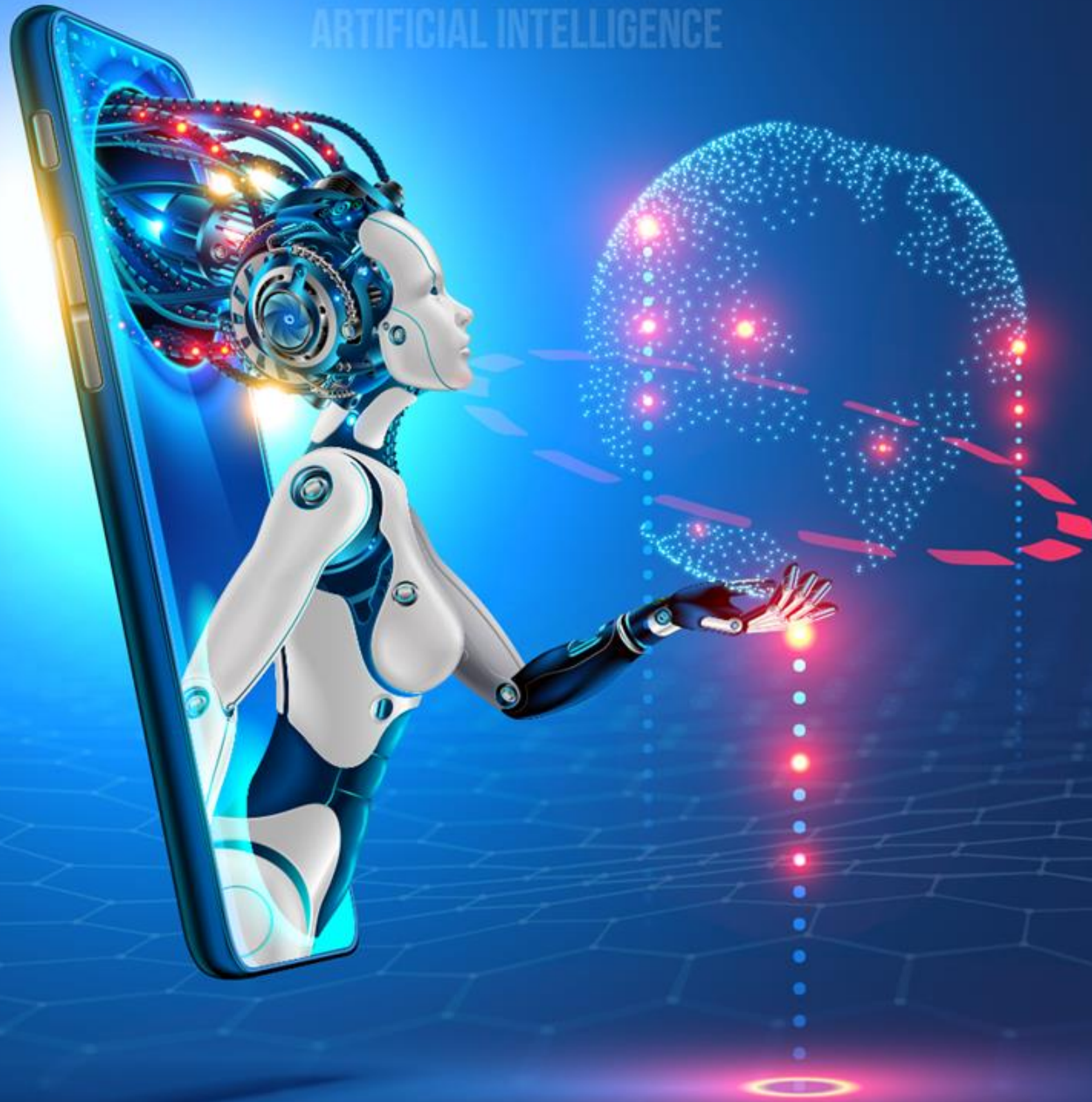


DATA AND
ARTIFICIAL INTELLIGENCE



Programming Basics and Data Analytics with Python

DATA AND ARTIFICIAL INTELLIGENCE



Mathematical Computing Using NumPy

Learning Objectives

By the end of this lesson, you will be able to:

- 🕒 Explain NumPy and its importance
- 🕒 Discuss the basics of NumPy, including its fundamental objects
- 🕒 Demonstrate how to create and print a NumPy array
- 🕒 Analyze and perform basic operations in NumPy
- 🕒 Utilize shape manipulation and copying methods
- 🕒 Demonstrate how to execute linear algebraic functions
- 🕒 Build basic programs using NumPy



DATA AND ARTIFICIAL INTELLIGENCE

NumPy

Quick Recap: Lists

Below are some of the properties of lists:

List

```
distance=[10,15,17,26]  
time=[.30,.47,.55,1.20]
```

Collection of values

Multiple types (heterogeneous)

Add, remove, update

Limitations of Lists

Though you can change individual values in a list, you cannot apply a mathematical operation over the entire list.

```
distance=[10,15,17,26]  
time=[.30,.47,.55,1.20]
```

```
speed=distance/time
```

 ← Mathematical operation over the entire distance and time lists

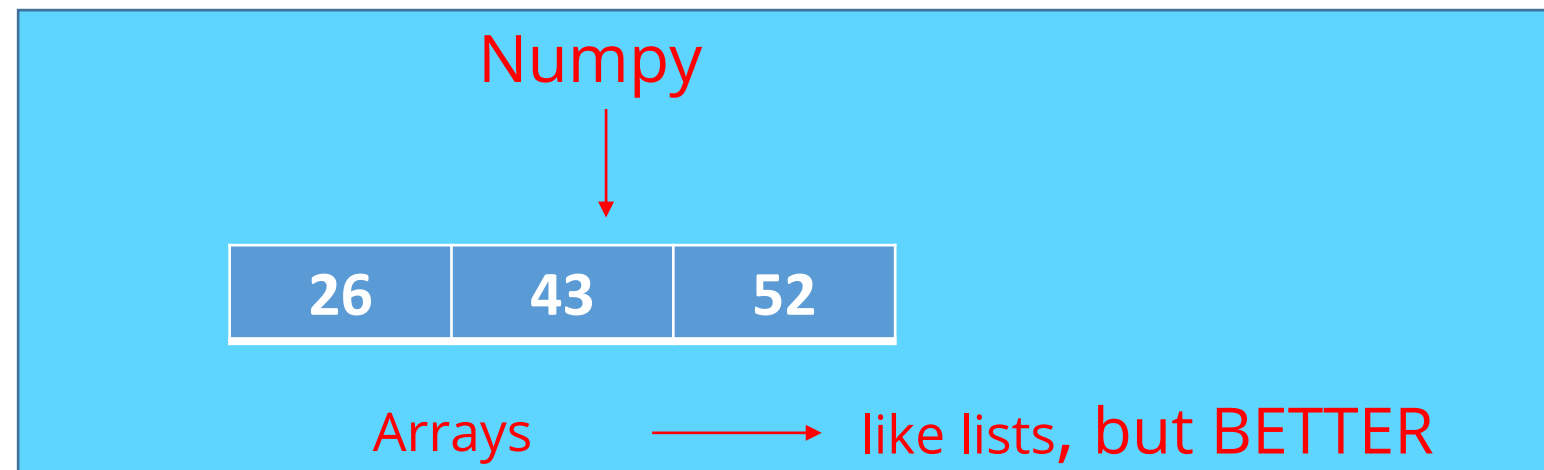
```
-----  
TypeError                                Traceback (most recent call last)  
<ipython-input-37-b779bad68500> in <module>()  
----> 1 speed=distance/time
```

```
TypeError: unsupported operand type(s) for /: 'list' and 'list'
```

 ← Error

Why NumPy?

Numerical Python (NumPy) supports multidimensional arrays over which you can easily apply mathematical operations.



```
distance=[10,15,17,26]  
time=[.30,.47,.55,1.20]
```

```
import numpy as np
```

 ← Import NumPy

```
np_distance = np.array(distance)  
np_time=np.array(time)  
speed=np_distance/np_time
```

 } Create "distance" and "time" NumPy arrays
← Mathematical function applied over the entire "distance" and "time" arrays

```
speed
```

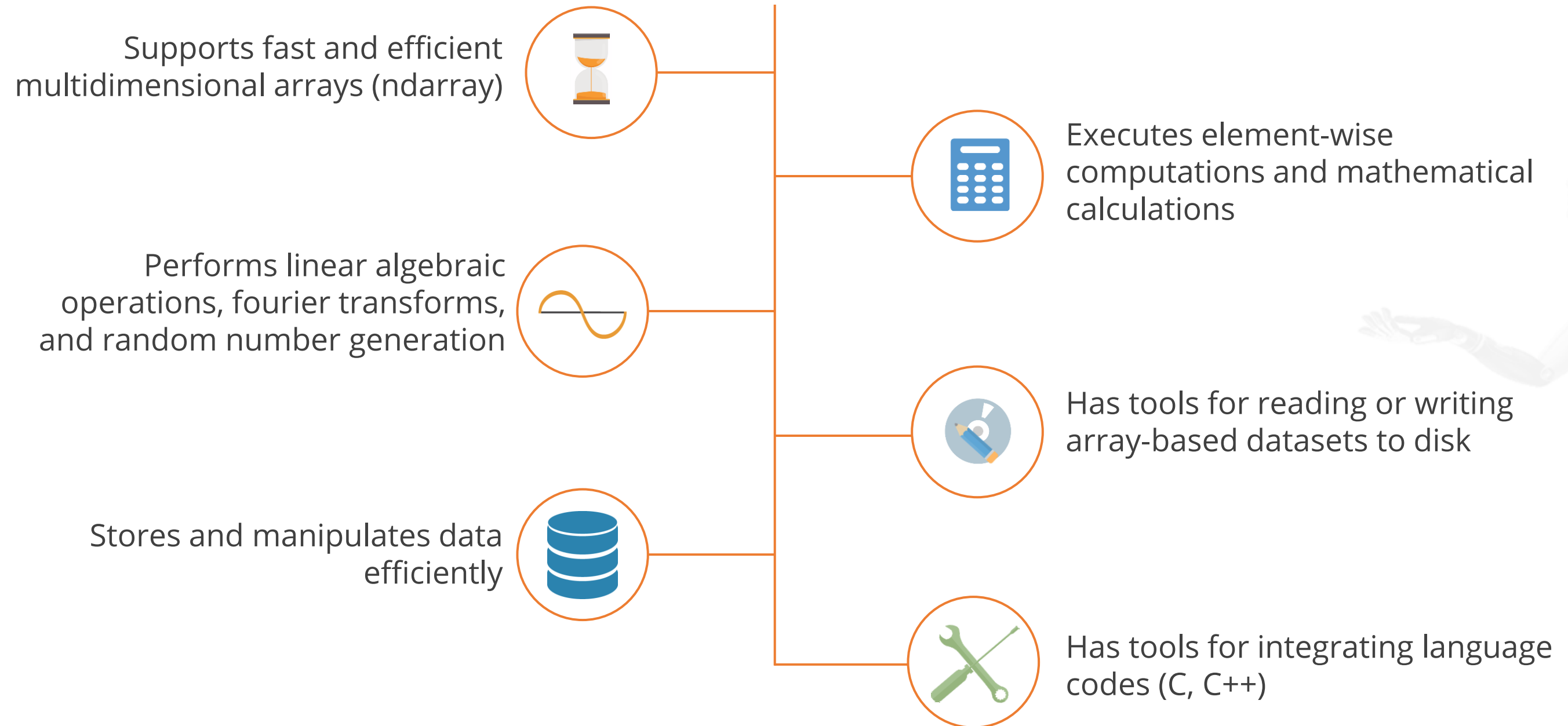
```
array([ 33.33333333,  31.91489362,  30.90909091,  21.66666667])
```

 ← Output

NumPy: Overview

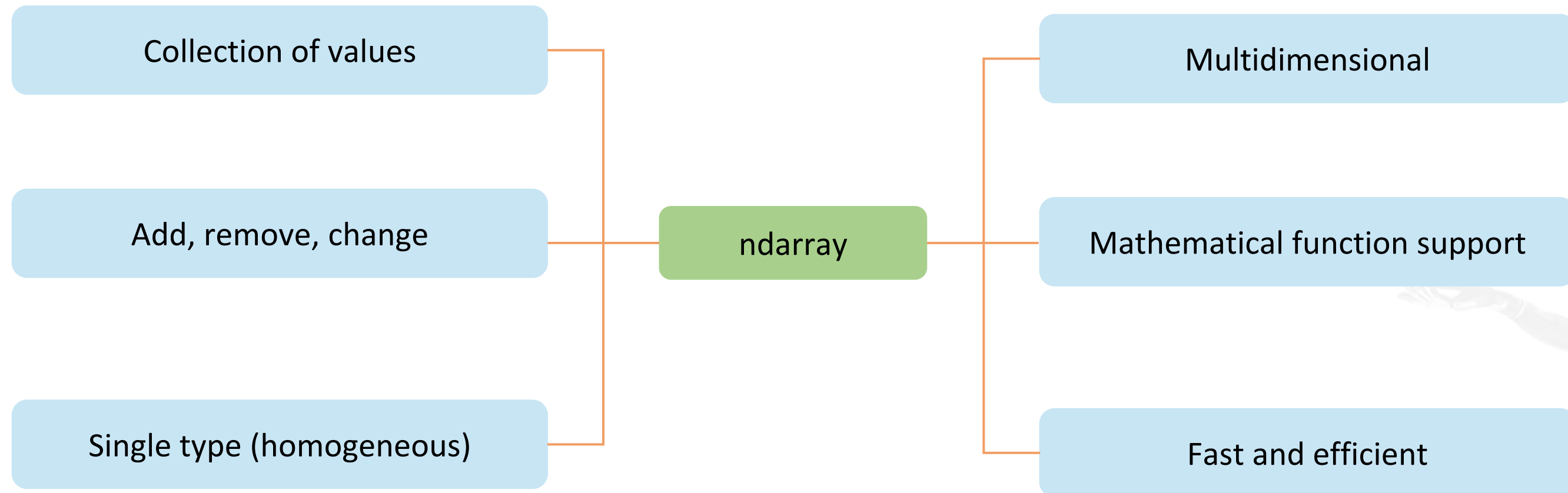
NumPy is the foundational package for mathematical computing in Python.

It has the following properties:



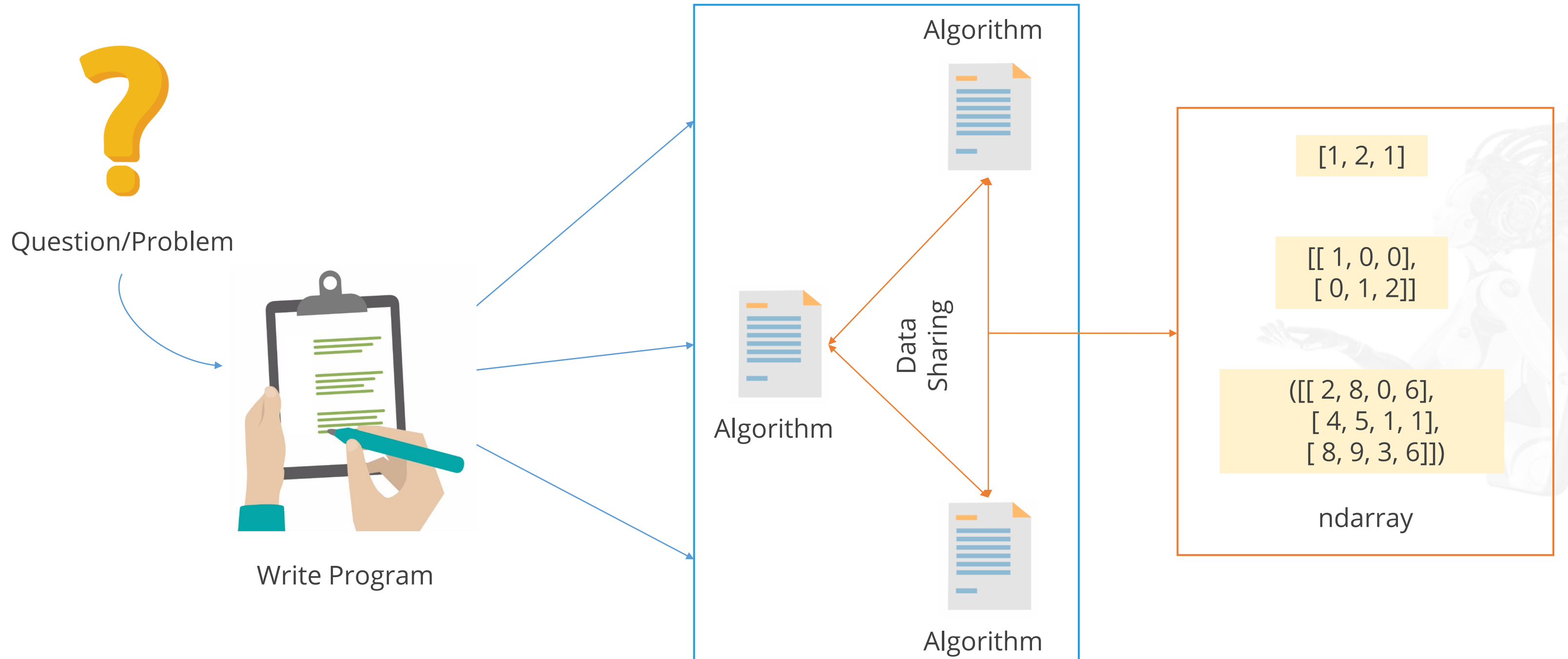
Properties of ndarray

An array in NumPy has the following properties:



Purpose of ndarray

The ndarray in Python is used as the primary container to exchange data between algorithms.



Types of Arrays

Arrays can be one-dimensional, two-dimensional, three-dimensional, or multidimensional.

One-Dimensional Array

Printed as rows

`array([5, 7, 9])`

1 axis
rank 1

Length = 3

5	7	9
0	1	2
x axis		

Two-Dimensional Array

Printed as matrices (2x3)

`array([[0, 1, 2],
[5, 6, 7]])`

2 axes
rank 2

Length = 3

y axis	0 (0,0)	1 (0,1)	2 (0,2)
	5 (1,0)	6 (1,1)	7 (1,2)
x axis			

Three-Dimensional Array

Printed as list of matrices (3x3x3)

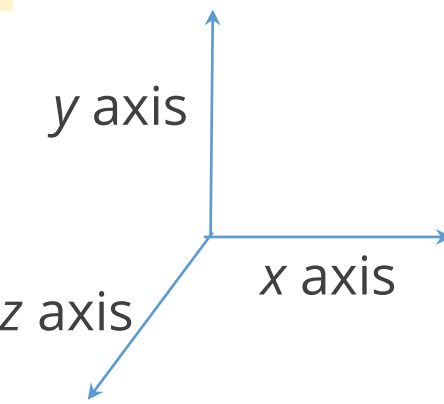
`array([[[0, 1, 2],
[3, 4, 5],
[6, 7, 8]],`

`[[9, 10, 11],
[12, 13, 14],
[15, 16, 17]],`

3 axes
rank 3

`[[18, 19, 20],
[21, 22, 23],
[24, 25, 26]])]`

Length = 3



Create and Print NumPy Arrays



Objective: Create the following types of NumPy arrays:

- One-dimensional array
- Array with zeros
- Array with ones
- Two-dimensional array
- Three-dimensional array

Access: To execute the practice, follow these steps:

- Go to the **PRACTICE LABS** tab on your LMS
- Click the **START LAB** button
- Click the **LAUNCH LAB** button to start the lab

ASSISTED PRACTICE

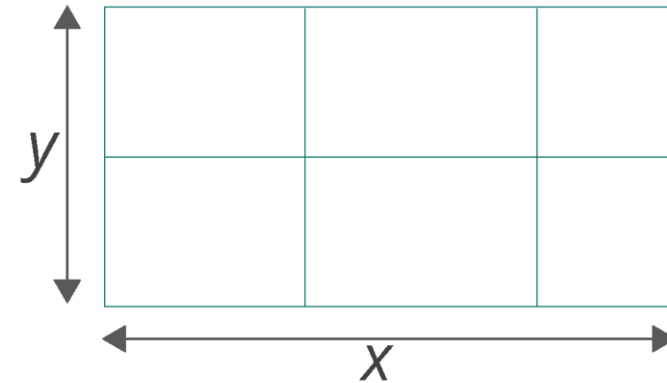
Class and Attributes of ndarray: .ndim

Numpy array class is ndarray, also referred to as numpy.ndarray. The attributes of ndarray are:

ndarray.ndim

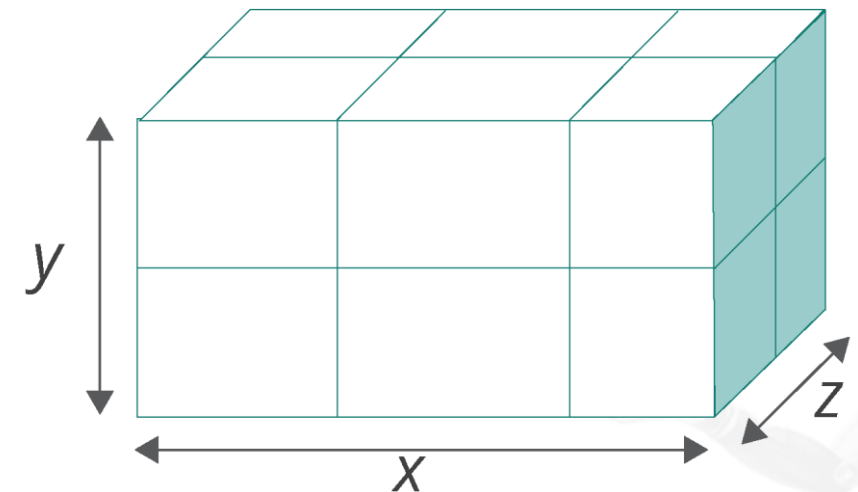
This refers to the number of axes (dimensions) of the array. It is also called the rank of the array.

ndarray.shape



Two axes or 2D array

ndarray.size



Three axes or 3D array

ndarray.dtype

Concept

Example

Class and Attributes of ndarray: .ndim

ndarray.ndim

The array np_city is one-dimensional, while the array np_city_with_state is two-dimensional.

ndarray.shape

```
In [108]: np_city = np.array(['NYC', 'LA', 'Miami', 'Houston'])
```

```
In [109]: np_city.ndim
```

```
Out[109]: 1
```

ndarray.size

```
In [110]: np_city_with_state = np.array([[ 'NYC', 'LA', 'Miami', 'Houston'], [ 'NY', 'CA', 'FL', 'TX']])
```

```
In [111]: np_city_with_state.ndim
```

```
Out[111]: 2
```

ndarray.dtype

Concept

Example

Class and Attributes of ndarray: .shape

Numpy array class is ndarray, also referred to as numpy.ndarray. The attributes of ndarray are:

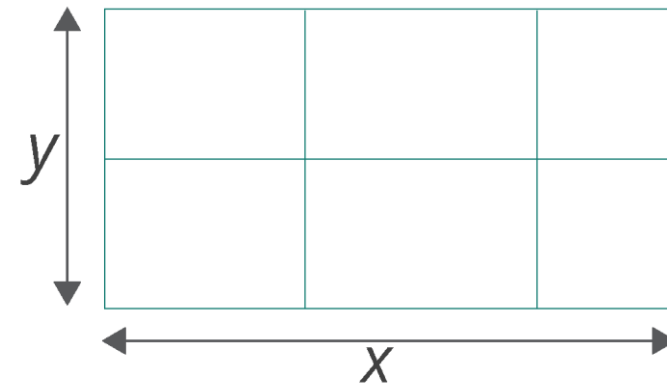
ndarray.ndim

ndarray.shape

ndarray.size

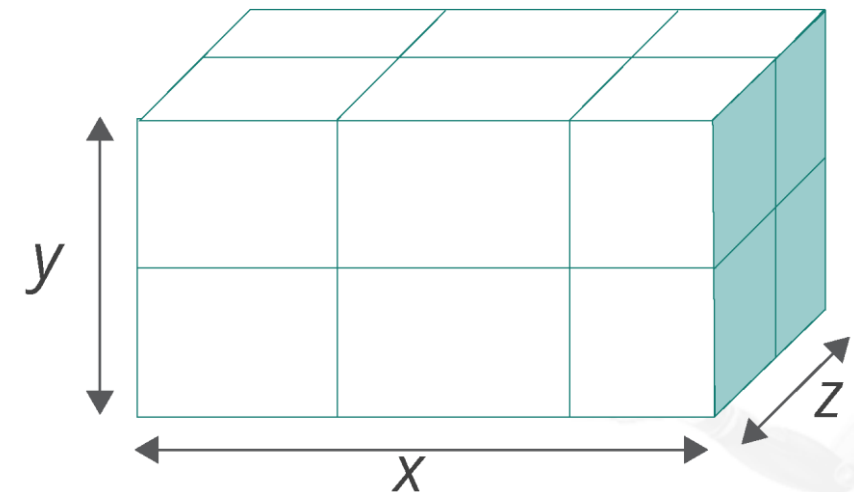
ndarray.dtype

This consists of a tuple of integers showing the size of the array in each dimension. The length of the shape tuple is the rank or ndim.



2 rows, 3 columns

Shape: (2, 3)



2 rows, 3 columns, 2 ranks

Shape: (2, 3, 2)

Concept

Example

Class and Attributes of ndarray: .shape

Numpy's array class is "ndarray," also referred to as "numpy.ndarray." The attributes of ndarray are:

ndarray.ndim

ndarray.shape

ndarray.size

ndarray.dtype

The shape tuple of both the arrays indicate their size along each dimension.

```
In [108]: np_city = np.array(['NYC', 'LA', 'Miami', 'Houston'])
```

```
In [110]: np_city_with_state = np.array([[ 'NYC', 'LA', 'Miami', 'Houston'], [ 'NY', 'CA', 'FL', 'TX']])
```

```
In [112]: np_city.shape
```

```
Out[112]: (4L,)
```

```
In [113]: np_city_with_state.shape
```

```
Out[113]: (2L, 4L)
```

Concept

Example

Class and Attributes of ndarray: .size

Numpy's array class is "ndarray," also referred to as "numpy.ndarray." The attributes of ndarray are:

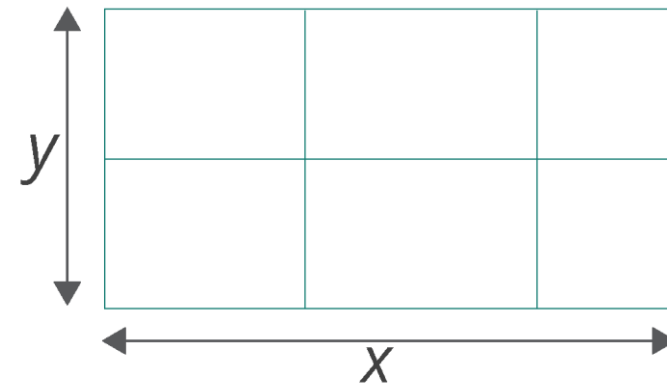
ndarray.ndim

ndarray.shape

ndarray.size

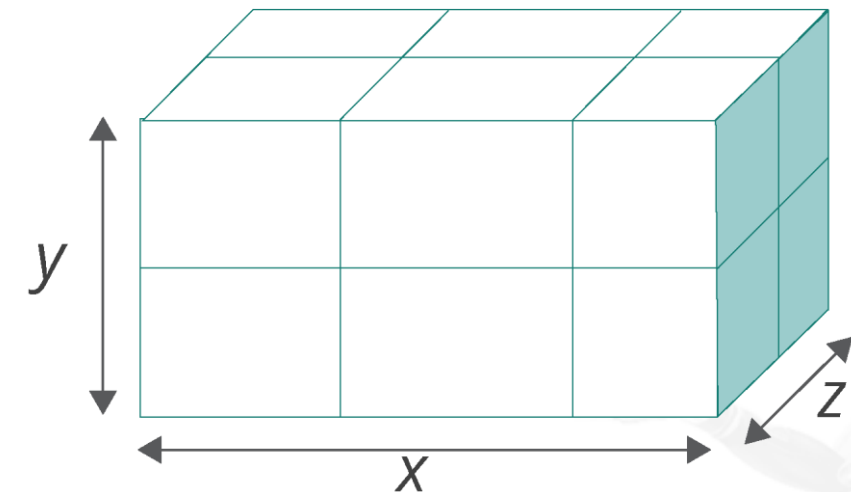
ndarray.dtype

It gives the total number of elements in the array. It is equal to the product of the elements of the shape tuple.



Array contains 6 elements

Array a = (2, 3)
Size = 6



Array contains 12 elements

Array b = (2, 3, 2)
Size = 12

Concept

Example

Class and Attributes of ndarray: .size

Numpy's array class is "ndarray," also referred to as "numpy.ndarray." The attributes of ndarray are:

ndarray.ndim

ndarray.shape

ndarray.size

ndarray.dtype

Look at the examples to see how shape tuples of the arrays are used to calculate their size.

```
In [112]: np_city.shape
```

```
Out[112]: (4L,)
```

```
In [113]: np_city_with_state.shape
```

```
Out[113]: (2L, 4L)
```

```
In [114]: np_city.size
```

```
Out[114]: 4
```

```
In [115]: np_city_with_state.size
```

```
Out[115]: 8
```

Concept

Example

Class and Attributes of ndarray: .dtype

Numpy's array class is "ndarray," also referred to as "numpy.ndarray." The attributes of ndarray are:

ndarray.ndim

ndarray.shape

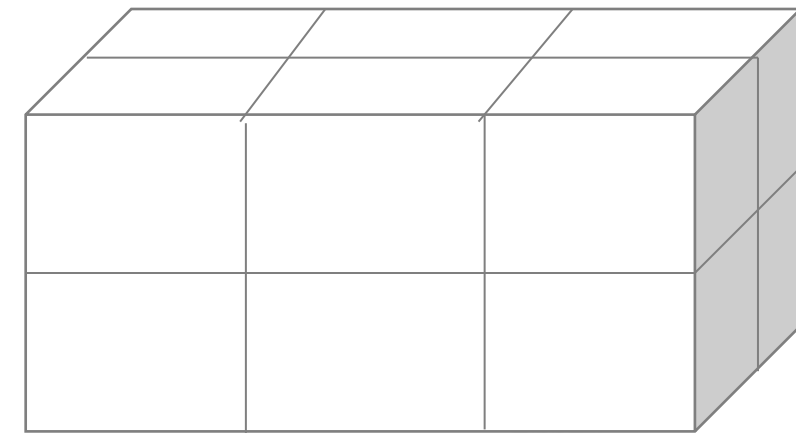
ndarray.size

ndarray.dtype

It's an object that describes the type of the elements in the array. It can be created or specified using Python.

Array contains integers

Array a = [3, 7, 4]
[2, 1, 0]



Array contains floats

Array b = [1.3, 5.2, 6.7]
[0.2, 8.1, 9.4]

[2.6, 4.2, 3.9]
[7.8, 3.4, 0.8]

Concept

Example

Class and Attributes of ndarray: .dtype

Numpy's array class is "ndarray," also referred to as "numpy.ndarray." The attributes of ndarray are:

ndarray.ndim

ndarray.shape

ndarray.size

ndarray.dtype

Both the arrays are of string data type (dtype) and the longest string is of length 7, which is Houston.

```
In [116]: np_city
```

```
Out[116]: array(['NYC', 'LA', 'Miami', 'Houston'],  
               dtype='<S7')
```

```
In [117]: np_city_with_state
```

```
Out[117]: array([[ 'NYC', 'LA', 'Miami', 'Houston'],  
                [ 'NY', 'CA', 'FL', 'TX']],  
               dtype='<S7')
```

```
In [118]: np_city_with_state.dtype
```

```
Out[118]: dtype('<S7')
```

Concept

Example

Operations

Basic Operations

Using the following operands, you can easily apply various mathematical, logical, and comparison operations on an array.

Mathematical Operations

Addition	+
Subtraction	-
Multiplication	*
Division	/
Exponentiation	**

Logical Operations

And	&
Or	
Not	~

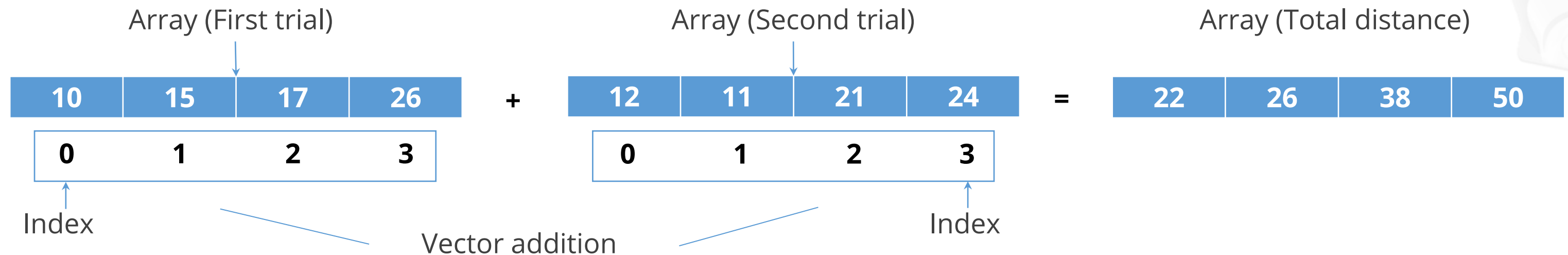
Comparison Operations

Greater	>
Greater or equal	>=
Less	<
Less or equal	<=
Equal	==
Not equal	!=

Basic Operations: Example

NumPy uses the indices of the elements in each array to carry out basic operations. In this case, where we are looking at a dataset of four cyclists during two trials, vector addition of the arrays gives the required output.

```
In [99]: first_trial_cyclist = [10, 15, 17, 26] ← First trial
In [100]: second_trial_cyclist = [12, 11, 21, 24] ← Second trial
In [101]: np_first_trial_cyclist = np.array(first_trial_cyclist)
In [102]: np_second_trial_cyclist = np.array(second_trial_cyclist)
In [103]: np_first_trial_cyclist + np_second_trial_cyclist ← Total distance
Out[103]: array([22, 26, 38, 50])
```



Executing Basic Operations in NumPy Array



Objective: Create a NumPy array and perform the following basic operations:

- Mathematical operations
- Comparison operations
- Logical operations

Access: To execute the practice, follow these steps:

- Go to the **PRACTICE LABS** tab on your LMS
- Click the **START LAB** button
- Click the **LAUNCH LAB** button to start the lab

ASSISTED PRACTICE

Performing Operations Using NumPy Array



Objective: Perform the following operations using NumPy array:

- Count the number of times each value appears in an array of integers
- Create a NumPy array `[[0, 1, 2], [3, 4, 5], [6, 7, 8],[9, 10, 11]]` and filter the elements greater than five
- Create a NumPy array having NaN(Not a Number) and print it; also, print the same array omitting all

elements which are NaN

Example: `array([nan, 1., 2., nan, 3., 4., 5.])`

- Create a 10x10 array with random values and find the minimum and maximum values

Access: To execute the practice, follow these steps:

- Go to the **PRACTICE LABS** tab on your LMS
- Click the **START LAB** button
- Click the **LAUNCH LAB** button to start the lab

UNASSISTED PRACTICE

Unassisted Practice: Operations Using NumPy Array

```
[5]: #Q5
import numpy
arr = numpy.array([0, 5, 4, 0, 4, 4, 3, 0, 0, 5, 2, 1, 1, 9])
print(numpy.bincount(arr))
```

← Counts the occurrence of each element

[4 2 1 1 3 2 0 0 0 1] ← Output

```
[6]: #Q6
import numpy as np
x = np.array([[ 0,  1,  2],[ 3,  4,  5],[ 6,  7,  8],[ 9, 10, 11]])
print('Our array is: ')
print(x)
print('\n')
# Now we will print the items greater than 5
print('The items greater than 5 are: ')
print(x[x > 5])
```

← Checks the elements greater than five

Our array is:

```
[[ 0  1  2]
 [ 3  4  5]
 [ 6  7  8]
 [ 9 10 11]]
```

The items greater than 5 are:

```
[ 6  7  8  9 10 11]
```

← Output

Unassisted Practice: Operations Using NumPy Array

```
[1]: import numpy
a = numpy.array([numpy.nan, 1,2,numpy.nan,3,4,5])
print(a)
print(a[~numpy.isnan(a)])
```

← NumPy array with NaN

← Eliminate the NaN from the array

```
[nan  1.  2. nan  3.  4.  5.]
[1.  2.  3.  4.  5.]
```

← Output

```
[2]: import numpy as np
Z = np.random.random((10,10))
Zmin, Zmax = Z.min(), Z.max()
print(Zmin, Zmax)
```

← NumPy array of random values

← Minimum and maximum value in the array

```
0.004119875834011522 0.9922366003764415
```

← Output

Accessing Array Elements: Indexing

You can access an entire row of an array by referencing its axis index.

1st set data 2nd set data

```
In [117]: cyclist_trials = np.array([[10, 15, 17, 26], [12, 11, 21, 24]])
```

 ← Create 2D array using cyclist trial data shown earlier

```
In [118]: first_trial = cyclist_trials[0]
```

 ← First trial data

```
In [119]: first_trial
```

```
Out[119]: array([10, 15, 17, 26])
```

```
In [120]: second_trial = cyclist_trials[1]
```

 ← Second trial data

```
In [121]: second_trial
```

```
Out[121]: array([12, 11, 21, 24])
```

2D array containing cyclists' data

10	15	17	26
12	11	21	24

← First trial (axis 0)

← Second trial (axis 1)

Accessing Array Elements: Indexing

You can refer the indices of the elements in an array to access them. You can also select a particular index of more than one axis at a time.

```
In [122]: first_cyclist_firstTrial = cyclist_trials[0][0] ← First cyclist: first trial data
```

```
In [123]: first_cyclist_firstTrial
```

```
Out[123]: 10
```

```
In [124]: first_cyclist_all_trials = cyclist_trials[:,0] ← First cyclist: all trial data  
(Use ":" to select all the rows of an array)
```

```
In [125]: first_cyclist_all_trials
```

```
Out[125]: array([10, 12])
```

Cyclist 1: first trial data →

(0, 0)	(0, 1)	(0, 2)	(0, 3)
10	15	17	26
12	11	21	24
(1, 0)	(1, 1)	(1, 2)	(1, 3)

Cyclist 1: all trials data

(0, 0)	(0, 1)	(0, 2)	(0, 3)
10	15	17	26
12	11	21	24
(1, 0)	(1, 1)	(1, 2)	(1, 3)

Accessing Array Elements: Slicing

Use the slicing method to access a range of values within an array.

```
In [152]: cyclist_trials.shape
```

```
Out[152]: (2L, 4L)
```

Shape of the array

```
In [153]: two_cyclist_trial_data=cyclist_trials[:,1:3]
```

```
In [154]: two_cyclist_trial_data
```

```
Out[154]: array([[15, 17],  
                [11, 21]])
```

Slicing the array data `[:, 1 : 3]`
where 1 is inclusive but 3 is not

Shape of the array

10	15	17	26
12	11	21	24

2 rows

4 columns

Use ":" to
select all rows

Slicing the array

10	15	17	26
12	11	21	24

0 1 2 3

Starting index (1)

Ending index (2)

Accessing Array Elements: Iteration

Use the iteration method to go through each data element present in the dataset.

```
In [117]: cyclist_trials = np.array([[10,15,17,26],[12,11,21,24]])
```

```
In [153]: two_cyclist_trial_data=cyclist_trials[:,1:3]
```

```
In [154]: two_cyclist_trial_data
```

```
Out[154]: array([[15, 17],  
                [11, 21]])
```

```
In [159]: for iterate_cyclist_trials_data in cyclist_trials:  
          print (iterate_cyclist_trials_data)
```

```
[10 15 17 26]  
[12 11 21 24]
```

```
In [160]: for iterate_two_cyclist_trial_data in two_cyclist_trial_data:  
          print (iterate_two_cyclist_trial_data)
```

```
[15 17]  
[11 21]
```

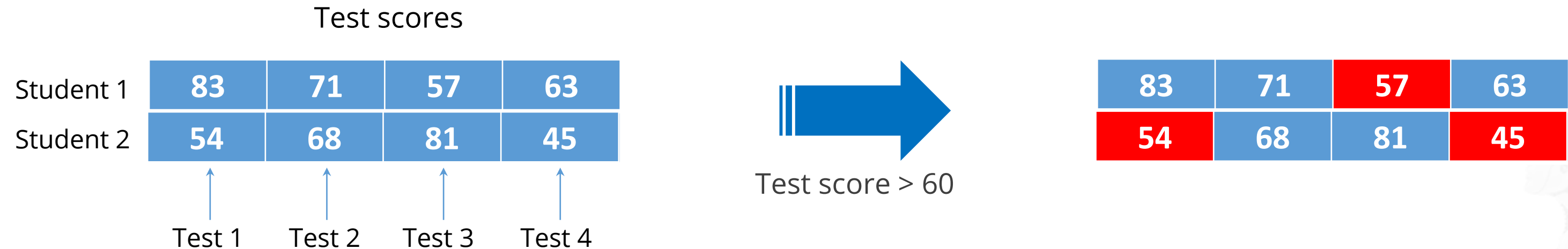
Iterate with “for loop” through the entire dataset

Iterate with “for loop” through the “two cyclist” datasets

Indexing With Boolean Arrays

Boolean arrays are useful when you need to select a dataset according to a set criteria.

Here, the original dataset contains test scores of two students. A Boolean array is used to choose only the scores that are above a given value.



```
In [234]: test_scores = np.array([[83, 71, 57, 63], [54, 68, 81, 45]])
```

```
In [235]: passing_score = test_scores > 60
```

Set the passing score

```
In [236]: passing_score
```

```
Out[236]: array([[ True,  True, False,  True],
                [False,  True,  True, False]], dtype=bool)
```

Shows data elements which fit the criteria (Boolean array)

```
In [237]: test_scores[passing_score]
```

Send passing score as an argument to test scores object

```
Out[237]: array([83, 71, 63, 68, 81])
```

Copy and Views

When working with arrays, data is copied into new arrays only in some cases.
Following are the three possible scenarios:



Simple Assignments

In this method, a variable is directly assigned the value of another variable. No new copy is made.

```
In [303]: NYC_Borough = np.array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Queens'])
```

```
In [294]: NYC_Borough
```

```
Out[294]: array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Queens'],  
              dtype='<S13')
```

← Original dataset

```
In [295]: Boroughs_in_NYC = NYC_Borough
```

```
In [296]: Boroughs_in_NYC
```

```
Out[296]: array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Queens'],  
              dtype='<S13')
```

← Assigned dataset

```
In [297]: Boroughs_in_NYC is NYC_Borough
```

```
Out[297]: True ← Shows both objects are the same
```



View or Shallow Copy



Deep Copy

Copy and Views



Simple Assignments



View or Shallow Copy



Deep Copy

A view, also referred to as a shallow copy, creates a new array object.

```
In [296]: Boroughs_in_NYC
```

```
Out[296]: array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Queens'],  
              dtype='<S13') ← Original dataset
```

```
In [298]: View_of_Borough_in_NYC = Boroughs_in_NYC.view()
```

```
In [299]: len(View_of_Borough_in_NYC)
```

```
Out[299]: 5
```

```
In [300]: View_of_Borough_in_NYC[4] = 'Central Park' ← Change value in "view" object
```

```
In [301]: View_of_Borough_in_NYC
```

```
Out[301]: array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Central Park'],  
              dtype='<S13')
```

```
In [302]: Boroughs_in_NYC
```

```
Out[302]: array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Central Park'],  
              dtype='<S13') ← Original dataset  
                             changed
```

Copy and Views



Simple Assignments



View or Shallow Copy



Deep Copy

Copy is also called deep copy because it entirely copies the original dataset. Any change in the copy will not affect the original dataset.

```
In [304]: Copy_of_NYC_Borough = NYC_Borough.copy()
```

```
In [305]: Copy_of_NYC_Borough is NYC_Borough
```

◀ Shows copy and original object are different

```
Out[305]: False
```

```
In [306]: Copy_of_NYC_Borough.base is NYC_Borough
```

◀ Shows copy object data is not owned by the original dataset

```
Out[306]: False
```

```
In [307]: Copy_of_NYC_Borough[4]='Central Park'
```

◀ Change value in copy

```
In [308]: NYC_Borough
```

```
Out[308]: array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Queens'],  
              dtype='<S13')
```

◀ Copy object changed

```
In [309]: Copy_of_NYC_Borough
```

```
Out[309]: array(['Manhattan', 'Bronx', 'Brooklyn', 'Staten Island', 'Central Park'],  
              dtype='<S13')
```

◀ Original dataset retained

Demonstrate the Use of Copy and Views



Objective: Demonstrate how the following copies and views are generated from a memory location:

- Simple Assignment
- View or Shallow Copy
- Deep Copy

Access: To execute the practice, follow these steps:

- Go to the **PRACTICE LABS** tab on your LMS
- Click the **START LAB** button
- Click the **LAUNCH LAB** button to start the lab

ASSISTED PRACTICE

Universal Functions (ufunc)

NumPy provides useful mathematical functions called universal functions. These functions operate element-wise on an array, producing another array as output. Some of these functions are:

sqrt function provides the square root of every element in the array.

sqrt

cos function gives cosine values for all elements in the array.

cos

floor function returns the largest integer value of every element in the array.

floor

exp function performs exponentiation on every element in the array.

exp

ufunc: Examples

```
In [186]: np_sqrt = np.sqrt([2,4,9,16])
```

Numbers for which square root will be calculated

```
In [187]: np_sqrt
```

```
Out[187]: array([ 1.41421356,  2.          ,  3.          ,  4.          ])
```

Square root values

```
In [188]: from numpy import pi  
np.cos(0)
```

Import pi*

```
Out[188]: 1.0
```

```
In [189]: np.sin(pi/2)
```

Trigonometric functions

```
Out[189]: 1.0
```

```
In [190]: np.cos(pi)
```

```
Out[190]: -1.0
```

```
In [191]: np.floor([1.5,1.6,2.7,3.3,1.1,-0.3,-1.4])
```

Return the floor of the input element-wise

```
Out[191]: array([ 1.,  1.,  2.,  3.,  1., -1., -2.])
```

```
In [192]: np.exp([0,1,5])
```

Exponential functions for complex mathematical calculations

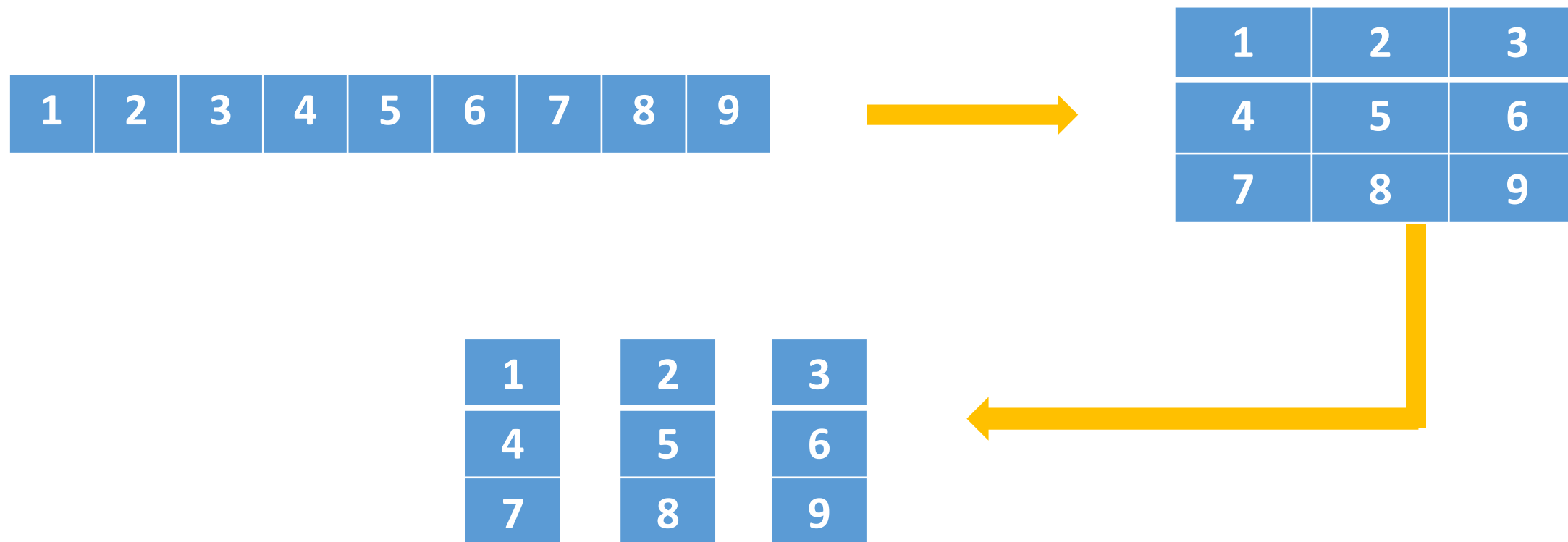
```
Out[192]: array([ 1.          ,  2.71828183, 148.4131591 ])
```



Shape Manipulation

You can use certain functions to manipulate the shape of an array.

The shape of an array can be changed according to the requirement using the NumPy library functions.

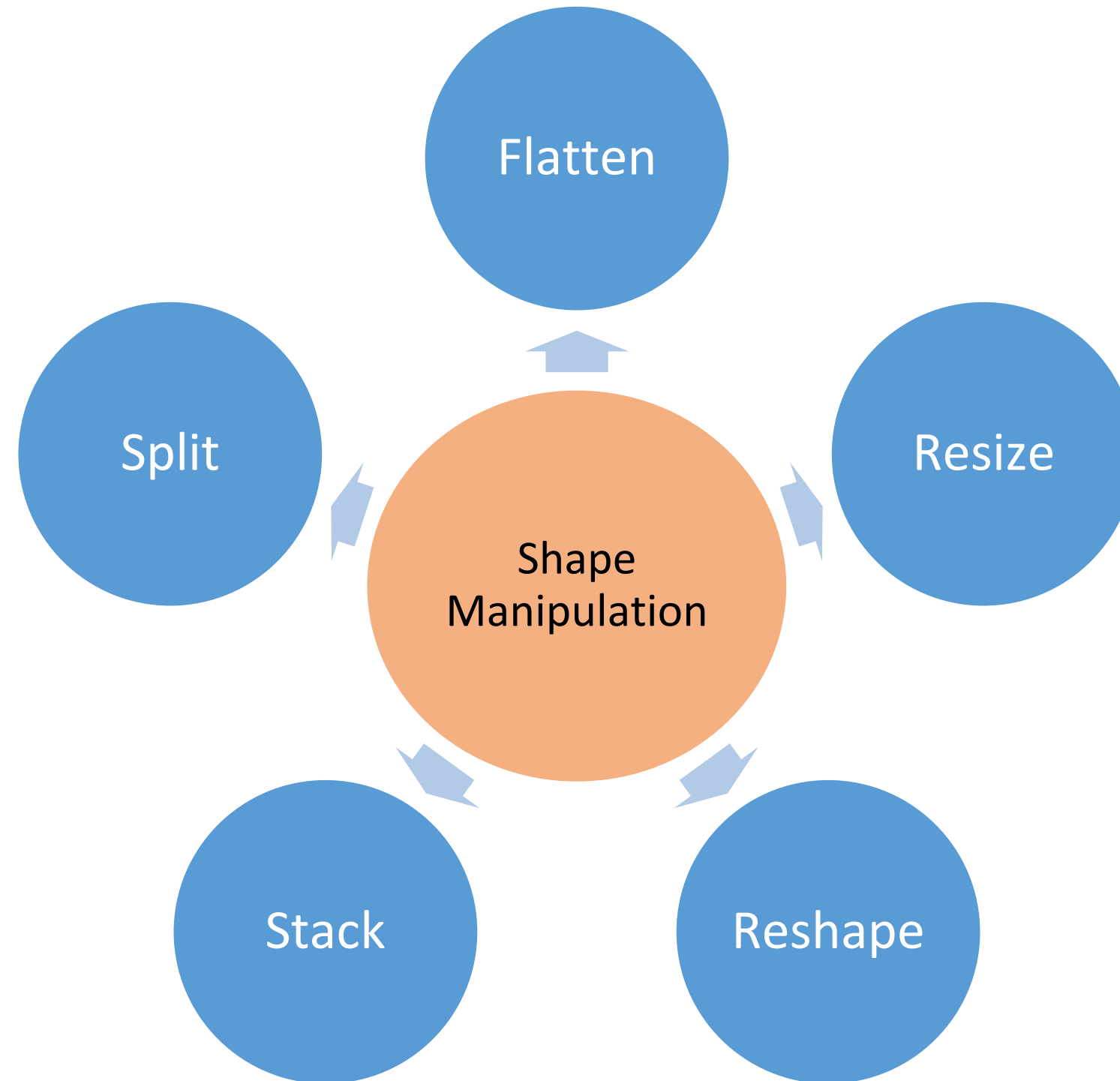


Array shape
manipulation
methods

Data
Wrangling

Shape Manipulation

Some common methods for manipulating shapes are:



Manipulate the Shape of an Array



Objective: Use common manipulation functions like `ravel`, `reshape`, `resize`, `hsplit`, and `hstack` to manipulate the shape of a NumPy array.

Access: To execute the practice, follow these steps:

- Go to the **PRACTICE LABS** tab on your LMS
- Click the **START LAB** button
- Click the **LAUNCH LAB** button to start the lab

ASSISTED PRACTICE

Broadcasting

NumPy uses broadcasting to carry out arithmetic operations between arrays of different shapes. In this method, NumPy automatically broadcasts the smaller array over the larger array.

```
In [9]: import numpy as np

In [10]: #Create two arrays of the same shape
array_a = np.array([2, 3, 5, 8])
array_b = np.array([.3, .3, .3, .3])

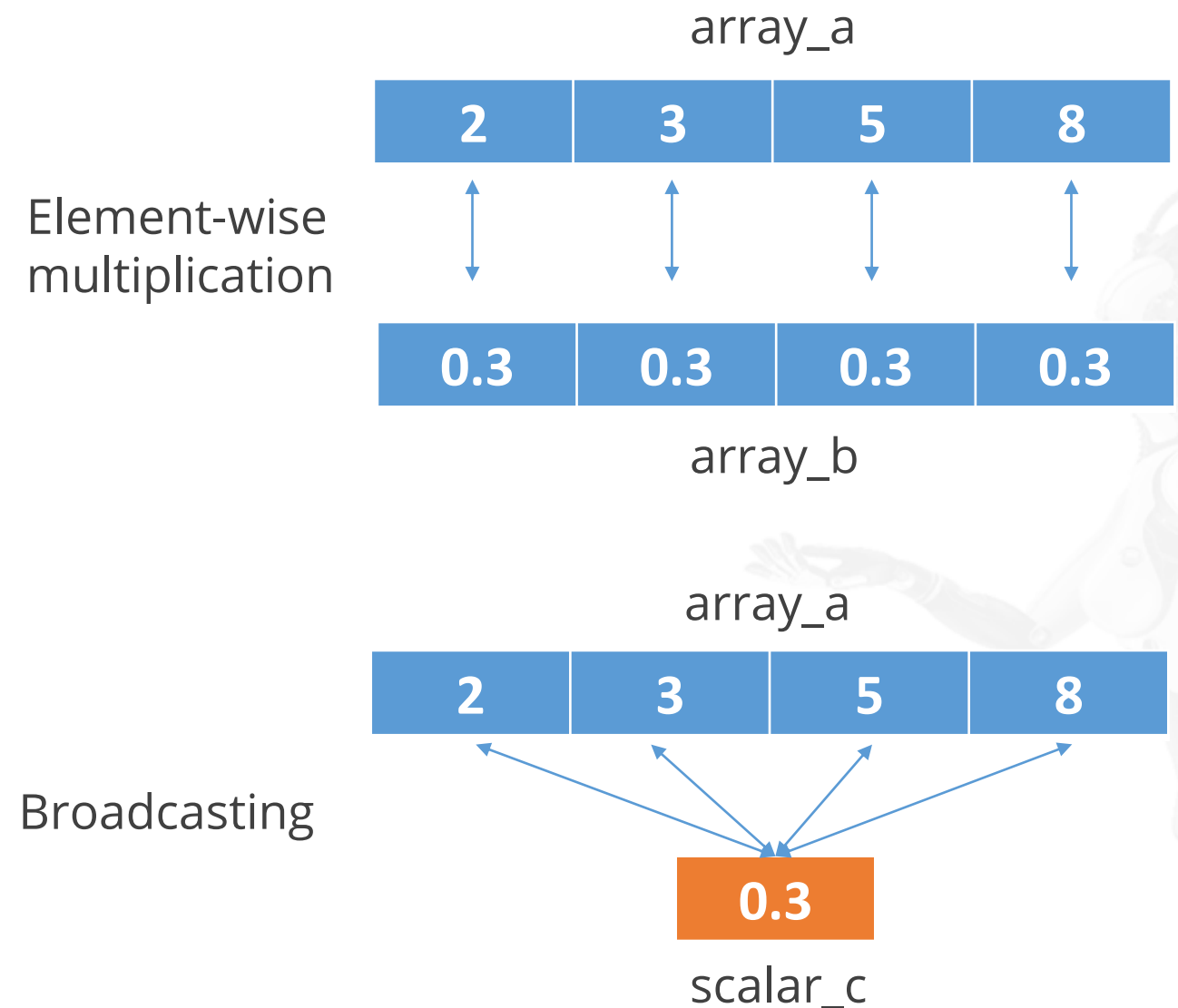
In [11]: #Multiply arrays
array_a * array_b

Out[11]: array([ 0.6,  0.9,  1.5,  2.4])

In [12]: #Create a variable with a scalar value
scalar_c = .3

In [13]: #Multiply 1D array with a scalar value
array_a * scalar_c

Out[13]: array([ 0.6,  0.9,  1.5,  2.4])
```



If the shape doesn't match with array_a, NumPy doesn't have to create copies of scalar values. Instead, broadcast scalar value over the entire array to find the product.

Broadcasting: Constraints

Though broadcasting can help carry out mathematical operations between different-shaped arrays, they are subject to certain constraints as listed below:

```
In [9]: import numpy as np
```

```
In [10]: #Create two arrays of the same shape
array_a = np.array([2, 3, 5, 8])
array_b = np.array([.3, .3, .3, .3])
```

```
In [11]: #Multiply arrays
array_a * array_b
```

```
Out[11]: array([ 0.6,  0.9,  1.5,  2.4])
```

```
In [14]: #Create array of a different shape
array_d = np.array([4, 3])
```

```
In [15]: array_a * array_d
```

```
-----
ValueError                                Traceback (most recent call last)
<ipython-input-15-43adcf6f7a54> in <module>()
----> 1 array_a * array_d

ValueError: operands could not be broadcast together with shapes (4,) (2,)
```

- When NumPy operates on two arrays, it compares their shapes element-wise. It finds these shapes compatible only if:
 - Their dimensions are the same or
 - One of them has a dimension of size 1
- If these conditions are not met, a `ValueError` is thrown, indicating that the arrays have incompatible shapes.

Broadcasting: Example

Let's look at an example to see how broadcasting works to calculate the number of working hours of a worker per day in a certain week.

```
In [246]: np_week_one = np.array([105, 135, 195, 120, 165])  
np_week_two = np.array([123, 156, 230, 200, 147])
```

← Week one earnings
← Week two earnings

```
In [247]: total_earning = np_week_one + np_week_two
```

```
In [248]: total_earning
```

```
Out[248]: array([228, 291, 425, 320, 312])
```

← Total earning for 2 weeks

```
In [249]: np_week_one_hrs = np_week_one / 15
```

← Calculate week one hours

```
In [250]: np_week_one_hrs
```

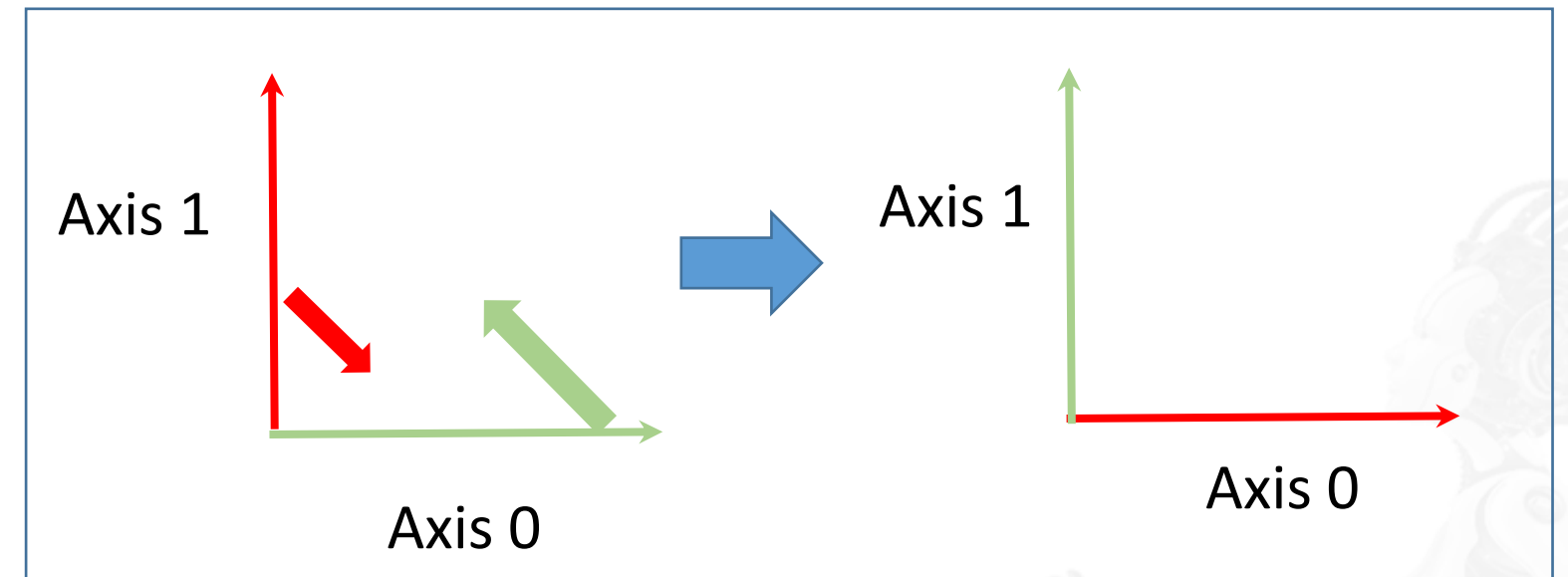
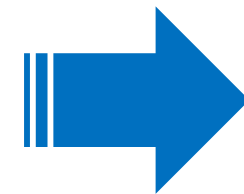
```
Out[250]: array([ 7,  9, 13,  8, 11])
```

← Number of working hours per day in week one

Linear Algebra: Transpose

NumPy can carry out linear algebraic functions as well. The `transpose()` function can help you interchange rows as columns, and vice-versa.

transpose()			
83	71	57	63
54	68	81	45



```
In [397]: test_scores = np.array([[83, 71, 57, 63], [54, 68, 81, 45]])
```

```
In [398]: test_scores.transpose()
```

```
Out[398]: array([[83, 54],  
                [71, 68],  
                [57, 81],  
                [63, 45]])
```

Linear Algebra: Inverse and Trace Functions

Using NumPy, you can also find the inverse of an array and add its diagonal data elements.

np.linalg.inv()

```
In [411]: inverse_array = np.array([[10, 20], [15, 25]])
```

```
In [412]: np.linalg.inv(inverse_array)
```

```
Out[412]: array([[ -0.5,  0.4],  
                [ 0.3, -0.2]])
```

Inverse of the given array

* Can be applied **only** on a square matrix

np.trace()

```
In [420]: trace_array = np.array([[10, 20], [22, 31]])
```

```
In [421]: np.trace(trace_array)
```

```
Out[421]: 41
```

Sum of diagonal elements "10" and "31"

Key Takeaways

You are now able to:

- 🕒 Explain NumPy and its importance
- 🕒 Discuss the basics of NumPy, including its fundamental objects
- 🕒 Demonstrate how to create and print a NumPy array
- 🕒 Analyze and perform basic operations in NumPy
- 🕒 Utilize shape manipulation and copying methods
- 🕒 Demonstrate how to execute linear algebraic functions
- 🕒 Build basic programs using NumPy





Knowledge Check

Knowledge Check

1

Which of the following arrays is valid?

- a. [1, 0.3, 8, 6.4]
- b. ["Lucy", 16, "Susan", 23, "Carrie", 37]
- c. [True, False, "False", True]
- d. [3.14j, 7.3j, 5.1j, 2j]



Knowledge Check

1

Which of the following arrays is valid?

- a. [1, 0.3, 8, 6.4]
- b. ["Lucy", 16, "Susan", 23, "Carrie", 37]
- c. [True, False, "False", True]
- d. [3.14j, 7.3j, 5.1j, 2j]



The correct answer is **d**

A NumPy ndarray can hold only a single data type, which makes it homogenous. NumPy supports integers, floats, Booleans, and even complex numbers. Of all the options provided, only the array containing complex numbers is homogenous. All the other options contain more than one data type.

Knowledge Check

2

Which function is most useful to convert a multidimensional array into a one-dimensional array?

- a. `ravel()`
- b. `reshape()`
- c. `resize()` and `reshape()`
- d. All of the above



Knowledge Check

2

Which function is most useful to convert a multidimensional array into a one-dimensional array?

- a. `ravel()`
- b. `reshape()`
- c. `resize()` and `reshape()`
- d. All of the above



The correct answer is **a**

The function `ravel()` is used to convert a multidimensional array into a one-dimensional array. Though `reshape()` also functions in a similar way, it creates a new array instead of transforming the input array.

Knowledge Check

3

The `np.trace()` method gives the sum of ____.

- a. the entire array
- b. the diagonal elements from left to right
- c. the diagonal elements from right to left
- d. consecutive rows of an array



Knowledge Check

3

The `np.trace()` method gives the sum of ____.

- a. the entire array
- b. the diagonal elements from left to right
- c. the diagonal elements from right to left
- d. consecutive rows of an array



The correct answer is **b**

The `trace()` function is used to find the sum of the diagonal elements in an array. It is carried out in an incremental order of the indices. Therefore, it can only add diagonal values from left to right and not vice-versa.

Knowledge Check

4

The function `np.transpose()` when applied on a one-dimensional array gives ____.

- a. a reverse array
- b. an unchanged original array
- c. an inverse array
- d. all elements with zeros



Knowledge
Check

4

The function `np.transpose()` when applied on a one-dimensional array gives ____.

- a. a reverse array
- b. an unchanged original array
- c. an inverse array
- d. all elements with zeros



The correct answer is **b**

Transposing a one-dimensional array does not change it in any way. It returns an unchanged view of the original array.

Country GDP



Evaluate the dataset containing the GDPs of different countries to:

- Find and print the name of the country with the highest GDP
- Find and print the name of the country with the lowest GDP
- Print out text and input values iteratively
- Print out the entire list of the countries with their GDPs
- Print the highest GDP value, lowest GDP value, mean GDP value, standardized GDP value, and the sum of all the GDPs

Olympic 2012 Medal Tally



Evaluate the dataset of the Summer Olympics, London 2012, to:

- Find and print the name of the country that won maximum number of gold medals
- Find and print the countries who won more than 20 gold medals
- Print the medal tally
- Print each country name with the corresponding number of gold medals
- Print each country name with the total number of medals won

Thank You