

Article

Driving Risk Assessment and Classification Using Near-miss Events Based on Panel Poisson Regression and Panel Negative Binomial Regression

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Abstract: The identification and evaluation of driving risk was the primary step to calculate premiums in the newly emerging usage-based insurance. Telematics data obtained from Internet of vehicles contains a large number of near-miss events, which could be regarded as a supplement to claims or accidents in driving risk score. In this study, Poisson regression and Negative binomial regression were applied to processed summary data set and panel data set containing near-miss events, i.e. over speed, high speed brake, harsh acceleration and harsh deceleration, and driving behavior parameters without claims and accidents. Negative binomial regression performed better, and its results revealed different driving behavior parameters impact on different near-miss events and classified the vehicles according to the driving risk score. This study provided a research basis for actuarial insurance premiums and precise supervision of dangerous driving behaviors based on driving risks.

Keywords: usage-based insurance; driving risk assessment; driving risk classification; telematics; near-miss event; driving behavior; panel data regression; Poisson; Negative binomial

1. Introduction

Near-miss events provide support for actuarial premiums in the auto insurance industry. Reporting of near-miss event as an established error reduction technique has been used by many industries to manage risk and reduce accidents. In the auto insurance industry, the insurer calculated the premium by knowing how many claims the insured person made all the time. However, it was a loose calculation, when the insured one had taken accidents but did not claim. In other words, it was not accurate to use claims or accidents alone to calculate premiums. Fortunately, the advent of internet of vehicles has given an improved solution to this problem, using near-miss events to identify driving risk and calculate premiums.

This study purposes to explore how to evaluate driving risks and score drivers in the short term without claims and accidents. The model obtained in this study has important significance for driving risk identification. Not only can the model reflect the risk factors of each near-miss event, but the coefficients obtained by the model can also help us evaluate drivers' risks and rank them according to their risks. The modeling method and results are valuable for insurance companies to develop usage-based insurance (UBI) personalizing premiums and for traffic regulatory authorities to manage drivers and prevent accidents.

Near-miss events need to be extracted from the original data according to the actual requirements for further processing and analysis. Because the original telematics data in this study does not contain

claims or accidents, the extraction of near-miss events that are highly relevant to driving patterns is critical. This study was carried out on a summary data set and a panel data set containing four newly extracted near-miss events and several key parameters after data processing. Over speed, high speed braking, harsh acceleration and harsh deceleration, had been defined based on actual driving conditions and local laws and regulations. Since extracted near-miss events were unbounded non-negative integers, Poisson regression and Negative binomial regression are suitable for modeling that dependent variable conforms to this distribution law.

Poisson regression, Negative binomial regression, Zero-inflated Poisson regression and Zero-inflated Negative binomial regression were respectively applied to summary data set. The parameters in the data set, such as average speed, brake times, accelerator pedal position, engine fuel rate etc., were selected as independent variables. In particular, mileage or fuel consumption was chose as exposure variables to offset the impact of non-unit capacity on model accuracy. In order to have a clear understanding of risky factors of different near-miss events, each near-miss event was individually used as dependent variables. However, no matter which one was selected as the dependent variable, Negative binomial regression is the method more suitable than the others for the summary data in this study.

Negative binomial regression also performed better than Poisson regression on panel data sets. Individual effects and time effects were estimated using panel Poisson regression and panel Negative binomial regression on short panel data set of 5 days in length. The regression results not only confirmed the existence of individual effect and time effect but also rated the driving risk of each vehicle. Then, according to these scores, the driving risk level of vehicles can be classified, providing an important reference for further accurate calculation of premiums.

The rest of this article is organized as follows. The development of UBI and previous efforts on driving risk assessment are summarized in Section 2. Section 3 described the data and introduced the key parameters used in modeling. Section 4 listed the model expression of Poisson regression and Negative binomial regression in this study. Negative binomial regression results on summary data set and panel data set were reported and analysed in Section 5. The results were discussed and the conclusions were presented in Section 6.

2. Literature Review

The auto insurance industry has never stopped pursuing actuarial premiums. Traditional auto insurance business has been limited by the difficulty of obtaining information of policy holder, which mainly focused on the utilization of basic information of drivers, vehicles and driving sections[1]. With the continuous progress of information technology, a new type of insurance business, UBI, based on multi-source data and personalized premium calculation is becoming the mainstream. It has experienced the pay-as-you-drive (PAYD) mode of charging premiums according to the driving mileage or fuel consumption which indicates the probability of accidents[2]. Then it is transiting to the pay-how-you-drive (PHYD) mode of calculating premiums based on multiple sources of data including driving behavior data that reflect driving risk[3]. As the development of 5G communication technology, it may be possible to realize the manage-how-you-drive (MHYD) mode i.e. real-time calculation of premiums based on multi-source data and providing real-time information to drivers to restrain bad driving behavior[1,4]. However, due to various reasons such as technologies, policies, regulations and privacy[5], there is even no mature PHYD product on the market at present[6,7]. As the core issue of UBI, driving risk needs to be further studied to produce products that are more suitable for demands[8].

Traffic accidents all over the world cause a large number of casualties every year, and high risk driving is one of the main factors that cause traffic accidents[1]. Therefore, the research on driving risk has been a hot topic in recent years. Fundamentally, there were simulation experiments in the laboratory setting designed to identify driving risk factors and predict driving risks[9–12]. Further, there were real vehicle experiments on real road environment conducted to evaluate driving risk[13–17].

In addition, there were studies to make a questionnaire survey for driving risk assessment[18,19]. In fact, the naturalistic driving data collected by the Internet of vehicles or smart phones, telematics data, can effectively reduce the influence of subjective factors and unreasonable assumptions, so as to obtain more objective and meaningful research results[20–24].

In the research of driving risk assessment in the auto insurance industry, machine learning and generalized linear model coexist. With strong ability to process big data efficiently, machine learning is increasingly explored to auto insurance business due to increasing amounts of data. Logistic regression[25], cluster analysis[26], decision tree[3], support vector machine[27], neural network[28] and other machine learning models[29–31] have been widely studied in the field of driving risk assessment, and the results also show that machine learning has a good effect in that[32]. However, since most machine learning algorithms as black box algorithms do not have good interpretability and stability, they cannot completely replace the conventional generalized linear models in the auto insurance industry[6].

Generally, the conventional generalized linear models paid more attention to the correlation between influencing factors and claims or accidents in the study of driving risk[7,22,23,33]. Most of the databases used in the study contain claims and accidents. But the study of near-miss events due to the lack of claims and accidents should not be ignored[13,34], on the contrary, they could be good complements to previous studies and have important significance for driving risk assessment.

To sum up, this study put forward a novel approach of driving risk assessment. In the absence of claims and accidents, the Negative binomial regression results on the panel data set of naturalistic driving data could not only reflect the causal relationship between independent variable driving behavior factors and dependent variable near-miss events, but also provided individual effects as driving risk scores for each observation. This approach gave consideration to both interpretability and practicability, and had reference value for the promotion of UBI.

3. Data Description

The telematics data used in this study is collected from an internet-of-vehicle information service provider in China. The original data set contains 182 data files representing sensor data for 182 vehicles runs from July 3, 2018 to July 8, 2018[8]. Each data file contains 62 parameters, but after data processing[35], less than one-third of the available parameters related to this study remain. Since the original data cannot be directly used for modeling, the summary data set is aggregated according to the custom statistical rules. It is basically that taking the difference value of the accumulated type, the mean value of the continuous type and the sum value of the discrete type. A summary of the processed data can be found in Table 1. Among them, *kilo*, *fuel*, *brakes*, *speed*, *rpm*, *acceleratorpedalposition* and *enginefuelrate* are obtained according to the above basic statistical rules for the original parameters, while *range* is calculated from the longitude and latitude numerical values[8].

Table 1. Descriptive statistics of summary data set.

Variable	Mean	Standard Deviation	Minimum	Maximum	Defination
overspeed	19.19	45.37	0	330	Cumulative times of driving speed greater than 90km/h
highspeedbrake	44.23	108.3	0	942	Cumulative times of braking when the driving speed is greater than 60km/h
harshacceleration	139.0	134.7	0	899	Cumulative times of the acceleration is greater than $6m/s^2$
harshdeceleration	141.9	137.8	1	913	Cumulative times of the acceleration is less than $6m/s^2$
kilo	2,223	1,674	3.73	7,164	Cumulative driving distance (km)
fuel	621.7	470.9	10.25	2,018	Cumulative fuel consumption (L)
brakes	1,588	1,426	6	9,243	Cumulative number of brakes
range	5.201	5.021	0.027	26.78	Range of driving (geographical units)
speed	36.88	16.37	0.297	67.84	Mean of speed (km/h)
rpm	1,028	188.3	233.1	1,620	Mean of revolutions per minute (r/min)
acceleratorpedalposition	21.05	7.110	0.187	39.29	Mean of acceleration pedal position (%)
enginefuelrate	11.52	4.464	1.868	22.01	Mean of engine fuel rate (%)

^a The number of each parameter is 182.

In particular, *overspeed*, *highspeedbrake*, *harshacceleration* and *harshdeceleration* are individually filtered by combining the rules of traffic law and driving code. Firstly, previous studies have confirmed that over speed is a dangerous driving behavior that is likely to cause traffic accidents[1]. And China's traffic safety regulations stipulate a maximum speed for the each type of vehicles on all types of

roads. Secondly, if the emergency braking of a car running at a high speed is operated improperly or subjected to lateral force, it is prone to side-slip or even cartwheel, thus high-speed braking is a risky near-miss event worthy of study. Thirdly, both harsh acceleration and harsh deceleration are near-miss events that need to be avoided in terms of driving safety and fuel economy. Previous studies have been referred to in defining the threshold value of harsh acceleration and harsh deceleration[34]. It can be seen from Figure 1 that near-miss events are all non-negative integers with no upper limit of frequency. Combined with the relationship between expectation and variance shown in Table 1, the four near-miss events are suitable as dependent variables of Poisson regression and Negative binomial regression.

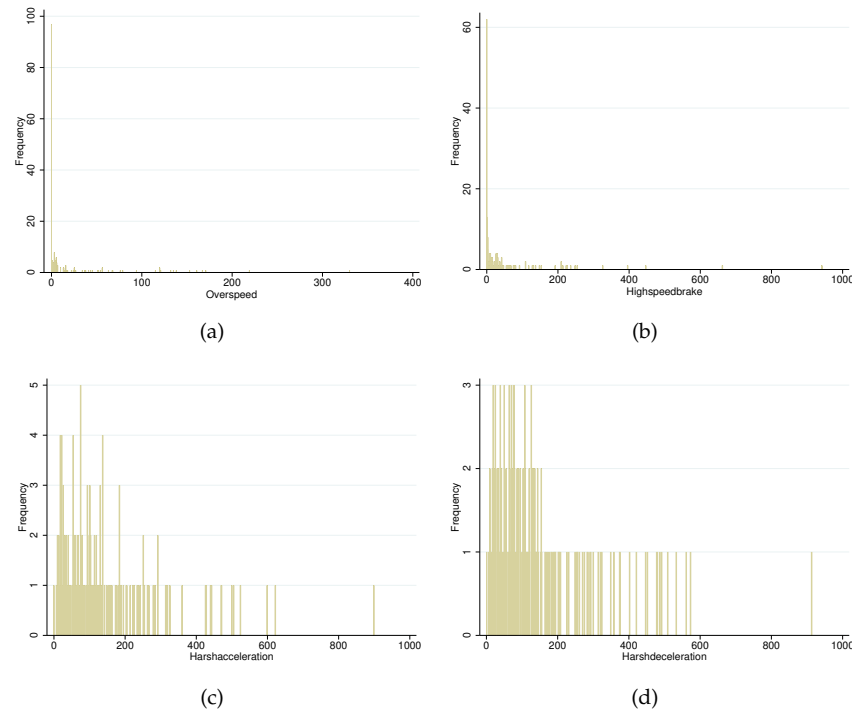


Figure 1. Histogram of frequency distribution of four near-miss events: (a)Over speed;(b)High speed brake;(c)Harsh acceleration;(d)Harsh deceleration.

The panel data set is based on the summary data set. Statistical rules and processing methods are similar to summary data sets, except that each observed value is divided into six observed values in days. The statistics of panel data set are shown in the Table 2.

4. Methods

Poisson model and Negative binomial model are both generalized linear models. Generally speaking, Negative binomial regression can be considered as a special case of Poisson regression with over-dispersion of explained variables. The probability density function of the Poisson distribution is:

$$P(Y_i = y_i | x_i) = \frac{e^{-\lambda_i} \lambda_i^{y_i}}{y_i!} \quad (1)$$

where λ_i is the Poisson arrival rate determined by explanatory variable x_i to represent the average number of events, which is equal to the expectation and variance of the explained variable $E(Y_i | x_i) = V(Y_i | x_i) = \lambda_i$.

Negative binomial is a mixture of a Poisson(λ) and a Gamma(a, b). The probability density function of the Negative binomial distribution follows the Poisson distribution:

Table 2. Descriptive statistics of panel data set.

Variable	N	Mean	Standard Deviation	Minimum	Maximum
overspeed	1,092	3.199	14.37	0	315
highspeedbrake	1,092	7.435	21.74	0	215
harshacceleration	1,092	23.37	29.78	0	223
harshdeceleration	1,092	23.86	30.16	0	233
kilo	1,092	372.6	373.2	0	1,739
fuel	1,092	104.1	105.7	0	565.8
brakes	1,092	264.7	291.0	0	1,940
range	1,092	2.406	2.963	0	14.07
speed	1,092	31.96	21.58	0	77.74
rpm	1,092	894.3	346.9	0	1,731
acceleratorpedalposition	1,092	17.51	10.19	0	45.74
enginefuelrate	1,092	9.794	5.835	0	26.18

$$f(y | a, b) = \int_0^\infty f(y | \lambda)g(\lambda | a, b)d\lambda = \frac{\Gamma(y+a)}{\Gamma(y+1)\Gamma(a)} \left(\frac{b}{1+b}\right)^a \left(\frac{1}{1+b}\right)^y \quad (2)$$

where $E(y) = \frac{a}{b} = \bar{\lambda}$ and $V(y) = \frac{a}{b} \left(1 + \frac{1}{b}\right) = \bar{\lambda} \left(1 + \frac{\bar{\lambda}}{a}\right)$.

The conditional expectation function of Negative binomial distribution, which is similar to Poisson regression, is:

$$E(y_i | x_i) = \lambda_i = t_i \times \exp(\beta_{0i} + \beta_{1i}x_{1i} + \cdots + \beta_{ki}x_{ki} + \alpha_{1i}d_{1i} + \cdots + \alpha_{ji}d_{ji} + \varepsilon_i) \quad (3)$$

where i is the serial number of the observation, k depends on the number of independent variables, j depends on the existence of time effect and individual effect, t_i takes *kilo* or *fuel* as the exposure variable, $x_{1i} \dots x_{ki}$ represent the independent variables such as *brakes*, *range*, *speed*, *rpm*, *acceleratorpedalposition* and *enginefuelrate*, dummy variable $d_{1i} \dots d_{ji}$ represent the time effect and individual effect, $\beta_{0i} \dots \beta_{ki}$ and $\alpha_{1i} \dots \alpha_{ji}$ are unknown parameters that need to be estimated, random variables ε_i represents the heterogeneity of individuals in the conditional expectation function. Regression to the Negative binomial model can be accomplished using the econometric statistics software STATA.

5. Results

Both Poisson regression and Negative binomial regression were applicable to this study, and the Zero-inflated model was taken as a consideration for the large number of zero values of dependent variables. In order to determine the most suitable model for this study, the performance of models on different dependent variables was compared. Furthermore, the fittest model on different data performed different.

5.1. Results of summary data set

In summary data set, four near-miss events were respectively treated as dependent variables. Parameters *brakes*, *speed*, *rpm*, *acceleratorpedalposition* and *enginefuelrate* were taken as independent variables. And parameter *kilo* was chosen as exposure variable. Poisson regression, Zero-inflated Poisson regression, Negative binomial regression and Zero-inflated Negative binomial regression were conducted. The regression effect of the four models on each dependent variable is shown in Table 3. It indicates that no matter which near-miss event is the dependent variable, Negative binomial regression has minimum log-likelihood value, AIC value and BIC value. That is, Negative binomial regression has the best performance and is most suitable for modeling in this data set.

Table 3. Model performances of Poisson, Zero-inflated Poisson, Negative binomial and Zero-inflated Negative binomial in summary data set.

Variable	Model	N	log-likelihood	df	AIC	BIC
overspeed	POS	182	-3518.92	7	7051.846	7074.274
	ZIP	182	-2369.82	8	4755.64	4781.272
	NB	182	-490.517	8	997.0338	1022.666
	ZINB	182	-490.516	9	999.0315	1027.868
highspeedbrake	POS	182	-2830.75	7	5675.498	5697.926
	ZIP	182	-2667.02	8	5350.034	5375.666
	NB	182	-627.422	8	1270.843	1296.476
	ZINB	182	-627.422	9	1272.843	1301.68
harshacceleration	POS	182	-5857.26	7	11728.51	11750.94
	ZIP	182	-5857.26	8	11730.51	11756.14
	NB	182	-1032.81	8	2081.623	2107.255
	ZINB	182	-1032.81	9	2083.623	2112.459
harshdeceleration	POS	182	-6269.47	7	12552.93	12575.36
	ZIP	182	-6269.47	8	12554.93	12580.56
	NB	182	-1037.14	8	2090.285	2115.917
	ZINB	182	-1037.14	9	2092.285	2121.121

According to the results of Negative binomial regression in different dependent variables (seeing Table 4), different near-miss events are affected by different driving risk factors with different influences. Relatively speaking, the number of braking has the most obvious influence on near-miss events, it has a significant positive effect on high speed braking(0.000191), harsh acceleration(0.000133) and harsh deceleration(0.000126). The impact of average speed on near-miss events is also significant. The higher the average driving speed, the less rapid acceleration(-0.0474) and rapid deceleration(-0.0402) occur. In addition, average RPM is positively correlated with harsh acceleration(0.000947), and average accelerator pedal position is positively correlated with harsh acceleration(0.0214) and harsh deceleration(0.0330). Interestingly, some influencing factors have opposite effects on different dependent variables. Range of driving has positive effect on high speed brake(0.0541) but negative effect on harsh deceleration(-0.0305). And average engine fuel rate has a significant positive effect on high speed braking(0.158) but a negative effect on sharp deceleration(-0.0351). What's more, the significance of the constant term indicates that in addition to the factors considered in this study, there are other factors that also influence near-miss events.

Table 4. Negative binomial regression results for four near-miss events.

Variable	overspeed	highspeedbrake	harshacceleration	harshdeceleration
Constant	-7.536*** (-3.363)	-8.456*** (-7.526)	-2.101*** (-4.006)	-1.903*** (-3.933)
brakes	0.000185 (1.293)	0.000191*** (2.601)	0.000133*** (3.384)	0.000126*** (3.450)
range	0.0369 (0.791)	0.0541** (2.052)	-0.0200 (-1.287)	-0.0305* (-1.942)
speed	-0.00690 (-0.200)	0.0152 (1.277)	-0.0474*** (-8.810)	-0.0402*** (-7.201)
rpm	0.000666 (0.431)	-0.000128 (-0.113)	0.000947* (1.896)	0.000515 (1.072)
acceleratorpedalposition	0.0407 (1.130)	0.0241 (1.028)	0.0214* (1.872)	0.0330*** (2.815)
enginefuelrate	0.0508 (0.987)	0.158*** (4.493)	-0.0198 (-1.116)	-0.0351** (-2.073)
log-likelihood	-490.5169	-627.4217	-1032.811	-1037.142
AIC	997.0338	1270.843	2081.623	2090.285
BIC	1022.666	1296.476	2107.255	2115.917
Observations	182	182	182	182

^a Robust z-statistics in parentheses ^b *** p<0.01, ** p<0.05, * p<0.1

5.2. Results of panel data set

As shown in Table 5, the evaluation index(log-likelihood, AIC and BIC) of Negative binomial regression is lower than that of Poisson regression under each dependent variable. Therefore, Negative binomial regression is better than Poisson regression on panel data.

The panel Negative binomial regression was used to estimate the two-way fixed effect model considering both individual effect and time effect on four dependent variables. The influencing factors reflected by it(seeing Table A1) are not all the same as the results of summary data. What remains is that rapid acceleration and rapid deceleration are positively affected by the number of brakes(0.000845&0.000869) and average accelerator pedal position(0.0244&0.0265) but negatively affected by the average speed(-0.0299&-0.0272) and average engine fuel rate(-0.0323&-0.0392). However, RPM which is not significant in the summary data is significantly positive for over speed(0.00485) and high speed braking(0.00371).

The advantage of panel data over summary data is that it can show individual effects and time effects of different observations. The time effect exists in most cases under high speed braking, rapid acceleration and rapid deceleration, which indicates that these three near-miss events are greatly influenced by time. The time effect of the over speed event is significant for only one day, suggesting that it is less influenced by time. Most importantly, the individual effects of the four near-miss events

Table 5. Model performances of Poisson and Negative binomial in panel data set.

Variable	Model	N	log-likelihood	df	AIC	BIC
overspeed	XTPOS	1092	-1926.78	188	4229.559	5168.763
	XTNB	1092	-957.497	189	2292.993	3237.193
highspeedbrake	XTPOS	1092	-2594.37	188	5564.733	6503.937
	XTNB	1092	-1527.05	189	3432.105	4376.305
harshacceleration	XTPOS	1092	-6117.44	188	12610.89	13550.09
	XTNB	1092	-3526.09	189	7430.186	8374.386
harshdeceleration	XTPOS	1092	-6042.02	188	12460.03	13399.24
	XTNB	1092	-3547.66	189	7473.311	8417.51

are significant in most cases, and the individual regression coefficient could be used to score each observation. It should be noted that the first individual has been omitted in the regression to avoid complete multicollinearity, and its value is expected to be zero in the subsequent driving risk score.

6. Discussions and Conclusions

In this study, driving risks can be evaluated by the regression coefficient of Negative binomial models on panel data. Four near-miss events have been used as dependent variables to obtain four sets of regression coefficients. Given the influencing factors and generating mechanisms of different near-miss events are different, so it is not recommended to combine the four groups of regression coefficients into one group. Within a group, a higher coefficient means a higher probability of the near-miss event.

In order to more intuitively reflect the risk relationship between observations, it is suggested to carry out driving risk grading. Firstly, winsorization could be done to avoid the influence of possibly spurious outliers (the double tail was winsorized with the threshold 0.01 in this study). Secondly, the regression coefficient need to be compressed to the interval of [0,1] through normalization. Then, the corresponding grade will be obtained by enlarging corresponding multiple according to actual demands. For example, we mapped each group of coefficients into an interval of [0,5] (seeing Table A2), each observation got a driving risk level from 1 to 5, i.e. excellent, good, medium, bad and terrible (seeing Figure 2). To be clear, the values of 0 and 5 are because the corresponding observations are the minimum and maximum values in their group and are Min-Max scaled. In *overspeed* and *highspeedbrake* groups, two types of observations with high risk or low risk can be clearly seen. It indicates that these two near-miss events are more sensitive to driving behavior than *harshacceleration* and *harshdeceleration* and can be considered with higher priority and weight in subsequent studies. Note that the same observation(id125) has different risk levels for different near-miss events, which also explains why multiple near-miss events cannot be analyzed together. Ultimately, the premium will be charged individually according to the driving risk level of the insured one.

The number and type of dependent variables and independent variables selected in this study are limited by the size and quality of original data. With the development and innovation of big data technology of IoV, the amount and dimension of data will be greatly increased. Therefore, near-miss events as dependent variables can be increased or decreased flexibly according to needs. It is recommended to include sharp turn as a risk event if possible, because sharp turn is highly studied and accident-proven patterns of high driving risk. For the same, more driving behavior parameters such as steering wheel angle speed and brake pedal position can be used as independent variables

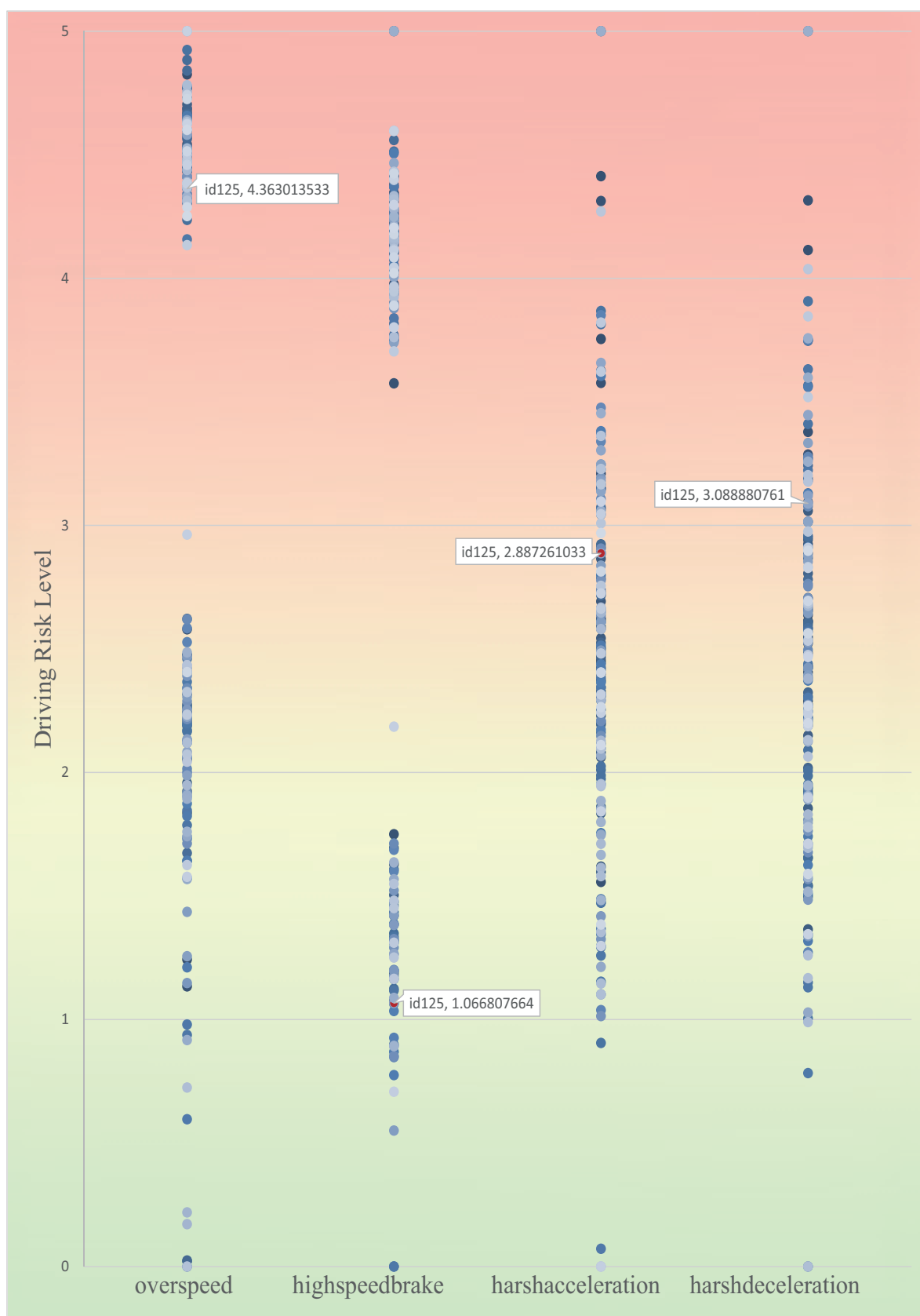


Figure 2. Driving risk rank of four near-miss events.

in the regression model. In addition, traditional auto insurance factor, driver information, vehicle information, road information, environment information etc. should be considered to provide more optional independent variables for the model.

In practical applications, near-miss events can be combined with claims and accidents to accurately evaluate driving risks. The study proves that near-miss events can be used as driving risk score when there is no claims and accidents. However, when claims or accidents exist, it is recommended to adopt the driving risk evaluation strategy as follows. The driving risk score obtained from claims or accidents can be used as the basis for premium calculation, while the driving risk rating obtained from near-miss events can be used to remind and warn drivers to reduce the corresponding dangerous driving habits.

In general, near-miss events can provide insurers with effective risk information in the absence of claims and accident data. Negative binomial regression is the most suitable modeling method for near-miss events as dependent variables. Negative binomial regression can score and rate the driving risk for the insured, and the evaluation result can help the insurer to actualize the auto insurance premium. This study provides a technical reference for the promotion and development of PHYD mode.

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Abbreviations

The following abbreviations are used in this manuscript:

POS	Poisson
ZIP	Zero-inflated Poisson
NB	Negative binomial
ZINB	Zero-inflated Negative binomial
XTPOS	Panel Poisson
XTNB	Panel Negative binomial
AIC	Akaike information criterion
BIC	Bayesian information criterion

Appendix A

Table A1. Panel Negative binomial regression results for four near-miss events.

Variable	overspeed	highspeedbrake	harshacceleration	harshdeceleration
Constant	-8.820***	-8.364***	-2.029***	-2.035***
brakes	-0.000138	0.000174	0.000845***	0.000869***
range	-0.0215	-0.00365	-0.00139	-0.0201
speed	-0.00188	-0.00447	-0.0299***	-0.0272***
rpm	0.00485**	0.00371***	0.000412	0.000417
acceleratorpedalposition	0.0384	0.0172	0.0244**	0.0265**
enginefuelrate	0.0193	0.0505	-0.0323*	-0.0392**
2018-07-04	0.273	0.216*	-0.111**	-0.216***
2018-07-05	-0.168	-0.0572	-0.206***	-0.317***
2018-07-06	-0.00718	-0.228**	-0.257***	-0.370***
2018-07-07	-0.477**	-0.200*	-0.485***	-0.600***

2018-07-08	0.206	0.117	-0.694***	-0.784***
id2	-29.70***	-2.001**	1.266***	1.342***
id3	-19.47***	-17.47***	2.004**	1.740***
id4	-18.62***	-16.69***	1.891***	1.960***
id5	-30.60***	-4.956***	-1.193***	-1.072***
id6	-1.478**	-0.554*	1.067***	0.935***
id7	-3.237***	-0.645	0.656***	0.835***
id8	-21.39***	-2.368***	-0.190	0.124
id9	-1.156	-0.0679	-0.251	-0.109
id10	-3.110***	-1.527***	-0.345**	-0.256
id11	-2.026**	-1.163***	-0.162	-0.272
id12	-1.342**	-0.772**	0.0781	0.0981
id13	-2.344***	-0.808**	-0.138	-0.129
id14	-3.178***	0.442	-0.629***	-0.365**
id15	-1.254**	0.167	-0.0894	0.0270
id16	-23.00***	-20.31***	0.271	0.439**
id17	-22.41***	-2.102***	-0.200	0.0983
id18	-21.61***	-0.805	-1.124***	-1.267***
id19	-0.998	0.380	0.587***	0.586***
id20	-24.78***	-3.749***	0.292	0.0926
id21	-22.39***	-2.577***	0.322	0.458***
id22	-2.642***	-0.229	0.496***	0.538***
id23	-0.792	0.00111	-0.474	-0.409*
id24	-24.05***	-21.10***	-0.329	-0.103
id25	-21.70***	-19.47***	-0.882***	-0.731**
id26	-2.739***	-1.000***	-0.440*	-0.667***
id27	-23.77***	-20.99***	-0.0464	0.0656
id28	-18.27***	-17.04***	0.0432	0.309
id29	-1.137	-0.872**	0.591***	0.625***
id30	-21.14***	-18.81***	-0.223	-0.102
id31	-0.407	-0.632**	-1.148***	-0.949***
id32	-3.255***	-2.923**	-0.110	0.143
id33	-19.47***	-18.27***	-0.177	-0.153
id34	-2.431***	-1.547***	-0.00573	-0.0439
id35	-3.832***	-1.041**	-0.607***	-0.552***
id36	-4.135***	-2.411***	-0.285	-0.343*
id37	-39.82***	-1.232*	-0.480	-0.218
id38	-20.79***	-1.364**	-1.484***	-1.121***
id39	-39.80***	10.89***	11.65***	11.77***
id40	-1.325	-0.416	-0.278	0.0791
id41	-2.443***	-1.020**	0.180	0.155
id42	-0.467	0.442	0.607	0.398
id43	-2.164**	0.219	-0.0359	0.0900
id44	-2.465***	-0.156	0.336	0.468*
id45	-2.110***	-1.315***	0.105	0.282
id46	0.132	-0.480	-0.312***	-0.235*
id47	-2.957***	-0.975	-0.853***	-0.656***
id48	0.486	1.381***	0.829***	0.787***
id49	-26.13***	-1.575***	-0.568***	-0.353*
id50	-2.556***	-1.907***	-0.413**	-0.331*

id51	-21.19***	-19.04***	1.123***	1.140***
id52	-21.82***	-20.71***	-0.354	-0.952***
id53	-21.26***	-19.27***	-0.133	0.200
id54	-4.881***	-1.082***	-0.686***	-0.639***
id55	-4.290***	-1.731***	0.472*	0.476
id56	-2.462***	-0.0866	0.119	0.377
id57	-21.86***	-0.700	0.110	0.719**
id58	-1.877*	-0.692	-0.344	0.0660
id59	-40.00***	-0.0709	-0.726**	-0.587*
id60	-3.117***	-3.813***	-0.711**	-0.565*
id61	0.821	1.078*	-1.288***	-1.076**
id62	-0.465	0.546	-0.670	-0.473
id63	-22.05***	-19.52***	1.393***	1.513***
id64	-2.529	-1.707	1.334***	1.339***
id65	-22.00***	-19.36***	-1.923***	-1.288***
id66	-1.389	-1.510***	0.504***	0.971***
id67	-26.39***	-3.400***	-0.371**	-0.304*
id68	-19.61***	-17.60***	-1.286***	-1.660***
id69	-25.19***	-20.76***	-0.589***	-0.625**
id70	-21.81***	-3.693***	-1.489***	-1.501***
id71	-32.23***	-28.28***	0.587***	1.212***
id72	-5.534***	-1.058*	-0.516	-0.643*
id73	-4.323***	-2.863***	-1.527***	-1.523***
id74	-31.88***	-27.94***	0.299	0.765***
id75	-2.868***	-1.677***	-0.267	-0.0911
id76	-21.77***	-22.16***	-1.646***	-1.903***
id77	-20.38***	-18.72***	0.835***	0.729***
id78	-24.70***	-3.260***	-2.855***	-2.759***
id79	-3.449***	-0.618	-0.232	-0.110
id80	-22.34***	-20.24***	-0.0149	0.0509
id81	-35.06***	-1.132**	-0.341**	-0.336**
id82	-1.391	-0.541	-0.312	-0.326
id83	-1.516***	0.157	-0.123	-0.242
id84	-24.88***	-1.866**	-0.750***	-0.855***
id85	-22.91***	-3.843***	-1.430***	-1.318***
id86	-29.96***	-2.036***	-1.272***	-1.111***
id87	-1.851**	1.034***	0.196	0.425**
id88	-20.59***	-18.45***	-0.208	-0.165
id89	-26.39***	-22.35***	1.100**	1.135**
id90	-4.008***	-0.841	-0.972***	-0.982***
id91	-20.05***	-19.02***	0.676***	0.818***
id92	-26.97***	-22.96***	0.848**	0.663**
id93	-24.47***	-21.29***	-0.290	-0.300
id94	-2.684***	-1.034***	-0.157	0.0139
id95	-25.60***	-21.99***	-0.503	-0.670
id96	-23.42***	-20.46***	1.374***	1.343***
id97	-21.44***	-19.45***	-0.464**	-0.282
id98	-19.05***	-17.65***	-1.405***	-0.887**
id99	-18.58***	-17.09***	-1.774***	-1.369***
id100	-4.226***	-20.22***	0.802**	0.824**

id101	-23.30***	-20.24***	0.955**	0.814*
id102	-25.66***	-22.49***	0.0308	-0.0294
id103	-18.28***	-16.93***	0.542**	0.606***
id104	-20.60***	-18.55***	0.131	0.262**
id105	-3.426***	-0.430	-0.464	-0.925**
id106	-25.81***	-22.46***	0.317*	0.252
id107	-21.63***	-19.42***	0.0144	0.147
id108	-24.10***	-2.647***	-0.532**	-0.635***
id109	-21.46***	-19.64***	-0.347***	-0.782***
id110	-21.03***	-20.38***	-1.801***	-1.044***
id111	-3.405***	-1.277***	0.173	0.198
id112	-20.18***	-18.15***	-1.453***	-0.831***
id113	-30.49***	-2.997***	-1.703***	-1.296***
id114	-24.22***	-21.07***	0.637***	0.537***
id115	-22.90***	-20.24***	-0.0179	-0.109
id116	-22.43***	-3.753***	-1.349***	-1.135***
id117	-21.32***	-19.05***	-0.156	-0.273**
id118	-19.53***	-0.705	0.116	0.00337
id119	-20.89***	-18.80***	-0.145	-0.143
id120	-28.10***	-24.40***	-0.0170	0.133
id121	-29.59***	-0.687*	0.239	0.387**
id122	-22.31***	-2.515**	0.623**	0.653**
id123	-23.52***	-3.892***	0.698	0.886**
id124	-4.268**	-2.612**	0.698***	0.361
id125	-3.828**	-21.08***	0.296	0.619*
id126	-2.023	-2.183**	0.576*	0.539*
id127	-22.73***	-19.80***	1.158***	1.010***
id128	-21.55***	-19.82***	0.762***	0.618**
id129	-1.540**	0.777**	0.0280	0.165
id130	-25.56***	-22.20***	-1.578***	-1.635***
id131	-1.659**	-0.403	-0.980***	-0.794***
id132	-19.92***	-17.86***	-0.863***	-0.435*
id133	-27.00***	-2.904***	-0.622***	-0.691***
id134	-32.40***	-2.618***	0.488**	1.176***
id135	-24.19***	-20.95***	0.930***	1.350***
id136	3.358***	4.212***	2.661***	2.709***
id137	-24.30***	-2.508***	0.0440	0.804***
id138	-19.39***	-17.42***	-0.827***	-0.890***
id139	-4.105***	-1.187**	-0.922***	-0.677
id140	-2.970***	-0.615	-1.276***	-1.035***
id141	-25.41***	-22.20***	-1.071***	-1.100***
id142	-38.18***	-0.873*	0.0500	0.175
id143	-38.58***	-0.397	-0.368	-0.157
id144	-0.585	0.551	0.0261	0.167
id145	-2.485**	-1.273**	-0.750	-0.631
id146	-23.85***	-1.250***	-1.130***	-0.758**
id147	-2.851***	-0.0796	-1.021***	-0.896***
id148	-3.737***	1.617***	-0.0483	-0.0520
id149	-3.202***	-1.184**	-0.554***	-0.343
id150	-3.616***	-0.905**	-1.167***	-0.905***

id151	-0.362	-1.167**	-1.654***	-1.677***
id152	-33.99***	-3.751***	-1.421***	-1.382***
id153	-1.598**	-0.169	-2.936***	-3.067***
id154	-22.42***	-2.716***	-1.703***	-1.483***
id155	-4.238***	-2.441**	-0.759***	-0.814***
id156	-44.40***	-1.456***	-0.590***	-0.429**
id157	-1.868**	0.337	-0.753***	-0.502**
id158	-19.82***	-17.98***	0.678***	0.744***
id159	-19.82***	-18.42***	0.827***	0.715***
id160	-3.790***	0.550	0.148	0.337*
id161	-22.82***	-19.90***	0.608***	0.494***
id162	-20.72***	-18.61***	0.431*	0.176
id163	-23.06***	-20.45***	1.844***	1.656***
id164	-2.923***	-2.557***	-0.245*	-0.301*
id165	-21.48***	-19.51***	1.341***	1.447***
id166	-26.53***	-2.439***	-0.158	-0.0534
id167	-2.696**	-4.124***	1.119***	1.089***
id168	-5.731***	-1.940***	0.0447	0.0115
id169	-26.92***	-23.39***	0.473**	0.422*
id170	-15.44***	-13.89***	-19.55***	-0.684
id171	-3.650***	-1.497***	-0.344	-0.313
id172	-3.659***	-1.951***	-0.427*	-0.367
id173	-3.036***	-3.500***	-0.874***	-0.888***
id174	1.453	0.361	-1.484***	-1.288***
id175	-0.688	1.615***	0.114	0.333
id176	-1.666*	-0.313	0.530	-0.0614
id177	-2.576***	-1.675***	-0.245	0.187
id178	-0.823	0.510	0.213	0.0436
id179	-20.05***	-1.071	-1.386***	-1.021*
id180	-4.457***	-2.934***	-0.402**	-0.277
id181	-1.850**	-0.909**	-0.573*	-0.354
id182	-4.755***	-2.082***	0.387	0.409
log-likelihood	-952.2391	-1519.954	-3479.969	-3488.38
AIC	2292.478	3427.908	7347.937	7364.76
BIC	3261.657	4397.086	8317.116	8333.939
Observations	1,092	1,092	1,092	1,092

^a *** p<0.01, ** p<0.05, * p<0.1

Table A2. Driving risk scores for four near-miss events after winsorizing and Min-Max scaling on regression coefficients.

VARIABLES	overspeed	highspeedbrake	harshacceleration	harshdeceleration
id1	4.824741	4.344986	2.622834	2.52286
id2	1.242371	4.033808	3.753797	3.75
id3	2.476298	1.628204	4.413078	4.113936
id4	2.578824	1.749502	4.312131	4.315106
id5	1.133814	3.574272	1.557084	1.542612
id6	4.646467	4.258833	3.576023	3.377835

id7	4.434299	4.244682	3.208862	3.286394
id8	2.244711	3.976736	2.4531	2.636247
id9	4.685306	4.334427	2.398606	2.423189
id10	4.449618	4.107521	2.314633	2.288771
id11	4.580368	4.164127	2.478113	2.27414
id12	4.662871	4.224932	2.692603	2.612564
id13	4.542011	4.219333	2.499553	2.404901
id14	4.441416	4.413722	2.060925	2.1891
id15	4.673486	4.370957	2.542969	2.547549
id16	2.050515	1.186551	2.864928	2.924287
id17	2.12168	4.018102	2.444167	2.612747
id18	2.218175	4.2198	1.618724	1.364301
id19	4.704364	4.404081	3.147222	3.058705
id20	1.835814	3.761974	2.883688	2.607535
id21	2.124092	3.944234	2.910488	2.941661
id22	4.506067	4.309374	3.065928	3.014813
id23	4.729211	4.345159	2.199393	2.148866
id24	1.923866	1.063697	2.328926	2.428676
id25	2.207319	1.317181	1.834912	1.854426
id26	4.494367	4.189475	2.229766	1.912948
id27	1.957639	1.080804	2.581383	2.582846
id28	2.621041	1.695073	2.661426	2.805413
id29	4.687598	4.20938	3.150795	3.094367
id30	2.274866	1.419818	2.42362	2.42959
id31	4.77565	4.246703	1.597284	1.655084
id32	4.432128	3.890427	2.524567	2.653621
id33	2.476298	1.503794	2.464713	2.382955
id34	4.531518	4.10441	2.617715	2.482718
id35	4.362531	4.183099	2.080579	2.018105
id36	4.325984	3.970049	2.368233	2.209217
id37	0.021711	4.153396	2.194033	2.323519
id38	2.317082	4.132869	1.297123	1.497805
id39	0.024124	5	5	5
id40	4.664922	4.280294	2.374486	2.59519
id41	4.53007	4.186365	2.783634	2.664594
id42	4.768412	4.413722	3.165088	2.886796
id43	4.563723	4.379043	2.590763	2.605157
id44	4.527417	4.320727	2.922994	2.950805
id45	4.570236	4.140489	2.716634	2.780724
id46	4.840663	4.270341	2.344113	2.307974
id47	4.468072	4.193363	1.860818	1.923007
id48	4.883362	4.559747	3.363409	3.242502
id49	1.672979	4.100056	2.115419	2.200073
id50	4.51644	4.048426	2.253886	2.22019
id51	2.268835	1.384051	3.62605	3.565289
id52	2.192845	1.124347	2.306593	1.652341
id53	2.260391	1.348283	2.50402	2.705743
id54	4.236002	4.176723	2.010005	1.938552
id55	4.307288	4.075796	3.044488	2.95812
id56	4.527778	4.331519	2.729141	2.867593

id57	2.18802	4.236128	2.721101	3.180322
id58	4.59834	4.237372	2.315526	2.583211
id59	0	4.333961	1.974272	1.986101
id60	4.448773	3.752022	1.987672	2.006218
id61	4.923769	4.512628	1.472217	1.538954
id62	4.768654	4.429895	2.024299	2.090344
id63	2.165103	1.309405	3.86725	3.906364
id64	4.519697	4.079528	3.814544	3.747257
id65	2.171134	1.334287	0.904949	1.345099
id66	4.657202	4.110164	3.073075	3.410753
id67	1.641618	3.816248	2.291406	2.244879
id68	2.459412	1.607987	1.474004	1.004938
id69	1.78636	1.116571	2.096659	1.951353
id70	2.194051	3.770683	1.292657	1.150329
id71	0.937206	0	3.147222	3.631127
id72	4.157238	4.180455	2.161872	1.934894
id73	4.303307	3.899757	1.25871	1.130212
id74	0.979422	0	2.889941	3.222385
id75	4.478807	4.084194	2.384313	2.439557
id76	2.198876	0.898855	1.152403	0.782736
id77	2.366536	1.433814	3.368769	3.189466
id78	1.845464	3.838019	0.07236	0
id79	4.408728	4.24888	2.41558	2.422275
id80	2.130123	1.197437	2.609523	2.569404
id81	0.595856	4.168947	2.318206	2.215618
id82	4.656961	4.260855	2.344113	2.224762
id83	4.641884	4.369402	2.512953	2.301573
id84	1.823752	4.054802	1.952832	1.741039
id85	2.061371	3.747356	1.345364	1.317666
id86	1.21101	4.028365	1.486511	1.50695
id87	4.601476	4.505785	2.797927	2.911485
id88	2.341206	1.475802	2.43702	2.371982
id89	1.641618	0.869308	3.605503	3.560717
id90	4.341302	4.214201	1.754511	1.624909
id91	2.40634	1.387161	3.226729	3.270849
id92	1.571659	0.774446	3.380382	3.129115
id93	1.873206	1.03415	2.363766	2.248537
id94	4.501001	4.184188	2.48258	2.535571
id95	1.736907	0.925292	2.173486	1.910205
id96	1.999855	1.163225	3.850277	3.750914
id97	2.23868	1.320291	2.208326	2.264996
id98	2.526958	1.600211	1.367697	1.711778
id99	2.583649	1.687298	1.038056	1.271031
id100	4.315007	1.200547	3.339289	3.276335
id101	2.014329	1.197437	3.475969	3.267191
id102	1.72967	0.847537	2.650348	2.495977
id103	2.619835	1.71218	3.107022	3.076993
id104	2.34	1.460251	2.739861	2.762436
id105	4.411502	4.278116	2.208326	1.67703
id106	1.711577	0.852202	2.906021	2.753292

id107	2.215762	1.324956	2.635698	2.657279
id108	1.917835	3.933348	2.147579	1.942209
id109	2.236268	1.290744	2.312846	1.807791
id110	2.288134	1.175666	1.013936	1.568215
id111	4.414035	4.146398	2.777381	2.703914
id112	2.390659	1.522456	1.324817	1.762985
id113	1.147082	3.878919	1.101483	1.337783
id114	1.90336	1.068363	3.191889	3.013899
id115	2.062577	1.197437	2.606843	2.423189
id116	2.119268	3.761352	1.417724	1.485004
id117	2.253154	1.382496	2.483473	2.273226
id118	2.469061	4.235351	2.726461	2.525942
id119	2.30502	1.421373	2.4933	2.392099
id120	1.435361	0.55051	2.607647	2.644477
id121	1.255639	4.23815	2.836341	2.876737
id122	2.133742	3.953875	3.179382	3.119971
id123	1.987793	3.739736	3.246382	3.333029
id124	4.309941	3.938791	3.246382	2.852963
id125	4.363014	1.066808	2.887261	3.088881
id126	4.58073	4.005505	3.137395	3.015728
id127	2.083082	1.265862	3.657316	3.446416
id128	2.225412	1.262752	3.303555	3.087966
id129	4.638989	4.465819	2.647847	2.673738
id130	1.741732	0.892635	1.21315	1.027798
id131	4.624635	4.282315	1.747365	1.796818
id132	2.42202	1.567554	1.851885	2.125091
id133	1.568041	3.893381	2.067179	1.891002
id134	0.916701	3.937858	3.058781	3.598208
id135	1.906979	1.087024	3.453636	3.757315
id136	5	5	5	5
id137	1.893711	3.954964	2.66214	3.258047
id138	2.485948	1.635979	1.884045	1.709034
id139	4.329602	4.160394	1.799178	1.903804
id140	4.466504	4.249347	1.482937	1.576445
id141	1.759824	0.892635	1.666071	1.517008
id142	0.219526	4.209225	2.6675	2.682882
id143	0.171278	4.283248	2.294086	2.379298
id144	4.754179	4.430673	2.64615	2.675567
id145	4.525004	4.14702	1.952832	1.945867
id146	1.947989	4.150597	1.613364	1.829737
id147	4.480858	4.332608	1.710738	1.703548
id148	4.37399	4.596448	2.579686	2.475311
id149	4.438521	4.160861	2.127926	2.209217
id150	4.388585	4.204249	1.580311	1.695318
id151	4.781077	4.163505	1.145256	0.989393
id152	0.724917	3.761663	1.353404	1.259144
id153	4.631993	4.318705	0	0
id154	2.120474	3.922618	1.101483	1.166789
id155	4.31356	3.965383	1.944792	1.77853
id156	0	4.118562	2.095766	2.130578

id157	4.599426	4.397394	1.950152	2.063826
id158	2.434082	1.548893	3.228515	3.203182
id159	2.434082	1.480468	3.361622	3.176664
id160	4.367597	4.430518	2.755047	2.831017
id161	2.072226	1.250311	3.165982	2.974579
id162	2.325525	1.450921	3.007861	2.683797
id163	2.043278	1.16478	4.270145	4.037125
id164	4.472173	3.947344	2.403966	2.247623
id165	2.233855	1.31096	3.820797	3.846013
id166	1.624732	3.965694	2.481687	2.474031
id167	4.499554	3.703658	3.622476	3.518654
id168	4.133476	4.043294	2.662766	2.533376
id169	1.57769	0.707577	3.045381	2.908742
id170	2.962391	2.184934	0	1.897403
id171	4.384484	4.112186	2.315526	2.23665
id172	4.383398	4.041584	2.241379	2.187271
id173	4.458543	3.800697	1.842058	1.710863
id174	5	4.401126	1.297123	1.345099
id175	4.741756	4.596137	2.724674	2.827359
id176	4.623791	4.296311	3.096302	2.466715
id177	4.514028	4.084505	2.403966	2.693855
id178	4.725472	4.424297	2.813114	2.562729
id179	2.40634	4.178434	1.38467	1.589247
id180	4.287144	3.888716	2.263713	2.269568
id181	4.601597	4.203627	2.110952	2.199159
id182	4.2512	4.021212	2.968555	2.896854

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