

## Chapter 5

# Elpi implementation of Inductive

We discuss the implementation of the `eiInd` command together with integrations in the `eiIntros` tactic and the `eiInductive` tactic.

**Structure of `eiInductive`** The `eiInductive` command consists of several steps we have outlined in the diagram below.

**Inductive tactics** In the last two sections we discuss how the tactics to use an inductive predicate are made. We first discuss the `eiInduction` tactic in section 5.9, which performs induction on the specified inductive predicate. Next, in section 5.10, we outline the extensions to the `eiIntros` tactic concerning inductive predicates.

### 5.1 Parsing inductive data structure

The `eiInd` command is called by writing a Coq inductive statement and prepending it with the `eiInd` command. We will use the below inductive statement as an example for this and any subsequent sections.

```
1  eiInd Coq  
2  Inductive is_R_list {A} (R : val → A → iProp) :  
3      val → list A → iProp :=  
4      | empty_is_R_list : is_R_list R NONEV []  
5      | cons_is_R_list l v tl x xs :  
6          l ↦ (v, tl) -* R v x -* is_R_list R tl xs -*  
7          is_R_list R (SOMEV #l) (x :: xs).
```

This inductive predicate relates a linked list to a Coq list by relation `R`. Since the Coq list can have an arbitrary type `A` and the predicate `R` is constant, we add them as parameters to the predicate.

When interpreting an inductive statement in Elpi, any binders in Coq are also binders in Elpi. Thus, every parameter consists of a binder. While descending into the binders we keep track of the list of binders, together with the name and type of each binder. Later, whenever we construct a term we use this list of parameters to abstract the term over the parameters.

In Elpi this is received as a data structure of type `indt-decl`.

```

1 parameter `A` maximal
2 X0
3 (a \ parameter `R` explicit
4   {{ val -> lp:a -> iProp }}
5   (_ \ inductive `is_R_list` tt
6     {{ val -> list lp:a -> iProp }}
7     (f \ [constructor `empty_is_R_list`
8           (arity ...),
9           constructor `cons_is_R_list`
10          (arity ...)])))

```

Elpi

The contents of the constructors is removed from this example for conciseness. When encoding a Coq data structure in Elpi, Coq-Elpi always translates a binder in Coq to a binder in Elpi. Thus, a parameter consists of the name, if it should be maximally inserted, the type, and the rest of the data structure. The first parameter has the name ``A``, is maximally inserted, and the type is not yet calculated, thus a variable. The second parameter depends on the first parameter in its type. Then the inductive statmen

- 5.2 Constructing the pre fixpoint function
- 5.3 Creating and proving propers
- 5.4 Constructing Fixpoint
- 5.5 Unfolding lemmas
- 5.6 Constructor lemmas
- 5.7 Iteration lemma
- 5.8 Induction lemma
- 5.9 `eiInductive` tactic
- 5.10 `eiIntros` integrations