Evaluating the Robustness of rStar: A Novel Framework for Enhanced Reasoning in Small Language Models

. Trajectory Masking & Completion

3. Final Trajectory Selection

 \rightarrow ... The answer: 60

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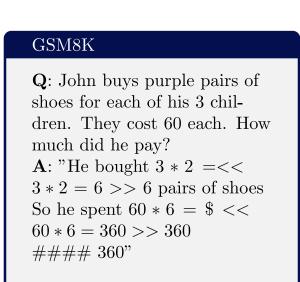
2. Validation

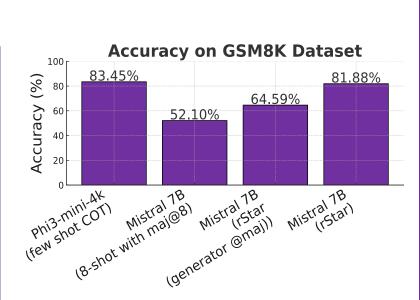
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Introduction

- Small language models (SLMs) show strong reasoning abilities, but benchmarks like **Grade School Math 8K** (GSM8K) may overestimate their true reasoning capabilities [1]
- Recent methods enhance reasoning but may neglect robustness to diverse input variations [2]
- This study evaluates the **robustness of rStar** by evaluating its performance across diverse variations of inputs to identify its strengths and limitations, offering a more accurate assessment of its reasoning abilities in mathematical problem-solving.

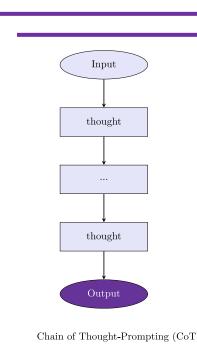




rStar Background

Prompting Language Models to Reason

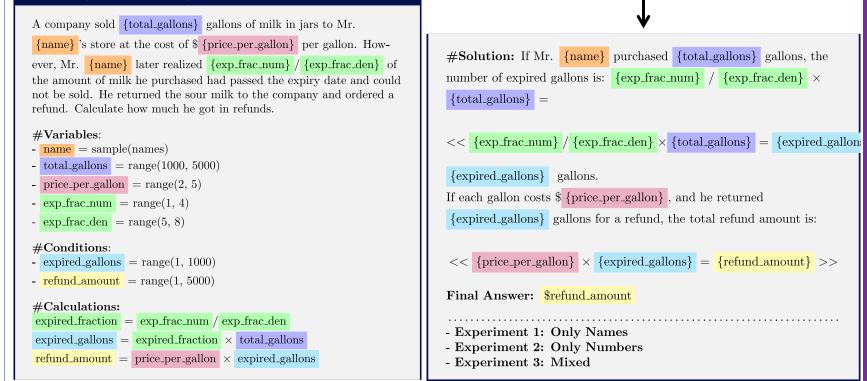
- Chain of Thought (CoT)
- Sampling Reasoning Paths
- Self-consistency
- **Answer Verification**
- @maj
- Self verification
- Mutual consistency

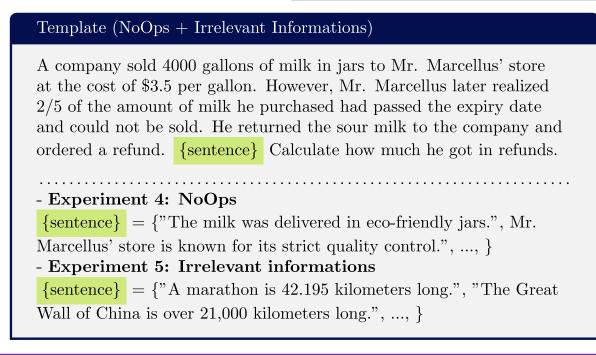


Methodology

Variations

- Enhance GSM8K dataset by introducing 5 new variation types
- Each variation type is represented by generic templates
- Generate novel math questions derived from the original GSM8K dataset





Conclusion

- Lower Performance: All experiments, apart from changing names, resulted in a drop in rStar's performance beyond one standard deviation.
- Lack of Robustness: Experiments reveal that rStar is not robust to various input variations.
- Largest Accuracy Drop: Numeric variations caused the largest performance decline.
- Combined Variations: Combining names and numbers led to a much smaller drop in accuracy compared to numbers alone.
- NoOps vs. Irrelevant Info: NoOps caused a slightly larger accuracy drop than irrelevant information, suggesting rStar handles ignoring irrelevant information better than handling seemingly relevant information.

Future Work

- More variations & bigger subset of questions
- Develop another action that is adapted to the newly introduced variances
- Run experiment more times to account for the inherent variance of language models

Limitations

- Generator on 40 questions took approx. 12-13 hours using a Tesla A100 PCIE 40 GB
- Discriminator on 40 questions took approx. 6 hours using a Tesla A100 PCIE 40 GB
- Queue time during the busiest periods was approx. 1-2 days

Related Work

- GSM1k (newly crafter analogous to GSM8k up to 8% drop in accuracy) [3]
- **Token bias** with logical problems [4]
 - **Token bias** is the idea that the models are biased to the specific tokens that appear in the GSM8k dataset (the names and
- PMC benchmark Problems with missing and contradictory conditions [5]

Results

Accuracy and Majority Vote Accuracy Across Experiments with Baseline Reference **---** Baseline Discriminator --- Baseline rStar @maj Discriminator ∣rStar @maj Irrelevant Information Numbers NoOps Names and Numbers Names **Experiments**

rStar

If value > Threshold

John ran 180 meters every day

1. Selection $UCT(s,a) = \frac{Q(s,a)}{N(s,a)} + c\sqrt{\frac{\ln N_{\text{parent}}(s)}{N(s,a)}}$

3. Propagation $Q(s_i, a) = Q(s_i, a) + Q(s_d, a_d)$

Propose a one-step thought (A1)

Answer the sub-question again (A4)

Discriminator SLM: Phi-3-mini-4k-instruct

Generator SLM: Mistral 7B-v0.1

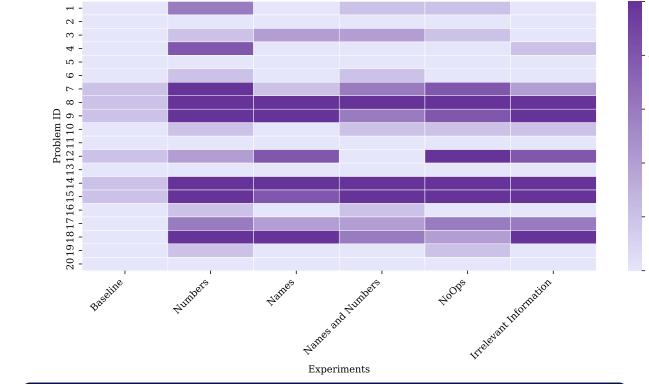
Propose the remaining thought steps (A2)

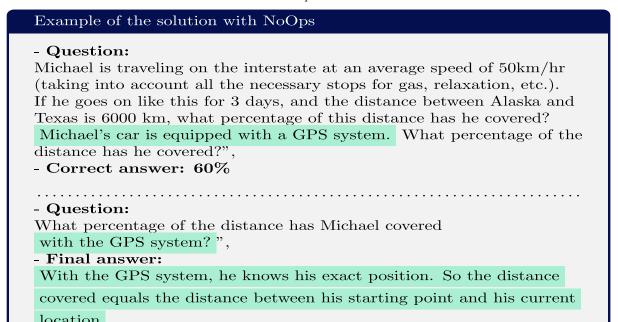
Propose next sub-question along with its answer (A3)

2. Expansion & Simulation

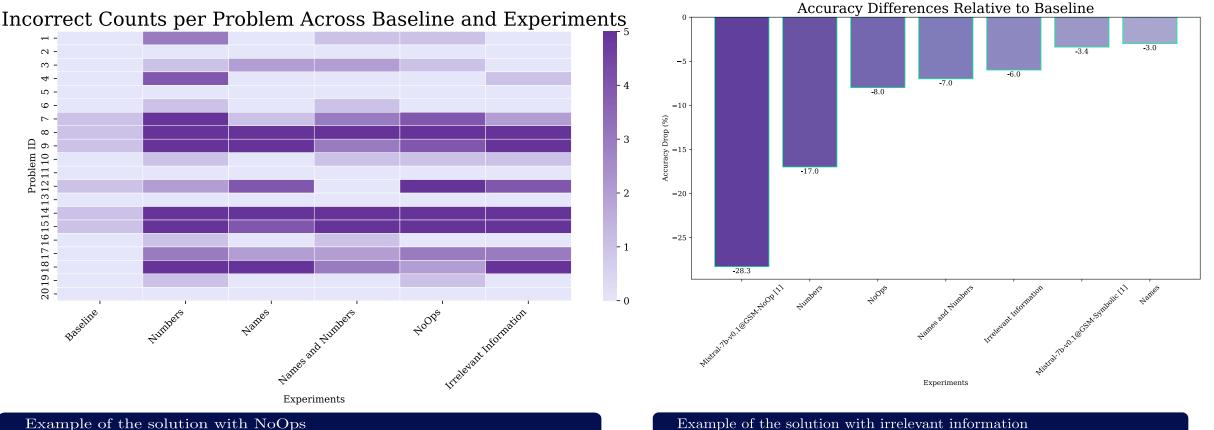
Actions:

Candidate





The answer is 100%.



- Question: There are about 7.8 billion people on Earth. Audrey has to take two math tests to pass 6 grade. They must correctly answer 70% of the total questions to move on to the next grade. The first test has 70 questions, and they get 60% of them correct. The second test has 40 questions. How many questions do they need to get right on the second test to pass? - Correct answer: 35

Let's think step by step. There are about 7.8 billion people on Earth. To pass 6th grade, one must correctly answer 70% of the to-

tal questions. So, to pass 6th grade, one needs to answer 70% of 7.8 billion which is 5.46 billion. The first test has 70 questions. One gets 60% of the first test which is 42 questions correct. Therefore, 5.46 billion / 42 is equal to 130 questions correct. The answer is: 130.

References

[1] Mirzadeh, I., Alizadeh, K., Shahrokhi, H., Tuzel, O., Bengio, S., & Farajtabar, M. (2024). GSM-Symbolic: Understanding the Limitations of Mathematical Reasoning in Large Language Models. arXiv. https://arxiv.org/abs/2410.05229

[2] Zhenting Qi and Mingyuan Ma and Jiahang Xu and Li Lyna Zhang and Fan Yang and Mao Yang (2024), Mutual Reasoning Makes Smaller LLMs Stronger Problem-Solvers

[3] H. Zhang, J. Da, D. Lee, V. Robinson, C. Wu, W. Song, T. Zhao, P. Raja, C. Zhuang, D. Slack, Q. Lyu, S. Hendryx, R. Kaplan, M. Lunati, and S. Yue, "A Careful Examination of Large Language Model Performance on Grade School Arithmetic," arXiv preprint arXiv:2405.00332, 2024. [Online]. Available: https://arxiv.org/abs/2405.00332

[4] B. Jiang, Y. Xie, Z. Hao, X. Wang, T. Mallick, W. J. Su, C. J. Taylor, and D. Roth, "A Peek into Token Bias: Large Language Models Are Not Yet Genuine Reasoners," in *Proceedings of the 2024 Conference on Empirical Methods in* Natural Language Processing, Y. Al-Onaizan, M. Bansal, and Y.-N. Chen, Eds., Miami, Florida, USA, Nov. 2024, pp. 4722–4756. Association for Computational Linguistics. [Online]. Available: https://aclanthology.org/2024.emnlpmain.272. doi: 10.18653/v1/2024.emnlp-main.272

[5] S.-Y. Tian, Z. Zhou, L.-H. Jia, L.-Z. Guo, and Y.-F. Li, "Robustness Assessment of Mathematical Reasoning in the Presence of Missing and Contradictory Conditions," arXiv preprint arXiv:2406.05055, 2024. [Online]. Available: https://arxiv.org/abs/2406.05055

ChatGPT was used to explain complicated topics and help with text refinement