Problem 2 Assignment 1 Isac Nordin

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September 2021

$1 \quad code$

```
1 %Main code
  %patterns
  -1, -1, \begin{bmatrix} -1, -1, 1, 1, 1, 1, 1, 1, -1, -1 \end{bmatrix}, \begin{bmatrix} -1, 1, 1, 1, -1, -1, 1, 1, 1, 1 \end{bmatrix}
        [-1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-1,1],[-
       -1]\,,[\quad -1,\ \ 1,\ \ 1,\ \ -1,\ \ -1,\ \ 1,\ \ 1,\ \ 1,\ \ -1]\,,[\quad -1,\ \ 1,\ \ 1,\ \ 1,\ \ -1,\ \ -1,\ \ 1,\ \ 1,\ \ 1,
       -1]\,,[\quad -1,\ \ 1,\ \ 1,\ \ -1,\ \ -1,\ \ 1,\ \ 1,\ \ 1,\ \ -1]\,,[\quad -1,\ \ -1,\ \ 1,\ \ 1,\ \ 1,\ \ 1,\ \ 1,\ \ 1,\ \ -1,
       [-1],[-1,-1,-1,-1,1,1,1,1,-1,-1,-1],[-1,-1,-1,-1,-1,-1,-1,-1,-1,-1,-1]
        -1, -1];
[-1],[-1,-1,-1,-1,1,1,1,1,-1,-1,-1],[-1,-1,-1,1,1,1,1,1,-1,-1,-1]
        1, -1, -1, -1;
-1, -1, -1, -1, 1, 1, 1, -1, -1, [-1, -1, -1, -1, -1, 1, 1, 1, -1, -1],
       -1, -1, -1, -1, -1, 1, 1, 1, -1, -1, \begin{bmatrix} -1, -1, -1, -1, -1, 1, 1, 1, -1, \\ -1, -1, -1, -1, -1, -1, \end{bmatrix}
       [-1], [-1, -1, -1, -1, -1, 1, 1, 1, -1, -1], [1, 1, 1, 1, 1, 1, 1, 1, -1, -1]
       -1]\,,[\ \ 1,\ \ 1,\ \ -1,\ \ -1,\ \ -1,\ \ -1,\ \ -1,\ \ -1]\,,[\ \ 1,\ \ 1,\ \ 1,\ \ -1,\ \ -1,\ \ -1,\ \ -1,\ \ -1,
       -1, -1, -1, \begin{bmatrix} 1, 1, 1, 1, 1, 1, 1, 1, 1, -1, -1 \end{bmatrix}, \begin{bmatrix} 1, 1, 1, 1, 1, 1, 1, 1, -1, -1 \end{bmatrix}
        -1];
1, -1, -1];
```

```
-1, -1, -1, 1, 1, -1;
10
 %initiate model
11
 patternBitsWidth=10;
12
 Patterns = [x1; x2; x3; x4; x5];
13
 weightMatrix=GetWeights(Patterns);
14
15
 -1, -1, -1, -1, 1, 1, -1];
17 %currentState=Sgn(2*rand(1,length(currentState))-1); %random state for
   experimentation
18
 PlotPattern (currentState, patternBitsWidth)
19
 pause (0.5)
20
21
 %start simulation
22
 while true
23
   oldState = currentState;
24
   currentState = UpdateState(currentState, weightMatrix);
25
   if currentState = oldState %if steady state
26
27
   end
   PlotPattern (currentState, patternBitsWidth)
29
   pause (0.2);
30
 end
31
 disp('simulation is done')
32
33
 %make steady state into a openTA friendly string
34
 openTa = PrintStateAsMatrix(currentState, patternBitsWidth)
35
 pause (0.5)
36
 close all
37
38
 %get weightMatrix (P x N size)
39
 function WeightMatrix = GetWeights(patterns)
40
   Npatterns = size(patterns, 1);
   Nbits = size (patterns, 2);
42
   WeightMatrix = zeros (Nbits, Nbits);
43
44
   for iPattern = 1: Npatterns
45
```

```
patternI = patterns(iPattern,:);
46
           WeightMatrix = WeightMatrix+mtimes(patternI', patternI);
47
       end
       WeightMatrix = WeightMatrix/Nbits;
49
50
       %modified hebbs rule
51
       for iBits = 1:Nbits
52
           WeightMatrix(iBits, iBits) = 0;
       end
54
  end
55
56
  %asynchronous update of state N times
   function newState = UpdateState(currentState, weightMatrix)
58
59
       newState = currentState;
60
       %N asynchronous updates in a row
       for iBit = 1:length(currentState)
62
           newState(iBit) = Sgn(weightMatrix(iBit,:)*currentState');
           currentState(iBit) = newState(iBit);
64
       end
66
  end
67
68
69
  \%sign(x) with if==0 \longrightarrow =1
70
   function sgn = Sgn(x)
71
       sgn = sign(x);
72
       if sgn = 0
73
           sgn = 1;
74
       end
75
76
  end
77
  %—code that helps answer questions—
79
  %visualizes pattern
81
   function p = PlotPattern(x, widthPx)
       xMatrix = zeros(length(x)/widthPx, widthPx);
83
       for i = 1: length(x) / widthPx
           xMatrix(i,:) = x(i*widthPx-(widthPx-1):i*widthPx);
85
       end
86
       imagesc(-xMatrix)
87
       colormap (gray)
88
  end
89
90
91
  %prints answer in a openTA friendly way
92
   function k = PrintStateAsMatrix(state, width)
93
       k = '[';
94
       for i = 1:length(state)/width
           s = state(i*width-width+1:i*width);
96
           s = string(regexprep(mat2str(s), {, , , }));%to string
97
           if i = length(state)/width
98
                k = k+s + ', ';
```

```
\begin{array}{cccc} {}_{100} & & & else \\ {}_{101} & & & k = k+s \,; \\ {}_{102} & & end \\ {}_{103} & & end \\ {}_{104} & & k = k+' \,] \,\, ; \\ {}_{105} & & \\ {}_{106} & end & & \end{array}
```