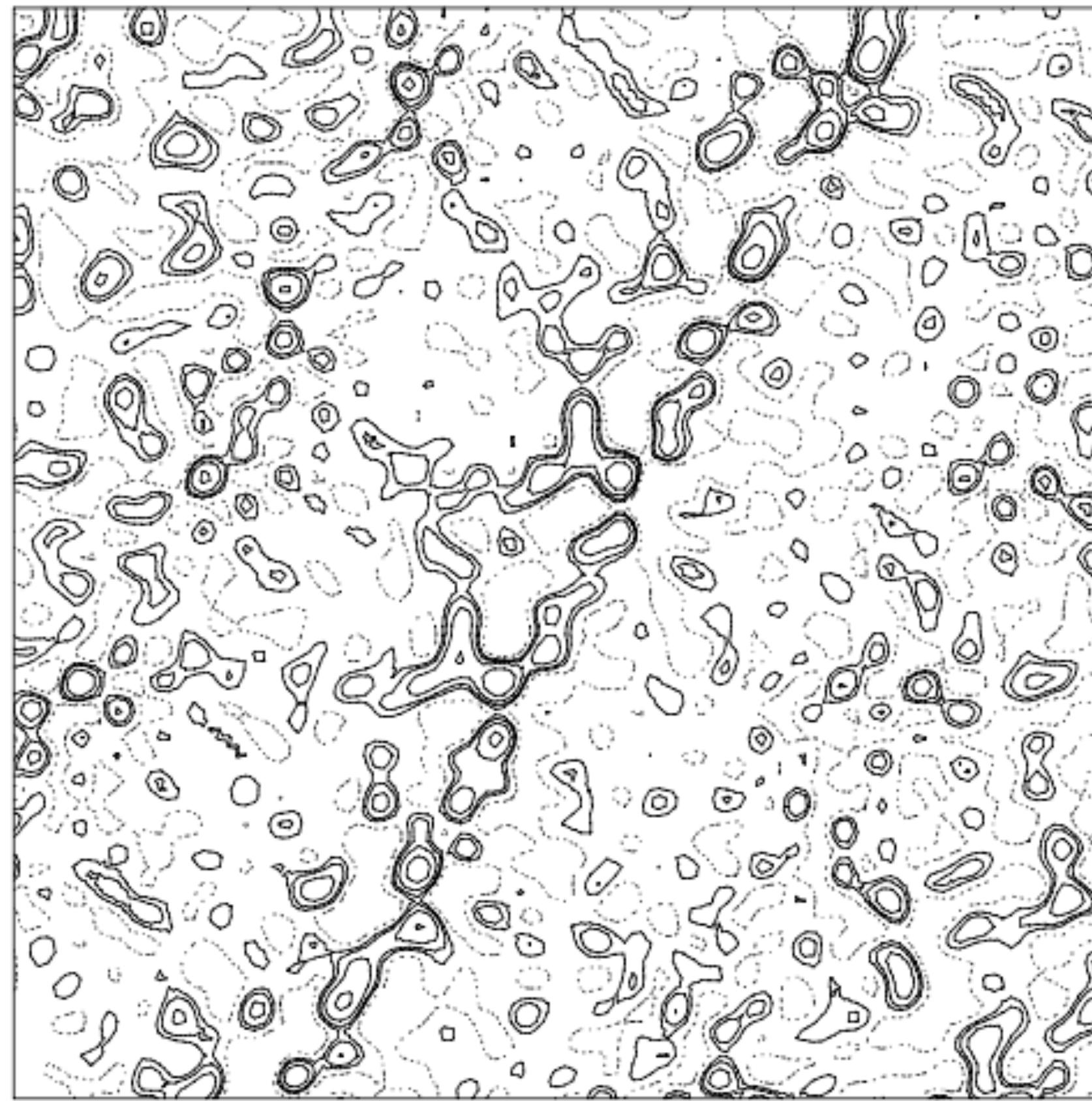


# CLEAN fundamentals

Jackson 2008

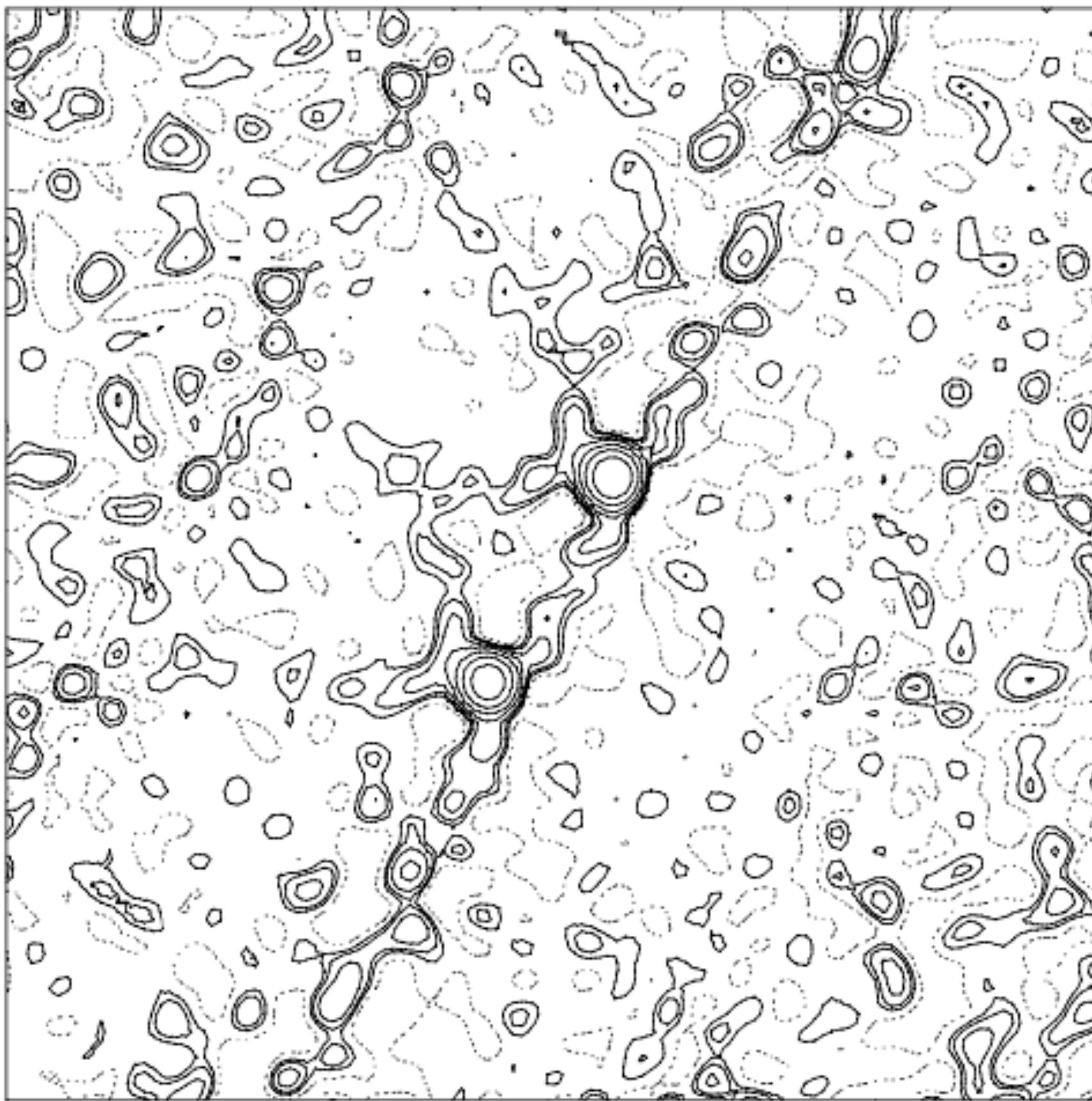
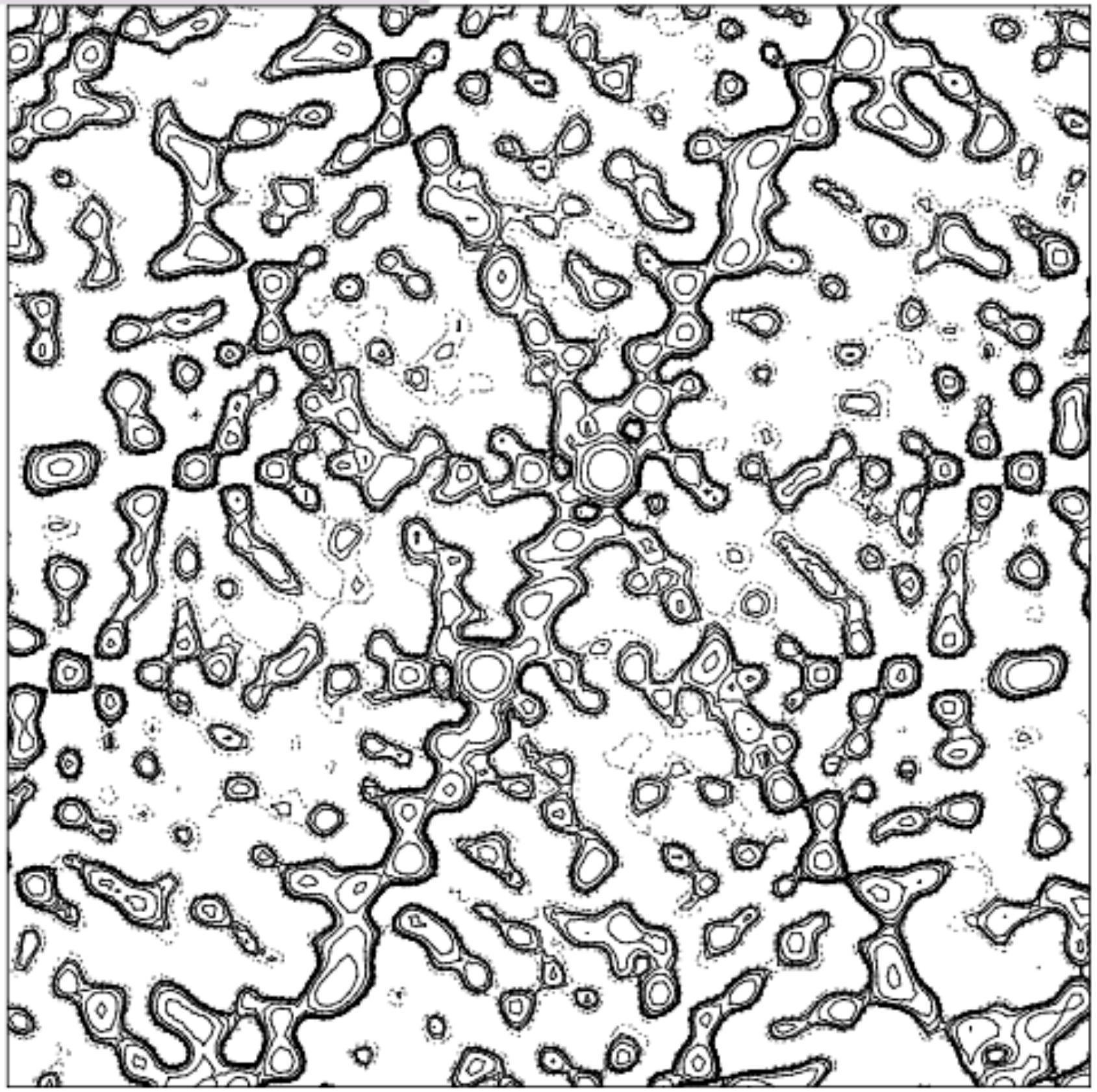


*remove  
PSF*



# CLEAN fundamentals

Jackson 2008



# Limitations of CLEAN

Arras+2021

Dealing with large scale emission

No error estimate

Negative signal

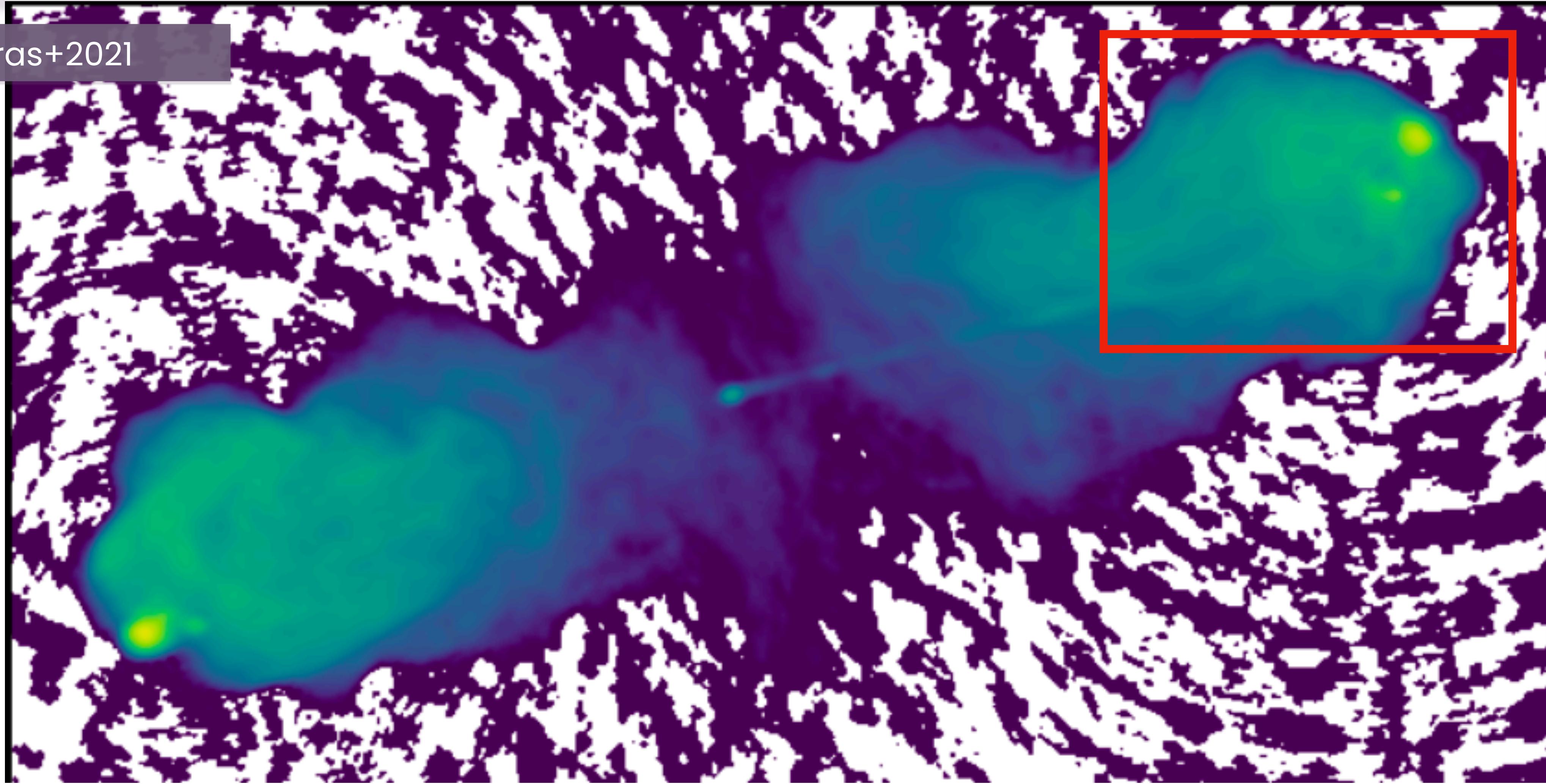
$$\mathcal{P}(s|d) = \frac{\mathcal{P}(d|s)\mathcal{P}(s)}{\mathcal{P}(d)}$$

## RESOLVE algorithm

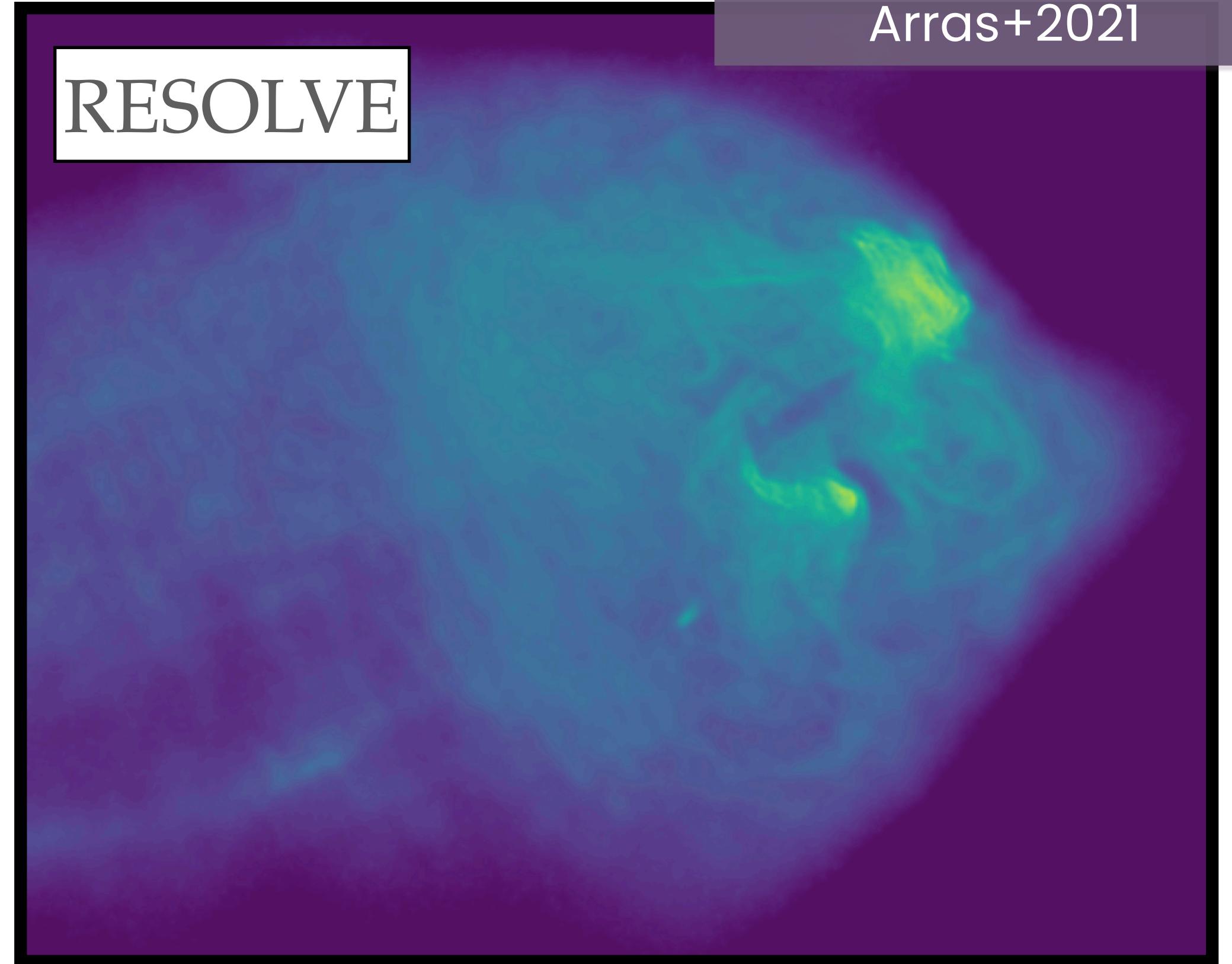
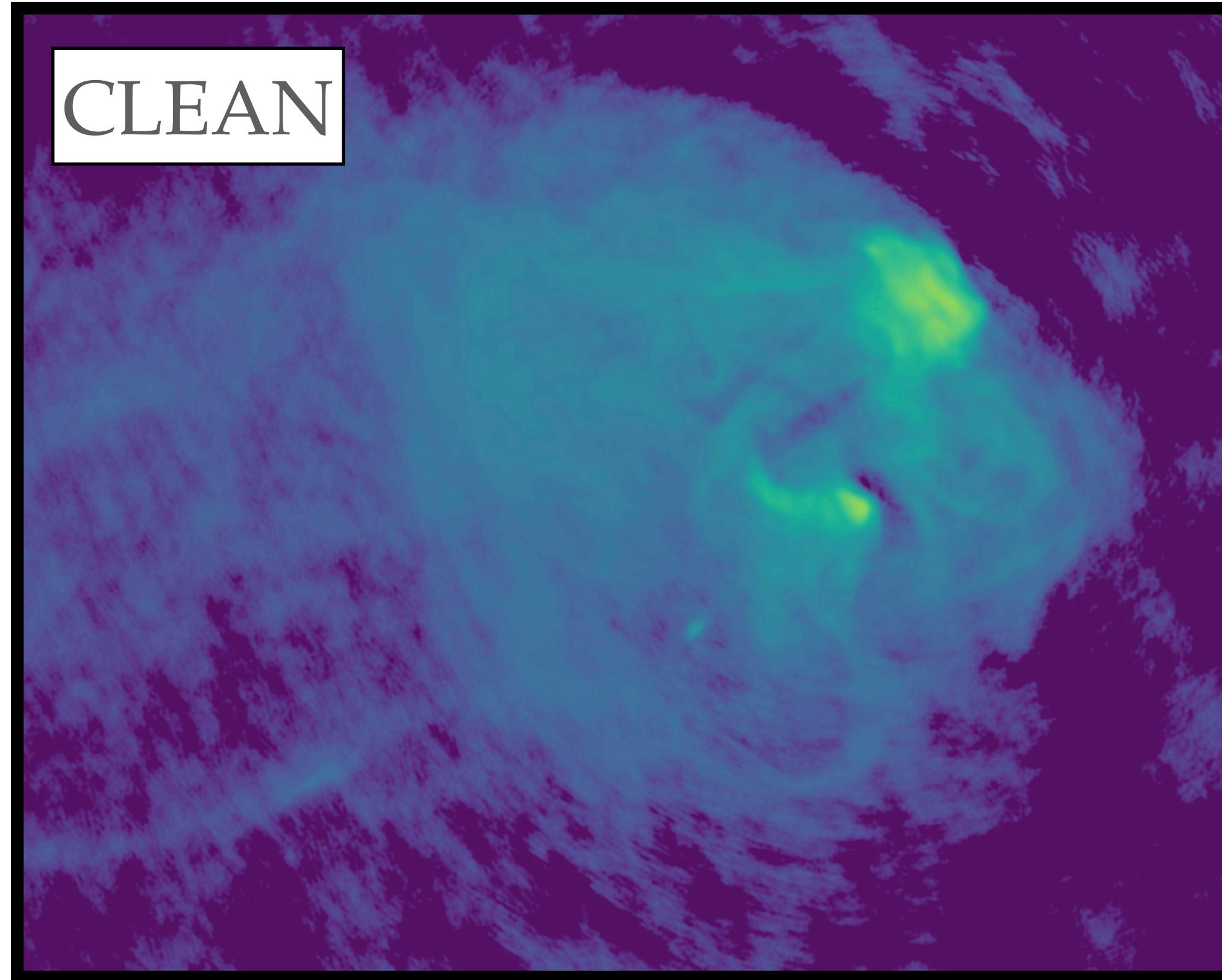
Enßlin+2009, Junklewitz+2014, Arras+2018

# Comparison of RESOLVE and CLEAN algorithms – VLA test

Arras+2021

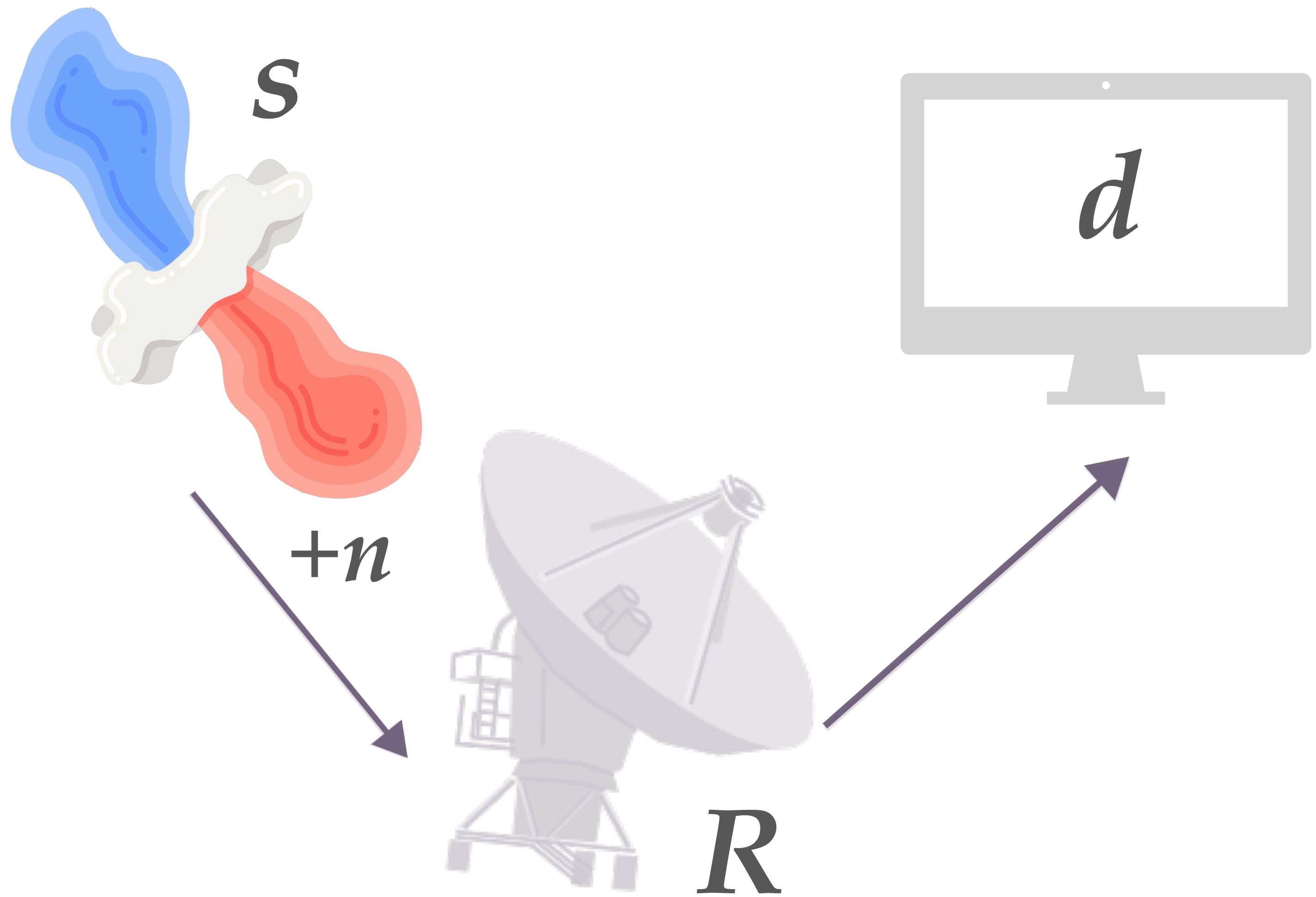


# Comparison of RESOLVE and CLEAN algorithms – VLA test



RESOLVE excels in retrieving large-scale emission

# Astronomical signal inference



$$d = Rs + n$$

$$\mathcal{P}(s|d) = \frac{\mathcal{P}(d|s)\mathcal{P}(s)}{\mathcal{P}(d)}$$

# Information Field Theory (IFT)

Enßlin+2009

- Enables to use Bayesian inference in the context of field theory
- Treats field as a continuous object (no pixelisation)
- Allows for field theory formalism
- Well fitted to the context of inference of sky brightness from interferometric observation
- Practically: NIFTy python package (Reinecke+2018, Selig+2013, Arras+2019)

# Minimum information on the field

- 1.Emitting sources have some unknown spatial correlation structure
- 2.Signal field is strictly positive
- 3.There is orders of magnitude difference in brightness within the field

# Minimum information on the field

Junklewitz+2014

1. Emitting sources have some unknown spatial correlation structure

*MaxEnt*  
→

*Gaussian probability distribution*

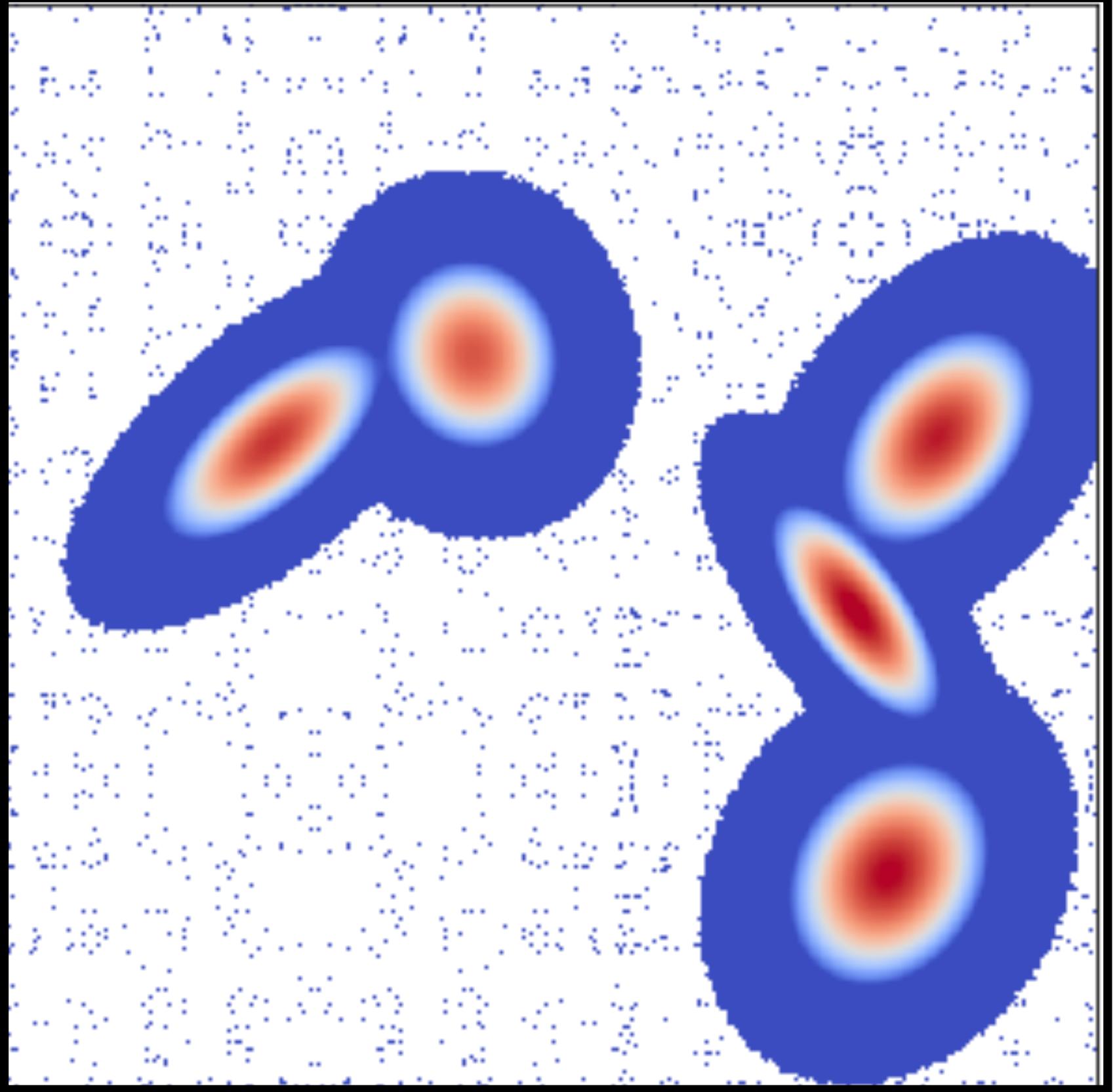
2. Signal field is strictly positive

→

*Logarithm of the signal field is Gaussian*

3. There is orders of magnitude difference in brightness within the field

$$d = RI + n = RI_0 e^s + n$$

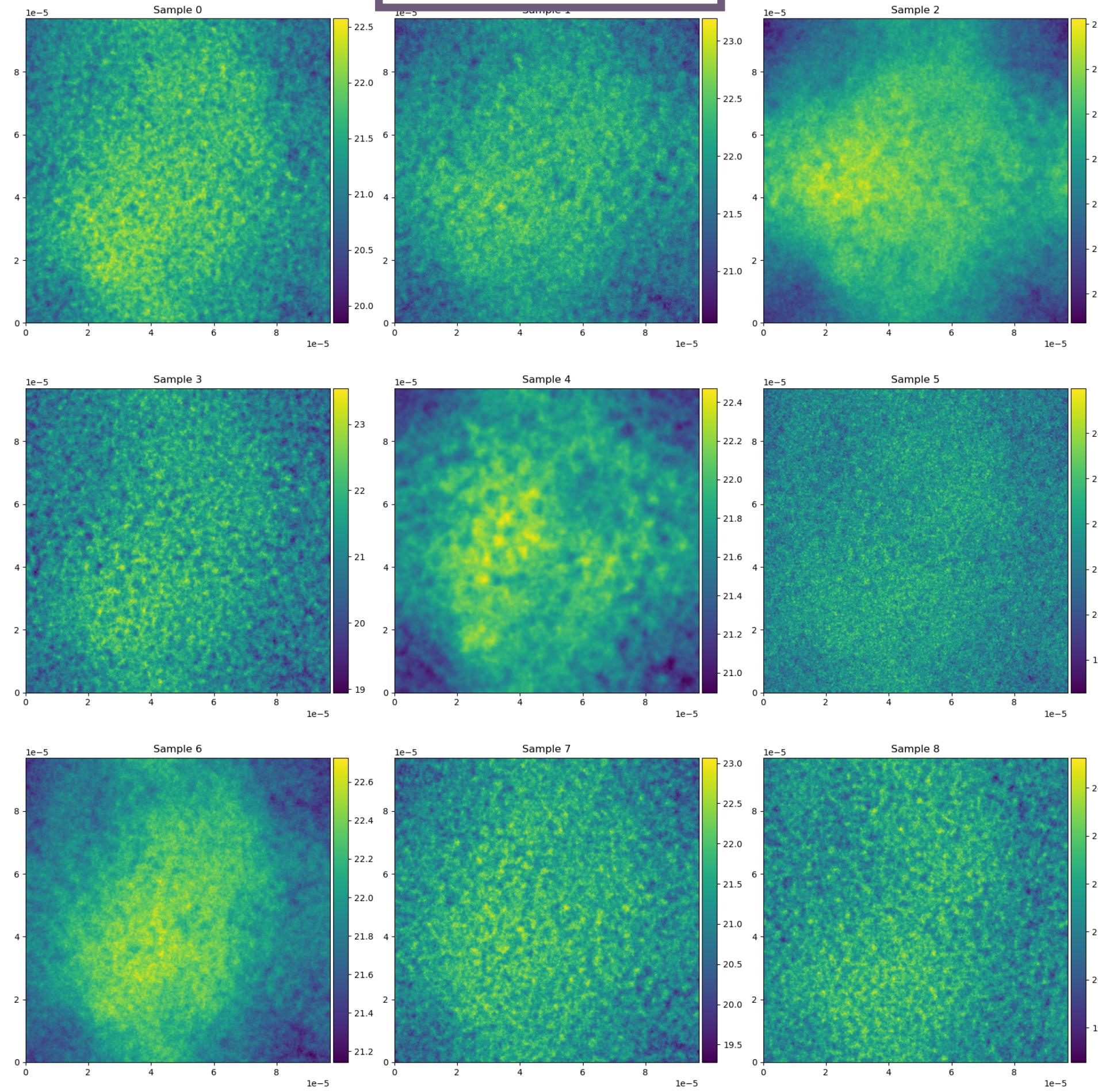


## RESOLVE application to simulated dataset

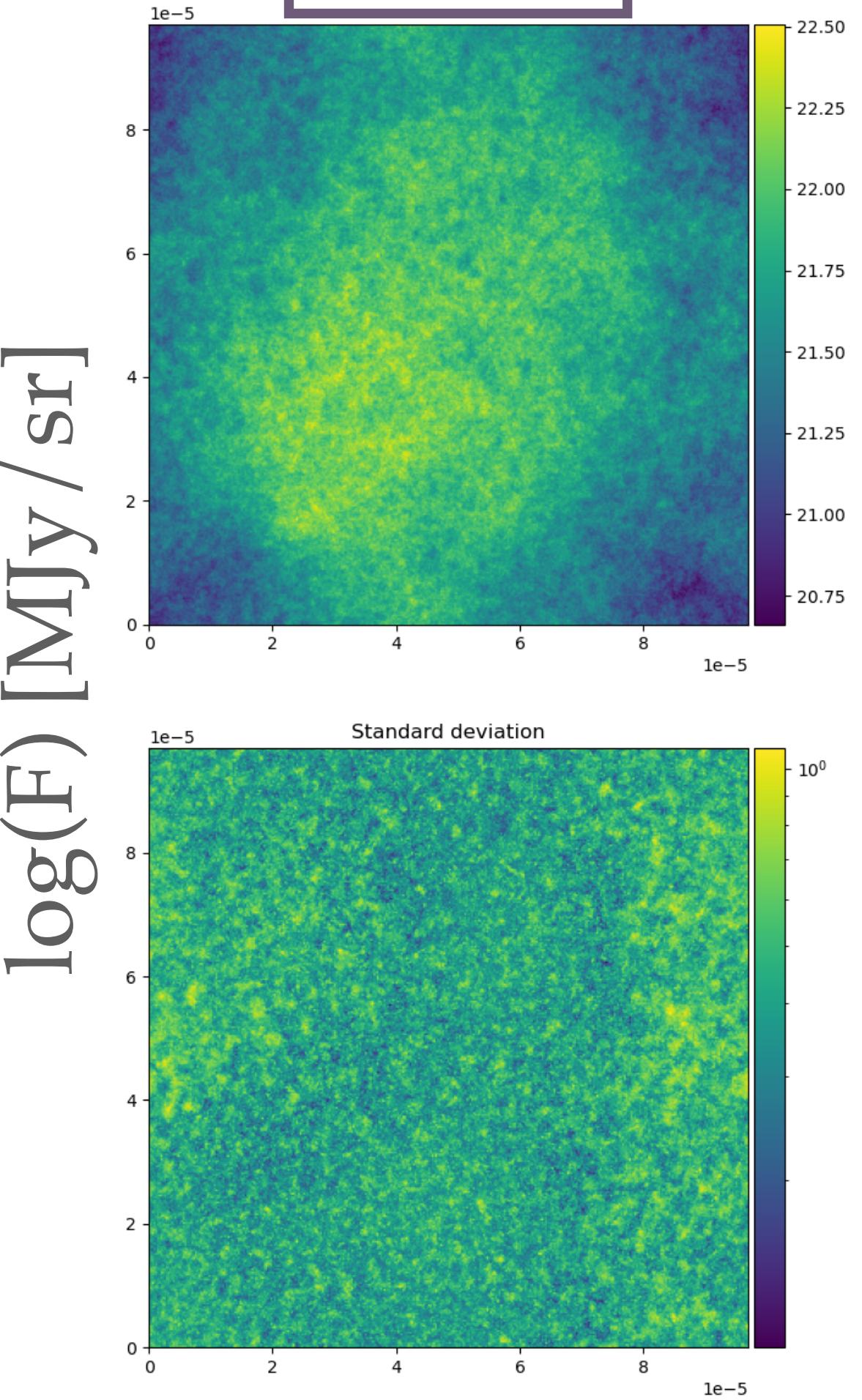
*A simulation of Gaussian continuum sources*

# Iterations of RESOLVE

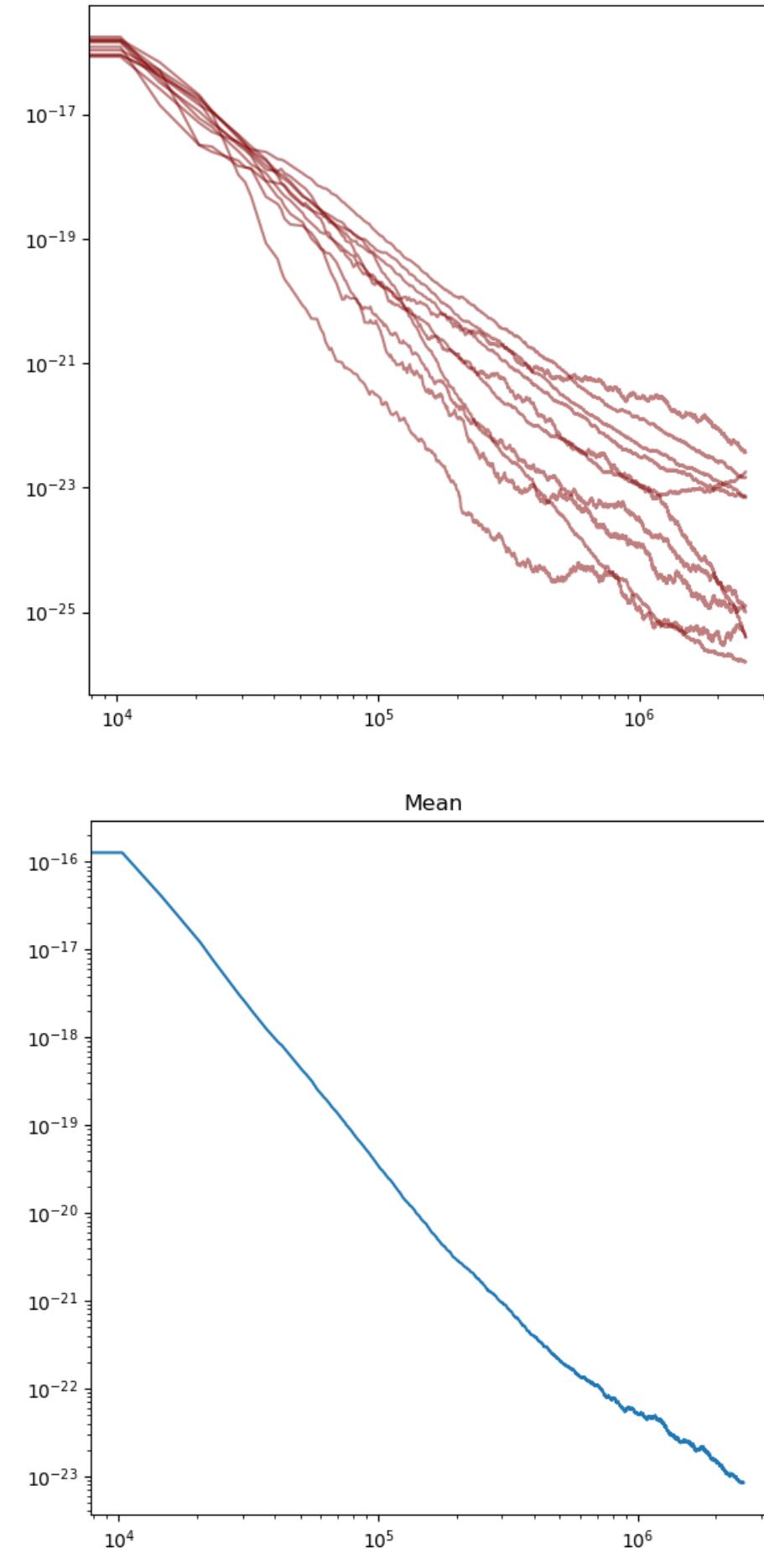
Samples



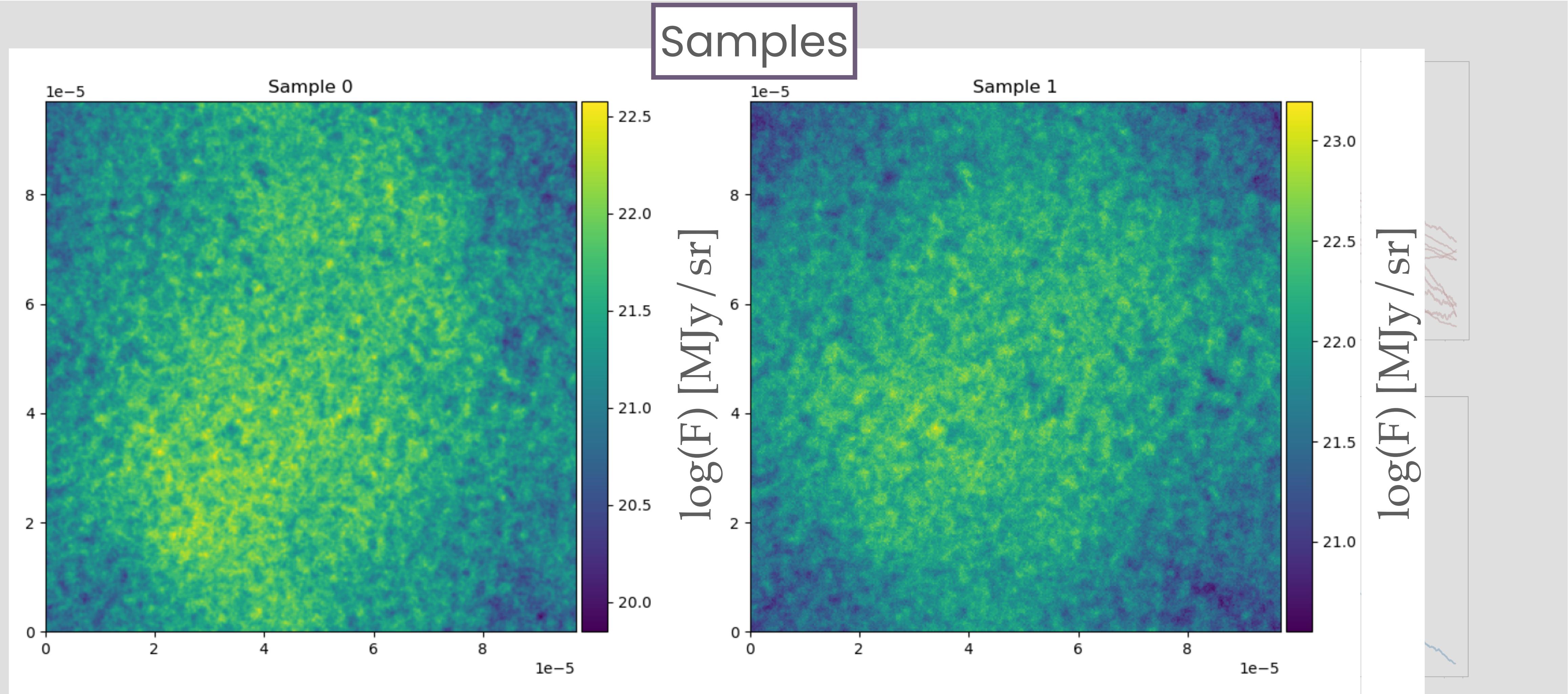
Means



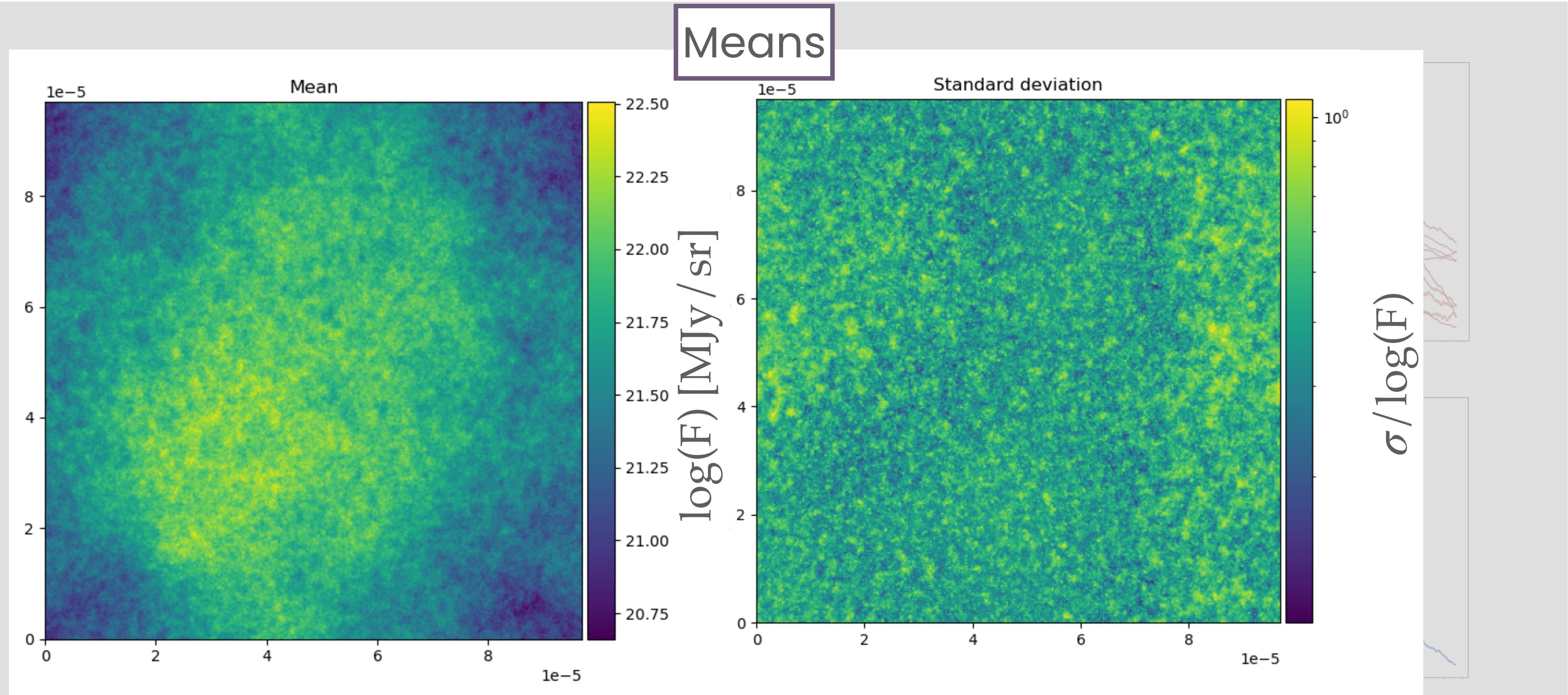
Power spectrum



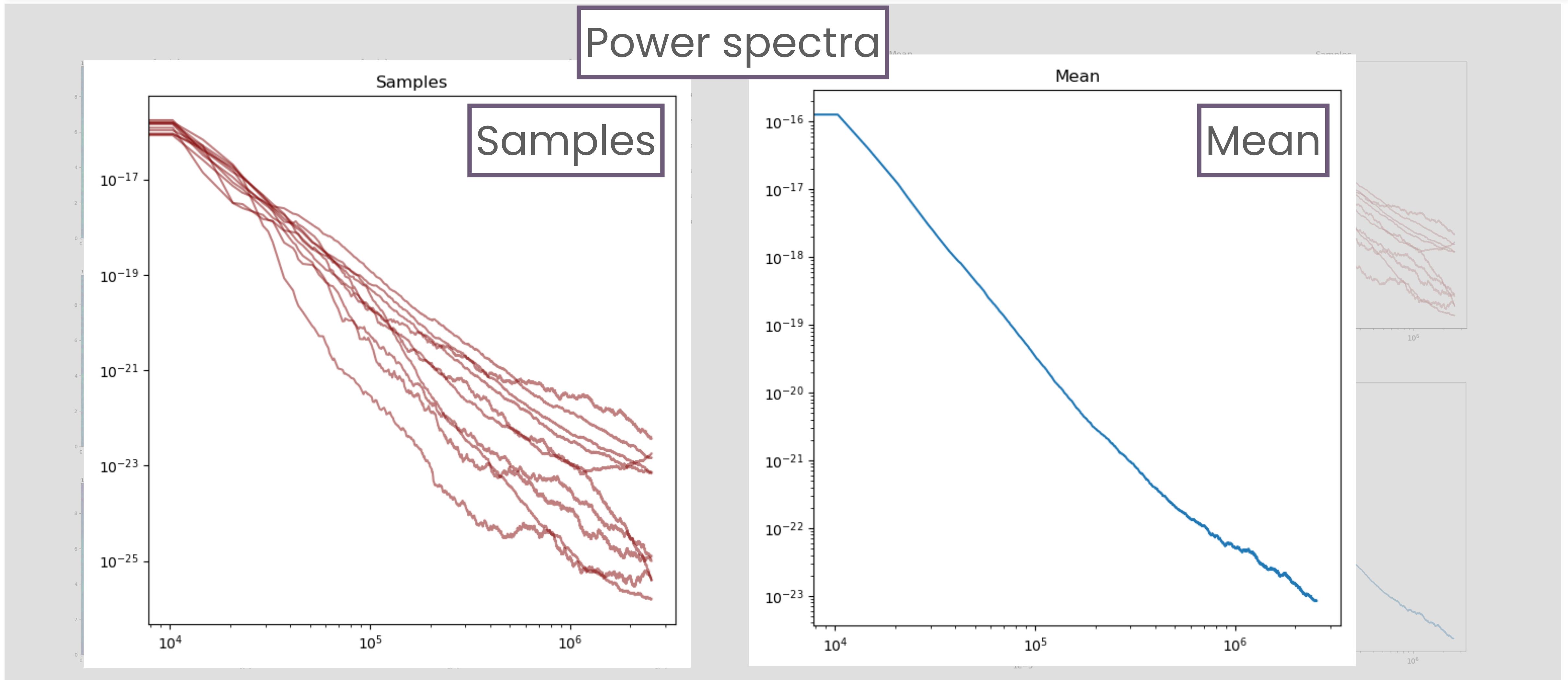
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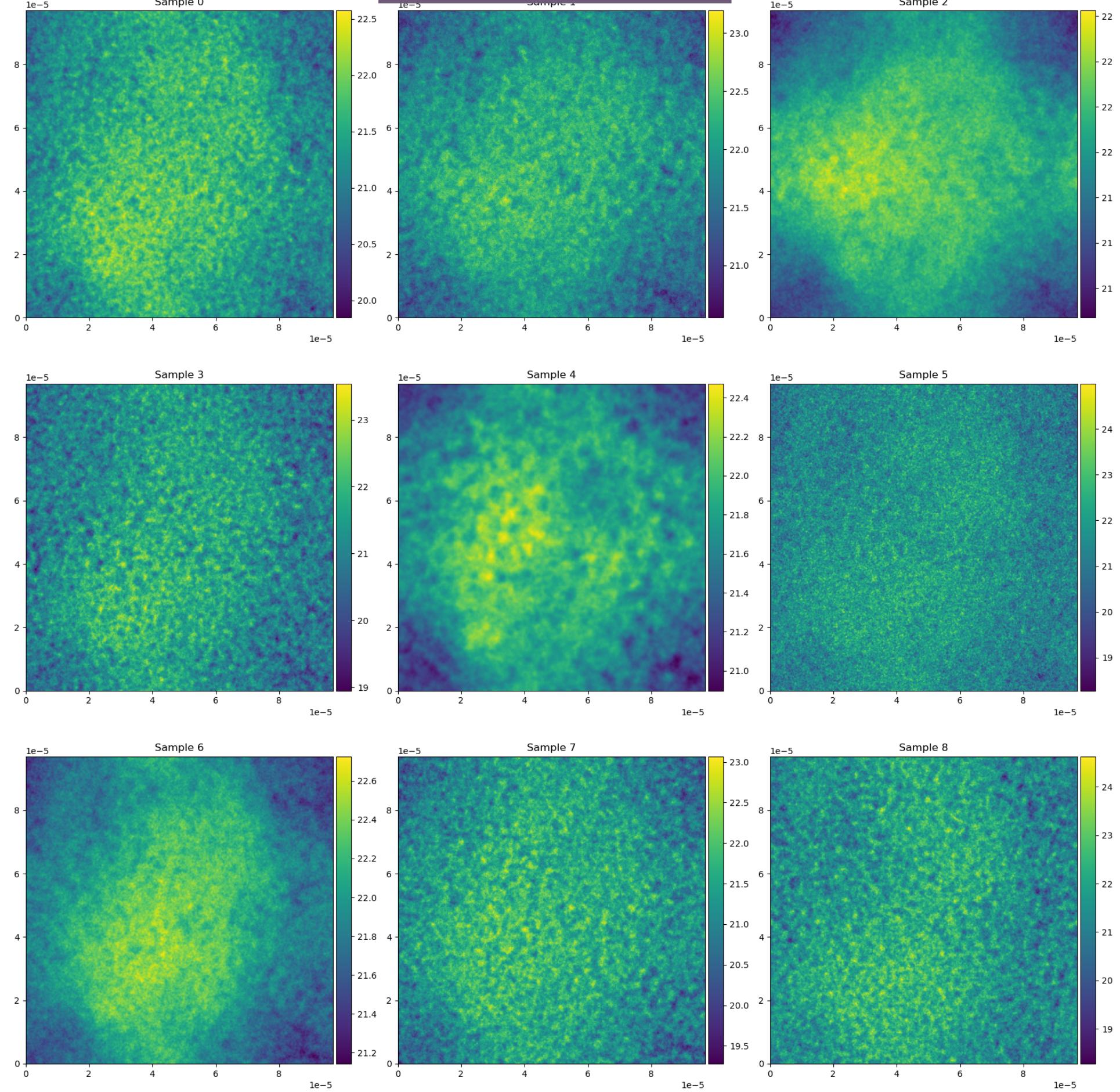
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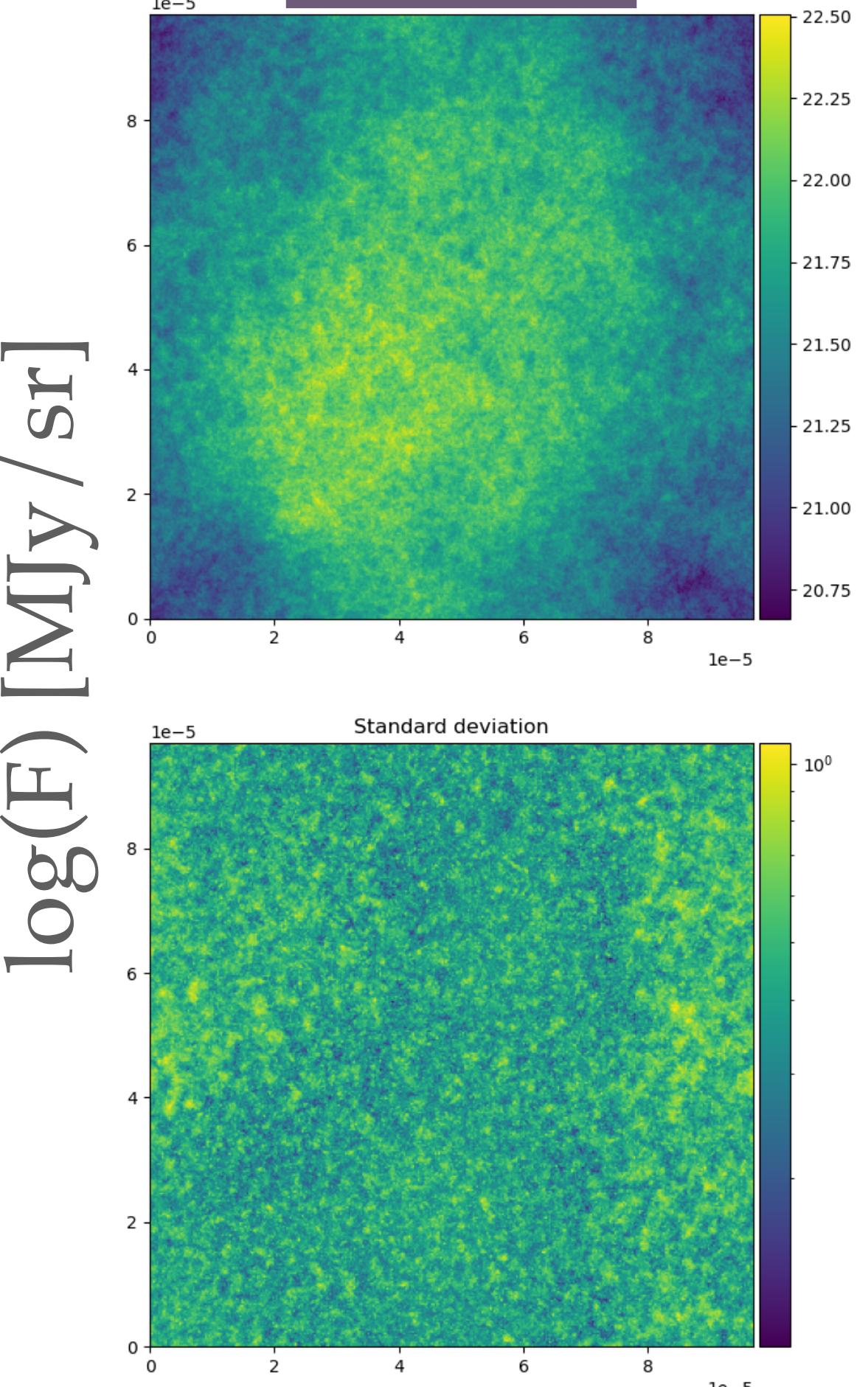
# Iterations of RESOLVE

Iter = 0

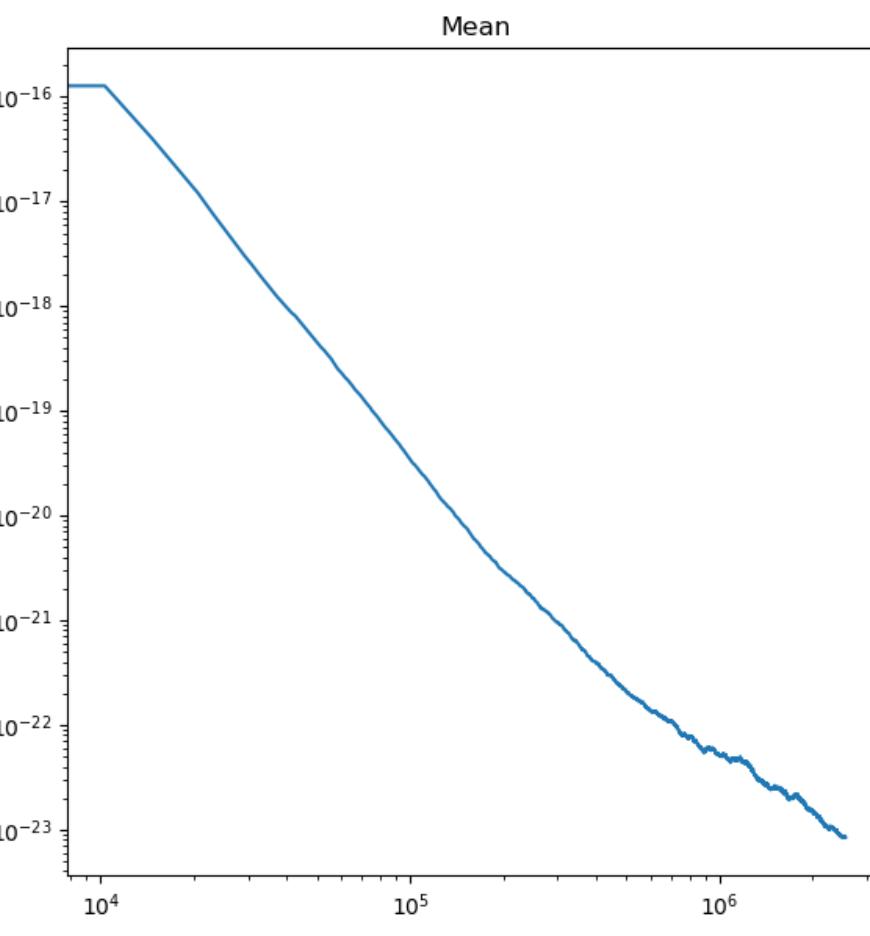
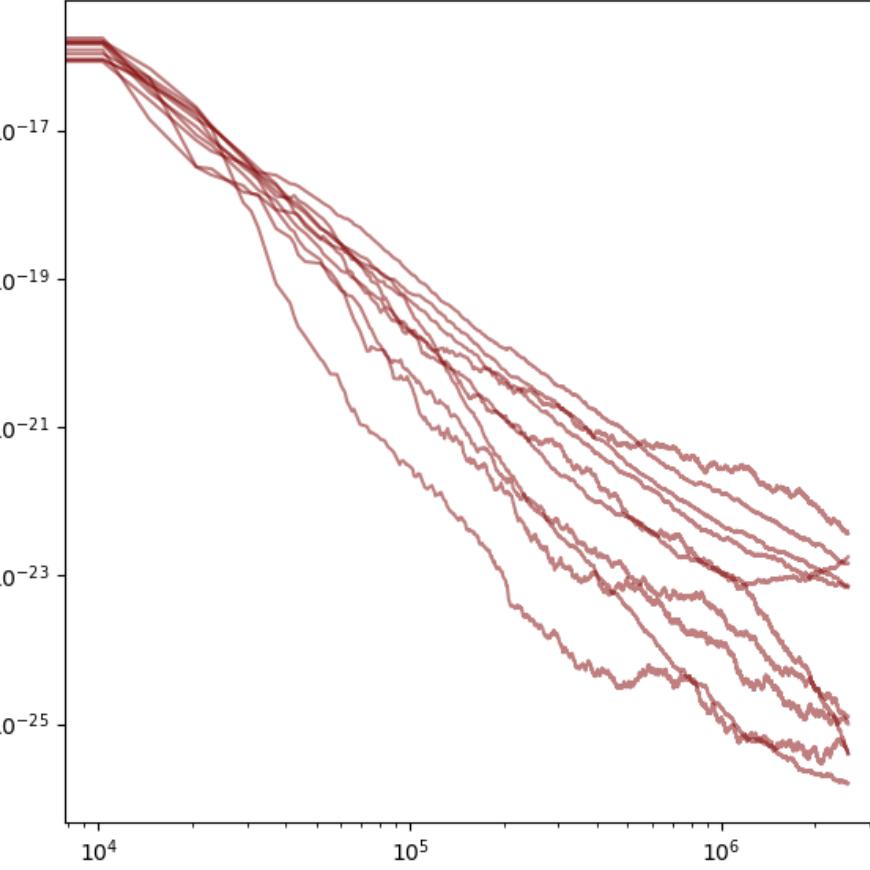
Samples



Means



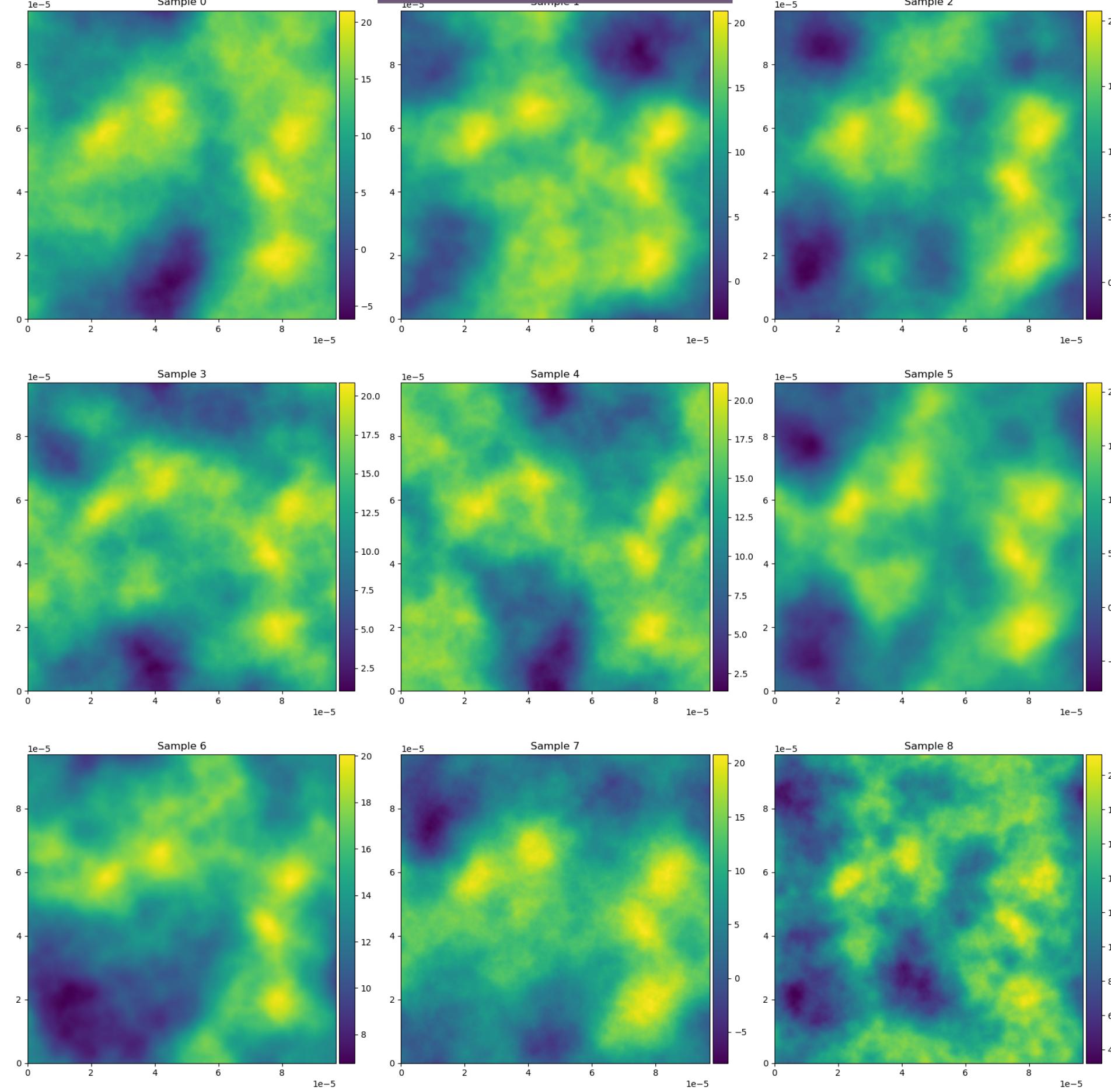
Power spectrum



# Iterative process

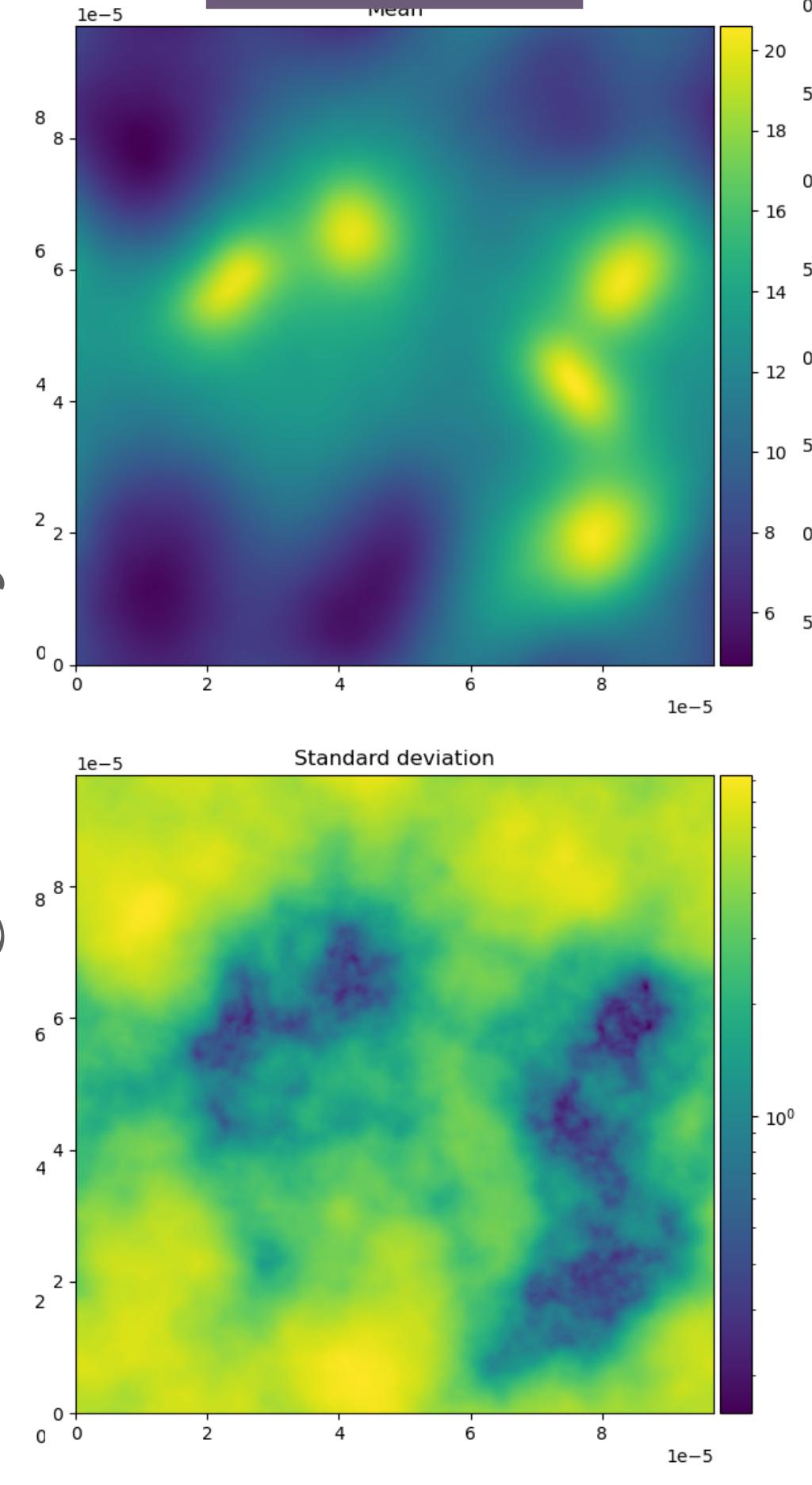
Iter = 5

Samples

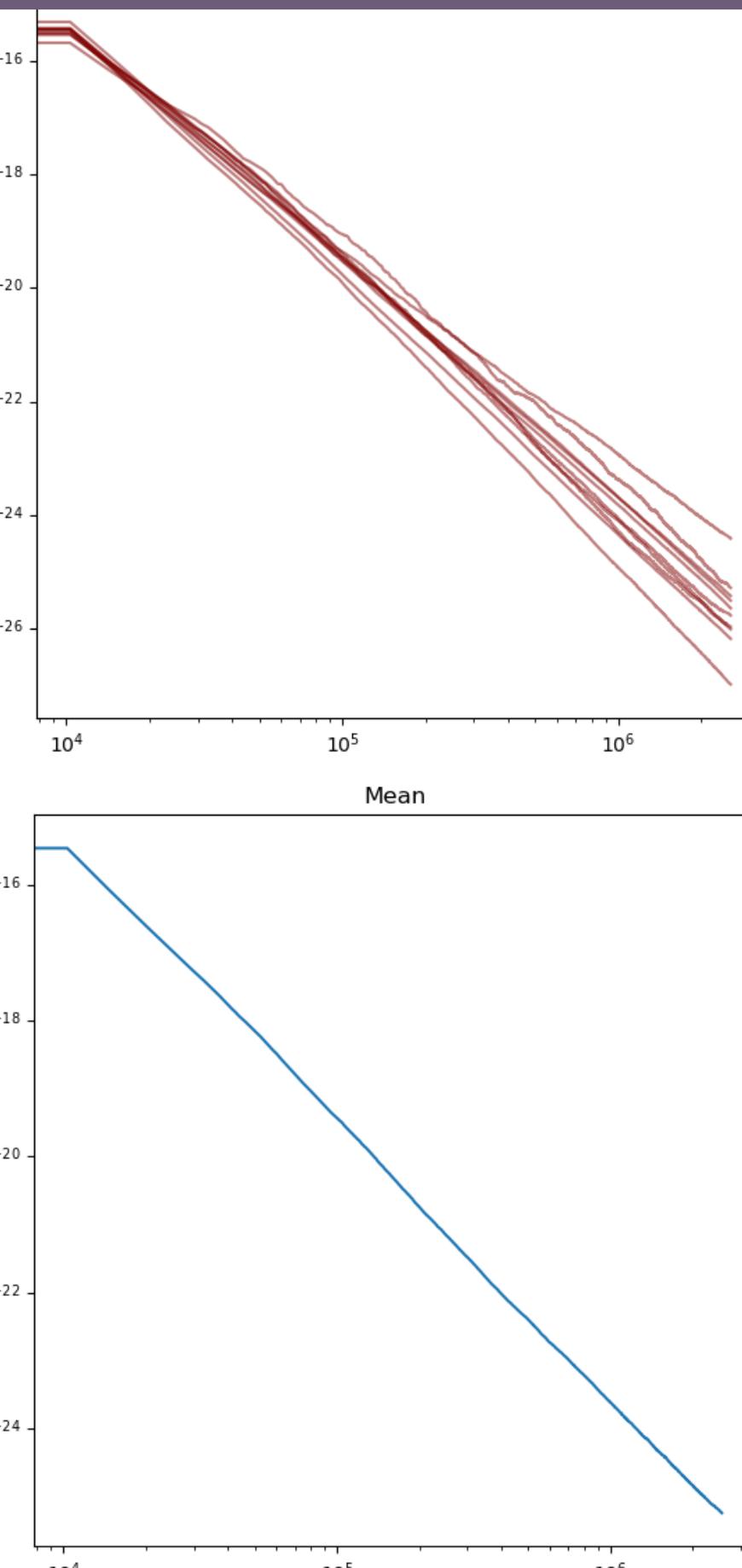


Means

log( $F$ ) [MJy / sr]



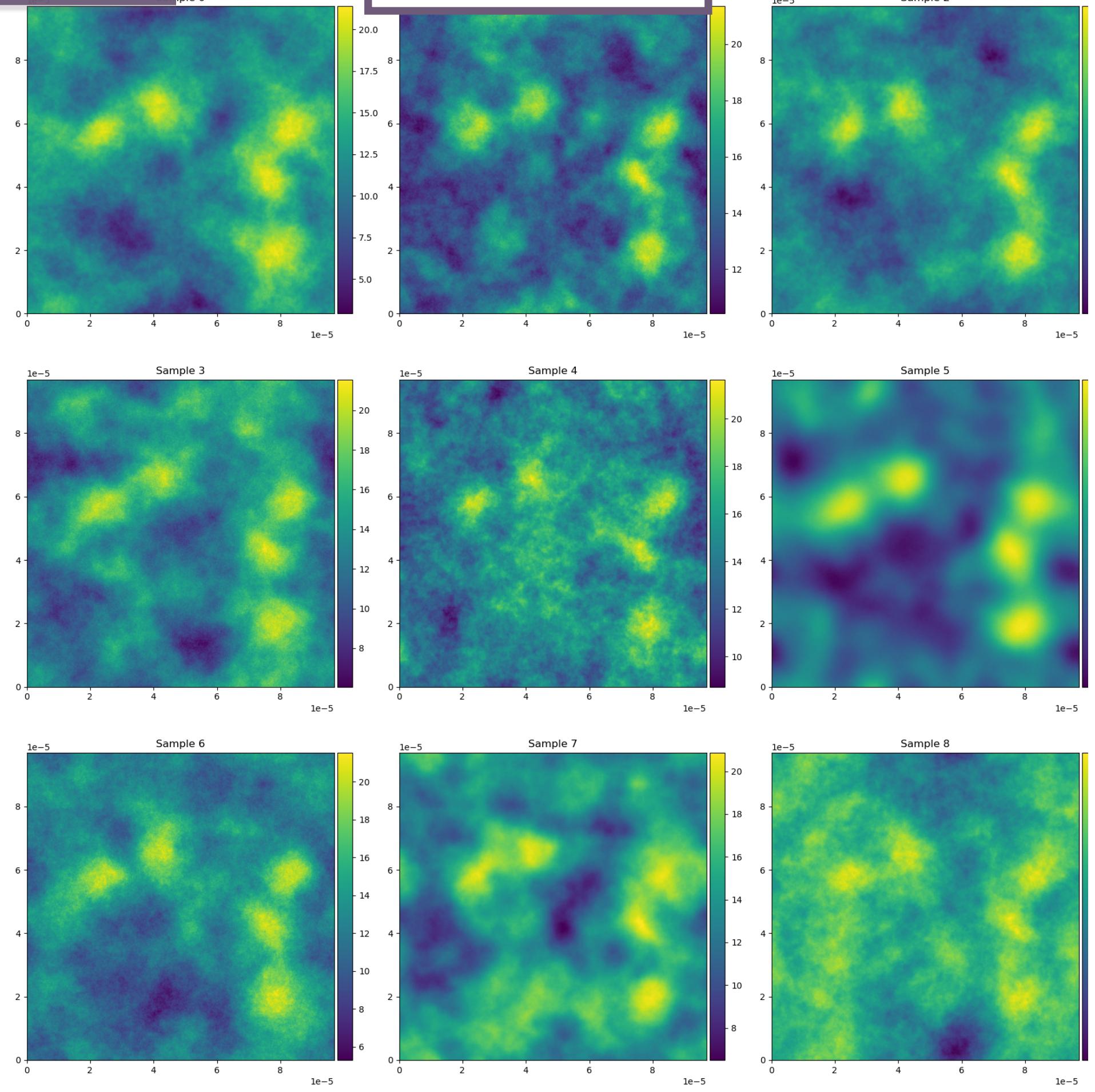
Power spectrum



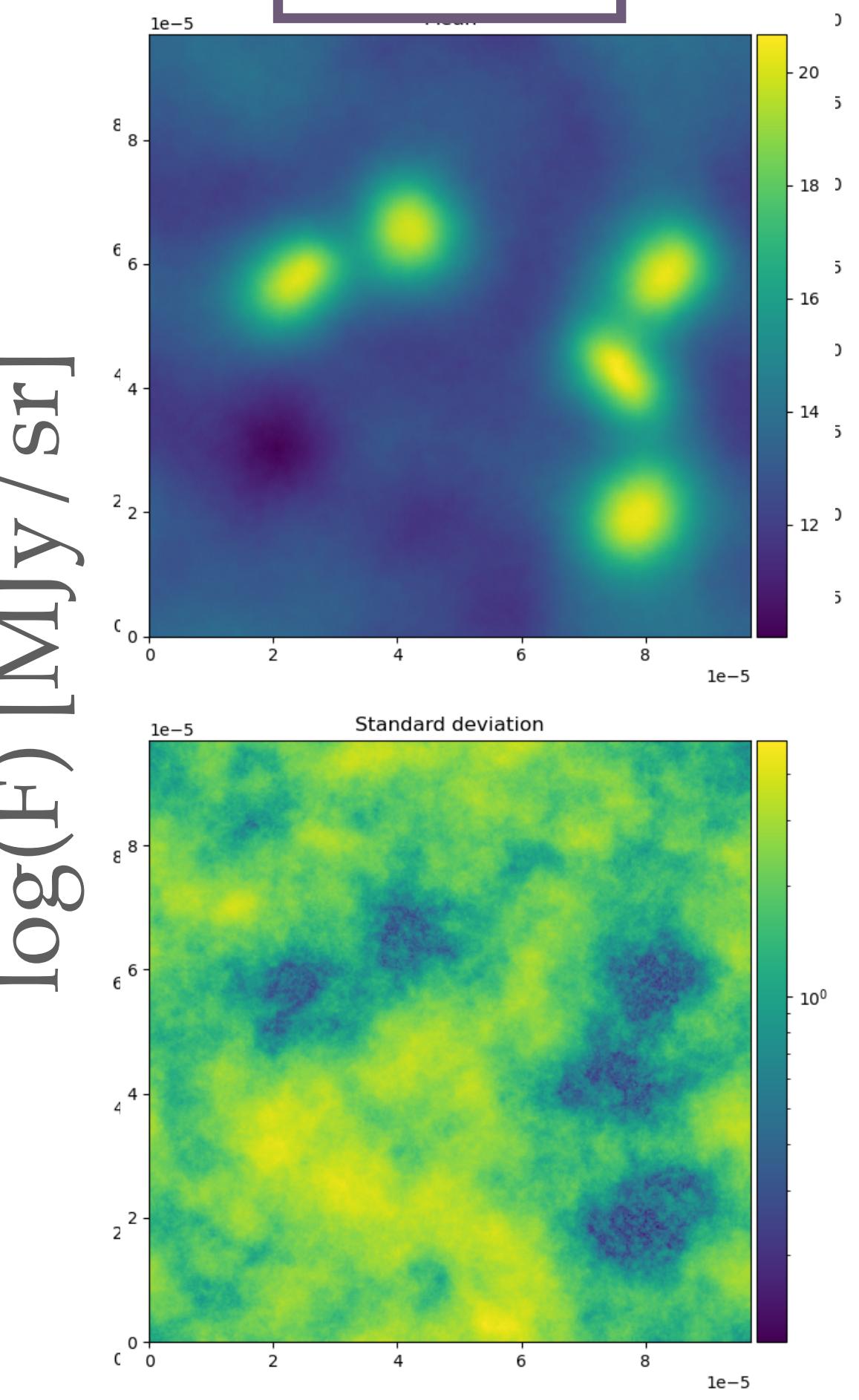
# Iterative process

Iter = 23

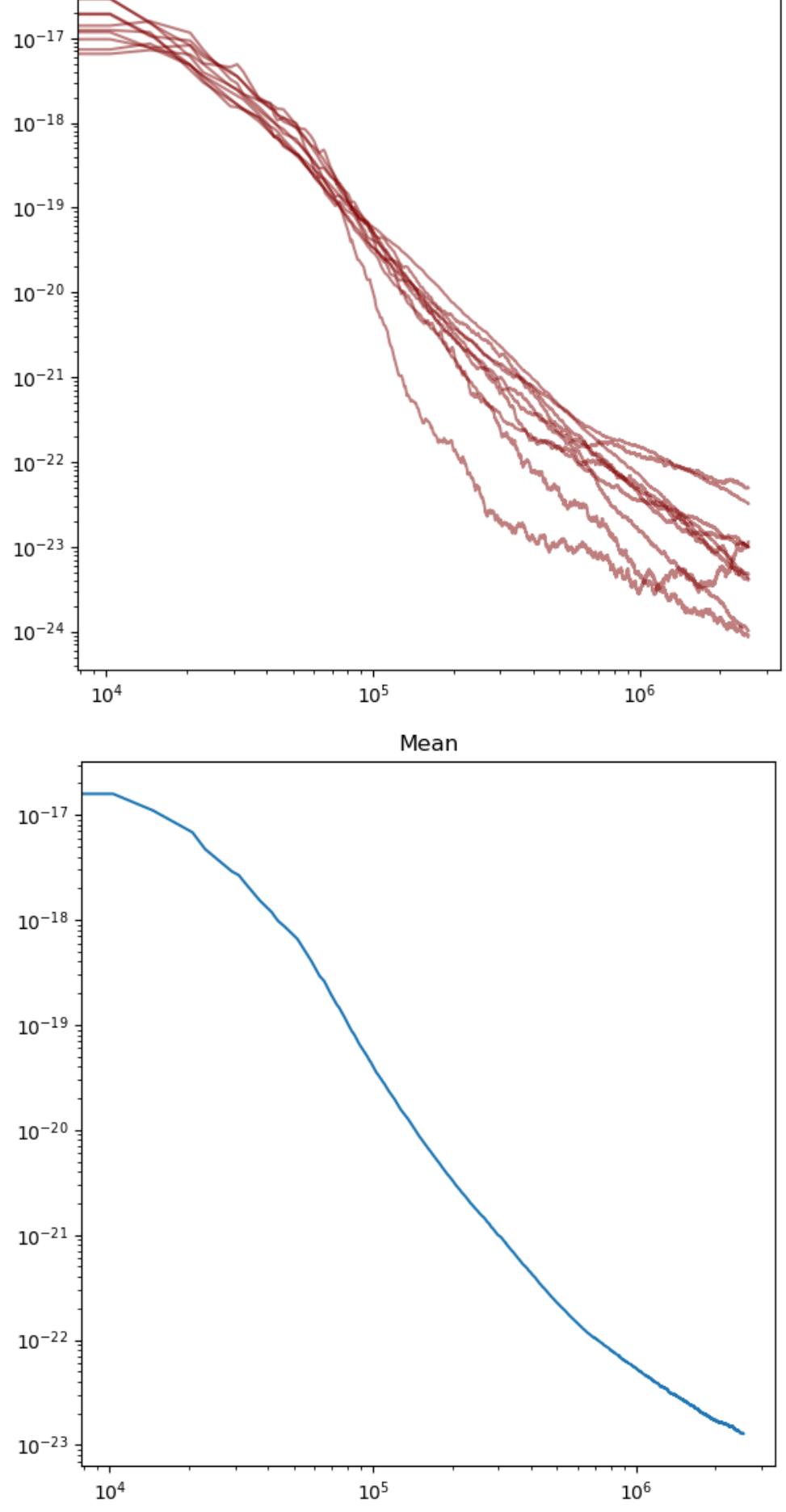
Samples



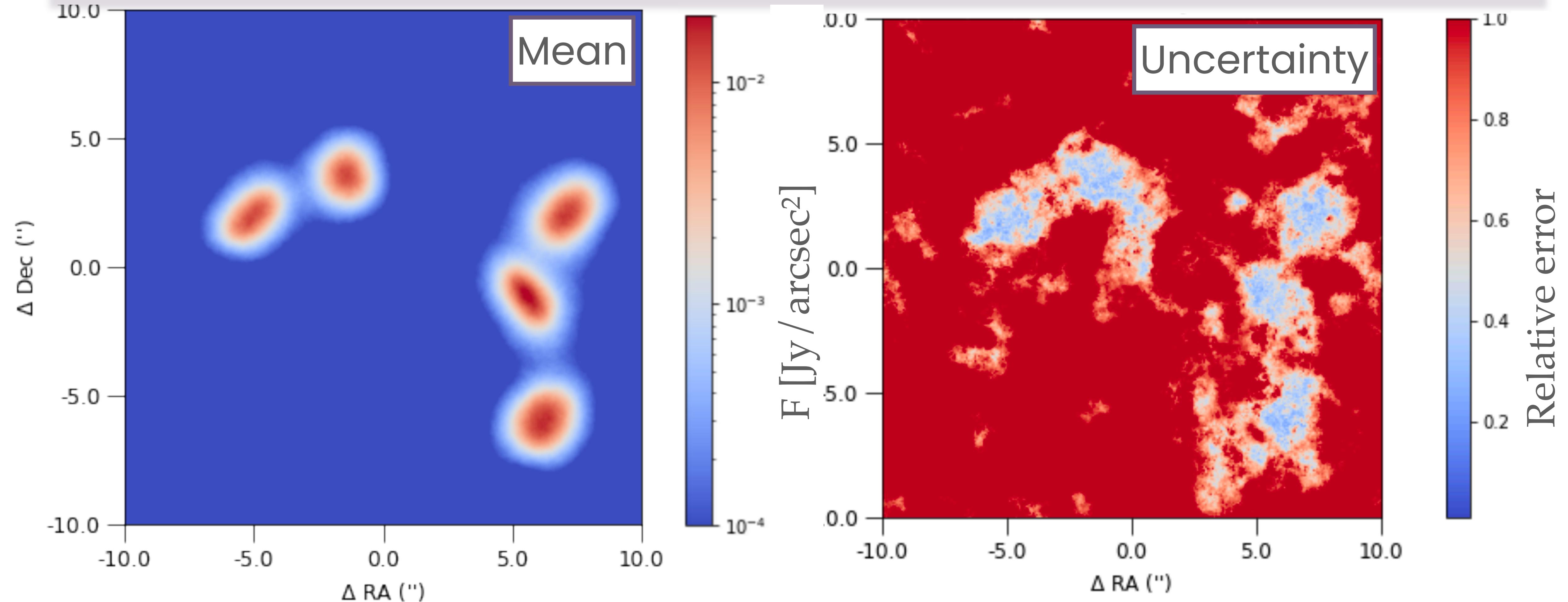
Means



Power spectrum

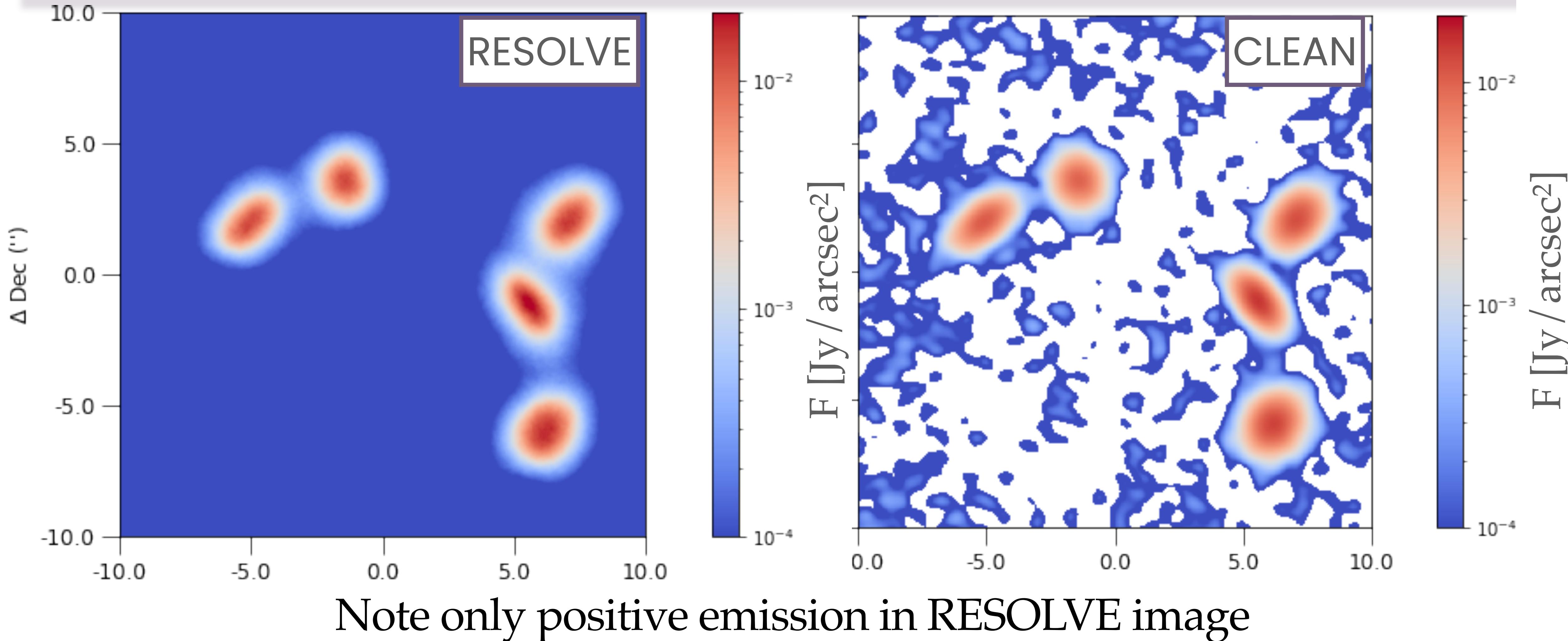


# Final results of RESOLVE imaging



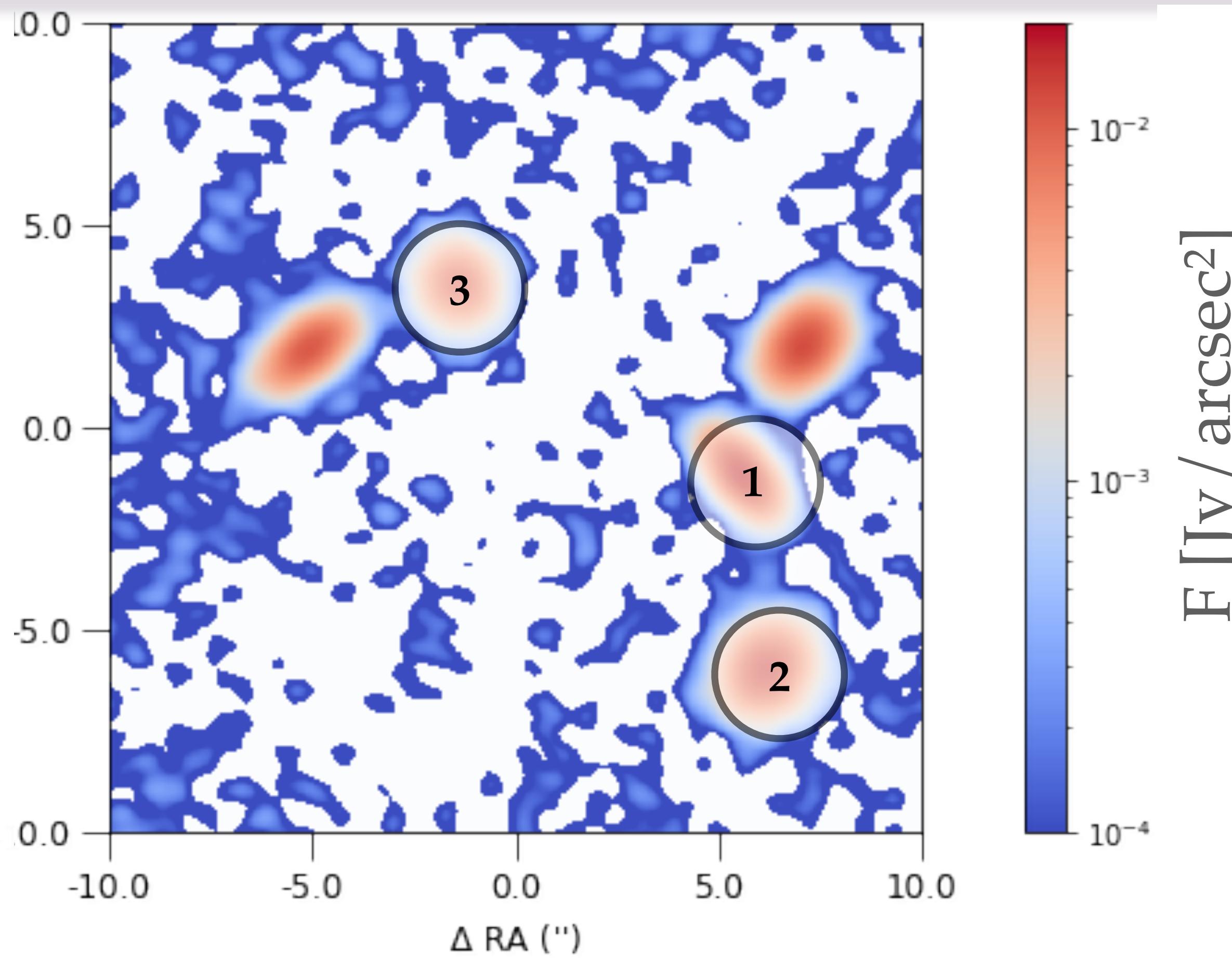
Five sources are recovered and uncertainty map is obtained

# Direct comparison of imaging for simulated datasets



Note only positive emission in RESOLVE image

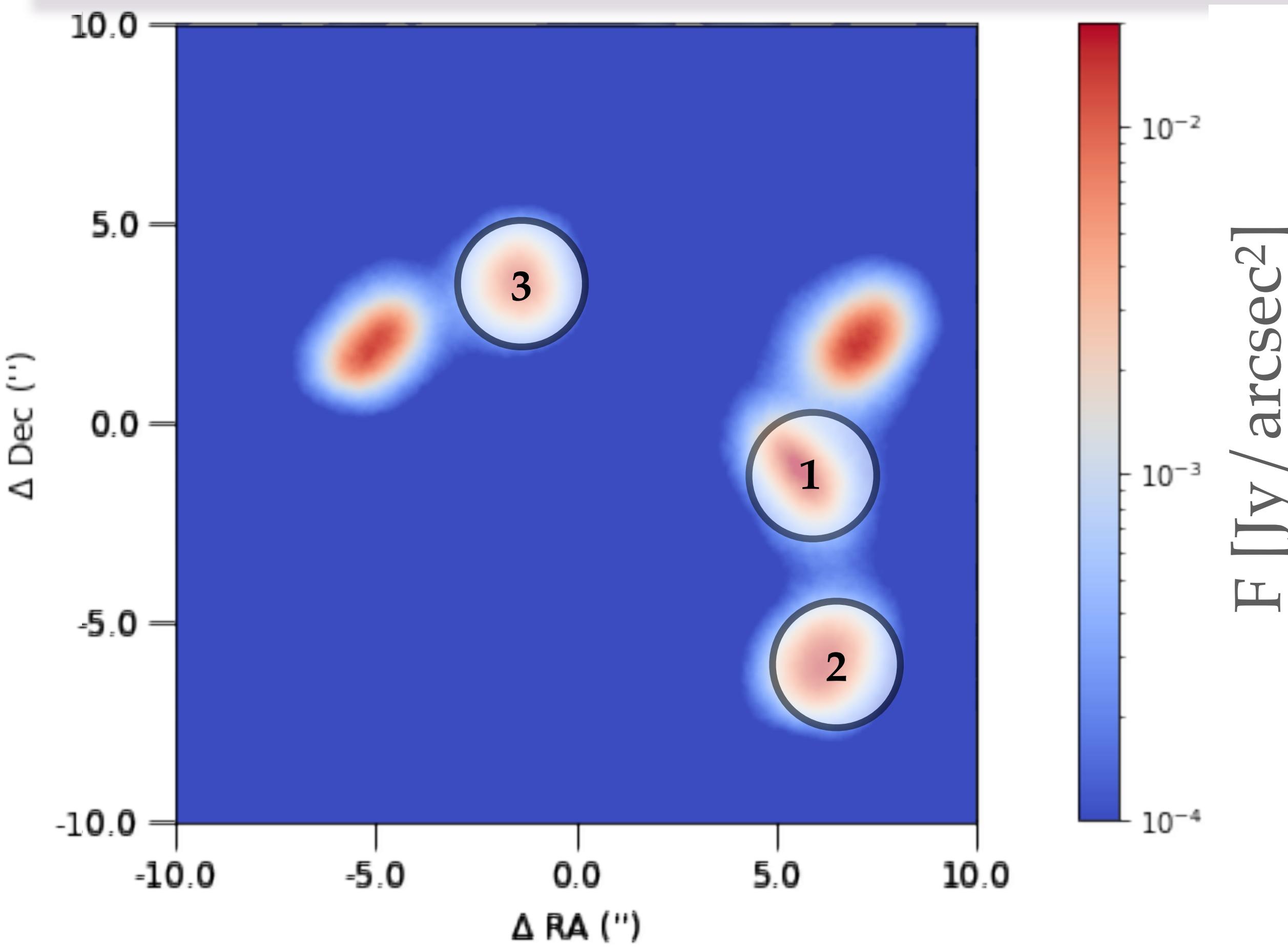
# Recovery of flux by CLEAN and RESOLVE



Source	CLEAN Flux [mJy]	RESOLVE Flux [mJy]	Model Flux [mJy]
1	24.96	26.68	34.11
2	23.59	23.59	23.31
3	17.82	17.82	16.69

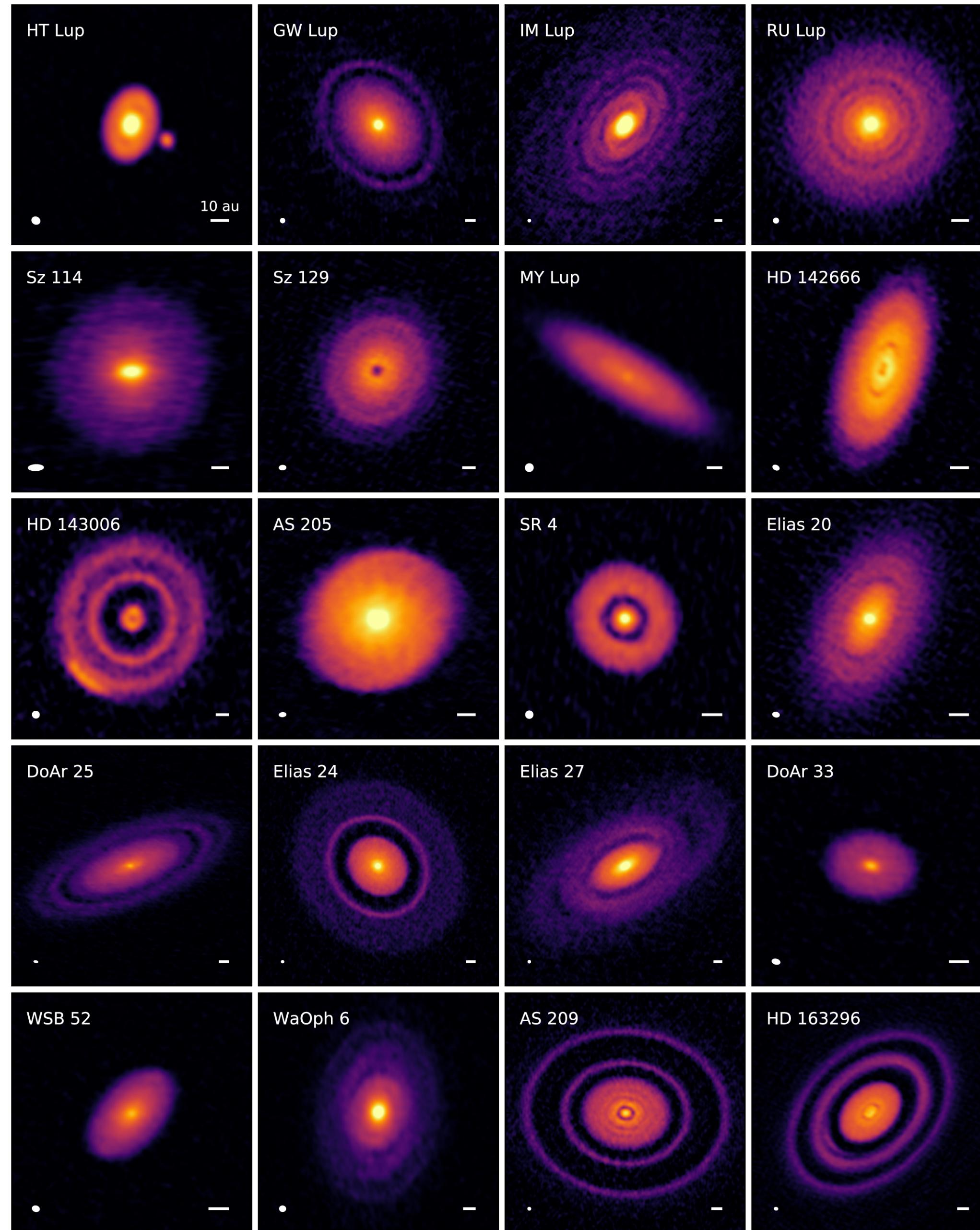
Comparable fluxes retrieved by CLEAN and RESOLVE

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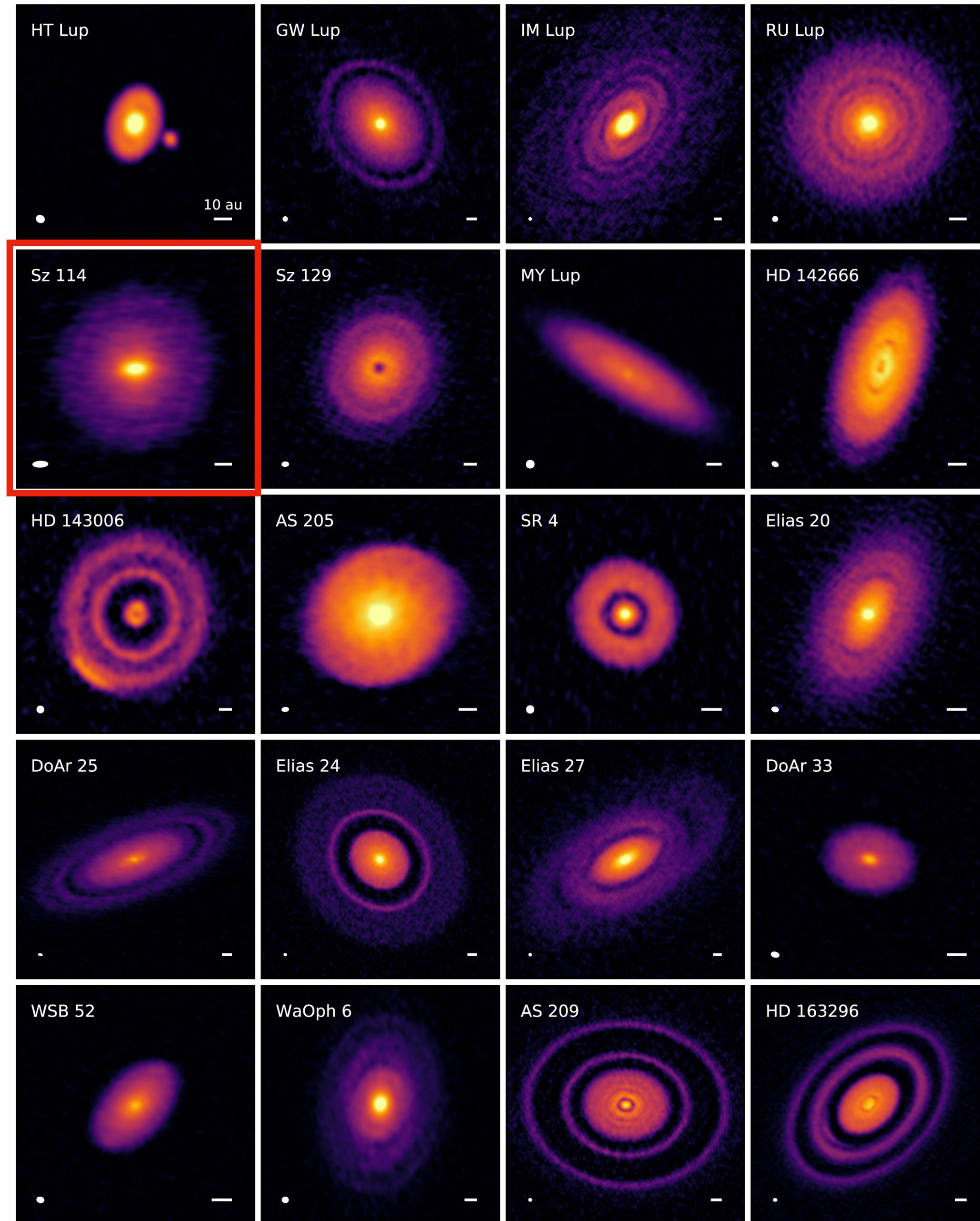
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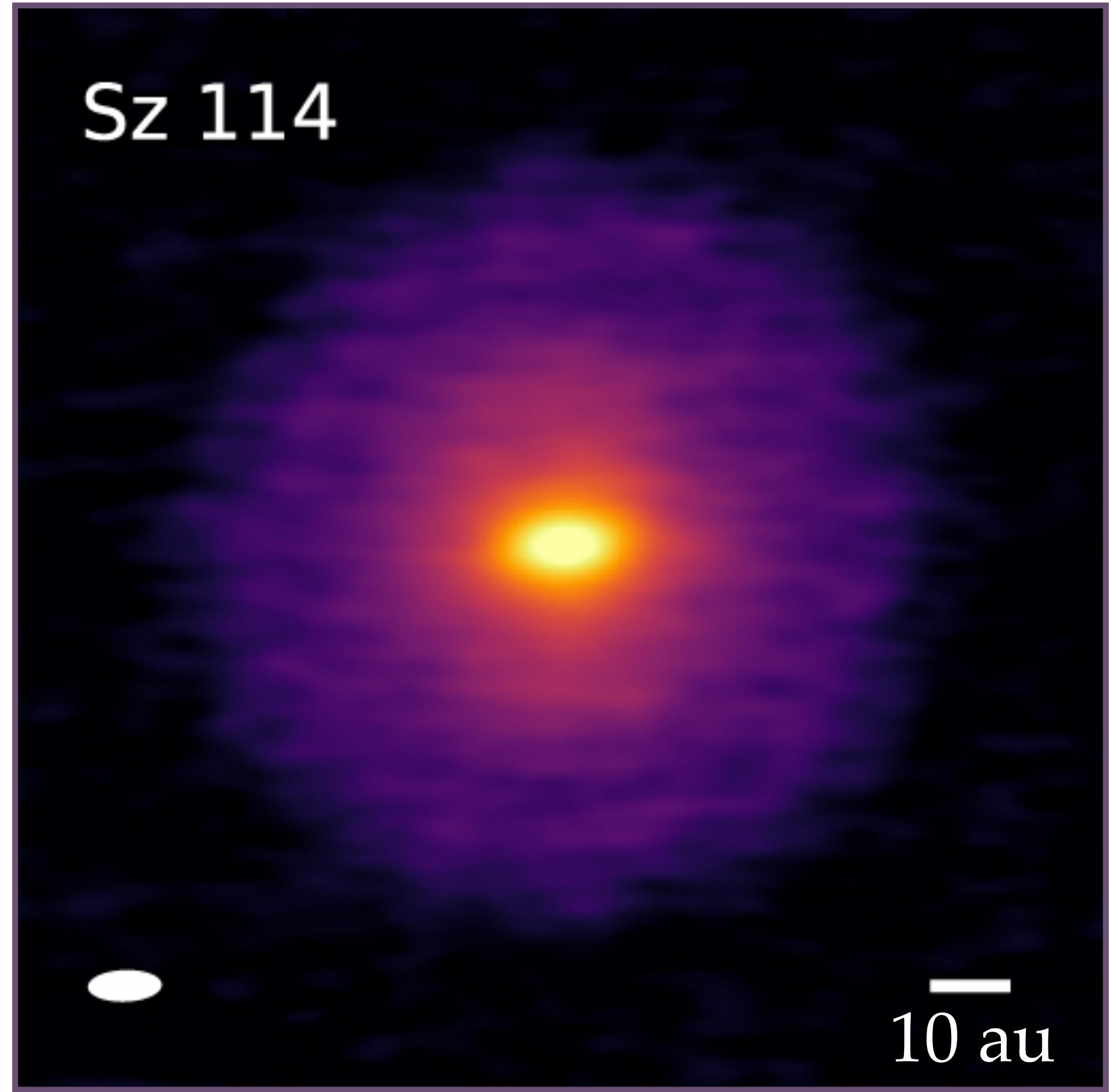
# RESOLVE application to real data

*Dust emission from planet-forming disk*



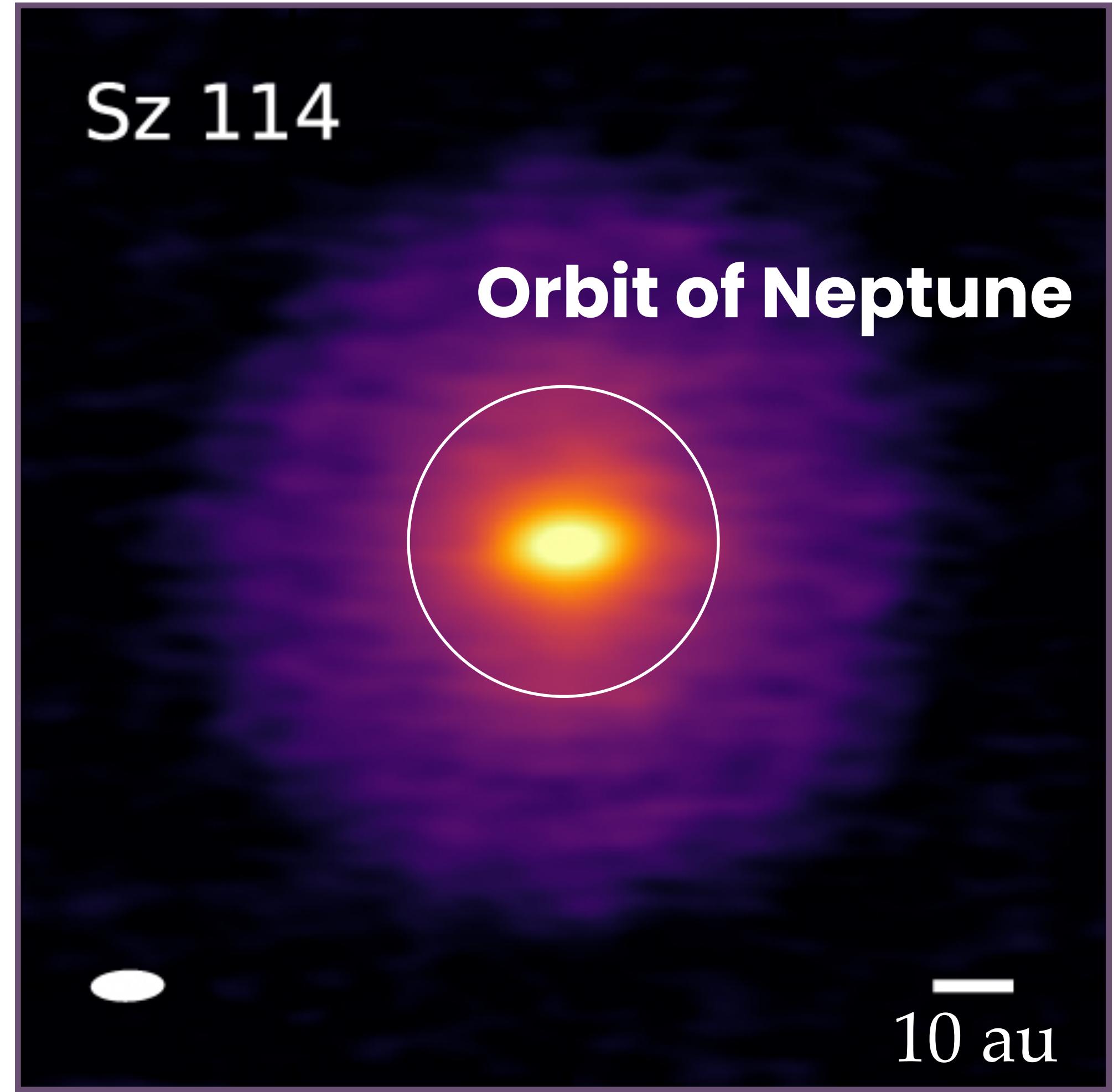
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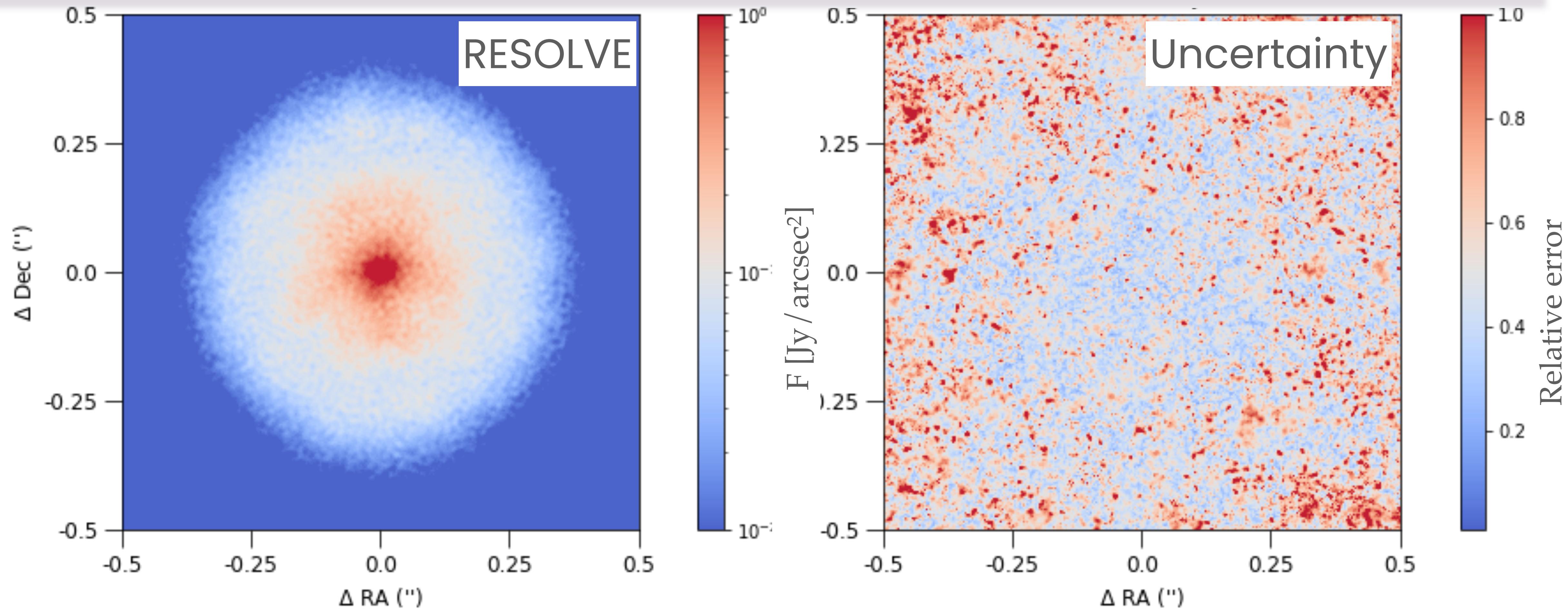
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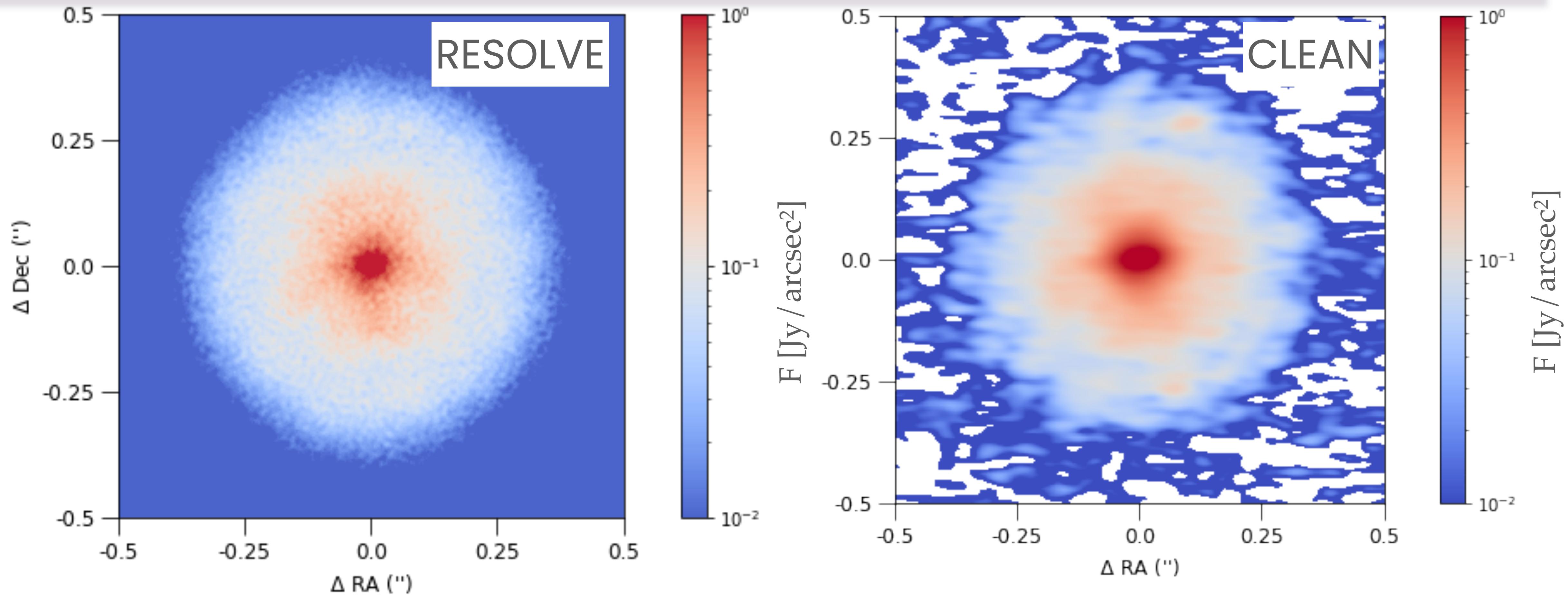
*Dust emission from planet-forming disk*

# Final image and uncertainty for Sz114 disk



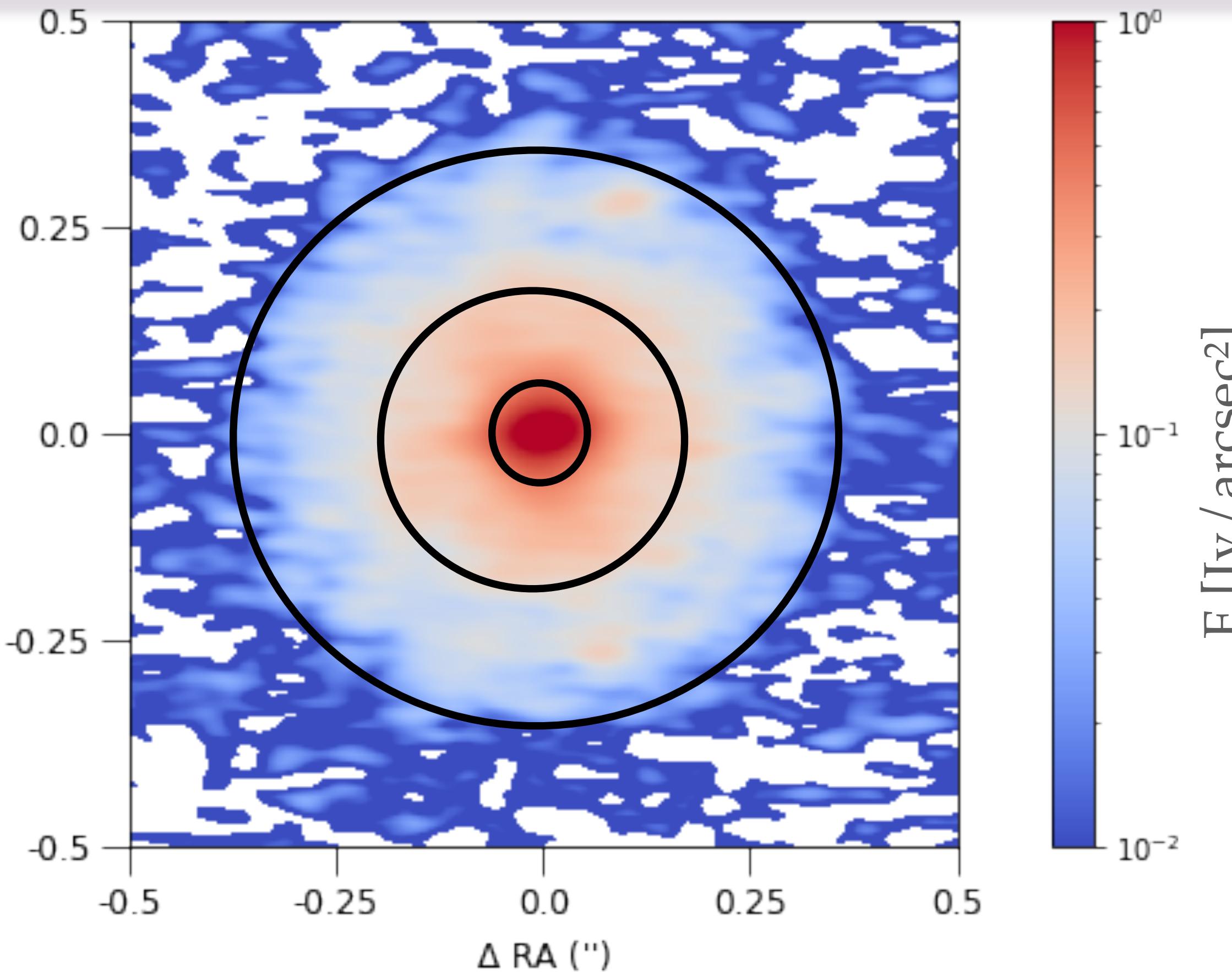
High-quality map of dust in protoplanetary disk obtained by RESOLVE

# Direct comparison of results for Sz 114 protoplanetary disk



RESOLVE reveals potential for ‘super-resolution’

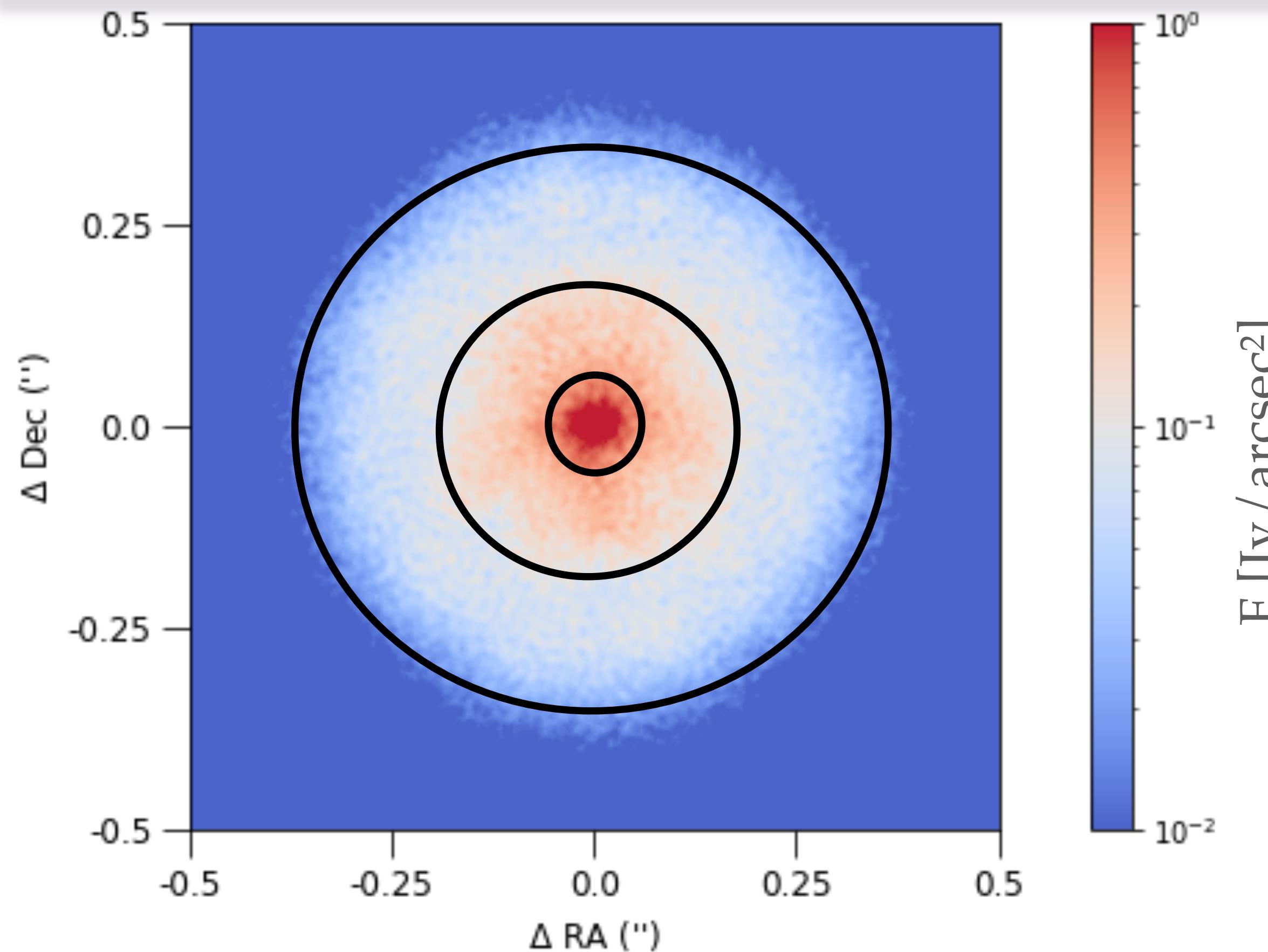
# Flux comparison of results for Sz 114 protoplanetary disk



$r$	CLEAN Flux [mJy]	RESOLVE Flux [mJy]	CLEAN/RESOLVE
$0.06''$	8.95	9.48	95 %
$0.15''$	22.53	23.21	97 %
$0.35''$	47.24	47.24	100 %

Comparable fluxes retrieved by CLEAN and RESOLVE

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- ✓ We successfully applied RESOLVE algorithm to ALMA data
- ✓ RESOLVE recovers flux with comparable accuracy to CLEAN in simulated data and real ALMA observations
- ✓ We achieve super-resolution image of planet-forming disk with RESOLVE along with uncertainty map
- ✓ RESOLVE presents a potential to push forward imaging procedures of interferometric observations and enhance/support capabilities of CLEAN