# Assignment 4: Hybrid MPI + FastFlow MergeSort

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The goal of this project was to develop a scalable MergeSort algorithm for a large array of records, combining intra-node parallelism with FastFlow and inter-node parallelism with MPI.

## 1 Implementation Strategy

At the outset, a key design decision was made regarding the Record data structure. While the assignment specified a fixed-size payload array (char rpayload [RPAYLOAD]), we opted for a more flexible structure with a dynamically allocated payload (char\* payload). This choice was motivated by the need for a versatile and robust benchmarking framework. Using a dynamic payload allows the record size to be configured at runtime via command-line arguments, which is essential for systematic performance analysis across various payload sizes without requiring code recompilation for each test. This design choice does not compromise the performance analysis. The memory for each record's payload is allocated once at the beginning of the tests and remains fixed throughout the sorting process. Within the core sorting algorithms, the cost of moving or comparing these records is dominated by the size of the payload, not by the fact that it is heap-allocated. The use of move semantics in our data structures ensures that during merge operations, only the pointer and size are transferred, not the payload data itself, preserving performance characteristics equivalent to those of a fixed-size struct for the purpose of this study.

#### 1.1 Single-Node Parallel Design (FastFlow)

For the shared-memory implementation, we adopted a pragmatic, performance-oriented approach. The MergeSort algorithm naturally decomposes into two distinct phases: an initial, highly parallel sorting of small data chunks, followed by a sequential series of merge passes. Our implementation mirrors this structure, using dedicated FastFlow farms for each phase to maximize performance.

**Phase 1: Parallel Sorting.** The first challenge is to break down the massive initial array into manageable pieces. We split the array into numerous small, cache-friendly chunks. The sorting of these chunks is an embarrassingly parallel problem. For this task, we employed an ff\_farm. An emitter node decomposes the array into tasks, and a pool of worker threads processes them concurrently. Each worker sorts its assigned chunk in-place using std::sort, which is highly optimized for small-to-medium datasets.

**Phase 2: Iterative Merging.** Once the initial chunks are sorted, they must be progressively merged. This is an inherently iterative process. We implemented this using a loop where, at each iteration, a new ff\_farm is created to perform a single merge pass in parallel. In each pass, pairs of adjacent sorted runs are merged into a new, larger sorted run. A critical optimization here is the use of a "ping-pong" buffer strategy. We allocate a single auxiliary buffer of the same size as the original data. In each merge pass, we read from a source buffer and write the merged results to a destination buffer. After the pass is complete, we simply swap the pointers, so the destination becomes the source for the next iteration. This avoids costly data copies between passes and is a standard, highly efficient technique for out-of-place merge algorithms.

#### 1.1.1 Architectural Considerations and Discarded Alternatives

The assignment suggested exploring FastFlow's building blocks, including ff\_pipeline and ff\_all2all. We implemented and evaluated these alternatives but ultimately discarded them for sound performance and algorithmic reasons.

Why not ff\_all2all? The ff\_all2all pattern is designed for data redistribution, where each worker sends a piece of its local data to every other worker. This is the core of algorithms like Radix Sort or Sample Sort, which partition data based on key values. MergeSort, however, relies on merging physically adjacent, sorted segments. Its communication pattern

is strictly pairwise and hierarchical, not all-to-all. Forcing MergeSort into an all-to-all pattern would be algorithmically incorrect.

Why not ff\_pipeline? An integrated pipeline architecture, such as feeder -> sort\_stage -> merge\_stage, seems theoretically elegant. We invested significant effort in implementing and benchmarking this alternative. However, it yielded a significant performance degradation, reducing the peak speedup of about 30%. This counter-intuitive result stems from two main factors. First, MergeSort is fundamentally a bulk-synchronous parallel (BSP) algorithm: the merge phase cannot begin until the entire sort phase is complete. There is no opportunity for true, overlapping pipelining. Second, the ff\_pipeline introduces communication and scheduling overhead between its stages. For a single, large task traversing the pipeline, this overhead outweighs any potential benefits, especially when compared to the lean approach of dedicating all parallel resources to a single, optimized farm for each distinct phase. We therefore concluded that the architecturally simpler two-farm approach was pragmatically superior for this specific problem.

### 1.2 Hybrid Multi-Node Design (MPI + FastFlow)

To scale the algorithm beyond a single node, we designed a hybrid implementation that uses MPI for inter-node coordination and our optimized FastFlow MergeSort for intra-node computation. The overall process is divided into three main phases.

**Phase 1: Data Distribution.** The root process (rank 0), holding the initial dataset, first partitions the global dataset into P contiguous blocks, where P is the number of MPI processes. The size of each block is calculated to ensure the workload is as balanced as possible. The root then uses MPI\_Scatterv to send each partition to its designated process. This is more robust than a simple MPI\_Scatter as it correctly handles cases where the total number of records is not perfectly divisible by P.

**Phase 2: Local Sorting.** Upon receiving its local data segment, each MPI process invokes the highly optimized, multithreaded parallel\_mergesort function. This step agglomerates fine-grained comparison operations into a coarse-grained local sort, leveraging all available cores on the node. This phase is entirely computation-bound and transforms the global problem into a set of distributed, sorted arrays.

**Phase 3: Hierarchical Merging.** After the local sort, the distributed sorted segments must be merged into a single, globally sorted array at the root. We chose a binary tree reduction pattern for this task, as illustrated in Figure 1. The merging occurs in  $\log_2(P)$  steps. In each step, active processes are paired up: one "sender" sends its data to a "receiver". The receiver merges its own data with the incoming data, and the sender then becomes idle. This pattern distributes the merge work effectively across multiple nodes in the early stages.

A critical design decision in this phase concerned the communication strategy. The assignment suggested maximizing computation-to-communication overlap, which typically implies the use of non-blocking primitives like MPI\_Irecv. We thoroughly investigated this path and developed a prototype based on this pattern. However, our analysis and benchmarking led to a deliberate engineering choice to use a simpler, more robust model based on blocking communication (MPI\_Recv) for each merge step. This decision was based on two key findings. First, the MergeSort algorithm itself offers limited opportunities for meaningful overlap; the core merge logic cannot proceed until it has received the initial segments of data from its partner, making it difficult to hide communication latency behind computation. Second, the management of non-blocking requests within an iterative algorithm like the binary tree reduction introduced significant complexity and a measurable performance overhead that negated the theoretical benefits. Therefore, the final implementation prioritizes correctness and real-world performance over a theoretically optimal but practically less effective strategy.

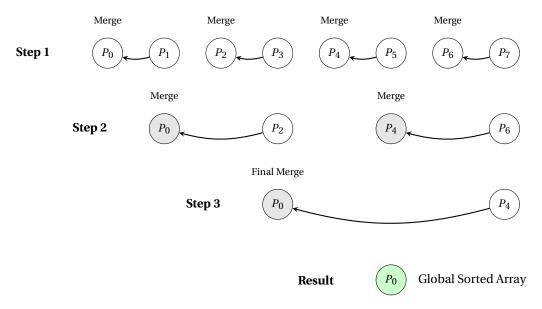


Figure 1: Illustration of the 8-process binary tree merge reduction. Active merging processes are shown in gray, with the final result in green.

#### 1.2.1 Alternative Merge Strategy: Centralized K-Way Merge

We also implemented and evaluated an alternative strategy for the final merge phase: a centralized k-way merge. In this model, all non-root processes (P-1) of them) send their locally sorted data directly to the root process in a single communication round. The root process then performs a k-way merge on all P partitions (including its own) using a min-heap.

Theoretically, this approach is attractive as it reduces the number of communication rounds from  $\log_2(P)$  to one. However, our benchmarks showed it to be less performant than the binary tree reduction. The primary reason is that it creates a massive bottleneck at the root process. The root must handle incoming network traffic from all other processes simultaneously while also performing the entire k-way merge. This serializes a large portion of the work and underutilizes the other nodes. In contrast, the binary tree approach distributes the merge workload across multiple nodes in the initial steps, leveraging the computational power of the entire system for longer before idling processes. The higher parallelism of the binary tree approach outweighed the benefit of fewer communication rounds for the problem scales tested.

## 2 Performance Analysis

We benchmarked our implementations to evaluate their strong and weak scaling properties. We define "absolute speedup" as the ratio between the execution time of the best sequential algorithm (std::sort) and our parallel implementation. The analysis is based on the data collected and visualized below.

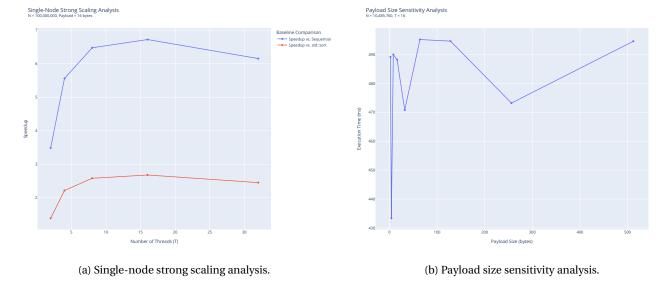


Figure 2: Performance characterization on a single node.

**Single-Node Strong Scaling.** Figure 2a shows the strong scaling of our FastFlow implementation. The speedup increases significantly up to 16 threads, reaching a peak of approximately 6.8x against our sequential implementation and 2.7x against std::sort. Beyond 16 threads, performance begins to degrade. This behavior is expected and illustrates a more realistic version of Amdahl's Law, where parallel overhead is not negligible. As more threads are added, the overhead of synchronization, thread management, and contention on the memory bus starts to dominate the gains from parallel computation.

**Payload Scaling.** The impact of payload size is shown in Figure 2b. The execution time remains relatively stable for payloads from 8 to 512 bytes. This indicates that the algorithm's performance is heavily influenced by memory bandwidth. The primary cost in the merge phase is moving data, and this cost scales linearly with the record size. For very small payloads, the algorithm may be more sensitive to memory latency and cache effects, explaining the initial volatility. As the payload grows, the problem becomes firmly memory-bandwidth bound, as the time spent in computation (key comparisons) becomes negligible compared to the time spent in std::move.

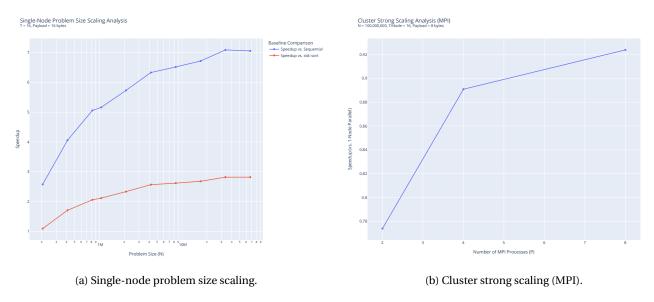


Figure 3: Problem size and distributed strong scaling analysis.

**Single-Node Problem Size Scaling.** Figure 3a presents a scaling analysis where the number of threads is fixed, and the total problem size is increased. The speedup continues to grow almost linearly with the problem size. This aligns with Gustafson's Law: by increasing the problem size along with the computational resources, the serial fraction of the work becomes less significant, and the performance scales well. With more data to process, the initial costs of setting up farms and threads are amortized over a longer execution time, leading to better efficiency.

**Cluster Strong Scaling.** Figure 3b provides an instructive view into the strong scaling characteristics of the hybrid algorithm. The speedup is measured relative to the optimized single-node parallel baseline. The results show that while the two-process run is slower due to initial communication overhead, the hybrid implementation achieves a positive speedup with four and eight processes. This demonstrates that for a sufficiently large problem size, distributing the computational load can effectively overcome the high cost of network communication. The diminishing returns in efficiency as more nodes are added are expected, as communication and synchronization costs begin to represent a larger fraction of the total execution time.

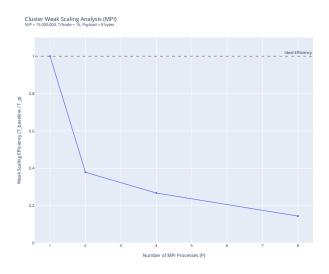


Figure 4: Cluster weak scaling analysis, showing efficiency relative to the single-node baseline. An efficiency of 1.0 represents ideal scaling.

Cluster Weak Scaling. To complete the performance study, we conducted a weak scaling test on the cluster. In this test, the problem size per node was kept constant, while the number of nodes was increased. Figure 4 plots the weak scaling efficiency, where an ideal algorithm would maintain an efficiency of 1.0. Our results show a significant drop in efficiency as more nodes are added. This behavior is characteristic of algorithms with non-scalable communication patterns, such as our distributed MergeSort. The primary reason for this poor scaling lies in the hierarchical merge phase. While the local sort phase scales perfectly, the communication costs do not. In each step of the binary tree reduction, processes must transmit increasingly large, already-merged partitions to their partners. The total volume of data communicated and the sequential dependency of the final merge steps grow with the number of processes. This communication overhead dominates the execution time, demonstrating the inherent scalability limits of this MergeSort algorithm in a distributed-memory environment.