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Assignment 4

The following pictures are the regression coefficients from the most accurate models predicting MPG between USA, Germany and Japan.

```
> leaps.lars(both=T,xmat=Auto.mat.usa2nd,yvec=Auto.mat.usa[,1],ncheck=5,int=F)
[1] 1
[1] "Press= 1048.0470934059"
[1] "MPSE= 4.53700040435454"
[1] "Cp= 7.78048836274499"
      Intercept      displacement      weight
      2.344534e+02      -4.656436e-01      3.314722e-02
      acceleration      year      cylindersweight
      -6.841730e+00      -4.514745e+00      5.360273e-04
cylindersacceleration      cylindersyear      displacementdisplacement
      2.319231e-01      -6.928483e-02      1.228204e-04
      displacementyear      horsepoweracceleration      weightyear
      5.278304e-03      -3.096444e-03      -5.351085e-04
      accelerationyear      yearyear
      7.166771e-02      3.237503e-02
[1] "LEAPS CORRELATION 0.955326000142054"
> leaps.lars(both=T,xmat=Auto.mat.germany2nd,yvec=Auto.mat.germany[,1],ncheck=5,int=F)
[1] 1
[1] "Press= 528.995880853274"
[1] "MPSE= 9.28062948865393"
[1] "Cp= -0.213330316766488"
      Intercept      horsepower      weight      year      cylindersweight
      3.850112e+02      2.364405e+00      -7.229320e-02      -1.017014e+01      8.212186e-03
cylindersyear      displacementyear      horsepoweryear      weightweight      weightyear
      -3.168925e-01      -1.053403e-03      -3.274818e-02      -6.778729e-06      9.297024e-04
      yearyear
      8.568144e-02
[1] "LEAPS CORRELATION 0.932441018514054"
> leaps.lars(both=T,xmat=Auto.mat.japan2nd,yvec=Auto.mat.japan[,1],ncheck=5,int=F)
[1] 1
[1] "Press= 751.265259710616"
[1] "MPSE= 10.434239718203"
[1] "Cp= 5.23147464526383"
      Intercept      cylinders      cylinderscylinders
      -1.142973e+02      5.421060e+01      -5.529733e+00
displacementacceleration      horsepoweracceleration      horsepoweryear
      -1.099489e-02      -2.665846e-02      4.829747e-03
      accelerationyear
      3.137588e-02
[1] "LEAPS CORRELATION 0.882593532687259"
```

Now, here are the coefficients used for the whole model disregarding origins.

```
> leaps.lars(both=T,xmat=Auto.mat2nd,yvec=Auto.mat[,1],ncheck=5,int=F)
[1] 1
[1] "Press= 2965.80019718738"
[1] "MPSE= 7.82533033558675"
[1] "Cp= 5.48237932178478"
      Intercept      displacement      acceleration
      3.672205e+02      -1.671374e-01      -6.112244e+00
      year      cylinderscylinders      cylindersweight
      -7.848981e+00      -3.463469e-01      1.436651e-03
displacementhorsepower      displacementyear      horsepoweryear
      2.187828e-04      1.652216e-03      -1.542533e-03
      weightyear accelerationacceleration      accelerationyear
      -1.596952e-04      4.104226e-02      6.029007e-02
      yearyear
      5.241731e-02
[1] "LEAPS CORRELATION 0.94044225990666"
```

Upon looking at the beta coefficients, I see that *year* is negatively correlated with MPG, but *yearyear* is positively correlated with MPG. *yearyear* is $\text{year} \times \text{year}$, which means it's year^2 , so the values multiplying with the smaller beta coefficient end up being larger -- meaning *year* is actually positively correlated with MPG.

Because our data is sorted with combined data, i.e. *displacementyear* (2nd order matrix)..., it is hard to tell from a glance which independent variables have more bearing on the model than others when a lot of the beta coefficients work in inverse ways like *yearyear* and *year*.

So, I re-inputted the matrix as a 1st order matrix to parse out independent variables' influence on each model. These were my results for USA, Germany, Japan:

```
      cylinders displacement      horsepower      weight acceleration      year
-0.997485969 -0.005917714 -0.010321260 -0.003423843 -0.447890391 0.625054647
[1] "LARS CORRELATION 0.922642771751773"
> leaps.lars(both=T,xmat=Auto.mat.germany[, -c(1,8)],yvec=Auto.mat.germany[,1],ncheck=5,int=F)
[1] 1
[1] "Press= 934.841417724904"
[1] "MPSE= 14.6068971519516"
[1] "Cp= 3.44682356342066"
      Intercept      weight acceleration      year
-44.53576635 -0.00889359 0.65862449 1.09307398
[1] "LEAPS CORRELATION 0.848025506034959"
```

```
> leaps.lars(both=T,xmat=Auto.mat.japan[,-c(1,8)],yvec=Auto.mat.japan[,1],ncheck=5,int=F)
[1] 1
[1] "Press= 1020.39165512687"
[1] "MPSE= 13.7890764206334"
[1] "Cp= 3.6141142306042"
Intercept displacement      weight acceleration      year
-25.51321316  0.06138308 -0.01366633  0.36850321  0.95626150
```

The models are less accurate, but it is clearer which variable has more impact. Throughout the data, it seems Year has the strongest positive correlation with MPG, while the other variables are mostly negatively correlated.

USA: Year is positively correlated; Cylinders, displacement, horsepower, weight, and acceleration are negatively correlated.

Germany: Year and acceleration are positively correlated; Weight is negatively correlated (weight has the largest values from 3,000-4,000).

Japan: Year, acceleration and displacement are positively correlated; Weight is negatively correlated (Again, weight has the largest values in the dataset ranging from 3,000 to 4,000)

It makes sense that Year would be positively correlated with MPG and weight be negatively correlated with MPG across all data.

It's interesting that the USA model, which was most accurate, takes cylinders and horsepower, whereas Japan and Germany don't. Because of the negative correlation, it makes me think of the muscle cars America has made famous-mustangs, stingrays, etc.-medium bodied gas guzzlers.

The German model seems quite basic in terms of inputs compared to the other models.

Japan is interesting because it has a positive correlation with displacement, which makes me wonder if they had a different method of engine displacement.