## image\_classifier\_on\_cifar\_10

## December 11, 2022

##Image Classification on CIFAR-10 In this problem we will explore different deep learning architectures for image classification on the CIFAR-10 dataset. Make sure that you are familiar with torch Tensors, two-dimensional convolutions (nn.Conv2d) and fully-connected layers (nn.Linear), ReLU non-linearities (F.relu), pooling (nn.MaxPool2d), and tensor reshaping (view).

We will use Colab because it has free GPU runtimes available; GPUs can accelerate training times for this problem by 10-100x. You will need to enable the GPU runtime to use it. To do so, click "Runtime" above and then "Change runtime type". There under hardware accelerator choose "GPU".

This notebook provides some starter code for the CIFAR-10 problem on HW4, including a completed training loop to assist with some of the Pytorch setup. You'll need to modify this code to implement the layers required for the assignment, but this provides a working training loop to start from.

Note: GPU runtimes are limited on Colab. Limit your training to short-running jobs (around 20mins or less) and spread training out over time, if possible. Colab WILL limit your usage of GPU time, so plan ahead and be prepared to take breaks during training. We also suggest performing your early coding/sweeps on a small fraction of the dataset (~10%) to minimize training time and GPU usage.

```
[1]: import torch
from torch import nn

from typing import Tuple, Union, List, Callable
from torch.optim import SGD
import torchvision
from torch.utils.data import DataLoader, TensorDataset, random_split
import matplotlib.pyplot as plt
from tqdm import tqdm, trange
```

Let's verify that we are using a gpu:

```
[]: assert torch.cuda.is_available(), "GPU is not available, check the directions

⇒above (or disable this assertion to use CPU)"

DEVICE = "cuda" if torch.cuda.is_available() else "cpu"

print(DEVICE) # this should print out CUDA
```

cuda

To use the GPU you will need to send both the model and data to a device; this transfers the model from its default location on CPU to the GPU.

Note that torch operations on Tensors will fail if they are not located on the same device.

```
model = model.to(DEVICE) # Sending a model to GPU

for x, y in tqdm(data_loader):
   x, y = x.to(DEVICE), y.to(DEVICE)
```

When reading tensors you may need to send them back to cpu, you can do so with x = x.cpu().

Let's load CIFAR-10 data. This is how we load datasets using PyTorch in the real world!

```
[]: train_dataset = torchvision.datasets.CIFAR10("./data", train=True, download=True, transform=torchvision.transforms.ToTensor())

test_dataset = torchvision.datasets.CIFAR10("./data", train=False, download=True, transform=torchvision.transforms.ToTensor())
```

```
Downloading https://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz to ./data/cifar-10-python.tar.gz

0%| | 0/170498071 [00:00<?, ?it/s]
```

Extracting ./data/cifar-10-python.tar.gz to ./data Files already downloaded and verified

Here, we'll use the torch DataLoader to wrap our datasets. DataLoaders handle batching, shuffling, and iterating over data; they can also be useful for building more complex input pipelines that perform transfoermations such as data augmentation.

```
test_loader = DataLoader(
    test_dataset,
    batch_size=batch_size,
    shuffle=True
)
```

Let's define a method to train this model using SGD as our optimizer.

```
[]: def train(
        model: nn.Module, optimizer: SGD,
        train_loader: DataLoader, val_loader: DataLoader,
        epochs: int = 20
        )-> Tuple [List[float], List[float], List[float]]:
       Trains a model for the specified number of epochs using the loaders.
      Returns:
        Lists of training loss, training accuracy, validation loss, validation ⊔
      ⇒accuracy for each epoch.
      loss = nn.CrossEntropyLoss()
      train_losses = []
      train_accuracies = []
      val_losses = []
      val_accuracies = []
      for e in range(epochs):
        model.train()
        train loss = 0.0
        train_acc = 0.0
         # Main training loop; iterate over train_loader. The loop
         # terminates when the train loader finishes iterating, which is one epoch.
        for (x_batch, labels) in train_loader:
          x_batch, labels = x_batch.to(DEVICE), labels.to(DEVICE)
           optimizer.zero_grad()
           labels_pred = model(x_batch)
           batch_loss = loss(labels_pred, labels)
```

```
train_loss = train_loss + batch_loss.item()
    labels_pred_max = torch.argmax(labels_pred, 1)
    batch_acc = torch.sum(labels_pred_max == labels)
    train_acc = train_acc + batch_acc.item()
   batch_loss.backward()
    optimizer.step()
 train_losses.append(train_loss / len(train_loader))
 train_accuracies.append(train_acc / (batch_size * len(train_loader)))
  # Validation loop; use .no_grad() context manager to save memory.
 model.eval()
 val_loss = 0.0
 val_acc = 0.0
 with torch.no_grad():
    for (v_batch, labels) in val_loader:
      v_batch, labels = v_batch.to(DEVICE), labels.to(DEVICE)
     labels_pred = model(v_batch)
      v_batch_loss = loss(labels_pred, labels)
     val_loss = val_loss + v_batch_loss.item()
     v_pred_max = torch.argmax(labels_pred, 1)
     batch_acc = torch.sum(v_pred_max == labels)
     val_acc = val_acc + batch_acc.item()
    val_losses.append(val_loss / len(val_loader))
    val_accuracies.append(val_acc / (batch_size * len(val_loader)))
return train losses, train_accuracies, val_losses, val_accuracies
```

```
[]: def evaluate(
    model: nn.Module, loader: DataLoader
) -> Tuple[float, float]:
    """Computes test loss and accuracy of model on loader."""
    loss = nn.CrossEntropyLoss()
    model.eval()
    test_loss = 0.0
    test_acc = 0.0
    with torch.no_grad():
        for (batch, labels) in loader:
            batch, labels = batch.to(DEVICE), labels.to(DEVICE)
        y_batch_pred = model(batch)
        batch_loss = loss(y_batch_pred, labels)
        test_loss = test_loss + batch_loss.item()

        pred_max = torch.argmax(y_batch_pred, 1)
```

```
batch_acc = torch.sum(pred_max == labels)
  test_acc = test_acc + batch_acc.item()
test_loss = test_loss / len(loader)
test_acc = test_acc / (batch_size * len(loader))
return test_loss, test_acc
```

```
[]: def fully_connected(M: int) -> nn.Module:
    model = nn.Sequential(
        nn.Flatten(),
        nn.Linear(3072, M),
        nn.ReLU(),
        nn.Linear(M, 10)
)

return model.to(DEVICE)
```

```
[]: def fully_connected_tune_hyperparams(train_loader: DataLoader,
                                           val_loader: DataLoader,
                                          model_fn:Callable[[], nn.Module]):
       num_iterations = 10
       best_loss = torch.inf
      best_lr = 0.0
       best_M = 0.0
       best_momentum = 0.0
       val_losses = []
      momentums_array = []
      learning_rates = []
      M_array = []
       Ms = torch.pow(2, torch.arange(5, 11))
       momentums = torch.linspace(10 ** (-6), 10 ** (-1), num_iterations)
       lrs = torch.linspace(10 ** (-6), 10 ** (-1), num_iterations)
      for M in Ms:
         for learning_rate in lrs:
           for momentum in momentums:
             print(f"lr : {learning_rate}, momentum : {momentum}, M : {M}")
             model = model_fn(M)
             optim = SGD(model.parameters(), learning_rate, momentum = momentum)
             train_loss, train_acc, val_loss, val_acc = train(
                 model, optim, train_loader, val_loader, epochs = 20
             val_losses.append(min(val_loss))
             learning_rates.append(learning_rate)
```

```
momentums_array.append(momentum)
             M_array.append(M)
       indices = torch.argsort(torch.tensor(val_losses))[:5]
      return torch.tensor(M_array)[indices], torch.tensor(learning_rates)[indices],_u
      →torch.tensor(momentums_array)[indices]
[]: best_M, best_lr, best_momentum = fully_connected_tune_hyperparams(train_loader,_u
      ⇔val_loader, fully_connected)
[]: print(f"M : {best_M}, learning_rate = {best_lr}, momentum = {best_momentum}")
    M : tensor([ 128, 128, 1024, 512, 1024]), learning_rate = tensor([0.0778,
    0.0667, 0.0333, 0.1000, 0.0556]), momentum = tensor([0.0444, 0.0667, 0.0889,
    0.0222, 0.0667])
[]: best M = torch.tensor([128, 128, 1024, 512, 1024])
     best_lr = torch.tensor([0.0778, 0.0667, 0.0333, 0.1000, 0.0556])
     best momentum = torch.tensor([0.0444, 0.0667, 0.0889, 0.0222, 0.0667])
     model1 = fully_connected(best_M[0])
     model2 = fully_connected(best_M[1])
     model3 = fully_connected(best_M[2])
     model4 = fully_connected(best_M[3])
     model5 = fully_connected(best_M[4])
     optimizer_1 = SGD(model1.parameters(), best_lr[0], momentum = best_momentum[0])
     optimizer_2 = SGD(model2.parameters(), best_lr[1], momentum = best_momentum[1])
     optimizer_3 = SGD(model3.parameters(), best_lr[2], momentum = best_momentum[2])
     optimizer_4 = SGD(model4.parameters(), best_lr[3], momentum = best_momentum[3])
     optimizer_5 = SGD(model5.parameters(), best_lr[4], momentum = best_momentum[4])
[]: train_loss, train_accuracy, val_loss, val_accuracy = train(
        model1, optimizer_1, train_loader, val_loader, 40)
     train_loss_2, train_accuracy_2, val_loss_2, val_accuracy_2 = train(
        model2, optimizer_2, train_loader, val_loader, 40)
     train_loss_3, train_accuracy_3, val_loss_3, val_accuracy_3 = train(
        model3, optimizer_3, train_loader, val_loader, 40)
     train_loss_4, train_accuracy_4, val_loss_4, val_accuracy_4 = train(
        model4, optimizer_4, train_loader, val_loader, 40)
     train_loss_5, train_accuracy_5, val_loss_5, val_accuracy_5 = train(
        model5, optimizer_5, train_loader, val_loader, 40)
```

printing out the test accuracy version of the fully connected linear neural network and saving the

arrays of the  $test\_acc$  and losses

[2]:

```
a5a_train_losses = [[1.9725063104521146, 1.797321759502996, 1.7197425345128232,__
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```

```
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```

```
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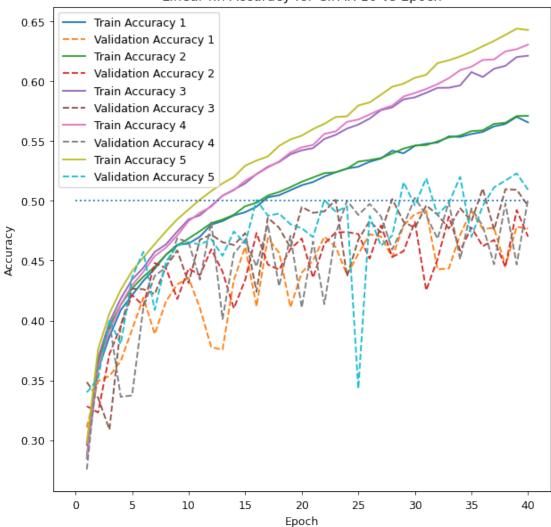
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```

```
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     459765625, 0.4685546875, 0.4357421875, 0.4642578125, 0.4736328125, 0.
     4740234375, 0.472265625, 0.4517578125, 0.4794921875, 0.453125, 0.4580078125, u
     40.482421875, 0.4251953125, 0.451171875, 0.4869140625, 0.4583984375, 0.
     477734375, 0.462109375, 0.4673828125, 0.4447265625, 0.4923828125, 0.
     4701171875], [0.3484375, 0.3353515625, 0.3087890625, 0.3958984375, 0.
     4265625, 0.426171875, 0.4220703125, 0.4451171875, 0.45859375, 0.43125, 0.
     467578125, 0.471875, 0.4654296875, 0.4630859375, 0.473046875, 0.4240234375, u
     ↔0.4859375, 0.4775390625, 0.4609375, 0.494921875, 0.4900390625, 0.4912109375, ⊔
     40.5009765625, 0.4369140625, 0.467578125, 0.483203125, 0.4736328125, 0.
     →5015625, 0.4826171875, 0.47734375, 0.4962890625, 0.4884765625, 0.476953125, ⊔
     40.4939453125, 0.4830078125, 0.5103515625, 0.47578125, 0.509765625, 0.509375, II
     ↔0.4958984375], [0.275390625, 0.365625, 0.398828125, 0.3361328125, 0.
     ↔0.4341796875, 0.4822265625, 0.401171875, 0.455859375, 0.467578125, 0.
     4451171875, 0.4802734375, 0.4287109375, 0.470703125, 0.4107421875, 0.
     466015625, 0.413671875, 0.47265625, 0.5001953125, 0.48828125, 0.4974609375, u
     →0.487109375, 0.459375, 0.4796875, 0.5025390625, 0.4880859375, 0.468359375, 0.
     498828125, 0.451171875, 0.49375, 0.4791015625, 0.4470703125, 0.4978515625, 0.
     446875, 0.5013671875], [0.33984375, 0.3513671875, 0.400390625, 0.3802734375, u.
     40.4361328125, 0.457421875, 0.4087890625, 0.44921875, 0.4625, 0.465625, 0.
     4634765625, 0.46796875, 0.4541015625, 0.4744140625, 0.464453125, 0.50078125, u
     40.4876953125, 0.489453125, 0.48046875, 0.4771484375, 0.4697265625, 0.
     →50078125, 0.4908203125, 0.4955078125, 0.34296875, 0.4875, 0.4625, 0.
     47109375, 0.515625, 0.4962890625, 0.5189453125, 0.4884765625, 0.498046875, 0.
     →5201171875, 0.469921875, 0.4958984375, 0.511328125, 0.5169921875, 0.
      →523046875, 0.509375]]
[7]: epochs = range(1, 41)
    plt.figure(figsize=(8, 8), dpi=90)
    plt.plot(epochs, a5a_train_accuracies[0], label="Train Accuracy 1")
    plt.plot(epochs, a5a_val_accuracies[0], label="Validation Accuracy 1", u
     ⇔linestyle = "dashed")
```

plt.plot(epochs, a5a\_train\_accuracies[1], label="Train Accuracy 2",) plt.plot(epochs, a5a\_val\_accuracies[1], label="Validation Accuracy 2", |

⇔linestyle = "dashed")

## Linear nn Accuracy for CIFAR-10 vs Epoch



```
[]: _, test_acc_1 = evaluate(model1, test_loader)
   _, test_acc_2 = evaluate(model2, test_loader)
   _, test_acc_3 = evaluate(model3, test_loader)
   _, test_acc_4 = evaluate(model4, test_loader)
   _, test_acc_5 = evaluate(model5, test_loader)
   print(f"Test Accuracy: {test_acc_1}")
   print(f"Test Accuracy: {test_acc_2}")
   print(f"Test Accuracy: {test_acc_3}")
   print(f"Test Accuracy: {test_acc_3}")
   print(f"Test Accuracy: {test_acc_4}")
   print(f"Test Accuracy: {test_acc_5}")
```

Test Accuracy: 0.482001582278481 Test Accuracy: 0.463310917721519 Test Accuracy: 0.5046479430379747

```
Test Accuracy: 0.5000988924050633
Test Accuracy: 0.5026700949367089
```

Test accuracies for the convolutional model

Test Accuracy: 0.482001582278481 \ Test Accuracy: 0.463310917721519 \ Test Accuracy: 0.5046479430379747 \ Test Accuracy: 0.5000988924050633 \ Test Accuracy: 0.5026700949367089 \

convolutional neural network

```
[]: def convolutional(M: int, k: int, N: int) -> nn.Module:
    model = nn.Sequential(
        nn.Conv2d(in_channels = 3, out_channels = M, kernel_size = k),
        nn.ReLU(),
        nn.MaxPool2d(kernel_size = N),
        nn.Flatten(),
        nn.Linear(in_features = M * (((33 - k) // 14) ** 2), out_features = 10)
    )
    return model.to(DEVICE)
```

i changed some of the hyperparameter ranges which hopefully work? print out test accuracies, this is the one i submit

```
[]: def a5b_conv_param_search(train_loader: DataLoader,
                           val_loader: DataLoader,
                           model_fn:Callable[[], nn.Module]):
       num_iter = 6
       epochs = 35
      Ms = torch.pow(2, torch.arange(5, 11))
       lr = torch.linspace(10 ** (-5), 10 ** (-1), 6)
      momentums = torch.linspace(0.3, 0.9, num_iter)
      k = 5
      N = 14
       stored_Ms = []
       stored_lrs = []
       stored_momentums = []
       stored_ks = []
       stored_Ns = []
       stored_val_losses = []
       i = 1
      for M in Ms:
         for momentum in momentums:
           print(f"({i}): trying M: {M}, lr: {lr}, momentum: {momentum}, k: {k}, N:
      ∽{N}")
```

```
i += 1
           model = model_fn(M.item(), k, N)
           optim = SGD(model.parameters(), lr, momentum=momentum)
           train_loss, train_acc, val_loss, val_acc = train(
             model,
             optim,
             train loader,
             val loader,
             epochs=35
           stored_Ms.append(M)
           stored_lrs.append(lr)
           stored_momentums.append(momentum)
           stored_ks.append(k)
           stored_Ns.append(N)
           stored_val_losses.append(min(val_loss))
       indices = torch.argsort(torch.tensor(stored_val_losses))[:5]
       return torch.tensor(stored Ms)[indices], torch.tensor(stored lrs)[indices],
      otorch.tensor(stored_momentums)[indices], torch.tensor(stored_ks)[indices],
      →torch.tensor(stored Ns)[indices]
[8]: a5b_stored_best_Ms = torch.tensor([1024, 1024, 1024, 1024, 1024])
     a5b_stored_best_lrs = torch.tensor([0.0800, 0.0200, 0.0600, 0.0400, 0.0600])
     a5b_stored_best_momentums = torch.tensor([0.6600, 0.9000, 0.6600, 0.7800, 0.
      <sup>4</sup>78001)
     a5b_stored_best_ks = torch.tensor([5, 5, 5, 5, 5])
     a5b_stored_best_Ns = torch.tensor([14, 14, 14, 14, 14])
[]: model_1 = convolutional(a5b_stored_best_Ms[0], 5, 14)
     model 2 = convolutional(a5b stored best Ms[1], 5, 14)
     model_3 = convolutional(a5b_stored_best_Ms[2], 5, 14)
     model 4 = convolutional(a5b stored best Ms[3], 5, 14)
     model_5 = convolutional(a5b_stored_best_Ms[4], 5, 14)
     optimizer_1 = SGD(model_1.parameters(), a5b_stored_best_lrs[0], momentum = __
      →a5b_stored_best_momentums[0])
     optimizer_2 = SGD(model_2.parameters(), a5b_stored_best_lrs[1], momentum = \Box
      →a5b_stored_best_momentums[1])
     optimizer_3 = SGD(model_3.parameters(), a5b_stored_best_lrs[2], momentum = __
      →a5b_stored_best_momentums[2])
     optimizer_4 = SGD(model_4.parameters(), a5b_stored_best_lrs[3], momentum = u
      →a5b_stored_best_momentums[3])
```

```
optimizer_5 = SGD(model_5.parameters(), a5b_stored_best_lrs[4], momentum = __
      →a5b_stored_best_momentums[4])
[]: train loss, train accuracy, val loss, val accuracy = train(
        model_1, optimizer_1, train_loader, val_loader, 40)
    train_loss_2, train_accuracy_2, val_loss_2, val_accuracy_2 = train(
        model_2, optimizer_2, train_loader, val_loader, 40)
    train_loss_3, train_accuracy_3, val_loss_3, val_accuracy_3 = train(
        model_3, optimizer_3, train_loader, val_loader, 40)
    train_loss_4, train_accuracy_4, val_loss_4, val_accuracy_4 = train(
        model_4, optimizer_4, train_loader, val_loader, 40)
    train_loss_5, train_accuracy_5, val_loss_5, val_accuracy_5 = train(
        model_5, optimizer_5, train_loader, val_loader, 40)
[]: a5b_train_losses = [train_loss, train_loss_2, train_loss_3, train_loss_4,__
     ⇔train_loss_5]
    a5b_train_accuracies = [train_accuracy, train_accuracy_2, train_accuracy_3,__
     a5b_val_losses = [val_loss, val_loss_2, val_loss_3, val_loss_4, val_loss_5]
    a5b_val_accuracies = [val_accuracy, val_accuracy_2, val_accuracy_3,_
     →val_accuracy_4, val_accuracy_5]
    print(a5b_train_losses)
    print(a5b_train_accuracies)
    print(a5b_val_losses)
    print(a5b_val_accuracies)
```

[9]:

```
a5b_train_losses = [[1.7784075506708839, 1.4377309486947276, 1.
 43318312188441104, 1.256117377599532, 1.2131349754265763, 1.165010241791606, u
 41.1315156819129533, 1.0927815461023287, 1.067361811006611, 1.
 →032843084836548, 1.0164639875292778, 1.0026831239123235, 0.9725683295929973, u
 →0.9623517433012073, 0.9416735792024569, 0.929081183265556, 0.
 →9112594906579364, 0.8971708113835617, 0.8868081810122187, 0.
 →8760893813927065, 0.8583813939582218, 0.8465221698649905, 0.
 48371764629740607, 0.8270039958032694, 0.8068326415324752, 0.
 48058258941905065, 0.7924882585013454, 0.7809077186340635, 0.
 47764605971222575, 0.7632395376197316, 0.7551901332018051, 0.
 47214435895227573, 0.7128545575859871, 0.7084208750589327, 0.
 →6912736768241633, 0.6846137275411324, 0.6765748827125538], [1.
 →7129530452869155, 1.4160366505384445, 1.3081939521838317, 1.
 42264667002653533, 1.1849401945417577, 1.1345273632217536, 1.100427525456656, u
 ↔1.0695301641456105, 1.044029350815849, 1.0068540894849733, 1.
 →0018949700011448, 0.9726522146639499, 0.9483239469541744, 0.
 935995574301156, 0.9096493250267073, 0.8947688027877699, 0.
 →8792217228222977, 0.8682330728254535, 0.8597941588271748, 0.
 →8364319152791392, 0.8369351261380044, 0.8131101586940613, 0.
 47951103138991378, 0.7858532552014698, 0.77134573798288, 0.7632630074566061, u
 →0.7609321969476613, 0.7479772021655332, 0.7304134815084663, 0.
 47262372079898011, 0.7004650619558312, 0.6953222519633445, 0.
 46768327269025824, 0.679365751502866, 0.6630337655713613, 0.6589514759623192, u
 →0.644906466149471, 0.6439351193098859, 0.6489429016682234, 0.
 →6253396835686131], [1.7365920645269481, 1.4410851750184188, 1.
 -3343578776852651, 1.2686960981650786, 1.2178432804278352, 1.
 41748396720398555, 1.1359420068223367, 1.100056325678121, 1.0745525578544899, u
 ار، 0560869743878192, 1.027101598510688, 1.00450223447247, 0.9877210648899729
 ↔0.9693884869868105, 0.9506288920952515, 0.9412067065184767, 0.
 9163380661471323, 0.9102237063714049, 0.8903572628782555, 0.
 →8747815503315493, 0.8562733581797644, 0.8512817873534831, 0.
 →8363145398484035, 0.827913474291563, 0.8142581102861599, 0.8114488407630812, u
 →0.7870432382280176, 0.7911911948838017, 0.7704978085715662, 0.
4762684249911796, 0.7545380224897102, 0.7475036723031239, 0.7256888585503806, U
 40.7208380074324933, 0.7169048419560898, 0.696293955668807, 0.69480115827173, u
 40.691177300600843, 0.6817119765857403, 0.6688155281272802], [1.
 472902572425929, 1.428882451558655, 1.326429053802382, 1.2552997202358462, 1.
 -2112315845760433, 1.15574713897976, 1.124009239233353, 1.1021092390133576, 1.
 →06770095737143, 1.0394391590221361, 1.0182694338939406, 0.9927973769266497, u
```

```
a5b_train_accuracies = [[0.3799715909090909, 0.4929421164772727, 0.
 →5354447798295454, 0.5599698153409091, 0.5757723721590909, 0.
 →5972123579545454, 0.6101296164772727, 0.6247114701704546, 0.
 →6323908025568182, 0.6470836292613636, 0.6540305397727273, 0.
 46573819247159091, 0.66796875, 0.6691450639204546, 0.677734375, 0.
 →6809303977272727, 0.6888982599431818, 0.6916281960227273, 0.
 46978204900568182, 0.69921875, 0.7071422230113636, 0.7091841264204546, 0.
 -7132013494318182, 0.7162420099431818, 0.7246315696022727, 0.724609375, 0.
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 △7515980113636364, 0.7524192116477273, 0.7565030184659091, 0.
 47576127485795454, 0.7630060369318182, 0.7660910866477273, 0.766357421875], u
 →[0.3916237571022727, 0.5060147372159091, 0.5419921875, 0.5774369673295454, 0.
 →5899325284090909, 0.6071111505681818, 0.621337890625, 0.633544921875, 0.
 →6412020596590909, 0.6545188210227273, 0.6566273082386364, 0.
 △6675470525568182, 0.6758478338068182, 0.6823064630681818, 0.
 46902965198863636, 0.6956232244318182, 0.7002618963068182, 0.
 →7047230113636364, 0.7078524502840909, 0.7139559659090909, 0.714111328125, 0.
 →7229669744318182, 0.7294034090909091, 0.7327547940340909, 0.
 -7359952059659091, 0.7401677911931818, 0.7412997159090909, 0.
 47433194247159091, 0.7513316761363636, 0.7529962713068182, 0.
 47606977982954546, 0.7652476917613636, 0.7703524502840909, 0.
 →7686434659090909, 0.7754572088068182, 0.7729714133522727, 0.
 47798295454545454, 0.778409090909090, 0.7783203125, 0.7852672230113636], [0.
 -387451171875, 0.4929865056818182, 0.5359330610795454, 0.5577281605113636, 0.
 →5773703835227273, 0.5941938920454546, 0.6086869673295454, 0.
 46210049715909091, 0.6332341974431818, 0.6369406960227273, 0.
 →6466841264204546, 0.6575150923295454, 0.6613325639204546, 0.
 46683460582386364, 0.6767134232954546, 0.6792436079545454, 0.
 →6880104758522727, 0.6888316761363636, 0.6959561434659091, 0.
 47016379616477273, 0.7094060724431818, 0.7094948508522727, 0.
 →7144664417613636, 0.7195712002840909, 0.7215243252840909, 0.
 47230335582386364, 0.7341752485795454, 0.728759765625, 0.7379483309659091, 0.
 →7393465909090909, 0.7425204190340909, 0.7445401278409091, 0.
 47535733309659091, 0.7549050071022727, 0.7549493963068182, 0.
 →7643821022727273, 0.7654252485795454, 0.7632501775568182, 0.
 47665127840909091, 0.771240234375], [0₁,38682972301136365, 0.
 49882368607954547, 0.5385520241477273, 0.5657848011363636, 0.
 →5819424715909091, 0.6000088778409091, 0.6109952059659091, 0.
 46215154474431818, 0.6325905539772727, 0.6442427201704546, 0.
```

```
a5b_val_losses = [[1.5655976742506028, 1.3963831067085266, 1.3190482884645462,__
  -1.285090345144272, 1.1842646718025207, 1.1781110033392905, 1.
  42044517546892166, 1.1658358544111251, 1.1269395604729653, 1.144325076043606, 1269395604729653
  ч1.1231994420289992, 1.1455506503582, 1.0182002529501915, 1.1665931209921836, ц
  →1.0535438820719718, 1.0705567941069603, 1.0929344102740288, 1.
  →0644094094634056, 1.0451778545975685, 1.1074789851903915, 1.
 ب0092910081148148, 1.0704100653529167, 1.0773278638720512, 1.033614307641983, المائية
  ↔0.9371625527739524, 1.080445683002472, 1.016153635084629, 1.
 40667413741350174, 0.9933030039072037, 1.0601032644510269, 1.
 -0384751126170157, 1.0301920726895333, 1.1099111706018447, 0.
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 →1.0233655765652656, 1.0458671301603317, 0.9734011679887772], [1.
 4513268408179283, 1.3747070342302323, 1.3019877135753632, 1.2758715957403184, u
 →1.1759078055620193, 1.1760823398828506, 1.1543381825089454, 1.
  ط098723790049553, 1.0578299179673194, 1.1890966176986695, 1.0396249800920487, المراحة المراحة
 9958298683166504, 1.0413264989852906, 1.1108571588993073, 1.047364141047001, u
 →0.981288594007492, 1.0091863930225373, 1.0793118178844452, 1.
 →0274139031767846, 0.9688847586512566, 0.9372925609350204, 1.
 40202151879668235, 0.945965439081192, 1.0281192481517791, 0.9344085216522217, u
 →0.9610651835799218, 0.9212571680545807, 0.9983295381069184, 0.
  →9096237152814866, 0.9598172143101692, 0.9618901014328003, 0.
 9990213632583618, 1.0358095958828926, 1.0074639916419983, 1.
 40772795021533965, 0.9557497963309288, 0.9335545226931572], [1.
 46622334122657776, 1.4224862158298492, 1.3248430237174034, 1.
  42902903407812119, 1.2557401299476623, 1.216827616095543, 1.2077743530273437, u
 →1.1106926679611206, 1.0985313400626182, 1.1716050073504447, 1.
 40718852132558823, 1.0947488024830818, 1.0802558809518814, 1.014692023396492, u
  ←1.1370791003108025, 1.0089283376932143, 1.0844287991523742, 1.
 40406236931681634, 1.0600083231925965, 1.0517213016748428, 1.073353184759617, u
 →1.0146382302045822, 1.0162255316972733, 1.1008418381214142, 0.
 9819896250963212, 1.1750887580215932, 1.0170021563768388, 1.
 40390363916754723, 1.0438886180520057, 1.050899587571621, 1.084867125749588, u
 →0.9853161200881004, 1.018677568435669, 1.0252774998545646, 1.
 4071724571287632, 0.9546704187989234, 0.9214951977133751, 1.007592961192131, u
 41.0354547321796417, 0.9933191135525703], [1.5239570379257201, 1.
  4112355917692185, 1.3159384429454803, 1.330892312526703, 1.344026692211628, u
  41.1783560037612915, 1.206761203706264 1.1922819584608078, 1.1922819584608078
  4137100425362587, 1.125764176249504, 1.100405828654766, 1.104533815383911, 1.
  40344666063785553, 1.0425182223320006, 1.1271056443452836, 1.
  -0592205673456192, 1.0610340416431427, 1.039922794699669, 1.2394075393676758, u
```

```
a5b_val_accuracies = [[0.42265625, 0.487109375, 0.5255859375, 0.5509765625, 0.
      457109375, 0.5796875, 0.5466796875, 0.58359375, 0.612109375, 0.597265625, 0.
      $\square$598046875, 0.590625, 0.6349609375, 0.5982421875, 0.634375, 0.619921875, 0.
      46158203125, 0.631640625, 0.633984375, 0.616796875, 0.641796875, 0.
      46357421875, 0.629296875, 0.64296875, 0.6673828125, 0.627734375, 0.651171875, u
      ↔0.63359375, 0.6494140625, 0.62265625, 0.6466796875, 0.637890625, 0.
      46330078125, 0.6611328125, 0.6353515625, 0.6609375, 0.6478515625, 0.6578125, 11
      ↔0.6439453125, 0.6720703125], [0.4427734375, 0.5025390625, 0.5419921875, 0.
      $40234375, 0.591015625, 0.5763671875, 0.584765625, 0.6095703125, 0.
      46255859375, 0.5662109375, 0.630859375, 0.60859375, 0.614453125, 0.613671875, 11
      40.6529296875, 0.634765625, 0.6248046875, 0.63359375, 0.6462890625, 0.
      →6423828125, 0.6216796875, 0.6423828125, 0.6587890625, 0.6740234375, 0.
      46490234375, 0.6740234375, 0.64609375, 0.6689453125, 0.66328125, 0.6796875, 0.
      46560546875, 0.67734375, 0.66484375, 0.665234375, 0.65859375, 0.6466796875, 0.
      46521484375, 0.64609375, 0.6775390625, 0.6791015625], [0.386328125, 0.
      4859375, 0.5177734375, 0.5322265625, 0.5455078125, 0.5705078125, 0.
      $\(\sigma 5654296875\), 0.6076171875\, 0.6115234375\, 0.5767578125\, 0.623828125\, 0.
      46197265625, 0.612890625, 0.6431640625, 0.590234375, 0.6443359375, 0.
      46134765625, 0.635546875, 0.6271484375, 0.6328125, 0.623828125, 0.637890625, u
      40.63515625, 0.61953125, 0.6482421875, 0.60390625, 0.6509765625, 0.
      →6380859375, 0.637890625, 0.6416015625, 0.63203125, 0.65859375, 0.6583984375, ⊔
      40.6423828125, 0.6306640625, 0.6666015625, 0.6796875, 0.6560546875, 0.
      △6513671875, 0.646484375], [0.4494140625, 0.48984375, 0.521484375, 0.
      $\infty$5119140625, 0.51875, 0.5791015625, 0.571875, 0.5775390625, 0.591015625, 0.
      46185546875, 0.6275390625, 0.6146484375, 0.6373046875, 0.6318359375, 0.
      $\operatorname{45962890625}, 0.62734375, 0.6265625, 0.6330078125, 0.573828125, 0.6451171875, 11
      →0.6271484375, 0.6365234375, 0.6373046875, 0.664453125, 0.6416015625, 0.
      46287109375, 0.6615234375, 0.6568359375, 0.659765625, 0.6576171875, 0.
      4657421875, 0.6517578125, 0.651171875, 0.67578125, 0.6337890625, 0.
      46458984375, 0.651953125, 0.6654296875, 0.6212890625, 0.684765625], [0.
      4728515625, 0.5126953125, 0.5005859375, 0.5474609375, 0.579296875, 0.
      △5685546875, 0.6068359375, 0.612109375, 0.6017578125, 0.61015625, 0.
      46166015625, 0.6294921875, 0.6103515625, 0.6416015625, 0.6423828125, 0.
      →648046875, 0.632421875, 0.634375, 0.6599609375, 0.6232421875, 0.64765625, 0.
      46578125, 0.620703125, 0.635546875, 0.6513671875, 0.6595703125, 0.6525390625, u
      40.64921875, 0.631640625, 0.6568359375, 0.66484375, 0.6640625, 0.6595703125,
      40.666015625, 0.6607421875, 0.6580078125, 0.6408203125, 0.636328125, 0.
      →655078125, 0.62578125]]
[]: print(max(val_accuracy))
     print(max(val_accuracy_2))
     print(max(val_accuracy_3))
     print(max(val_accuracy_4))
     print(max(val_accuracy_5))
```

[]: \_, test\_acc\_1 = evaluate(model\_1, test\_loader)
\_, test\_acc\_2 = evaluate(model\_2, test\_loader)

```
_, test_acc_3 = evaluate(model_3, test_loader)
_, test_acc_4 = evaluate(model_4, test_loader)
_, test_acc_5 = evaluate(model_5, test_loader)
print(f"Test Accuracy: {test_acc_1}")
print(f"Test Accuracy: {test_acc_2}")
print(f"Test Accuracy: {test_acc_3}")
print(f"Test Accuracy: {test_acc_3}")
print(f"Test Accuracy: {test_acc_4}")
print(f"Test Accuracy: {test_acc_5}")
```

Test Accuracy: 0.6798852848101266
Test Accuracy: 0.6870055379746836
Test Accuracy: 0.6590189873417721
Test Accuracy: 0.6926424050632911
Test Accuracy: 0.646064082278481

Test accuracies for the convolutional model

Test Accuracy:  $0.6798852848101266 \setminus \text{Test Accuracy}$ :  $0.6870055379746836 \setminus \text{Test Accuracy}$ :  $0.6590189873417721 \setminus \text{Test Accuracy}$ :  $0.6926424050632911 \setminus \text{Test Accuracy}$ :  $0.646064082278481 \setminus \text{Test Accuracy}$ 

```
[11]: epochs = range(1, 41)
      plt.figure(figsize=(12, 8), dpi=90)
      plt.plot(epochs, a5b_train_accuracies[0], label="Train Accuracy 1", linestyle = "
       →"dashed")
      plt.plot(epochs, a5b_val_accuracies[0], label="Validation Accuracy 1")
      plt.plot(epochs, a5b_train_accuracies[1], label="Train Accuracy 2",linestyle = "

¬"dashed")
      plt.plot(epochs, a5b_val_accuracies[1], label="Validation Accuracy 2")
      plt.plot(epochs, a5b_train_accuracies[2], label="Train Accuracy 3", linestyle = __

¬"dashed")

      plt.plot(epochs, a5b_val_accuracies[2], label="Validation Accuracy 3")
      plt.plot(epochs, a5b_train_accuracies[3], label="Train Accuracy 4", linestyle =__

¬"dashed")

      plt.plot(epochs, a5b_val_accuracies[3], label="Validation Accuracy 4")
      plt.plot(epochs, a5b_train_accuracies[4], label="Train Accuracy 5", linestyle = __

¬"dashed")

      plt.plot(epochs, a5b_val_accuracies[4], label="Validation Accuracy 5")
      plt.plot([0, 40], [0.65, 0.65], linestyle = "dotted", color = "black")
      plt.xlabel("Epoch")
      plt.ylabel("Accuracy")
      plt.legend(loc = "lower right")
      plt.title("Convolutional nn Accuracy for CIFAR-10 vs Epoch")
      plt.show()
```

