Correlations of Discrete Characters, and Ancestral State Reconstruction

April 9, 2009

The Mk Model

- Simple model for the evolution of discrete variables
- Constant instantaneous probability of changing between any two character states out of k possibilities
- Described by rate matrix Q:

$$Q = \alpha \begin{bmatrix} 1-k & 1 & \dots & 1 \\ 1 & 1-k & \dots & 1 \\ \vdots & \vdots & \ddots & \vdots \\ \end{array}$$

The Mk Model

- Generalized JC model (Mk with k=4)
- At equilibrium, stationary distribution of characters is [1/k, 1/k, ... , 1/k]
- Described by transition matrix
- m = exp(Qt)

Alternatives to Mk





$$Q = \begin{bmatrix} -\alpha & \alpha \\ \beta & -\beta \end{bmatrix}$$

Example

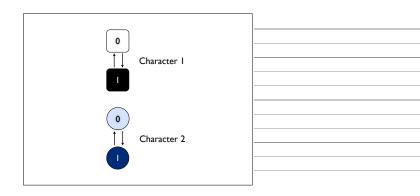


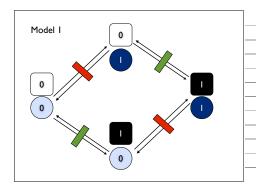


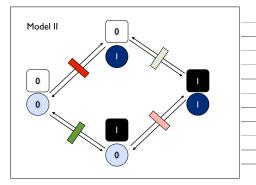
Figure 2. A phylogeny of the Hominoidea including one Old World Monkey. Two characters, social system and ocertous advertisement are secored for each species, where s = single male social system, s = multi-male, and t * t = the presence of ocertors as wellings, s = a shence, Home opines (s, -); P on (s, +); P (Gorline (s, -); P ongo (s, -); $H_Bibbetes (s, -)$; Colobus generas (s, -).

Consider two discrete characters

- Are they evolving in a correlated fashion?
- When character A changes to state I, is character B likely to change to I as well?

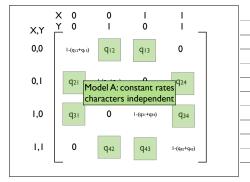


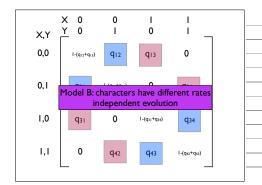


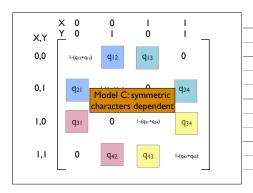


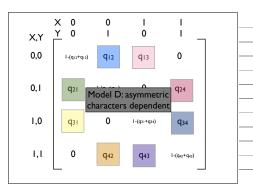
Correlation of Discrete Characters

- Does the rate of change of character 2 depend on the state of character 1?
- Compare models using maximum likelihood









Example

- Data on evolution of dewlap color (red, yellow) and perch behavior (high, low) of anoles
- Fit the four models to these data
- Obtain the following results:

Example

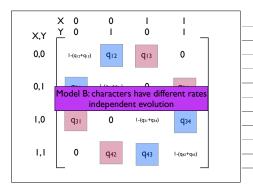
Model	InL	k	AIC
Α	-132.2	1	
В	-130.1	2	
С	-125.3	4	
D	-124.2	8	

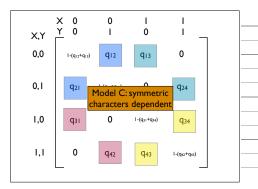
Example

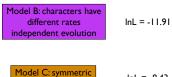




Figure 2. A phylogeny of the Hominoidea including one Old World Monkey. Two characters, social system and oestrous advertisement are secord for each species, where *s single male social system, *u = multi-male, and *t *= the presence of oestrous swellings, ** - absence. Homo spilear (*s, -*); Pongo (*s, --); Hylobater (*s, --); Colobar guerzac (*s, --);







characters dependent

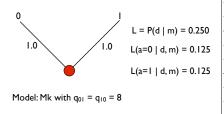
$$\Delta = 2*(-8.43 - -11.91) = 6.96$$

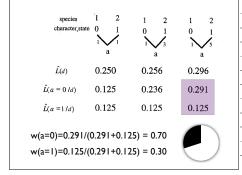
P = 0.12

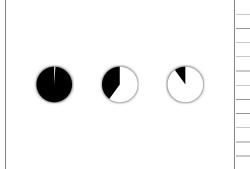
Reconstructing Ancestral **Character States**

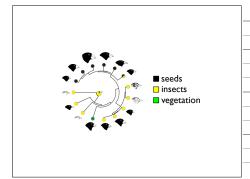
- Goal: to make inferences about the states of characters in ancestral lineages
- Usually make these inferences at nodes in the tree
- These inferences can be made using maximum likelihood

Discrete Ancestral State Reconstruction









Local and global

- There is a difference between:
- the set of characters that, together, maximize the likelihood
- the character that represents the maximumlikelihood estimate for a single node (marginal likelihood)
- Pagel (1999) even recommends reestimating model parameters (q₀₁, etc.) independently for each ancestral state (the "local" estimate)

Continuous Characters

- Can also reconstruct ancestral characters using likelihood
- Assume characters are evolving under a Brownian motion model

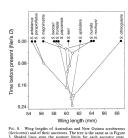
$$\Pr[y = x] = \frac{1}{\sigma \sqrt{2\pi t}} \exp\left(-\frac{(x - \theta)^2}{2\sigma^2 t}\right)$$

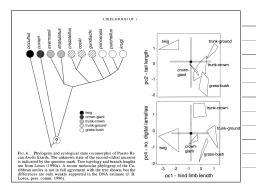
Continuous characters

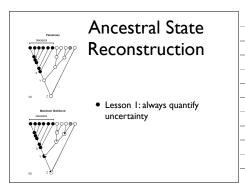
- ML ancestral states for continuous characters under BM are equivalent to ancestral states estimated under squared change parsimony
- Choose the ancestral states that minimize the amount of squared change on the tree

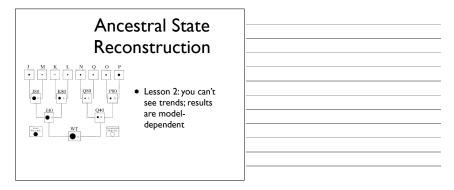
Maximum likelihood

- Find model parameters that maximize the likehood of obtaining the data
- Calculate P(a=x_i | model, tree, data)
- Can generate confidence intervals based on t-distribution (Schluter 1997)









Summary

- We can test for character correlations, or other patterns of interest, with discrete characters
- It is possible to estimate ancestral character states and incorporate uncertainty