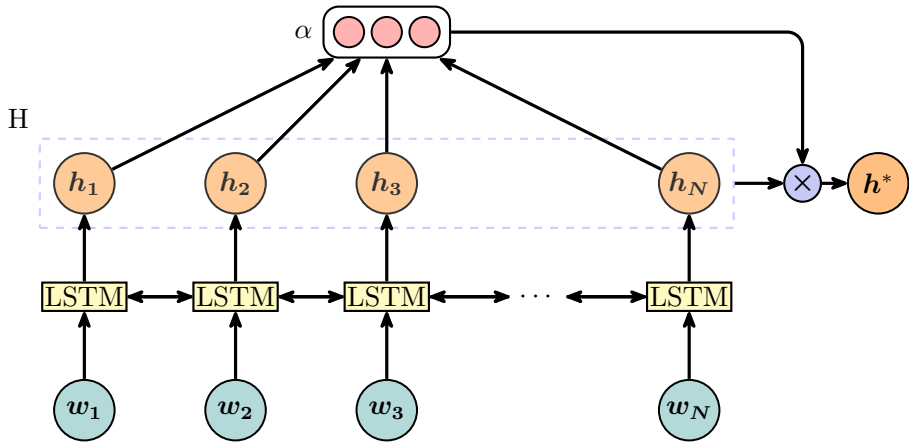
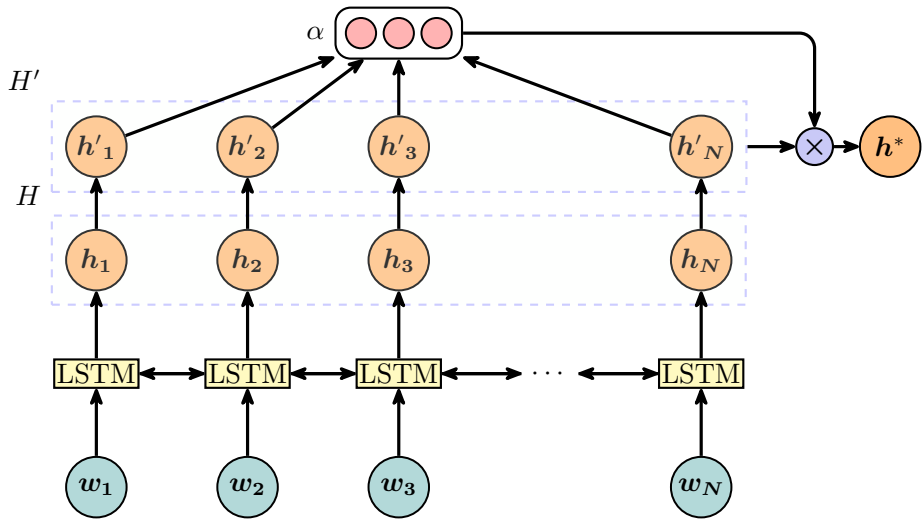


$$\begin{aligned}
X &= \begin{bmatrix} h_{t-1} \\ x_t \end{bmatrix} \\
f_t &= \sigma(W_f \cdot X + b_f) \\
i_t &= \sigma(W_i \cdot X + b_i) \\
o_t &= \sigma(W_o \cdot X + b_o) \\
\tilde{C}_t &= \tanh(W_c \cdot X + b_c) \\
c_t &= f_t \odot c_{t-1} + i_t \odot \tilde{C}_t \\
h_t &= o_t \odot \tanh(c_t)
\end{aligned} \tag{1}$$

$$\begin{aligned}
X &= \begin{bmatrix} h_{t-1} \\ x_t \\ v_a \end{bmatrix} \\
f_t &= \sigma(W_f \cdot X + b_f) \\
i_t &= \sigma(W_i \cdot X + b_i) \\
o_t &= \sigma(W_o \cdot X + b_o) \\
\tilde{C}_t &= \tanh(W_c \cdot X + b_c) \\
c_t &= f_t \odot c_{t-1} + i_t \odot \tilde{C}_t \\
h_t &= o_t \odot \tanh(c_t)
\end{aligned} \tag{2}$$



$$\begin{aligned}
M &= \tanh \left( \begin{bmatrix} W_h H \\ W_v v_a \otimes e_N \end{bmatrix} \right) \\
\alpha &= \text{softmax} \left( w^T M \right) \\
h^* &= H \alpha^T
\end{aligned} \tag{3}$$



$$v_a^{'}=v_a+p_a$$

$$H^{'}=H+P$$

$$\alpha = \text{softmax}\left(\frac{\left(W_v \textcolor{red}{v}_a^{'}\right)^T\left(W_h \textcolor{red}{H}^{'}\right)}{\sqrt{d_a}}\right) \tag{4}$$

$$h^*=H\alpha^T$$



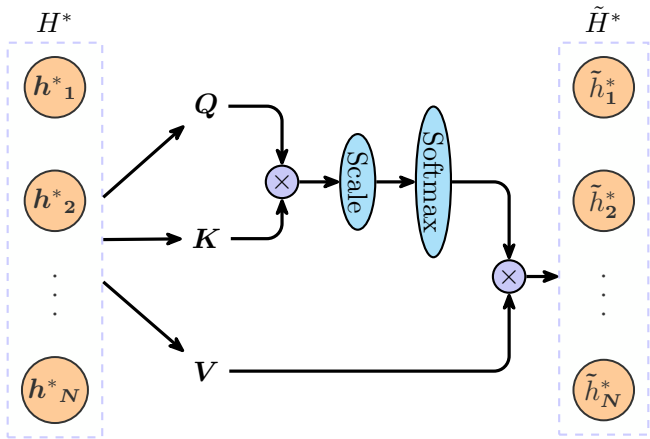
$$Q = H^*W_Q$$

$$K = H^*W_k$$

$$V = H^*W_V$$

$$\tilde{H}^* = \text{softmax}\left(\frac{Q \cdot K^\top}{\sqrt{d}}\right) \cdot V$$

(5)



$$\begin{aligned}
r_t &= \sigma \left( W_r \cdot \begin{bmatrix} h_{t-1} \\ x_t \\ v_a \end{bmatrix} + b_r \right) \\
z_t &= \sigma \left( W_z \cdot \begin{bmatrix} h_{t-1} \\ x_t \\ v_a \end{bmatrix} + b_z \right) \\
\tilde{h}_t &= \tanh \left( W \cdot \begin{bmatrix} r_{t*} h_{t-1} \\ x_t \\ v_a \end{bmatrix} \right) \\
h_t &= (1 - z_t) \cdot h_{t-1} + z_t \cdot \tilde{h}_t
\end{aligned} \tag{6}$$

