Lecture Three

February 25, 2016

1 Gaussian Classifiers

$$(\vec{x} - \vec{u})(\frac{1}{N} \sum (\vec{x} - \vec{\mu})(\vec{x} - \vec{\mu})^T)(\vec{x} - \vec{\mu})$$
 (1)

$$(\vec{x} - \vec{\mu})\Sigma^{-1}(\vec{x} - \vec{\mu})^T \tag{2}$$

Multi-dimensional Gaussian distribution

$$P(\vec{x}) = \frac{1}{\sqrt{||2\pi\Sigma||}} e^{-\frac{1}{2}(\vec{x}-\vec{\mu})^T \Sigma^{-1}(\vec{x}-\vec{\mu})}$$
(3)

Steps for developing a gaussian classifier

- 1. Center the data
- 2. Compute the covariance matrix

Projection of the Mean Value

$$\frac{1}{N} \sum_{i=1}^{N} (\vec{x}^T \vec{a}) = (\frac{1}{N} \sum_{i=1}^{N} \vec{x}_i)^T \vec{a} = \vec{\mu}^T \vec{a}$$
 (4)

Projection of the Variance

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{N} (\vec{a}^T \vec{x_i} - \vec{a}^T \vec{\mu}) (\vec{x_i}^T \vec{a} - \vec{\mu}^T \vec{a})$$
 (5)

2 Homework 2

- Part A: Redo Homework 1
 - Use Gaussian Classifiers
- Part B: Do the cancer problem in the book and apply subset selection
 - Redraw Chapter 3 Fig. 3.5 with the data from the book for the cancer set selection.

- prostate cancer example

If the covariance matrix is not invertable then you can add a piece of the identity matrix to make the matrix more invertible.

$$(\Sigma + \lambda I)^{-1} \tag{6}$$