

Chapter 1

Showcase of eIris Inductive

- Explain that we will show an example of the new iInductive system
- First we define the inductive and show the created lemma's and definitions
- Next we use the induction schema in our new tactic to proof a lemma

1.1 Defining a new inductive

- Able to use standard Coq inductive syntax
- Show example
- Show fix-point and explain
- Show other Lemmas and explain as well

```
1 EI.ind
2 Inductive is_list (q : Qp) : val → iProp :=
3   | empty_is_list : is_list q NONEV
4   | cons_is_list l v tl :
5     l ↗{#q} (v,tl) -* is_list q tl
6     -* is_list q (SOMEV #l).
```

1.2 Proving a lemma using the inductive

- Explain Lemma we will prove
- Show steps of proof

```

1  Lemma ind_test_1 (q q' : Qp) (v : val) :
2    is_list q v * is_list q' v *-* is_list (q+q') v.
3  Proof.
4    iSplit.
5    - eiIntros "[Hq Hq']".
6    iRevert "Hq'".
7    eiInduction "Hq" as "[IH | (%l' & %v' & %tl' & Hl' & IH & %Hy)]"; eiIntro
8    + iApply is_list_unfold_2.
9      iLeft.
10     iFrame.
11    + simplify_eq.
12     iApply is_list_unfold_2.
13     iRight.
14     iExists l', v', tl'.
15     eiDestruct "Hq'" as "[%Hl | (%l'' & %v'' & %tl'' & Hl & Hlq' & %Hv)]";
16     iCombine "Hl' Hl" as "Hl" gives %[_ ?]; simplify_eq.
17     iFrame.
18     iDestruct "IH" as "[IH _]".
19     iSplitL.
20     * iApply ("IH" with "[%$]").
21     * by iPureIntro.
22   - eiIntros "Hi".
23   eiInduction "Hi" as "[%Ha | (%l & %v' & %tl & [Hq Hq'] & [[Hiq Hiq'] _]]";
24   + simplify_eq.
25     iSplitL.
26     * iApply is_list_unfold.
27     iLeft.
28     by iPureIntro.
29     * iApply is_list_unfold.
30     iLeft.
31     by iPureIntro.
32   + iSplitL "Hq Hiq".
33     * iApply is_list_unfold.
34     iRight.
35     iExists l, v', tl.
36     iFrame.
37     by iPureIntro.
38     * iApply is_list_unfold.
39     iRight.
40     iExists l, v', tl.
41     iFrame.
42     by iPureIntro.
43  Qed.

```