

# Digital Transmitters and Receivers

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## 1 Lecture 1 - History of Communication

This is mt, I have not a copy of these notes. Mainly discussed how in the last 120 years we/society has gone from using semaphores to using modern fast as light coms.

## 2 Lecture 2 - A cont. of lecture 1

More info I don't have a copy of. . .

## 3 Lecture 3

## 4 Lecture ?

:DATE: <2018-02-05 Mon>

Use correlators to match input to possible transmitted waveforms

## 5 Lecture ?

### 5.1 Transmitter

### 5.2 Reciever

two bits per symbol - four possible wave forms

symbol	bits	four possible waveforms
0	00	$0^0$
1	01	$90^0$
2	10	$180^0$
3	11	$270^0$

## 6 Lecture ?

### 6.1 Fourier Transfrom

- $\mathbf{F} \{g(t)\} = G(f) = \int_{-\inf}^{\inf} g(t)e^{-j2\pi ft}$

- $\mathbf{F}^{-1} \{G(f)\} = g(t) = \int_{-\infty}^{\infty} G(f) e^{j2\pi ft} df$

### 6.1.1 TODO Properties: verify that 6.1.1 is correct

- Linearity

$$- \mathbf{F} a_1 x_1(t) + a_2 x_2(t) = a_1 \mathbf{F} x_1(t) + a_2 \mathbf{F} x_2(t)$$

- Time Shift

$$\begin{aligned} - \mathbf{F} x(t - T_0) &= \int_{-\infty}^{\infty} x(t - t_0) e^{-j2\pi ft} dt \\ \lambda &= t - t_0 \\ &= e^{-j2\pi f t_0} \int_{-\infty}^{\infty} x(\lambda + t_0) e^{-j2\pi f \lambda} d\lambda \quad (\text{EQ1}) \\ &= e^{-j2\pi f t_0} X(f) \end{aligned}$$

- Frequency Property

$$- \mathbf{F}^{-1} X(f - f_0) = e^{j2\pi f_0 t} \int_{-\infty}^{\infty} x(t) e^{-j2\pi (f - f_0) t} dt$$

## 6.2 TODO Graham-Schmidt: check matrix algebra book on this topic.

:DEADLINE: <2018-02-05 Mon>

- Signals  $S_1(t), \dots, S_m(t)$
- basis functions  $\phi_1(t), \dots, \phi_n(t)$ ,  $N \neq M$
- $S_i(t) = \sum_{n=1}^N S_{in} \phi_n(t)$
- $\mathbf{S}_i = [S_{i1} \ S_{i2} \ \dots \ S_{in}]$

### 6.2.1 1st signal

$$\begin{aligned} E_{s1} &= \|S_1\|^2 \\ \phi_1 &= \frac{S_1(t)}{\sqrt{E_{s1}}} \\ S_{11} &= \sqrt{E_{s1}} \end{aligned}$$

### 6.2.2 2nd – Nth signal

*Creating a new basis function*

$$S_{21} = \langle S_2(t), \phi_1(t) \rangle$$

$$r_2(t) = S_2(t) - S_{21} \phi_1(t) \leftarrow \text{orthogonal to } \phi_1(t)$$

If remained  $r_i(t) = 0$  skip the steps below

- The part of signal 2 that can't be represented by  $\phi_1(t)$ .

$$E_{r2} = \|r_2(t)\|^2$$

$$\phi_2(t) = \frac{r_2(t)}{\sqrt{E_{r2}}}$$

$$S_{22} = \sqrt{E_{r2}}$$

- others

$$S_{ni} = \langle S_n(t), \phi_i(t) \rangle \text{ for } \phi_i(t) \text{ which are defined.}$$

$$r_i(t) = S_i(t) - \sum \{S_{in}\} \phi_n(t)$$

:DATE: <2018-02-09 Fri>

## 6.3 Distortionless System

$$x(t) \rightarrow y(t)$$

### 6.3.1 Acceptable

- Amplification//

$$y(t) = K x(t)$$

- Delay

$$y(t) = x(t - t_0), \quad t_0: \text{positive integer, positive required for causality}$$

- Overall//

$$y(t) = Kx(t - t_0)$$

## 6.4 Freq representation

$$Y(f) = K e^{-j2\pi f t_0} X(f) = H(f) X(f) \text{ Linear time invariant. where } H(f) = K e^{-j2\pi f t_0}$$

$$h(t) = K \delta(t - t_0)$$

## 6.5 Bode rep

$$H(f) = K e^{-j2\pi f t_0}$$

$$H(f) = K < -constant Mag(gain)$$

$$\angle H(f) = -2\pi f t_0 < -linear, slope = -2\pi f$$

$$\text{Group Delay: } t_g(f) = \frac{-1}{2\pi} \frac{d}{df} (\angle H(f))$$

## 6.6 Filters

- ideal

- realistic

- Lowpass
- Highpass
- Bandpass
- Bandstop

filter type	ideal	realistic
lowpass	sharp rect	around center
highpass		hill flat top
bandpass		
bandstop		

## 7 LEcture ? -

:DATE: <2018-02-12 Mon>

### 7.1 TODO Project

### 7.2 Fourier Series - Fourier Transform Relationship

#### 7.2.1 Fourier Series

$$\text{F.S. } g(t) = \sum_{-\infty}^{\infty} G_n e^{jn2\pi f_0 t}$$

$$\text{F.T. } G(f) = \int_{-\infty}^{\infty} g(t) e^{-jn2\pi f t} dt = \sum_{-\infty}^{\infty} G_n \delta(f - f_0)$$

-> inf.

### 7.3 Energy spectral density???????????

$$E_g = \int_{-\infty}^{\infty} |G(f)|^2 df$$

$$x(t) \rightarrow h(t) \rightarrow y(t)$$

$$X(f) \rightarrow H(f) \rightarrow Y(f)$$

$$E_y = \int_{-\infty}^{\infty} |X(f)H(f)|^2 df = \int_{f_0-f}^{f_0+\Delta f} \text{Energy Spectral Density}$$

$$\Psi_x(f_0) = \lim_{\Delta f \rightarrow 0} \frac{1}{\Delta f} \int_{f_0-\frac{\Delta f}{2}}^{f_0+\frac{\Delta f}{2}} |X(f)|^2 df = |X(f_0)|^2$$

$$\text{Energy } E_x = \int \Psi_x(f) df$$

$$\text{Energy int bandwidth } B \text{ centered at } f_1 \int_{f_1-\frac{B}{2}}^{f_1+\frac{B}{2}} \Psi_x(f) df = \int_{f_1-\frac{B}{2}}^{f_1+\frac{B}{2}} \Psi_x(f) df$$

## 8 TODO get units for

$$\text{let: } \Psi_g(t) = \Pi(t) \frac{90}{\text{What bandwidth capacity do we need to pass exactly}}$$

$$E_g = \int |g(t)|^2 dt = \Psi_g(t) \rightarrow \text{"Ideal LPF bandwidth } B" \rightarrow y(t) \quad 90\% E_g =$$

0.9T energy

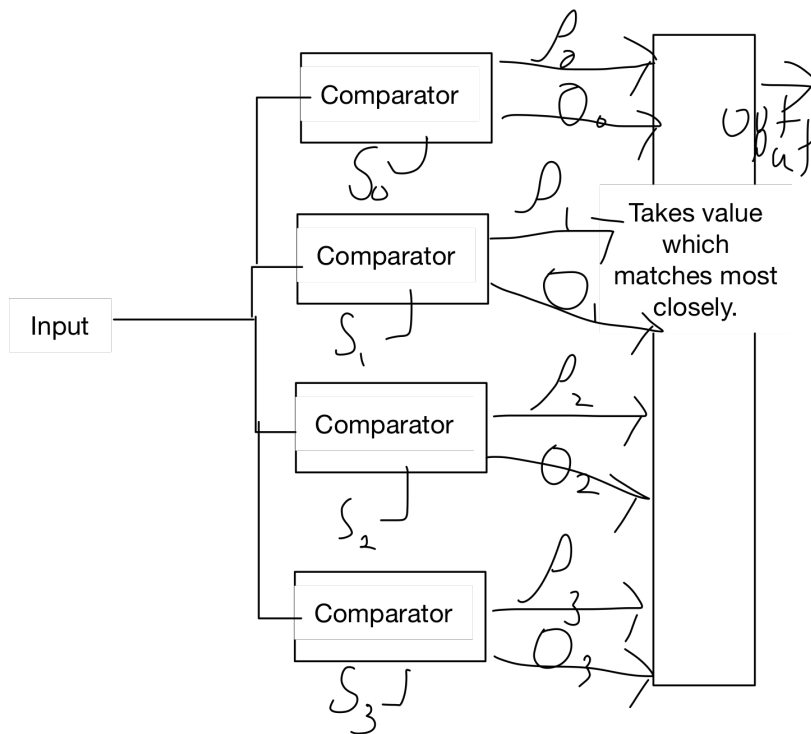


Figure 1: internals of Digital receiver with two-bit decode