

Digital Transmitters and Receivers

February 20, 2018

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1 Lecture 1 - History of Communication

This is mt, I have not a copy of these notes. Mainly discussed how in the last 120 years we/society has gone from using semaphores to using modern fast as light coms.

2 Lecture 2 - A cont. of lecture 1

More info I don't have a copy of. . . .

3 Lecture 3

4 Lecture ?

:DATE: <2018-02-05 Mon>

Use correlators to match input to possible transmitted waveforms

5 Lecture ?

5.1 Transmitter

5.2 Reciever

two bits per symbol - four possible wave forms

symbol	bits	four possible waveforms
0	00	0^0
1	01	90^0
2	10	180^0
3	11	270^0

6 Lecture ?

6.1 Fourier Transfrom

- $\mathbf{F} \{g(t)\} = G(f) = \int_{-\infty}^{\infty} g(t) e^{-j2\pi ft} dt$
- $\mathbf{F}^{-1} \{G(f)\} = g(t) = \int_{-\infty}^{\infty} G(f) e^{j2\pi ft} df$

6.1.1 TODO Properties: verify that 6.1.1 is correct

- Linearity

$$- \mathbf{F} \{a_1 x_1(t) + a_2 x_2(t)\} = a_1 \mathbf{F} \{x_1(t)\} + a_2 \mathbf{F} \{x_2(t)\}$$

- Time Shift

$$\begin{aligned} - \mathbf{F} \{x(t - T_0)\} &= \int_{-\infty}^{\infty} x(t - T_0) e^{-j2\pi ft} dt \\ \lambda &= t - T_0 \\ &= e^{-j2\pi f T_0} \int_{-\infty}^{\infty} x(\lambda) e^{-j2\pi f \lambda} d\lambda \quad (\text{EQ1}) \\ &= e^{-j2\pi f T_0} X(f) \end{aligned}$$

- Frequency Property

$$- \mathbf{F}^{-1} \{X(f - f_0)\} = e^{j2\pi f_0 t} \int_{-\infty}^{\infty} x(t) e^{-j2\pi f t} dt$$

6.2 TODO Graham-Schmidt: check matrix algebra book on this topic.

:DEADLINE: <2018-02-05 Mon>

- Signals $S_1(t), \dots, S_m(t)$
- basis functions $\phi_n(t), \dots, \phi_n(t)$, $N \neq M$
- $S_i(t) = \sum_n S_{in} \phi_n(t)$
- $\mathbf{S}_i = [S_{i1} \ S_{i2} \ \dots \ S_{in}]$

6.2.1 1st signal

$$E_{s1} = \|S_1\|^2$$

$$\phi_1 = \frac{S_1(t)}{\sqrt{E_{s1}}}$$

$$S_{11} = \sqrt{E_{s1}}$$

6.2.2 2nd – Nth signal

Creating a new basis function

$$S_{21} = \langle S_2(t), \phi_1(t) \rangle$$

$$r_2(t) = S_2(t) - S_{21} \phi_1(t) \leftarrow \text{orthogonal to } \phi_1(t)$$

If remainted $r_i(t) = 0$ skip the steps below

- The part of signal 2 that can't be represented by $\phi_1(t)$.

$$E_{r2} = \|r_2(t)\|^2$$

$$\phi_2(t) = \frac{r_2(t)}{\sqrt{E_{r2}}}$$

$$S_{22} = \sqrt{E_{r2}}$$

- others

$$S_{ni} = \langle S_n(t), \phi_i(t) \rangle \text{ for } \phi_i(t) \text{ which are defined.}$$

$$r_i(t) = S_i(t) - \sum \{S_{in}\} \phi_n(t)$$

:DATE: <2018-02-09 Fri>

6.3 Distortionless System

$$x(t) \rightarrow y(t)$$

6.3.1 Acceptable

- Amplification//

$$y(t) = K x(t)$$

- Delay

$$y(t) = x(t - t_0), \quad t_0: \text{positive integer, positive required for causality}$$

- Overall//

$$y(t) = Kx(t - t_0)$$

6.4 Freq representation

$$Y(f) = Ke^{-j2\pi ft_0} X(f) = H(f)X(f) \quad \text{Linear time invariant. where } H(f) = Ke^{-j2\pi ft_0}$$

$$h(t) = K\delta(t - t_0)$$

6.5 Bode rep

$$H(f) = Ke^{-j2\pi ft_0}$$

$$H(f) = K < -\text{constant Mag}(\text{gain})$$

$$\angle H(f) = -2\pi ft_0 < -\text{linear, slope} = -2\pi f$$

$$\text{Group Delay: } t_g(f) = \frac{-1}{2\pi} \frac{d}{df} (\angle H(f))$$

6.6 Filters

- ideal

- realistic

– Lowpass

– Highpass

– Bandpass

– Bandstop

filter type	ideal	realistic
lowpass	sharp rect around center	hill flat top
highpass		
bandpass		
bandstop		

7 Lecture ? -

DATE: <2018-02-12 Mon>

7.1 TODO Project

7.2 Fourier Series - Fourier Transform Relationship

7.2.1 Fourier Series

$$\text{F.S. } g(t) = \sum_{-\infty}^{\infty} G_n e^{jn2\pi f_0 t}$$

$$\text{F.T. } G(f) = \int_{-\infty}^{\infty} g(t) e^{-jn2\pi f t} dt = \sum_{-\infty}^{\infty} G_n \delta(f - f_0)$$

7.3 Energy spectral density????????????

$$E_g = \int_{-\infty}^{\infty} |G(f)|^2 df$$

$$x(t) \rightarrow h(t) \rightarrow y(t)$$

$$X(f) \rightarrow H(f) \rightarrow Y(f)$$

$$E_y = \int_{-\infty}^{\infty} |X(f)H(f)|^2 df = \int_{f_0 - \delta f}^{f_0 + \delta f} \text{Energy Spectral Density}$$

$$\Psi_x(f_0) = \lim_{\Delta f \rightarrow 0} \frac{1}{\Delta f} \int_{f_0 - \frac{\Delta f}{2}}^{f_0 + \frac{\Delta f}{2}} |X(f)|^2 df = |X(f_0)|^2$$

$$\text{Energy } E_x = \int \Psi_x(f) df$$

$$\text{Energy int bandwidth } B \text{ centered at } f_1 \int_{f_1 - \frac{B}{2}}^{f_1 + \frac{B}{2}} \Psi_x(f) df = \int_{f_1 - \frac{B}{2}}^{f_1 + \frac{B}{2}} \Psi_x(f) df$$

8 TODO get units for

$$\text{let: } S_g(t) = \Pi\left(\frac{t}{\text{What bandwidth capacity does need to pass exactly}}\right) 90$$

$$E_g = \int |g(t)|^2 dt = S_g(t) \rightarrow \text{"Ideal LPF bandwidth } B" \rightarrow y(t) 90\% E_g = 0.9 E$$

9 TODO insert lecture from previous week in here.

10 TODO Lecture ? - HW2 review: Hw4; due 2/21; 3.4-2; 3.6-1; 3.7-3 – see next page; 3.7-4

DATE: <2018-02-14 Wed>

10.1 Freq shift

$$g(t)\cos(2\pi f_0 t) \Leftrightarrow \frac{1}{2}[G(f - f_0) + G(f + f_0)]$$

10.2 Project specs

10.2.1 Important params

- F_s = sample Rate; 8000
- bit rate R_b 214
- $\frac{F_s}{R_b} = \text{Samplesperbit}; 37.3$

$$g(t) = \Pi(t/\tau) \quad \tau = \tau_g$$

$$y(t) = g(t) * h(t)$$

$$Y(f) = G(f)H(f)$$

$H(f)$ ideal LPF bandwidth B

What is B to obtain: $E_y = 0.9 E_g$

$$E_y = \int_{-\infty}^{\infty} |Y(f)|^2 df = \int_{-\infty}^{\infty} |G(f)H(f)|^2 df = \int_{-B}^B |G(f)|^2 df = 2 \int_0^B |G(f)|^2 df = 2 \int_0^B \text{sinc}^2(\pi f \tau) df = 0.9 E_g$$

11 Lecture ? - Bell 103 modems specs?


:DATE: <2018-02-19 Mon>

11.1 A history of Modem Sounds:

200 Baud to 56K

- Early modems sounds tonal, and later, highspeed modems sounds noisy.
- Connection sequence occurs
- YT: [ckc6XSSh52w](#)
- oona.windytan.com/posters/dialup-final.png
 - Short time fourier transform


11.2 DONE Choices: Get clarification of stopbits; Use two '1' bits as stop signal.

- Answering and originating tones, we will use higher tones.
 - High tones are answer tones
 - Data rate 100 bps
 - USE 2 stop bits. Not the same as the 0start and 1 stop bit.
 - Use continuous phase, no discontinuity. 

11.3 TODO HW 5 due 2/26; 3.8-4, 4.2-1, 4,2-7

11.4 Power Spectral Density PSD

Almost a perfect parallel to ESD Watts/Hz

- Computed differently
 - **Autocorrelation** $R_g(\tau) = \liminf \frac{1}{T} \int -TT/2g * (t)G(t + \tau)$
 - **Power Spectral Density** $S_g(f) = \mathbf{F} \{R_g(\tau)\}$
- ESD
 - autocorrelation
 - $\psi_g(\tau) = \int_{-\infty}^{\infty} g * (t)g(t + \tau)dt$
 - ESD $\Psi_g(f) = \mathbf{F} \{\psi_g(\tau)\}$
- Where would we use PSD?
- A set of data 
- Can't take the FT of binary data.

11.5 LTI Systems

$x(t) \rightarrow y(t)$

$$\text{ESD } \Psi_y(f) = \Psi_x(f)|H(f)|^2$$

$$\text{ESP } S_y(f) = S_x(f)|H(f)|^2$$

11.6 Noise - AWGN Additive White Gaussian Noise

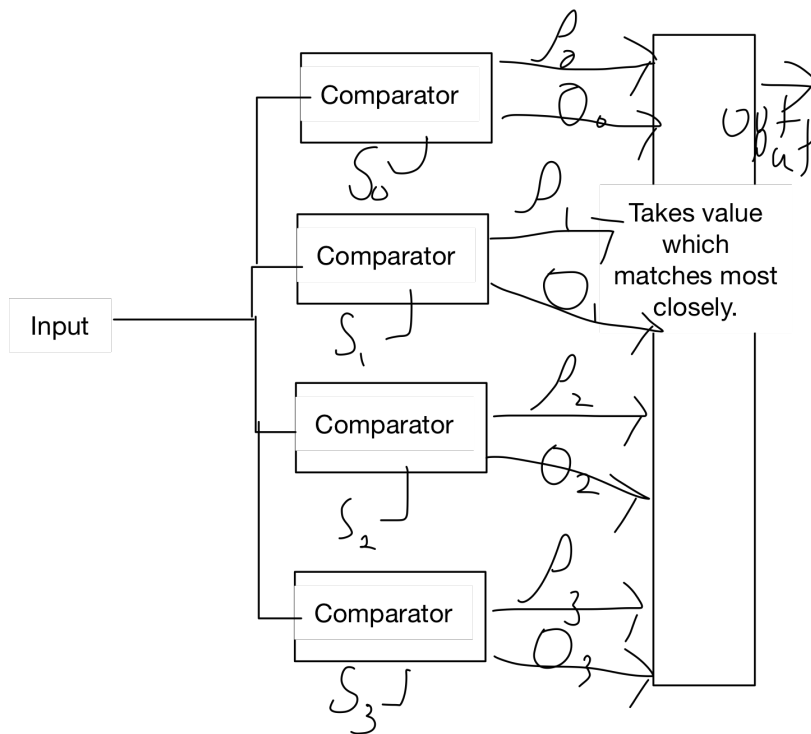


Figure 1: internals of Digital receiver with two-bit decode