

Combining 3D Shape, Color, and Motion for Robust Anytime Tracking

Paper by Held, Levinson, Thrun, and Savarese [1]

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Seminar Current Topics in Computer Vision and Machine Learning

RWTH Aachen University



Agenda

- 1 Motivation
- 2 Baseline Methods
- 3 Probabilistic Model
- 4 Searching the State Space
- 5 Evaluation
- 6 Conclusion



Tracking for Autonomous Cars

Chances

- Free use of driving time
 - Help disabled persons
 - Computers do not get tired or drunk
 - Faster reaction time
- ⇒ Safe 26k lives per year in EU



Tracking for Autonomous Cars

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Challenges

- Precise tracking
- Robustness
- Occlusion
- Real time



Tracking for Autonomous Cars

Subtasks of Tracking

- Segment sensor data into objects
- Associate objects in successive frames
- Position and velocity estimation
- Object and trajectory classification



Tracking for Autonomous Cars

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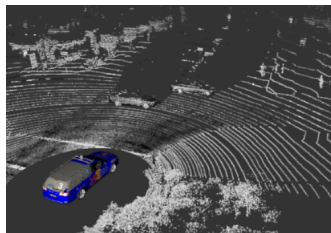
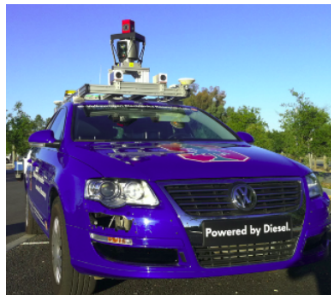
Topic of this presentation

Position and velocity estimation

Given Sensor Data

Sensor

- Dense 3D laser sensor
- Generates point cloud
- Additional panorama image
- Similar to stereo cameras
but more precise and expensive



[2]

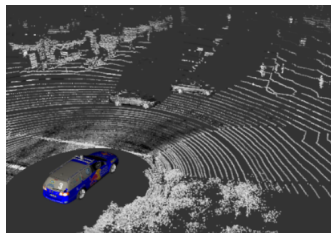
Given Sensor Data

Sensor

- Dense 3D laser sensor
- Generates point cloud
- Additional panorama image
- Similar to stereo cameras
but more precise and expensive

Given for us

- Point clouds of detected objects
- Association between frames
already done



[2]



Teaser Paper Ideas

How to find a precise alignment?

- Utilize whole object shape
- Additional cues from color
- Use motion model



Teaser Paper Ideas

How to find a precise alignment?

- Utilize whole object shape
- Additional cues from color
- Use motion model

How to search the state space fast?

- Histogram with coarse initial resolution
- Refine resolution important areas
- Consider resolution in the probabilistic model

Baseline Methods



[3]

Kalman Filter

Baseline Methods

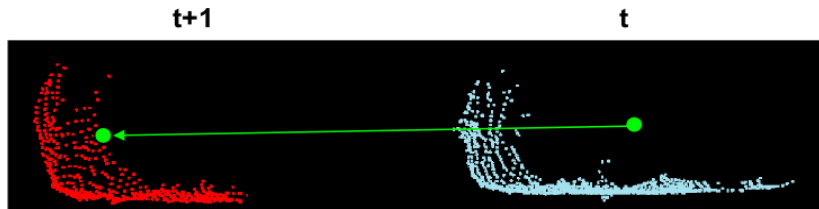


[3]

Kalman Filter

- Aligns centroids

Baseline Methods

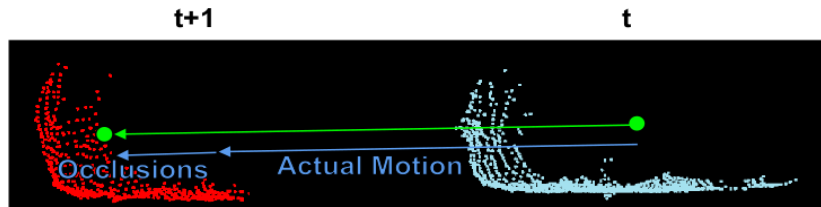


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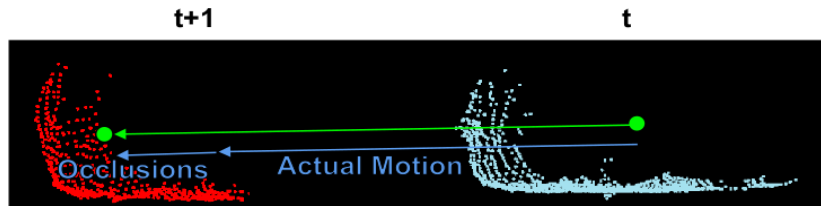


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Kalman Filter

- Aligns centroids
- Problems with occlusion

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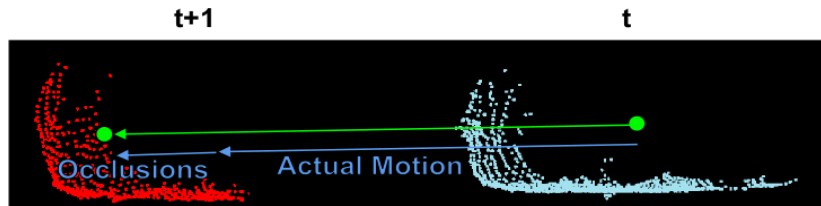


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Kalman Filter

- Aligns centroids
- Problems with occlusion
- Robustness through motion model

Baseline Methods



[3]

Kalman Filter

- Aligns centroids
- Problems with occlusion
- Robustness through motion model
- Very fast



Baseline Methods

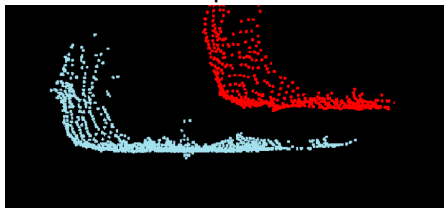
Iterative Closest Point (ICP)

- Iterative hill climbing approach
- Minimizes quadratic distance of closest points
- Uses whole point cloud

Baseline Methods

Iterative Closest Point (ICP)

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- Minimizes quadratic distance of closest points
- Uses whole point cloud
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- Problem: local optima

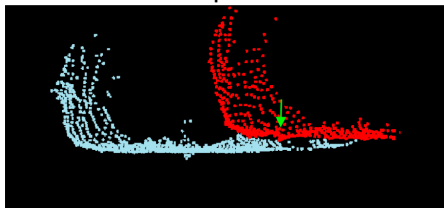


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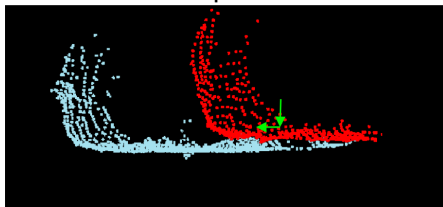


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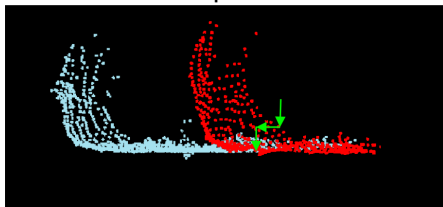


[3]

Baseline Methods

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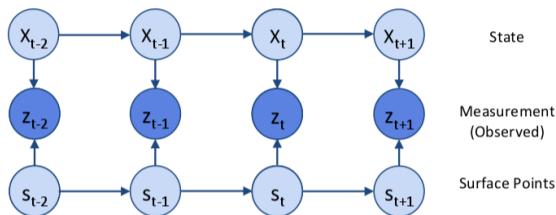
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- Depends on good initialization
- Problem: local optima



[3]

- No motion model

Probabilistic Model



[1]

Dynamic Bayesian Network

- Relates variables over successive frames
- State x_t (position relative to last frame and velocity)
 Surface points $s_t = \{s_{t,1}, \dots, s_{t,n}\}$
 Measured point cloud $z_t = \{z_{t,1}, \dots, z_{t,n}\}$
- Rotation not considered

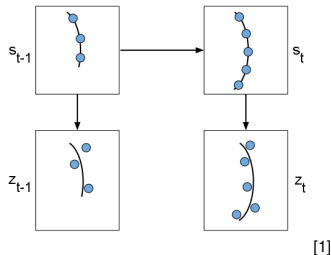
Probabilistic Model

Surface points

- Sampled from the visible surface
- Indirectly observable
- Visible surface varies due to occlusion and viewpoint changes

$$p(s_{t,i}|s_{t-1}) = p(V) * p(s_{t,i}|s_{t-1}, V) + p(\neg V) * p(s_{t,i}|s_{t-1}, \neg V)$$

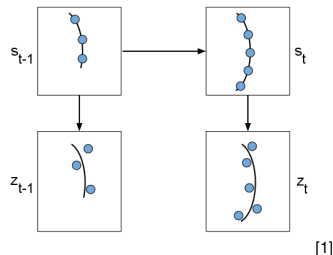
$$\Rightarrow p(s_t|s_{t-1}) = \eta(\mathcal{N}(s_t; s_{t-1,i}, \Sigma_r) + k)$$



Probabilistic Model

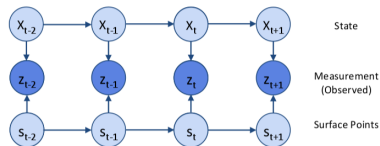
Measurement points

- Depending on surface points
- Gaussian sensor noise Σ_e
- $z_{t,i} \sim \mathcal{N}(s_{t,i}, \Sigma_e) + x_{t,p}$
 $z_{t-1,i} \sim \mathcal{N}(s_{t-1,i}, \Sigma_e)$



Probabilistic Model

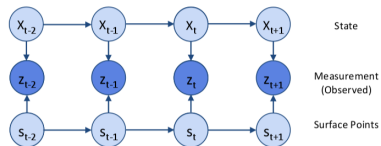
Measurement Model



$$p(z_t | x_t, z_1, \dots, z_{t-1})$$

Probabilistic Model

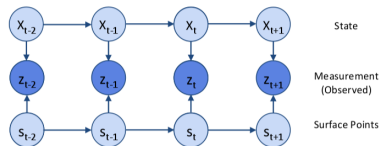
Measurement Model



$$p(z_t | x_t, z_1, \dots, z_{t-1}) \approx p(z_t | x_t, z_{t-1})$$

Probabilistic Model

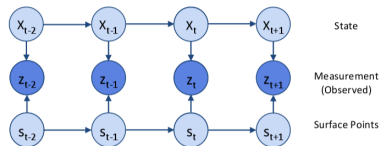
Measurement Model



$$\begin{aligned}
 p(z_t | x_t, z_1, \dots, z_{t-1}) &\approx p(z_t | x_t, z_{t-1}) \\
 &= \int \int p(z_t, s_t, s_{t-1} | x_t, z_{t-1}) ds_t ds_{t-1}
 \end{aligned}$$

Probabilistic Model

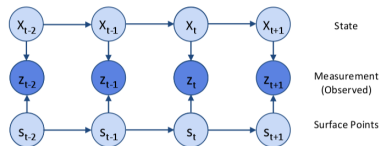
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 &= \underbrace{\int p(z_t | s_t, x_t) \underbrace{\int p(s_t | s_{t-1}) \eta p(z_{t-1} | s_{t-1}) ds_t ds_{t-1}}_{\text{convolution}}}_{\text{convolution}}
 \end{aligned}$$

Probabilistic Model

Measurement Model



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 p(z_t | x_t, z_1, \dots, z_{t-1}) &\approx p(z_t | x_t, z_{t-1}) \\
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 &= \eta(\mathcal{N}(z_t; z_{t-1} + x_{t,p}, \Sigma_r + 2\Sigma_e) + k)
 \end{aligned}$$



Probabilistic Model

Measurement Model Computation

- $ccp(z_{t,i})$: closest correspondence point in $z_{t-1} + x_{t,p}$

Measurement Probability

$$p(z_t | x_t, z_{t-1}) = \eta \prod_{z_{t,i} \in z_t} \exp \left(-\frac{1}{2} (z_{t,i} - ccp(z_{t,i}))^T \Sigma^{-1} (z_{t,i} - ccp(z_{t,i})) \right) + k$$



Probabilistic Model

Measurement Model Computation

- $ccp(z_{t,i})$: closest correspondence point in $z_{t-1} + x_{t,p}$
- Covariance matrix $\Sigma = 2\Sigma_e + \Sigma_r$

Measurement Probability

$$p(z_t | x_t, z_{t-1}) = \eta \prod_{z_{t,i} \in z_t} \exp \left(-\frac{1}{2} (z_{t,i} - ccp(z_{t,i}))^T \Sigma^{-1} (z_{t,i} - ccp(z_{t,i})) \right) + k$$



Probabilistic Model

Measurement Model Computation

- $ccp(z_{t,i})$: closest correspondence point in $z_{t-1} + x_{t,p}$
- Covariance matrix $\Sigma = 2\Sigma_e + \Sigma_r$
- Normalization constant η
- Smoothing factor k

Measurement Probability

$$p(z_t | x_t, z_{t-1}) = \eta \prod_{z_{t,i} \in z_t} \exp \left(-\frac{1}{2} (z_{t,i} - ccp(z_{t,i}))^T \Sigma^{-1} (z_{t,i} - ccp(z_{t,i})) \right) + k$$

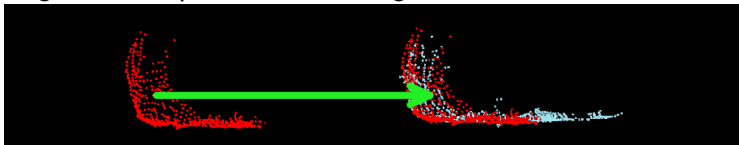
Probabilistic Model

- Align smaller point cloud in larger one



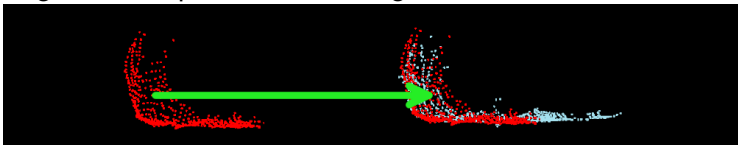
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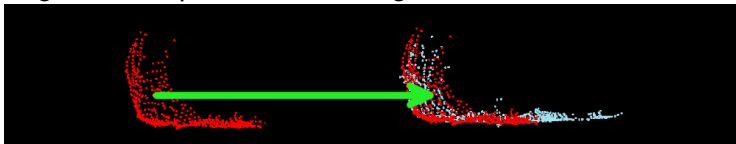


- Aligning larger point cloud in smaller one

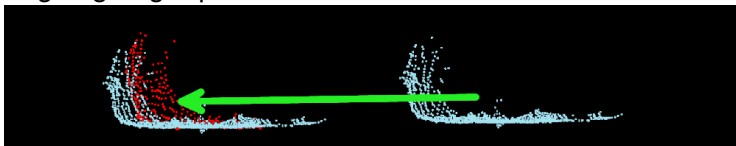


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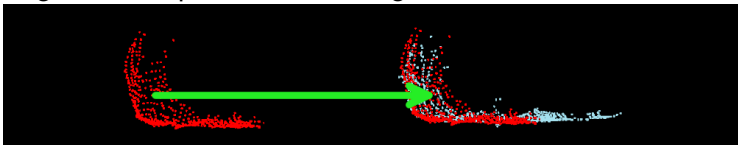


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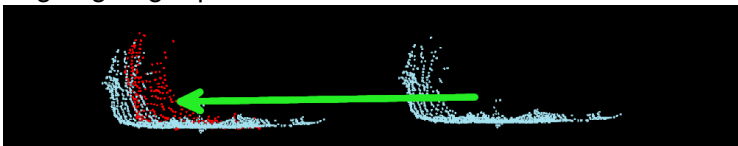


Probabilistic Model

- Align smaller point cloud in larger one



- Aligning larger point cloud in smaller one



⇒ Exchange z_t and z_{t-1} when $|z_t| > |z_{t-1}|$



Probabilistic Model

Adding Color

- Use available color information of measurement points
- Better alignment despite occlusions
- Embed color matching into measurement model

$$p_C(s_{t,i}|s_{t-1}, V) = p(C)p_C(s_{t,i}|s_{t-1}, V, C) + \\ p(\neg C)p_C(s_{t,i}|s_{t-1}, V, \neg C)$$

- $p(C)$: Color-model applicable
- $p(\neg C)$: Color-model not applicable (lens flare, reflections)
- $p_C(s_{t,i}|s_{t-1}, V, \neg C) = \frac{1}{255}$: Color mismatch
- $p_C(s_{t,i}|s_{t-1}, V, C)$: Color match



Probabilistic Model

Motion Model

- Take whole measurement history into account
- Robustness against single imprecise alignments



Probabilistic Model

Motion Model

- Take whole measurement history into account
- Robustness against single imprecise alignments
- Kalman filter with constant velocity model
- Measurement step: update with Gaussian distribution

$$\mu_t = \sum_i p(x_{t,i} | z_1, \dots, z_t) x_{t,i}$$

$$\Sigma_t = \sum_i p(x_{t,i} | z_1, \dots, z_t) (x_{t,i} - \mu_t)(x_{t,i} - \mu_t)^T$$

- Update step: apply velocity to position



Searching the State Space

Search the State Space



Searching the State Space

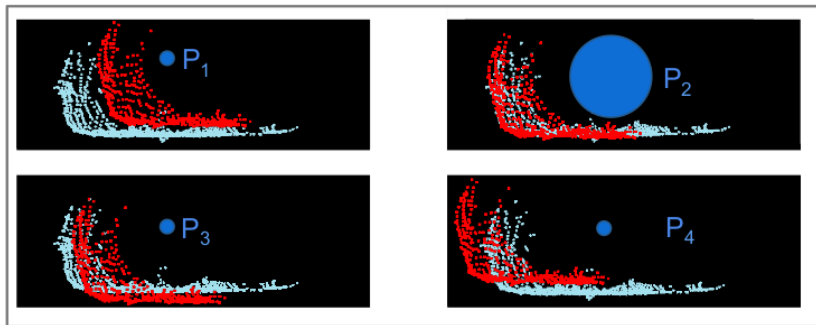
Search the State Space

- For most likely state
- Globally, without getting stuck in local optima
- Allow multiple hypotheses

Searching the State Space

Search the State Space

- For most likely state
 - Globally, without getting stuck in local optima
 - Allow multiple hypotheses
- ⇒ Use histogram

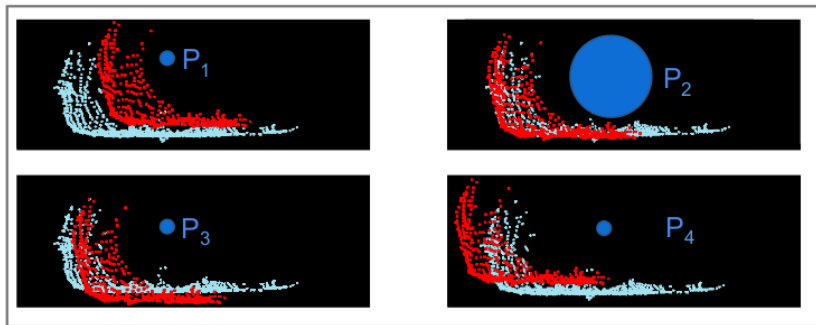


[3]

Searching the State Space

Search the State Space

- For most likely state
- Globally, without getting stuck in local optima
- Allow multiple hypotheses
- ⇒ Use histogram
- ⇒ Too slow for necessary resolution

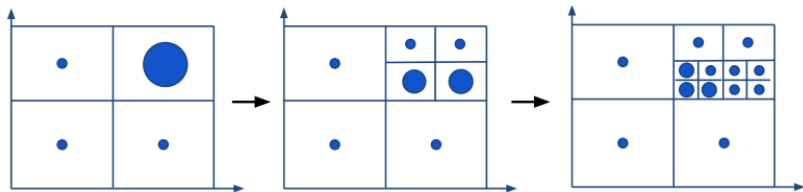


[3]

Searching the State Space

In Real Time

- Densely sample only areas with high probability
- Initial coarse resolution
- Stop at anytime during refinement

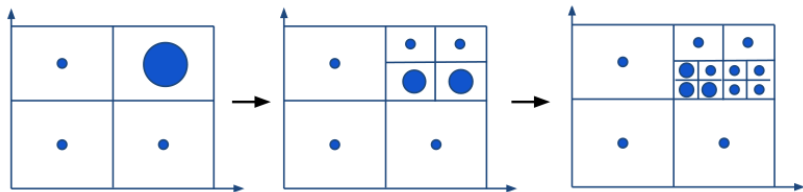


[1]

Searching the State Space

In Real Time

- Densely sample only areas with high probability
 - Initial coarse resolution
 - Stop at anytime during refinement
- ⇒ Use dynamic histogram



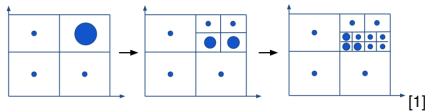
[1]



Searching the State Space

Derivation Step

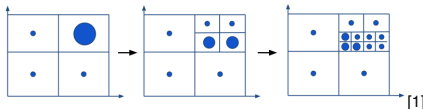
- Recursively expend cells



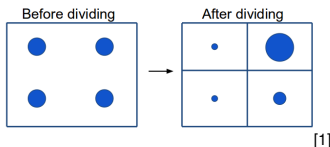
Searching the State Space

Derivation Step

- Recursively expend cells



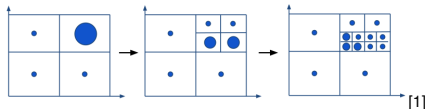
- Maximize information gain / Minimize KL-divergence



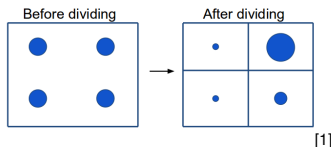
Searching the State Space

Derivation Step

- Recursively expend cells



- Maximize information gain / Minimize KL-divergence



- KL-divergence: information loss if A approximated by B

$$D_{KL}(A||B) = \sum_{j=1}^k p_j \ln \left(\frac{p_j}{P_i/k} \right)$$



Searching the State Space

Annealing Dynamic Histogram (ADH)

- No good alignment with coarse resolution
- Sampling resolution another error source
- ⇒ Consider sampling resolution in measurement model
- $\Sigma = 2\Sigma_e + \Sigma_r + \Sigma_g$
- Σ_g proportional to sampling resolution



Evaluation

What to evaluate

- Precision of the position and velocity estimation
- Root-Mean-Square error

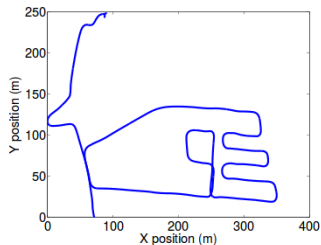
$$e_{RMS} = \sqrt{\mathbb{E}((\hat{v}_t - v_t)^2)}$$

- Runtime (real time requirements)
 - Comparison to baseline methods
- ⇒ Need for test data

Evaluation

Relative Reference Frame Approach

- Record sensor data while driving
- Static environment
- Assume car is standing still

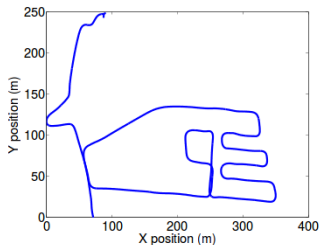


[1]

Evaluation

Relative Reference Frame Approach

- Record sensor data while driving
- Static environment
- Assume car is standing still
- Compute ground truth position and velocity from distance and car velocity



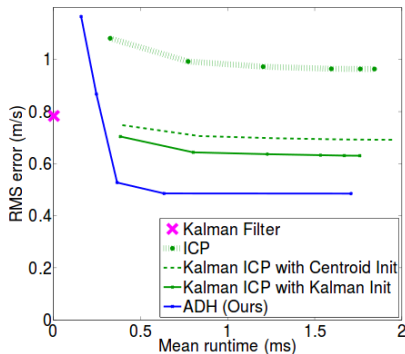
[1]



Evaluation

Kalman Filter

- Imprecise but very fast



[1]



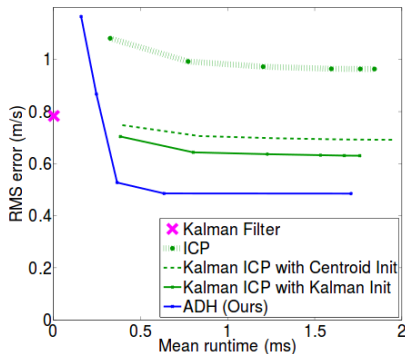
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Kalman Filter

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ICP

- Slow and very imprecise
- Variants with motion model perform better



[1]



Evaluation

Kalman Filter

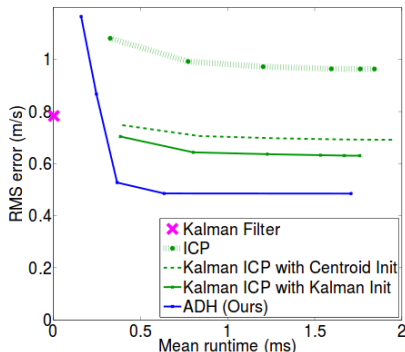
- Imprecise but very fast

ICP

- Slow and very imprecise
- Variants with motion model perform better

ADH

- Quick first result
- Outperforms all baseline methods

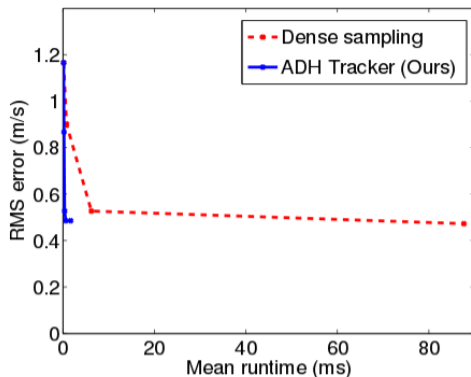


[1]



Evaluation

ADH acceleration



[1]



Evaluation

- Relative reference frame precise but not realistic



Evaluation

- Relative reference frame precise but not realistic

Model Crispness Approach

- Build a model of the tracked object
- Union object point clouds over all frames
- Point clouds aligned by position estimation



[1]

- Record sensor data in real traffic



Evaluation

Crispness Score

- Measure for distinctness of the build model

Evaluation

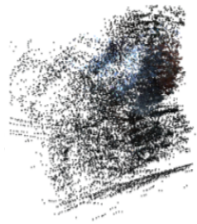
Crispness Score

- Measure for distinctness of the build model



[1]

- Presented tracker
- High crispness score



[1]

- Kalman ICP tracker
- Low crispness score



Evaluation

Tracking Method	Object Class		
	People	Bikes	Moving Cars
Kalman Filter	0.38	0.31	0.27
Kalman ICP	0.18	0.18	0.29
ADH (Ours)	0.42	0.38	0.33

[1]

- Highest score for all object classes
- Higher score for people than for cars



Evaluation

Improvement through color model

- RMS error decreased by 10.4%
- $p(C)$ very small (lens flare, heavy shadows)
- Works robust through day-times and seasons

Source Code

- Open Source
http://stanford.edu/~daveheld/anytime_tracking.html
- Easy to setup, integrate into C++
- Test-data available

Performance with stereo camera data?

- Cheaper sensor, more noisy data
- A lot of configuration values in the code



Conclusion

Combine 3D Shape, Color, Motion for Robust Anytime Tracking

Precise and robust tracking is possible in real-time

- Measurement model combines 3D shape, Color, Motion
- Derived from Dynamic Bayesian Network
- Annealed Dynamic Histogram for global and fast search
- Evaluation with local reference frame and model crispness
- Outperforms baseline methods

References I



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Combining 3D Shape, Color, and Motion for Robust
Anytime Tracking.

In: Proceedings of Robotics: Science and Systems,
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International Conference on, IEEE (2011) 4034–4041



Held, D., Levinson, J., Thrun, S., Savarese, S.:
Anytime Tracking.

[http://stanford.edu/~davheld/DavidHeld_files/
RSS2014_Poster.pdf](http://stanford.edu/~davheld/DavidHeld_files/RSS2014_Poster.pdf) (2015)



Backup slide

Crispness score formula



$$\frac{1}{T^2} \sum_{i=1}^T \sum_{j=1}^T \frac{1}{n_i} \sum_{k=1}^{n_i} G(x_k - \hat{x}_k, 2\Sigma)$$

Backup slide: RoboCup Logistics League

