

BRIEF ARTICLE

THE AUTHOR

1. ASSUMPTIONS

- (1) The samples for each centroid are evenly divided on each side of the centroid
- (2) The samples between centroids are uniformly distributed
- (3) If a centroid has $n = 2k + 1$ samples, then there are k samples on each side and one at the centroid
- (4) If a centroid has $n = 2k$ samples, then there $k - 1/2$ samples on each side
- (5) the first and last centroid will have only one sample

2. EQUAL SPACING MODEL

Take two centroids separated by x with n_{left} and n_{right} samples respectively. We know the following about the samples between these centroids

- (1) there will be no samples left of the first centroid or right of the last one
- (2) if $n_{\text{left}} = 1$ or $n_{\text{right}} = 1$ then the unique sample for the corresponding centroid is at the centroid
- (3) there will be $\lfloor n_{\text{left}}/2 \rfloor + \lfloor n_{\text{right}}/2 \rfloor$ samples between the centroids
- (4) samples will be spaced $\Delta x = 2x/(n_{\text{left}} + n_{\text{right}})$ apart
- (5) the left-most sample is at $((n_{\text{left}} \bmod 2) + 1)\Delta x/2$ from the left centroid
- (6) the right-most sample is at $((n_{\text{right}} \bmod 2) + 1)\Delta x/2$ from the left centroid