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and Applied Sciences

Measurement of sub-Femtonewton Optical Forces in Fluid

High-precision measurements
at the thermal limit using a
Brownian probe

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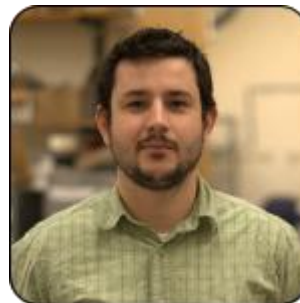
Collaborators, Visitors, Funders, PI



Andrea Di Donato



Federico Capasso - PI



Simon Kheifets



Vincent Ginis

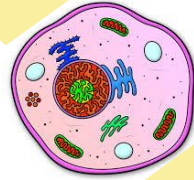


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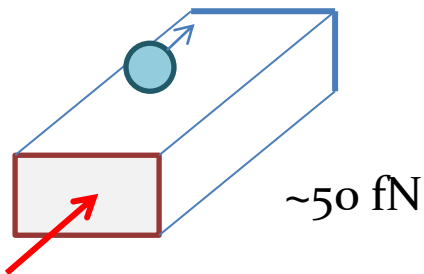


what's 1 fN?

optical force
of sunlight on
single cell

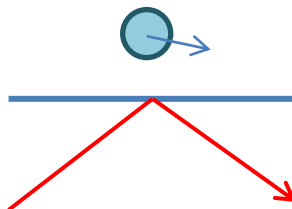


drag on bacterium moving through water



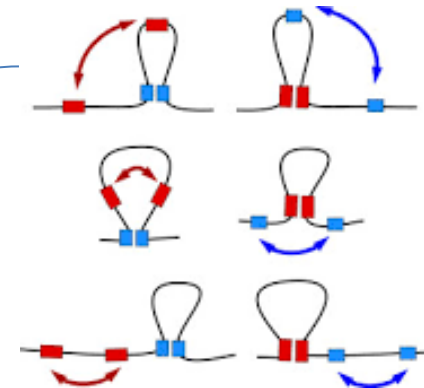
~50 fN

~10 fN



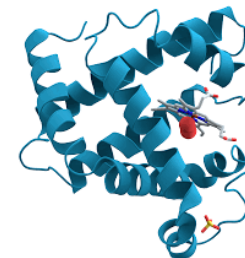
Forces in
Optics

Forces in
Biology



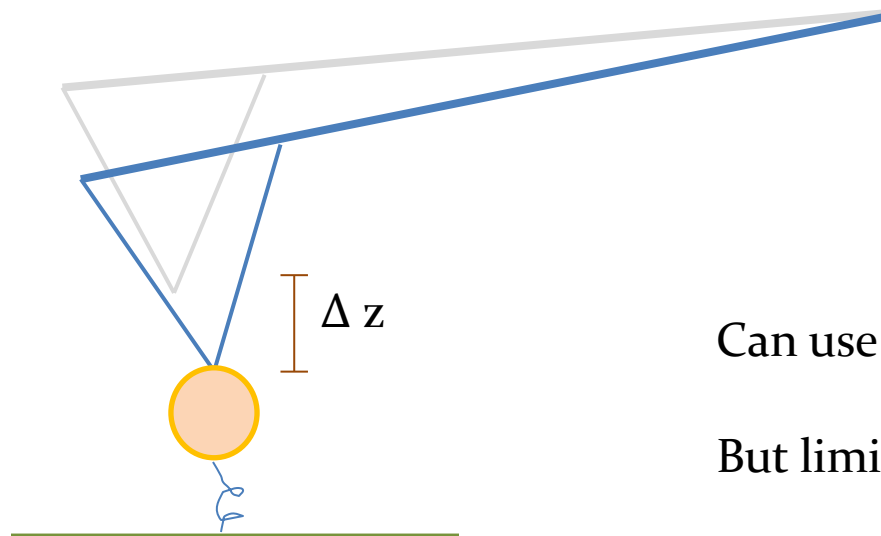
< 100 fN

Hfsp.org



~ 20 fN

AFM is the most commonly used instrument for performing force spectroscopy, but its sensitivity, especially in fluid, is limited



$$F = -K \Delta Z$$

Can use more compliant cantilever

But limited by thermal noise

Force Sensitivity: $\sim 0.1\text{-}1$ pN



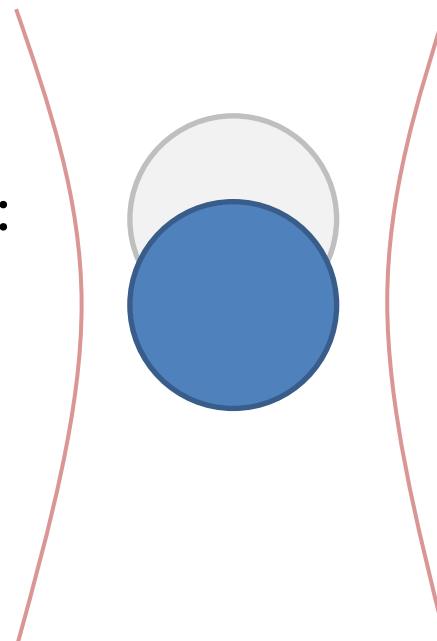
Thermal fluctuations is a dominant noise source at these scales

$$S_F^{th} = 2\gamma kT$$

Fluctuation-dissipation theorem:
Thermal noise scales with drag

Drag in liquid many times drag in air

1. Reduce the thermal limit:

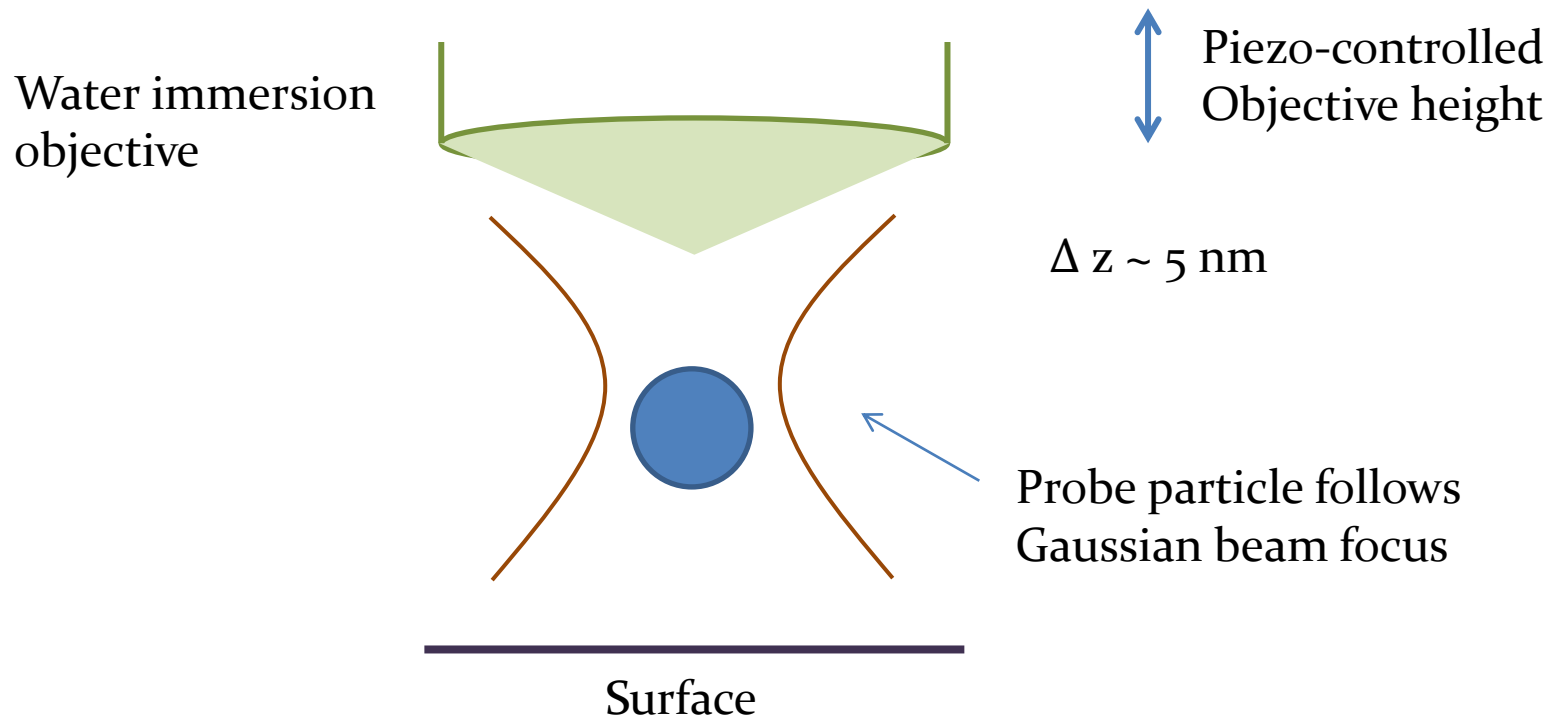


Δz

Replace AFM cantilever
with optically trapped
microsphere (PFM)

D. Prieve
E-L Florin

2. Scan focus of optical tweezer to precisely position trapped bead



3. Use light scattered from an evanescent wave to track particle position at ~ 1 ms time scale



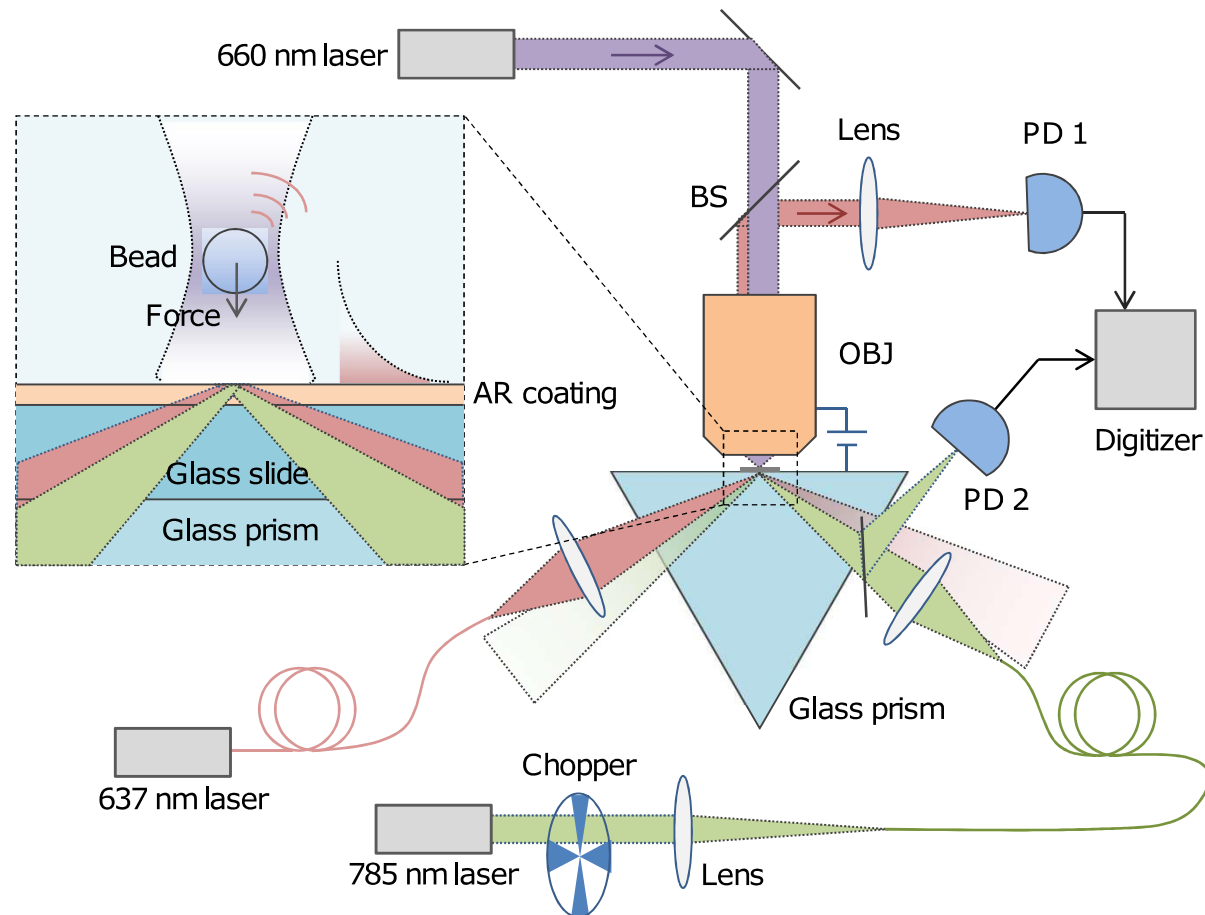
$$I(z) = I_0 e^{-\beta z} + C$$

Devised method to directly
measure each calibration
constant:

(Liu, L. (2014). PNAS)

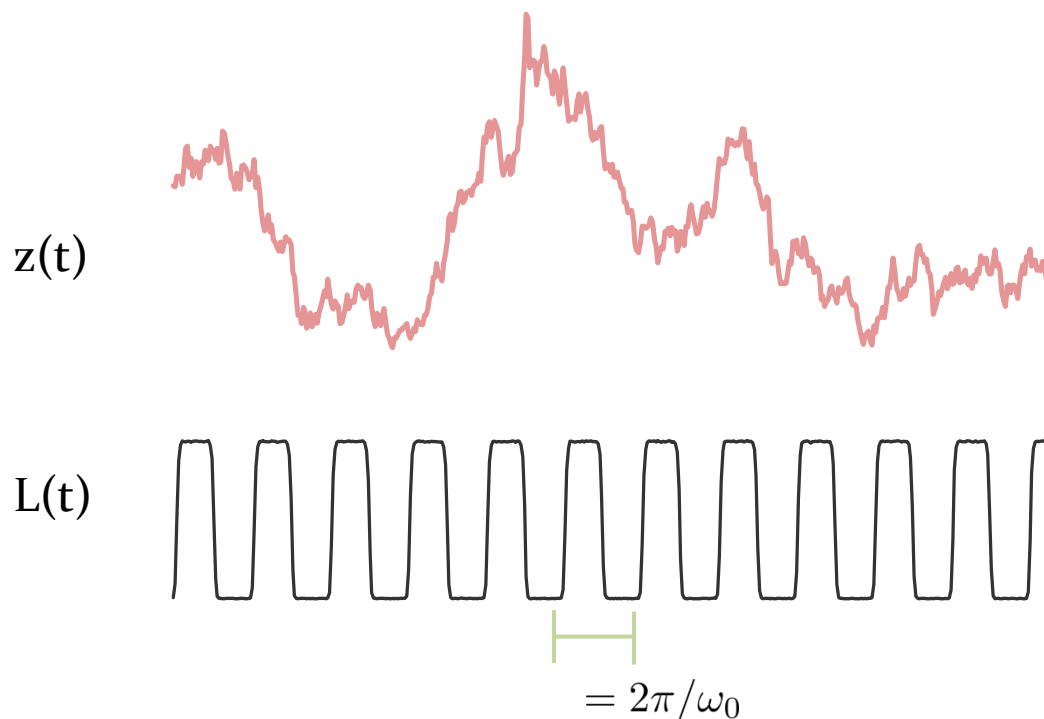
(Prieve, et al)

4. Use another totally internally reflected beam to generate attractive gradient optical force





5. Modulate optical force with chopper and use lock-in detection to extract response amplitude & phase



$$\tilde{z}_{tot}(\omega) = \tilde{z}_B(\omega) + \tilde{z}_{ext}(\omega)$$

noise

Response Amplitude: $|\tilde{z}_{ext}(\omega_0)|$

Response Phase: $\text{Arg}[\tilde{z}_{ext}(\omega_0)]$

Avoid 1/f noise, avoid noise peaks



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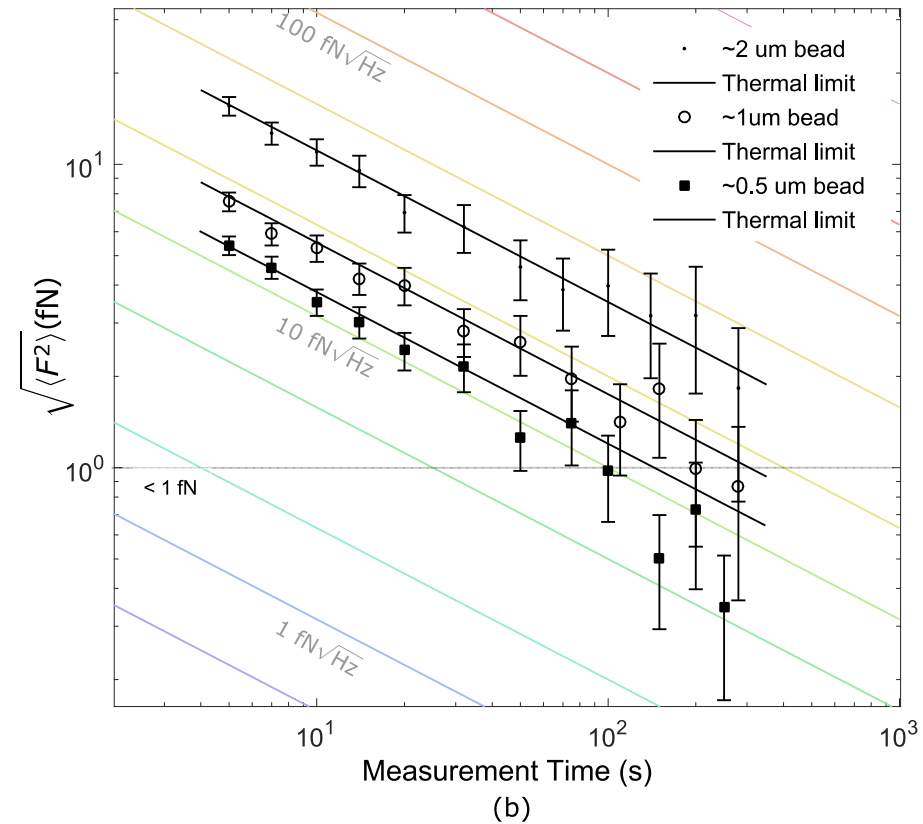
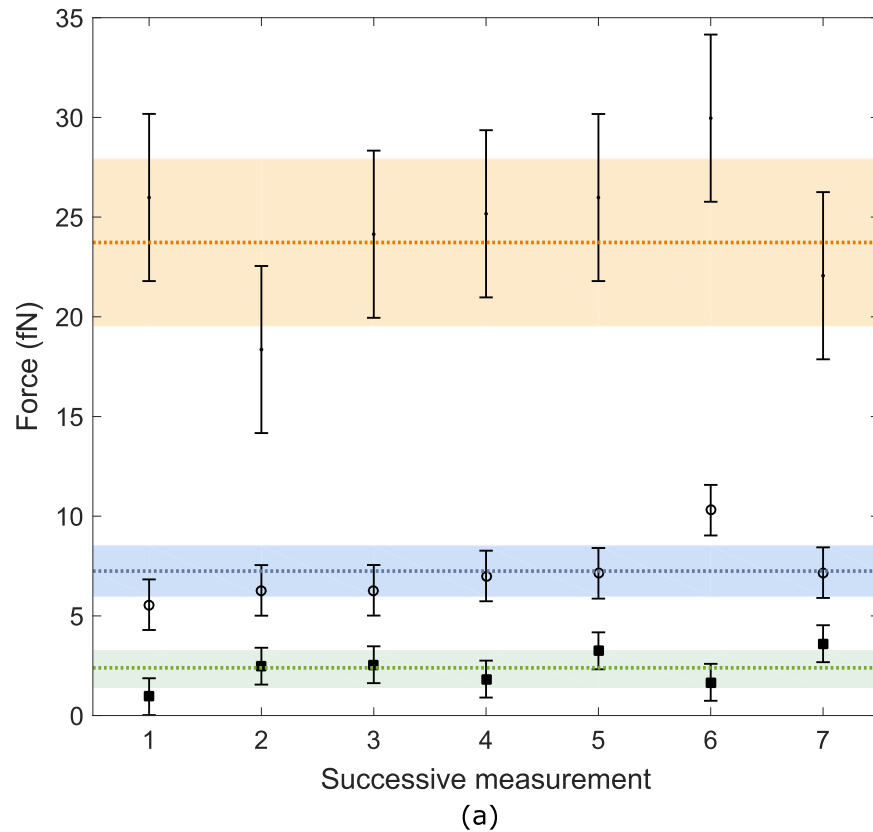
Etc.

For more details:

Liu, L., Kheifets, S., Ginis, V., & Capasso, F. (2016). PRL

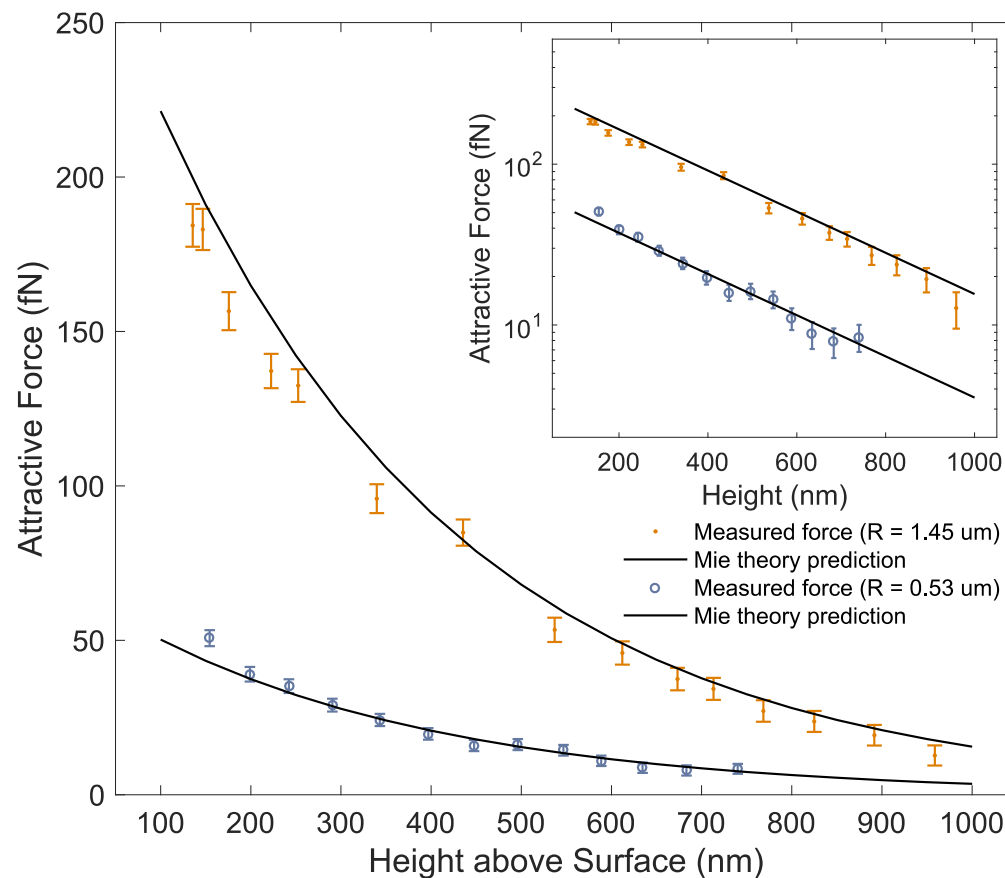


Measured noise agrees with thermal limit predictions





Measured $F(z)$ agrees quantitatively with Mie Theory predictions

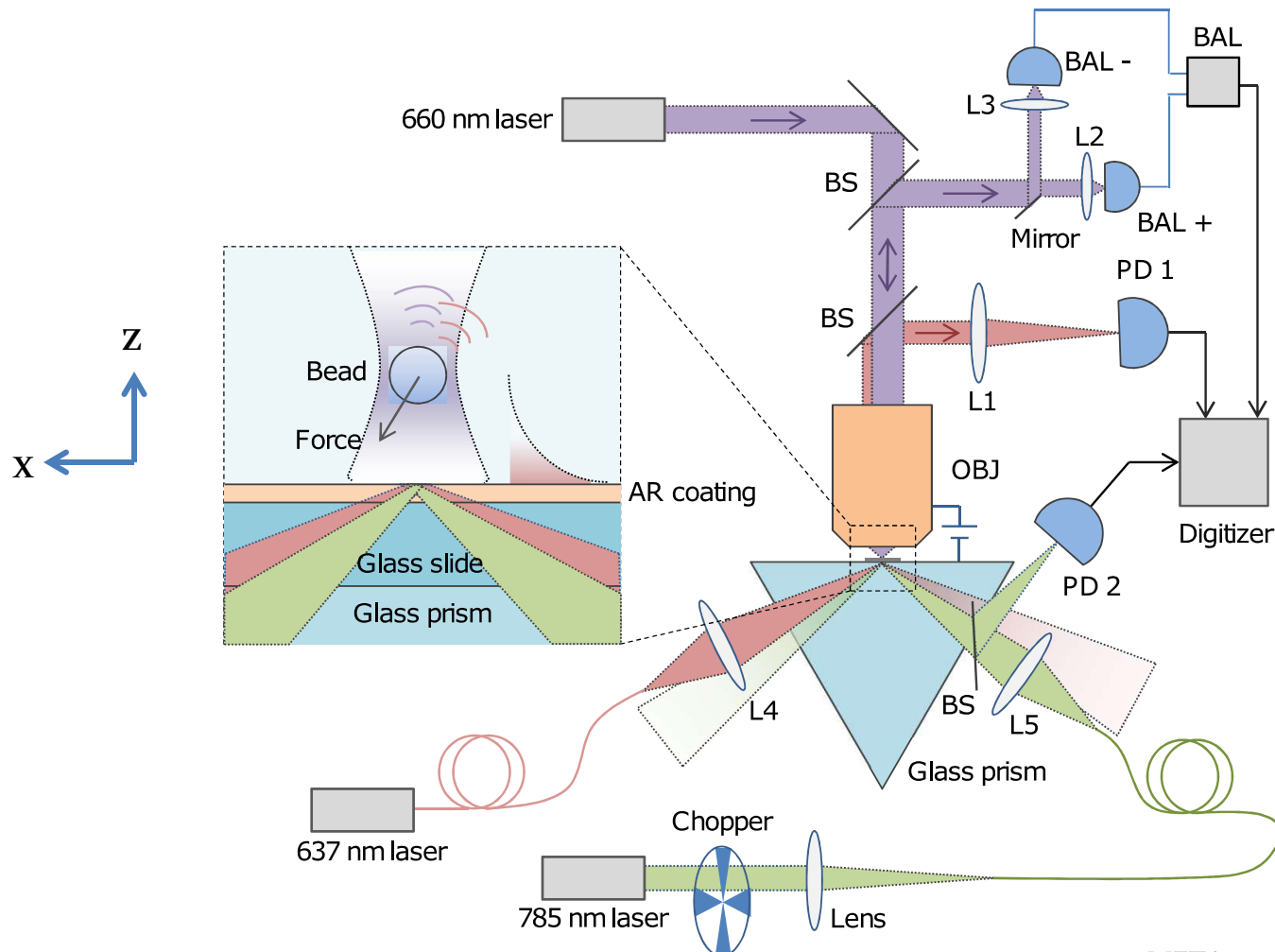




Summary

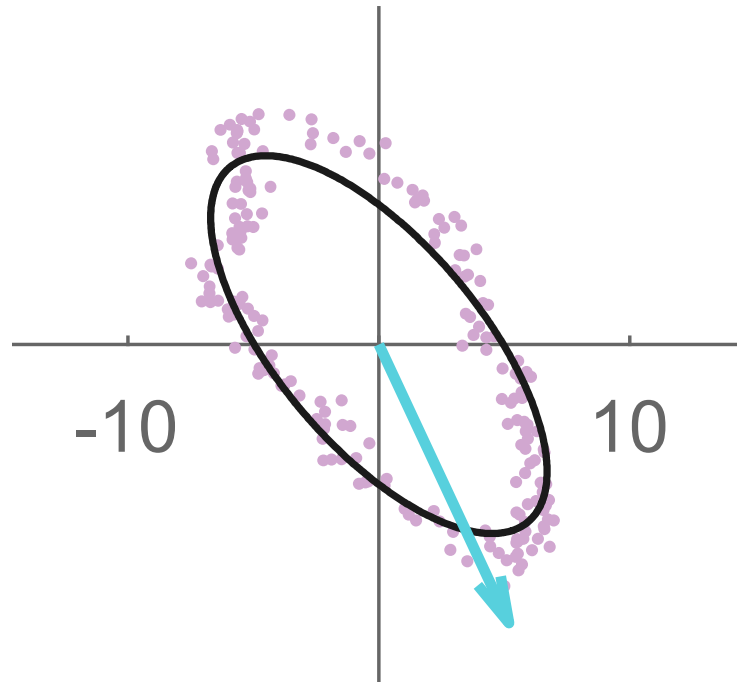
- > 100x improvement in sensitivity ($N/\sqrt{\text{Hz}}$) over previous methods (including PFM and AFM methods)
- First quantitative confirmation of Mie theory for forces from evanescent field.

For continuing work we added another dimension of detection





Discovered some interesting dynamics due to near-surface anisotropy



Paper in progress,
come talk to me!