## 1 Challenge 1: optimize-self-reference

It's common to see this pattern

if f.1 calls itself. But f.1 in the closure is redundant: under any circumstances, it's the same thing as cp.2. So you can safely remove it from the closure and replace every f.1 in the body with cp.2.

## 2 Challenge 2: optimize-free

In Scheme, procedures are first-class citizens. So we need a uniform representation, namely closure, to pass procedures around. But sometimes this is not necessary if we only use a procedure locally. Say we have

after convert-closure and optimize-known-call it becomes

This is nonsense, but you get the idea. We can well write this in the following equivalent form

because the only thing we do to f.1 or g.1 is to apply it. If a procedure is used otherwise, we say it escapes. We can avoid allocating closures for non-escape procedures.

Firstly we need to recognize non-escape procedures. The following simple criteria should suffice: f.1 is non-escape if it's only used in the form (f\$1 f.1 ...). We add a pass uncover-well-known to record them in the (closures (...) (well-known (...) ...)) form. The name "well-known" echoes optimize-known-call.

Then we remove their corresponding closures. Only those without free variables can be removed.

Or is it? the above example does not satisfies this, but we can still remove f.1 and g.2. So if all the free variables are well-known, we can still remove it.

Or is it? consider the following example:

g.2 is well-known, but we cannot remove g.2 because of x.5, and it prevent us from removing f.1. So you need to do some simple analysis on the graph to identify truly well-known procedures.

You can also do something so called "lambda lifting", but with caveats. The idea is to pass free variables as additional parameters. For example, the above code becomes

This is not always an optimization because if you call a procedure with a lot of free variables many times, they are repeatedly moved to stack as parameters and fetched by the procedure. But a closure avoids this. This approach also requires "propagating" additional parameters across procedures.