

# Digital Transmitters and Receivers

February 6, 2018

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## 1 Lecture 1 - History of Communication

This is mt, I have not a copy of these notes. Mainly discussed how in the last 120 years we/society has gone from using semaphores to using modern fast as light coms.

## 2 Lecture 2 - A cont. of lecture 1

More info I don't have a copy of. . . .

### 3 Lecture 3

### 4 Lecture ?

:DATE: <2018-02-05 Mon>

#### 4.1 Transmitter

two bits per symbol - four possible wave forms

symbol	bits	four possible waveforms
0	00	$0^0$
1	01	$90^0$
2	10	$180^0$
3	11	$270^0$

#### 4.2 Reciever

Use correlators to match input to possible transmitted waveforms

#### 4.3 TODO Graham-Schmidt: check matrix algebra book on this topic.

- Signals  $S_1(t), \dots, S_m(t)$
- basis functions  $\phi_n(t), \dots, \phi_N(t)$ ,  $N \neq M$
- $S_i(t) = \sum_n a_{in} \phi_n(t)$
- $\mathbf{S}_i = [S_{i1} \ S_{i2} \ \dots \ S_{iN}]$

##### 4.3.1 1st signal

$$E_{s1} = \|S_1\|^2$$
$$\phi_1 = \frac{S_1(t)}{\sqrt{E_{s1}}}$$
$$S_{11} = \sqrt{E_{s1}}$$

##### 4.3.2 2nd – Nth signal

*Creating a new basis function*

$$S_{21} = \langle S_2(t), \phi_1(t) \rangle$$

$$r_2(t) = S_2(t) - S_{21} \phi_1(t) \leftarrow \text{orthogonal to } \phi_1(t)$$

If remainted  $r_i(t) = 0$  skip the steps below

- The part of signal 2 that can't be represented by  $\phi_1(t)$ .

$$E_{r2} = ||r_2(t)||^2$$

$$\phi_2(t) = \frac{r_2(t)}{\sqrt{E_{r2}}}$$

$$S_{22} = \sqrt{E_{r2}}$$

- others

$$S_{ni} = \langle S_n(t), \phi_i(t) \rangle \text{ for } \phi_i(t) \text{ which are defined.}$$

$$r_i(t) = S_i(t) - \sum \{S_{in}\} \phi_n(t)$$

#### 4.4 Fourier Transform

- $\mathbf{F} \{g(t)\} = G(f) = \int_{-\infty}^{\infty} g(t) e^{-j2\pi ft} dt$
- $\mathbf{F}^{-1} \{G(f)\} = g(t) = \int_{-\infty}^{\infty} G(f) e^{j2\pi ft} df$

##### 4.4.1 TODO Properties: verify that 4.4.1 is correct

- Linearity

$$\mathbf{F} \{a_1 x_1(t) + a_2 x_2(t)\} = a_1 \mathbf{F} \{x_1(t)\} + a_2 \mathbf{F} \{x_2(t)\}$$

- Time Shift

$$\begin{aligned} \mathbf{F} \{x(t - T_0)\} &= \int_{-\infty}^{\infty} x(t - t_0) e^{-j2\pi ft} dt \\ \lambda &= t - t_0 \\ &= e^{-j2\pi f t_0} \int_{-\infty}^{\infty} x(\lambda + t_0) e^{-j2\pi f \lambda} d\lambda \quad (\text{EQ1}) \\ &= e^{-j2\pi f t_0} X(f) \end{aligned}$$

- Frequency Property

$$\mathbf{F}^{-1} \{X(f - f_0)\} = e^{j2\pi f_0 t} \int_{-\infty}^{\infty} X(f) e^{-j2\pi f t} df$$

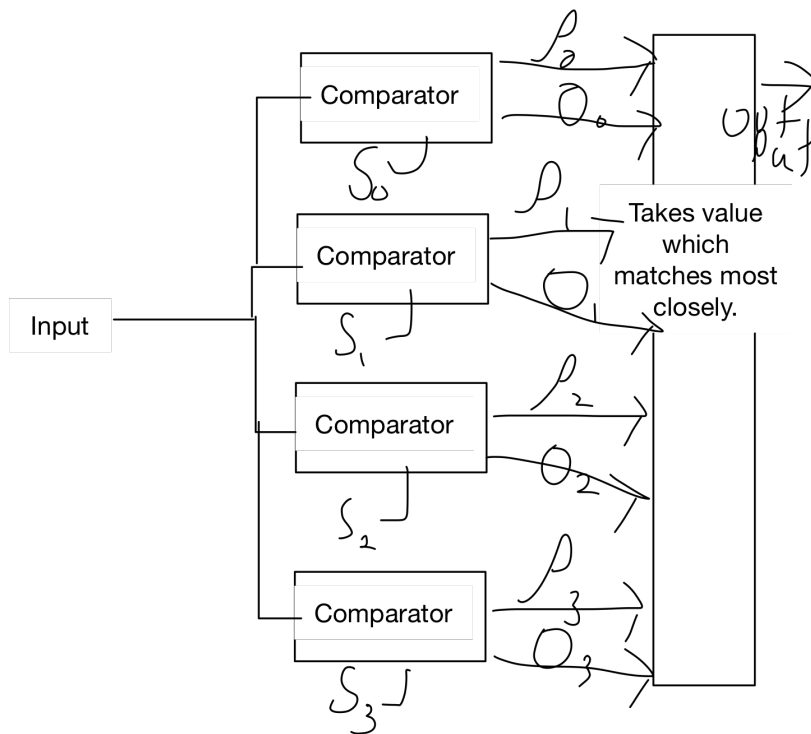


Figure 1: internals of Digital receiver with two-bit decode