

# Chapter 1

## Showcase of eIris Inductive

- Explain that we will show an example of the new iInductive system
- First we define the inductive and show the created lemma's and definitions
- Next we use the induction schema in our new tactic to proof a lemma

### 1.1 Defining a new inductive

- Able to use standard Coq inductive syntax
- Show example
- Show fix-point and explain
- Show other Lemmas and explain as well

```
1 EI.ind
2 Inductive is_list (q : Qp) : val → iProp :=
3   | empty_is_list : is_list q NONEV
4   | cons_is_list l v tl :
5     l ↪{#q} (v,tl) -* is_list q tl
6     -* is_list q (SOMEV #l).
```

### 1.2 Proving a lemma using the inductive

- Explain Lemma we will prove
- Show steps of proof

```

1  Lemma ind_test_1 (q q' : Qp) (v : val) :
2    is_list q v * is_list q' v *-* is_list (q+q') v.
3  Proof.
4    iSplit.
5    - eiIntros "[Hq Hq']".
6    iRevert "Hq'".
7    eiInduction "Hq" as "[IH | (%l' & %v' & %tl' & Hl' & IH & %Hy)]"; ei
8    + iApply is_list_unfold_2.
9      iLeft.
10     iFrame.
11    + simplify_eq.
12      iApply is_list_unfold_2.
13      iRight.
14      iExists l', v', tl'.
15      eiDestruct "Hq'" as "[%Hl | (%l'' & %v'' & %tl'' & Hl & Hilq' & %
16      iCombine "Hl' Hl" as "Hl" gives %[_ ?]; simplify_eq.
17      iFrame.
18      iDestruct "IH" as "[IH _]".
19      iSplitL.
20      * iApply ("IH" with "[$]").
21      * by iPureIntro.
22    - eiIntros "Hi".
23    eiInduction "Hi" as "[%Ha | (%l & %v' & %tl & [Hq Hq'] & [[Hiq Hiq']
24    + simplify_eq.
25      iSplitL.
26      * iApply is_list_unfold.
27      iLeft.
28      by iPureIntro.
29      * iApply is_list_unfold.
30      iLeft.
31      by iPureIntro.
32    + iSplitL "Hq Hiq".
33      * iApply is_list_unfold.
34      iRight.
35      iExists l, v', tl.
36      iFrame.
37      by iPureIntro.
38      * iApply is_list_unfold.
39      iRight.
40      iExists l, v', tl.
41      iFrame.
42      by iPureIntro.
43  Qed.

```