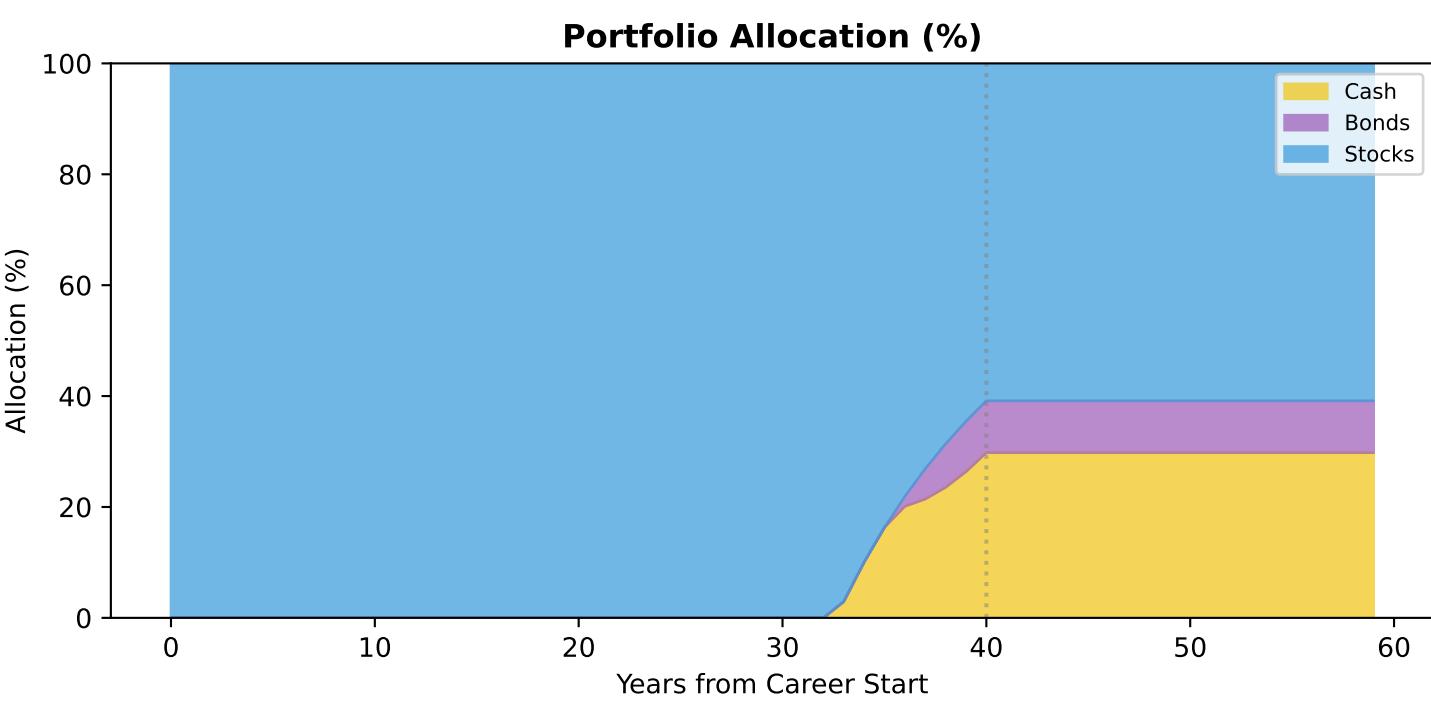
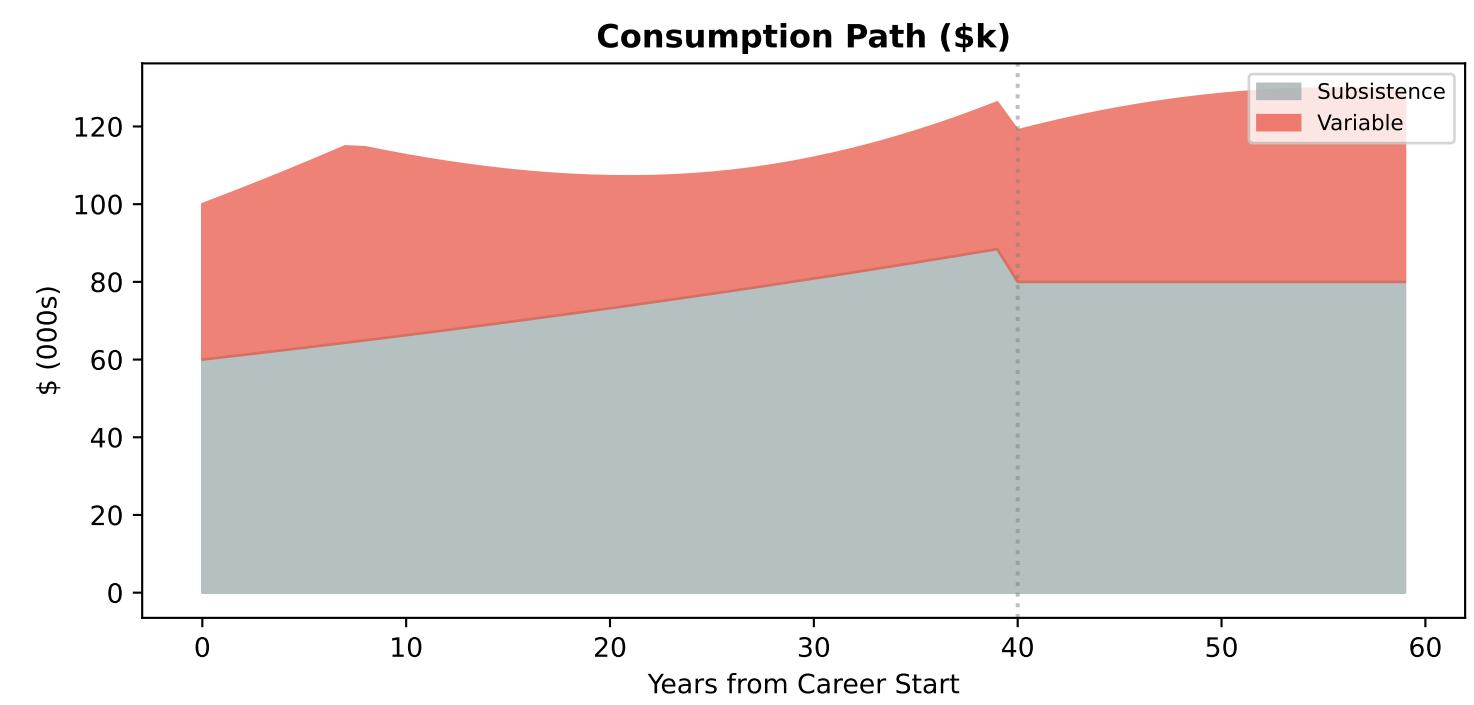
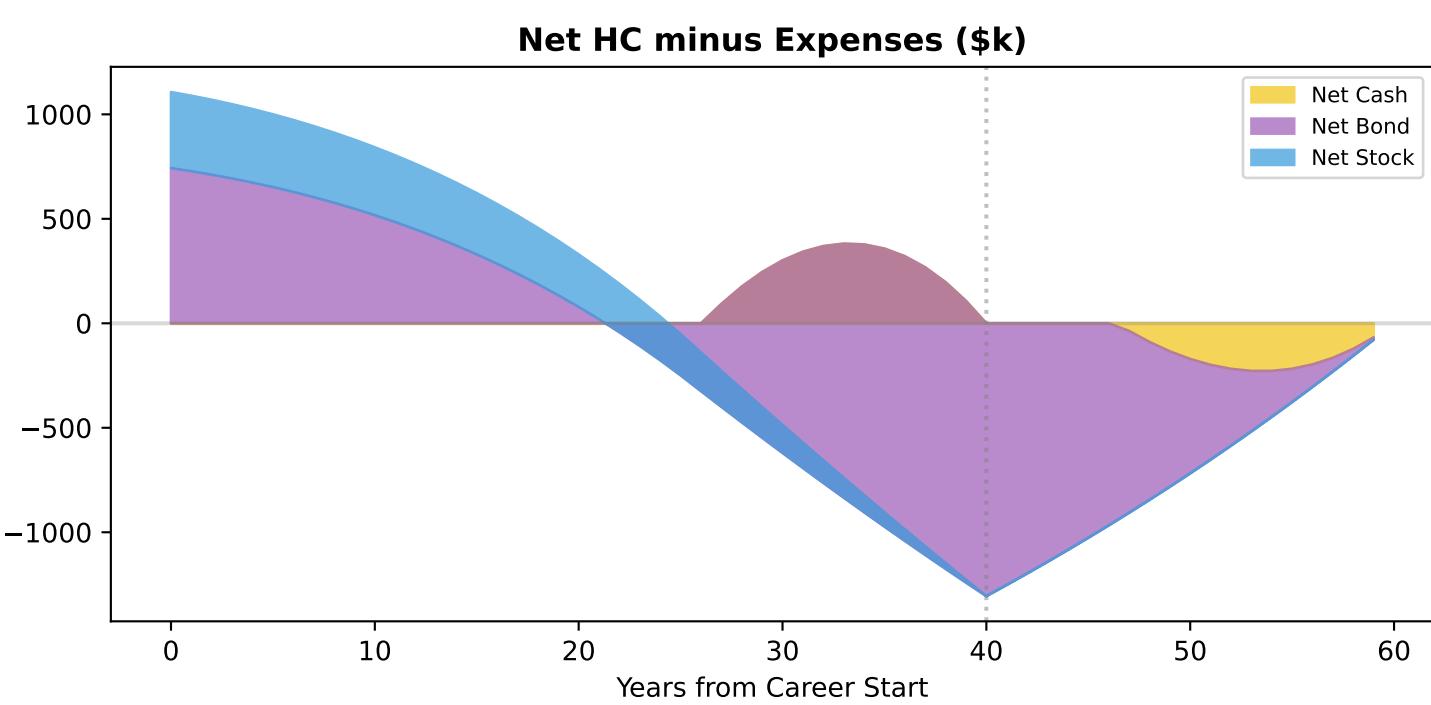
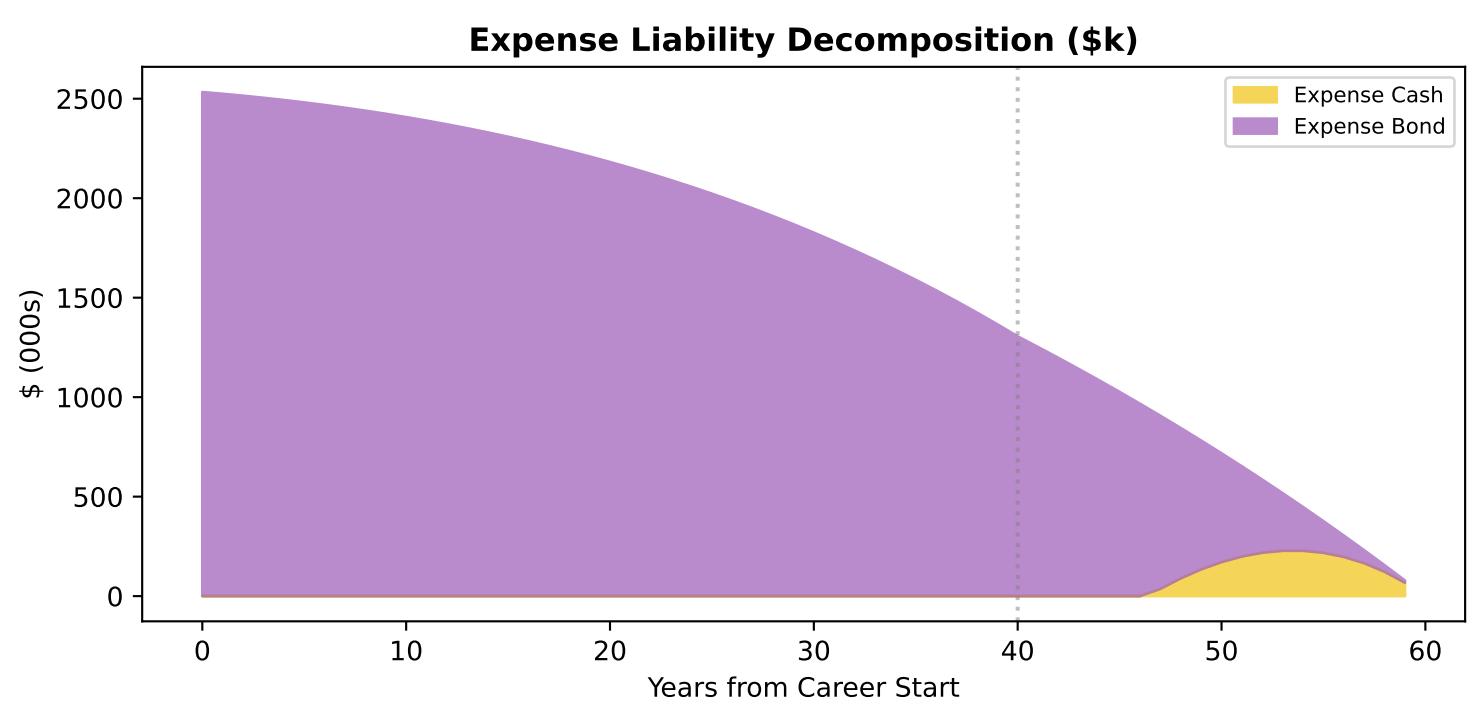
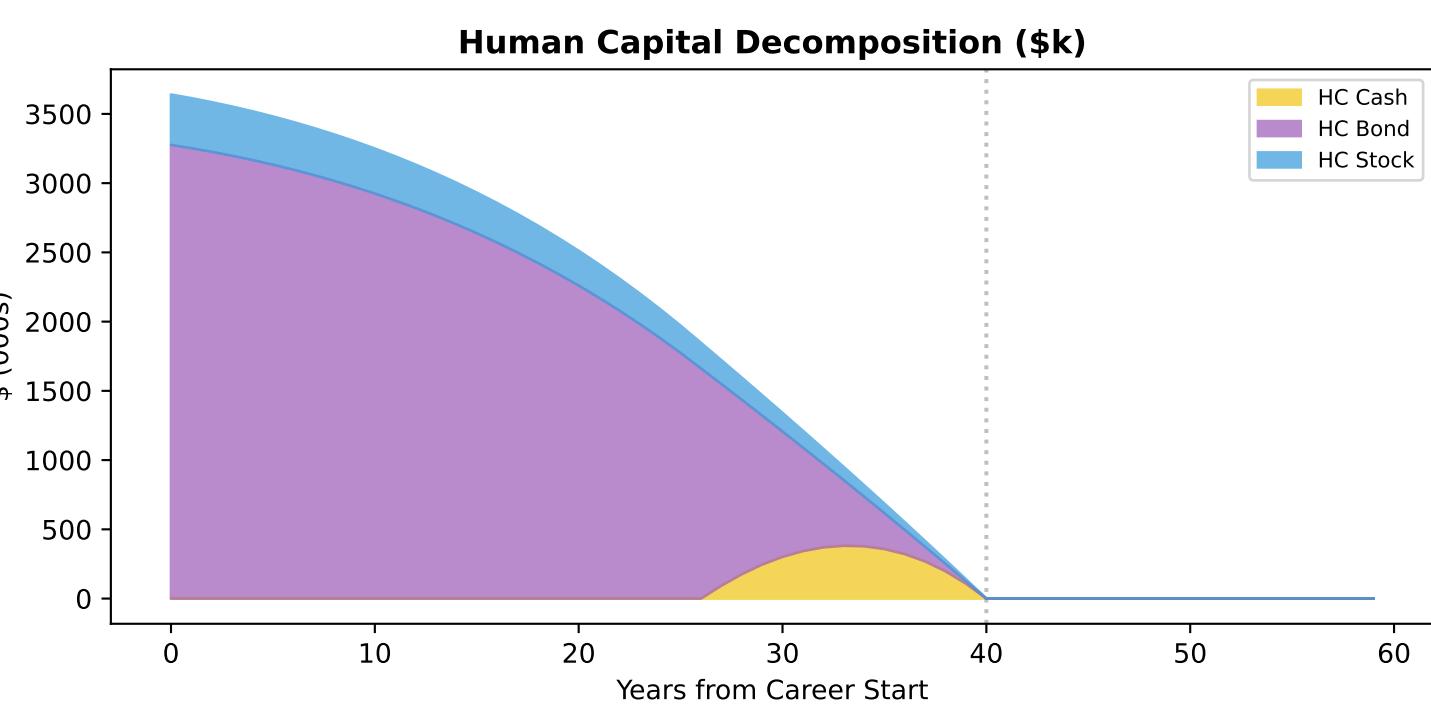
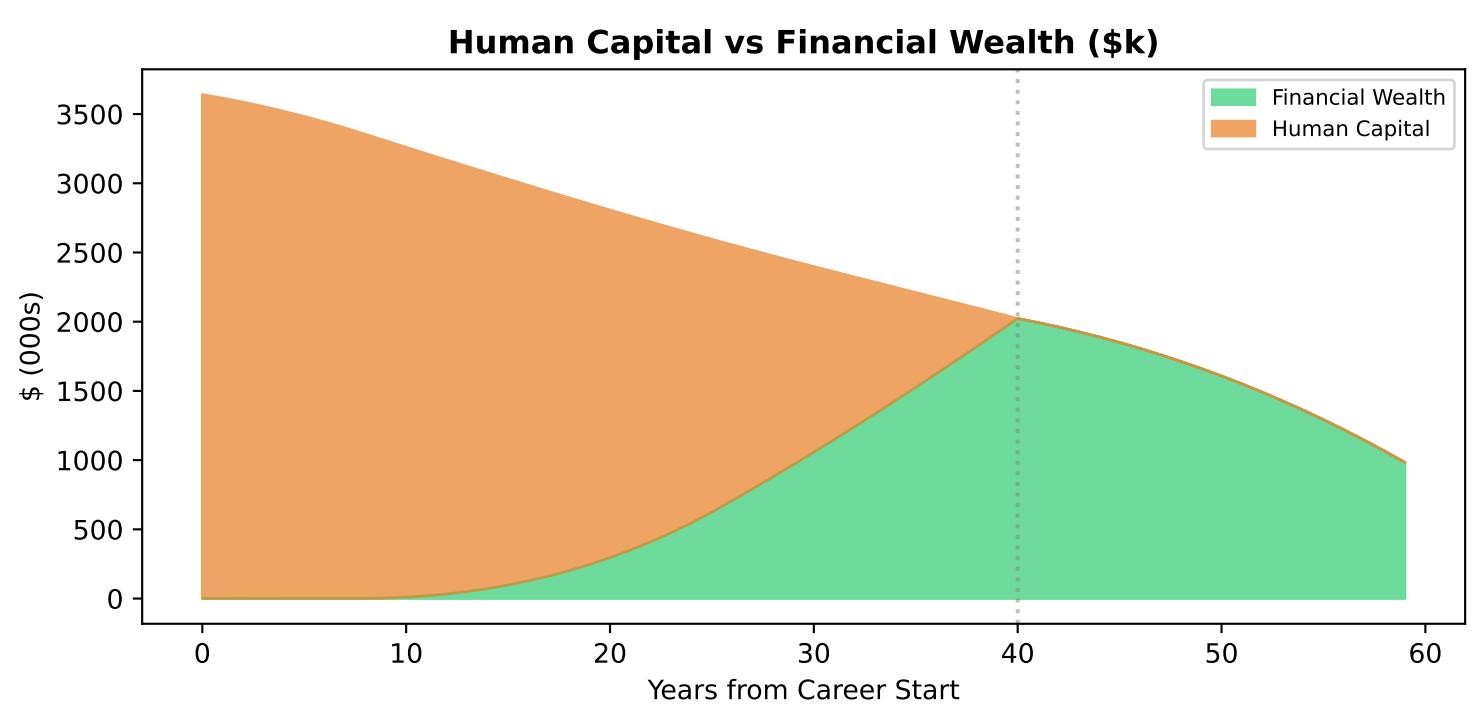
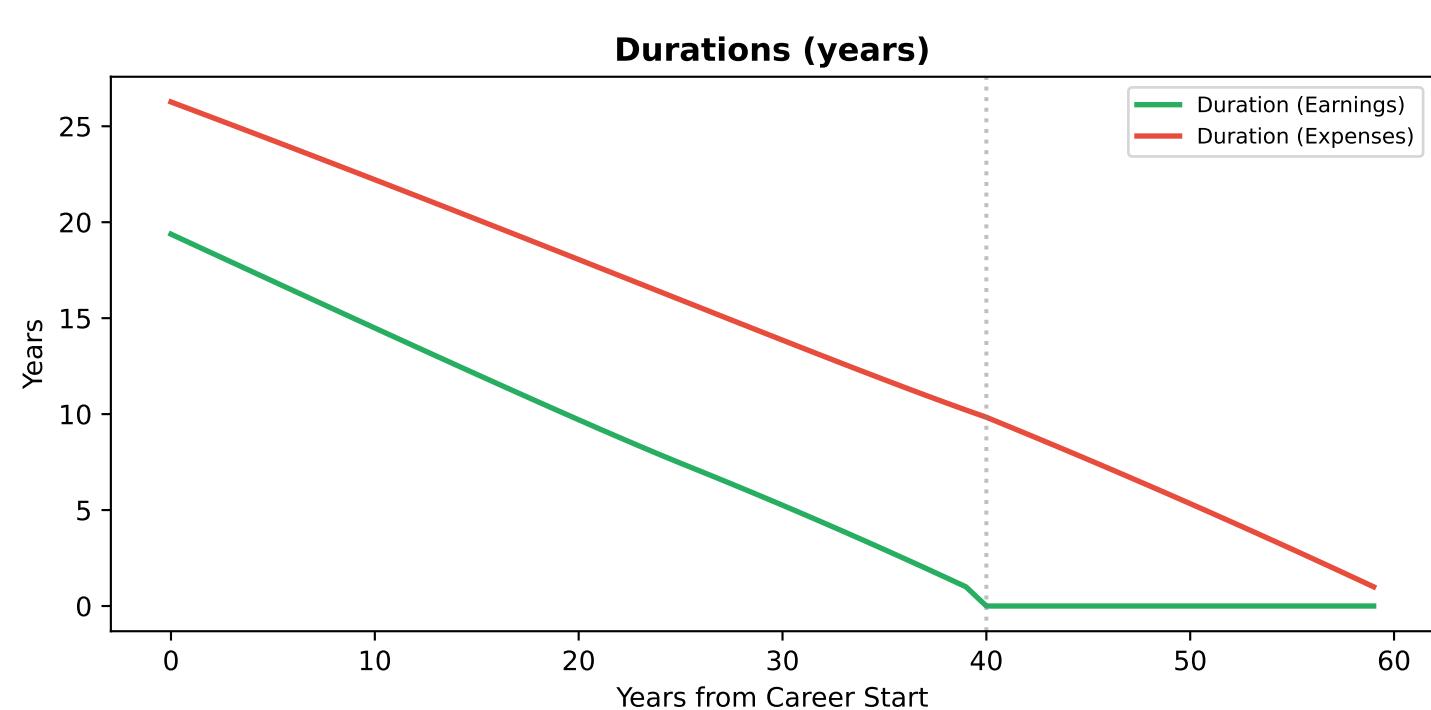
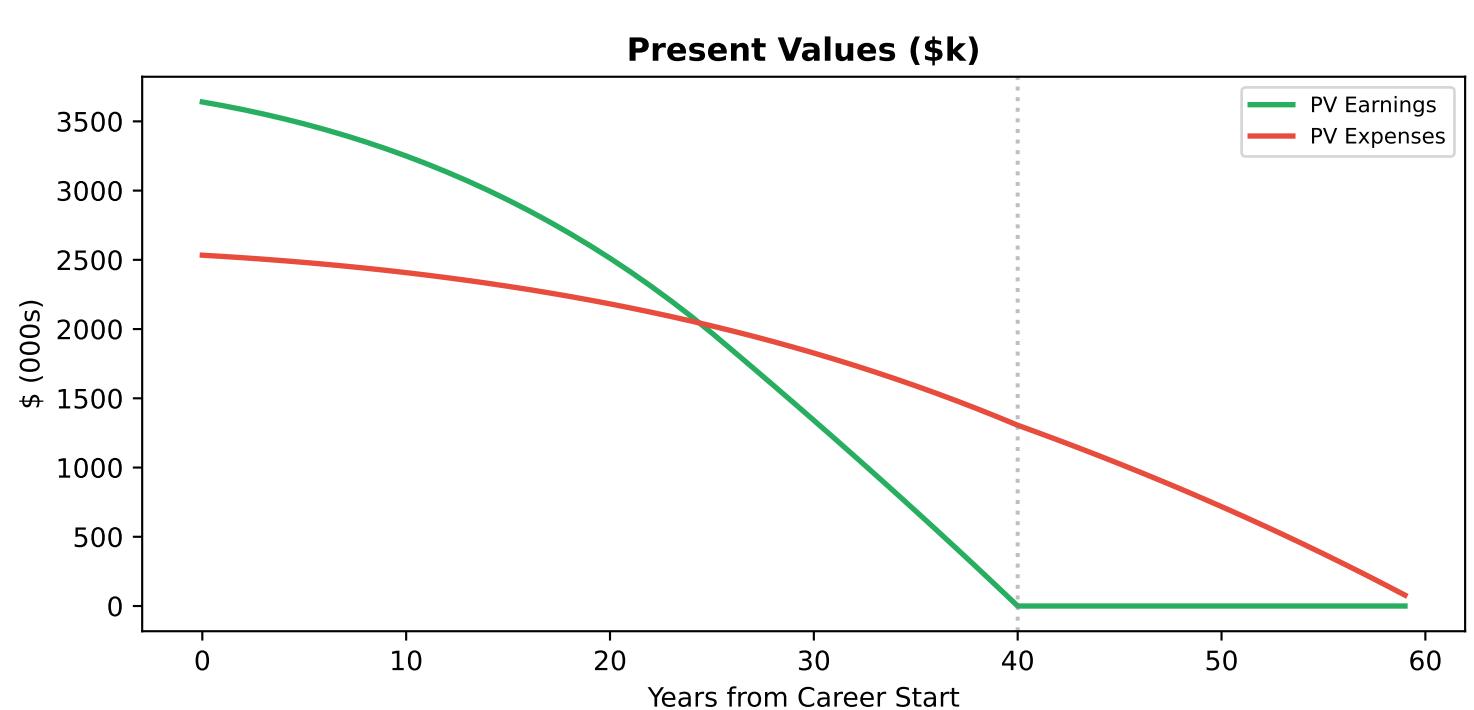
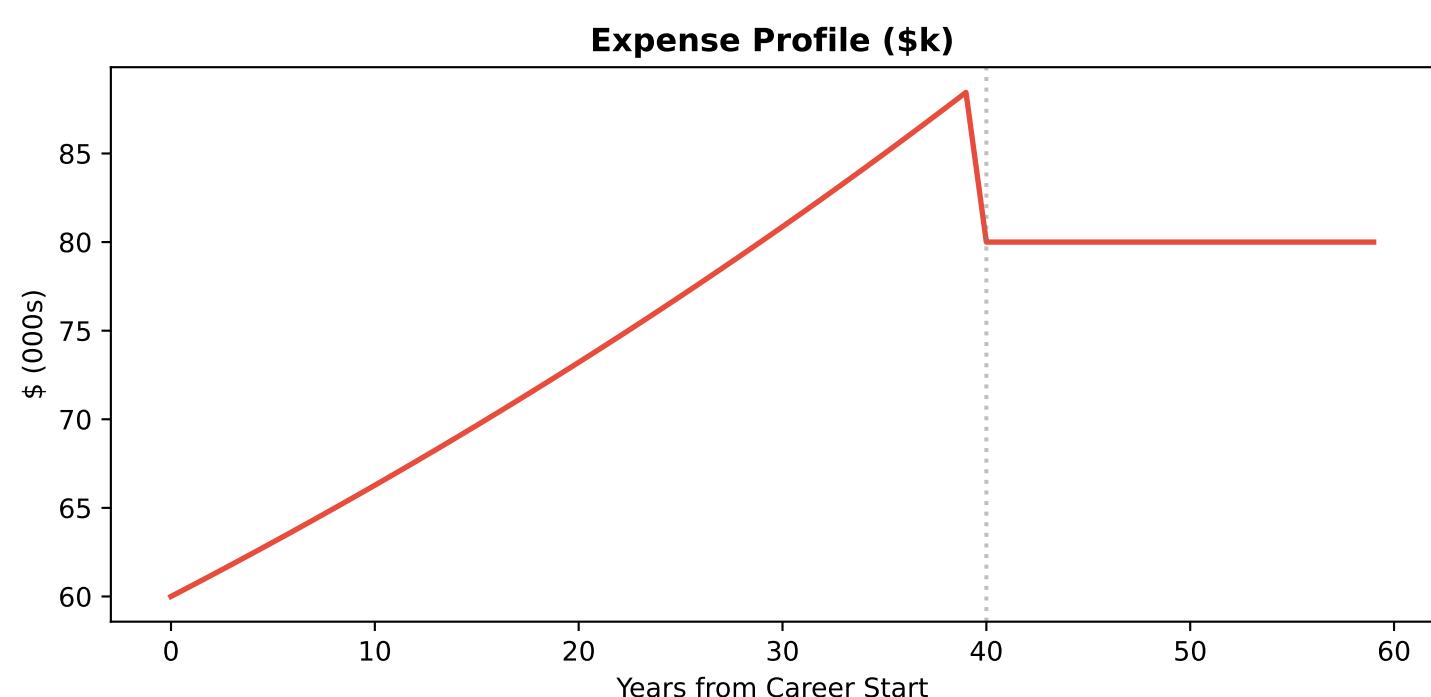
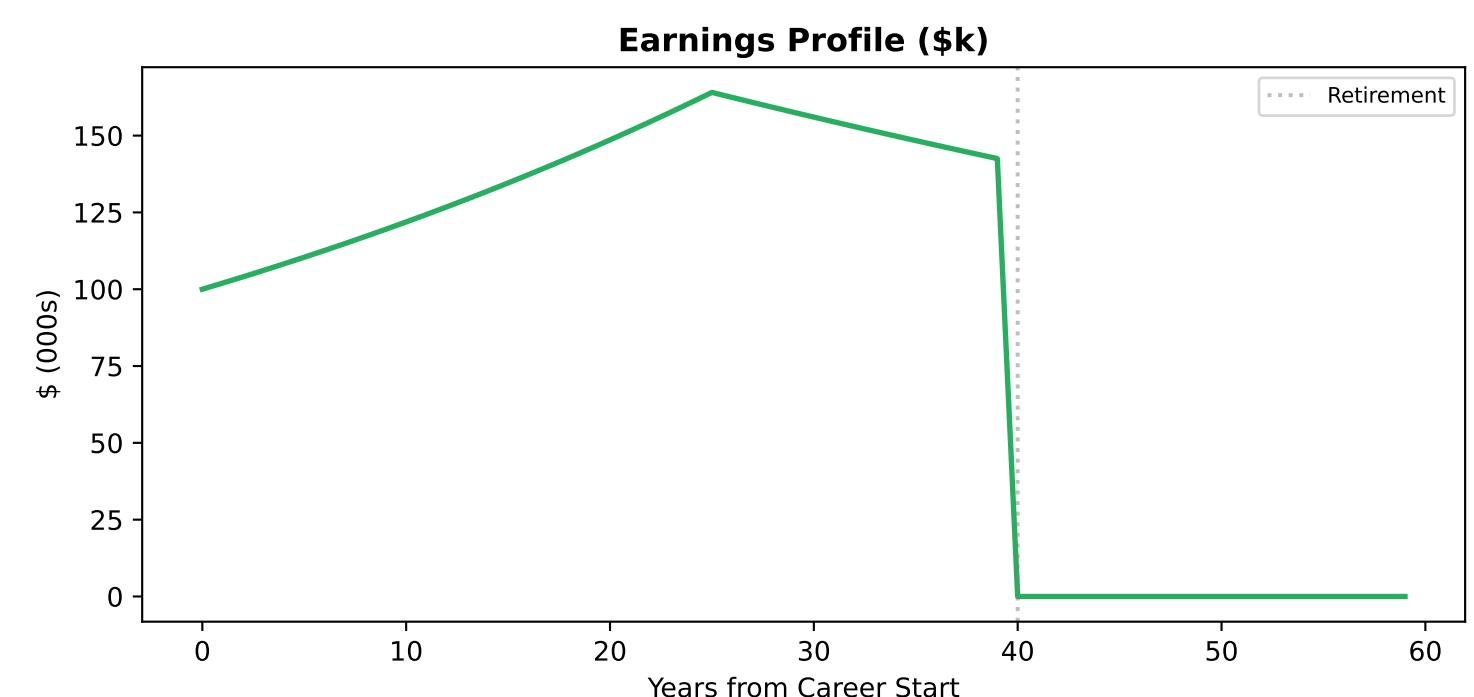
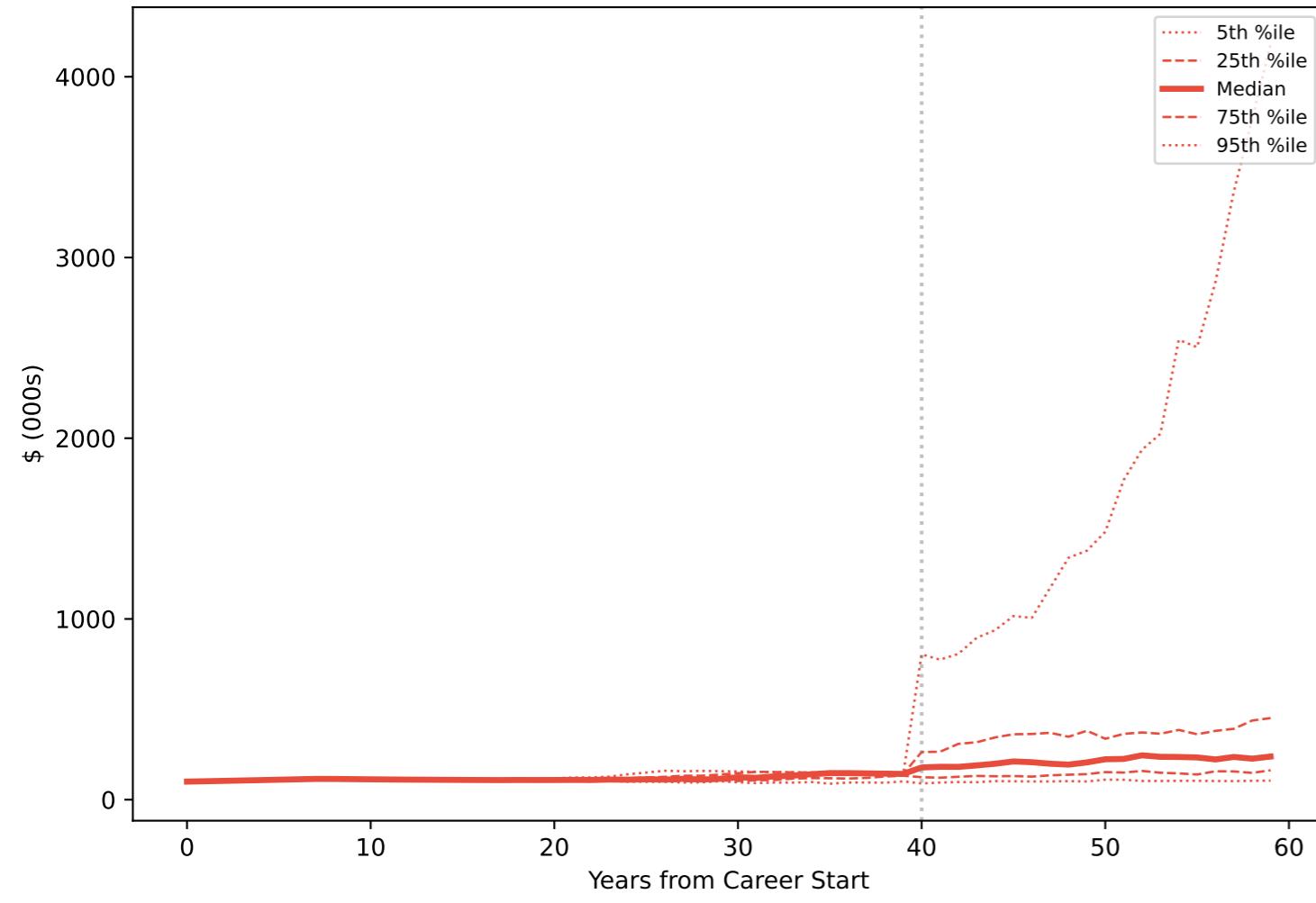


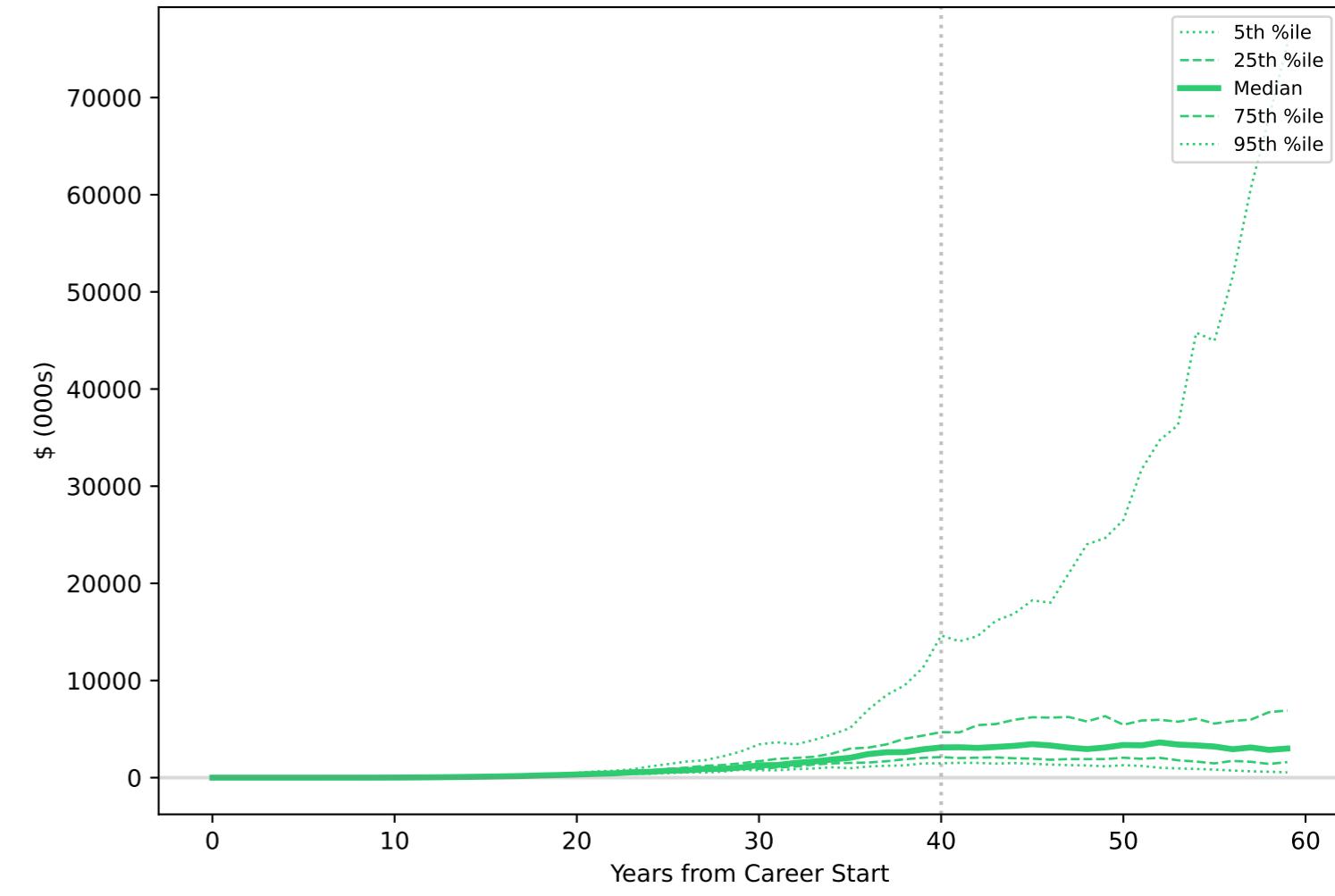
# PAGE 1: BASE CASE (Deterministic Median Path)



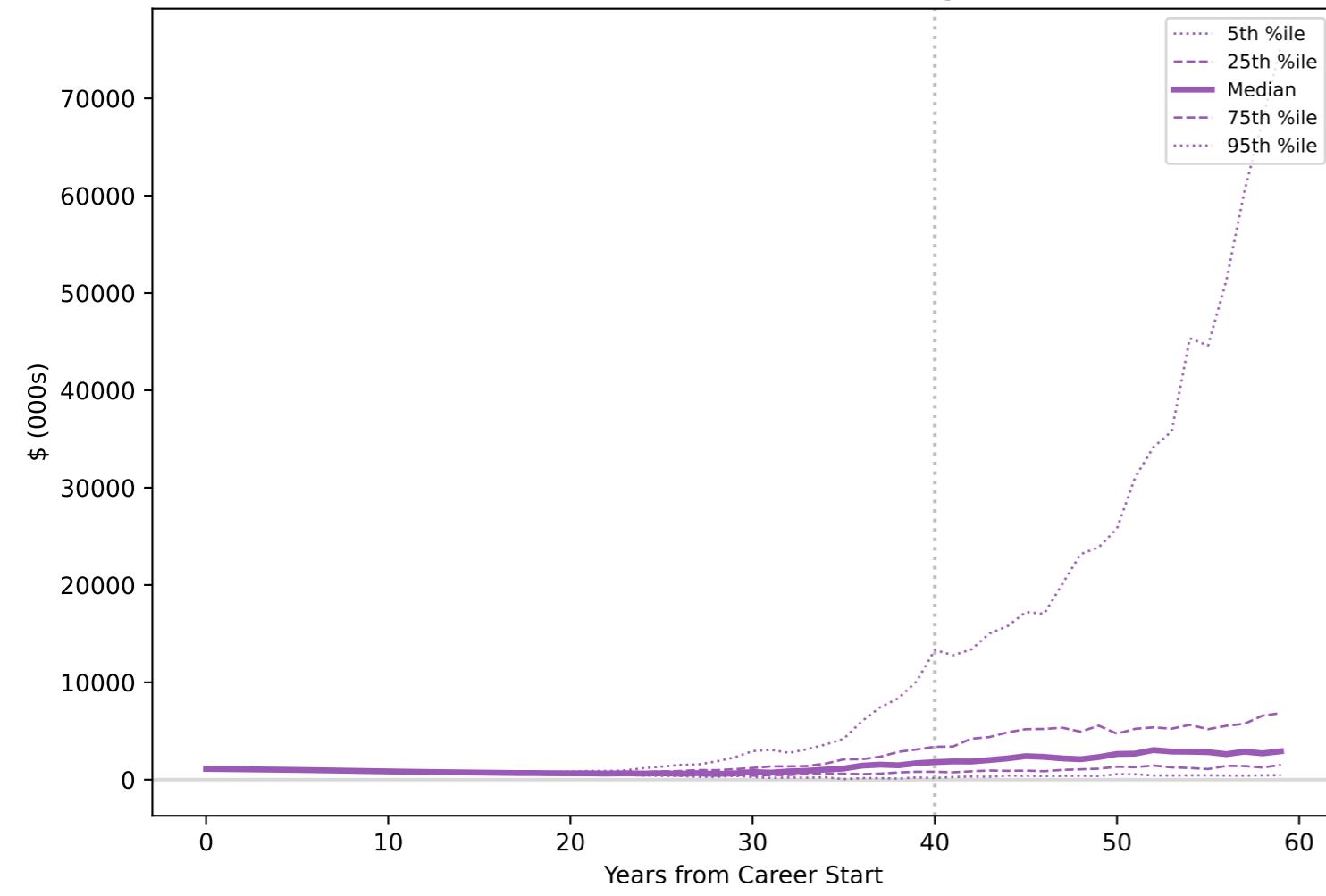
Consumption Distribution (\$k)



Financial Wealth Distribution (\$k)



Net Worth Distribution (HC + FW - Expenses) (\$k)



Terminal Values Grid

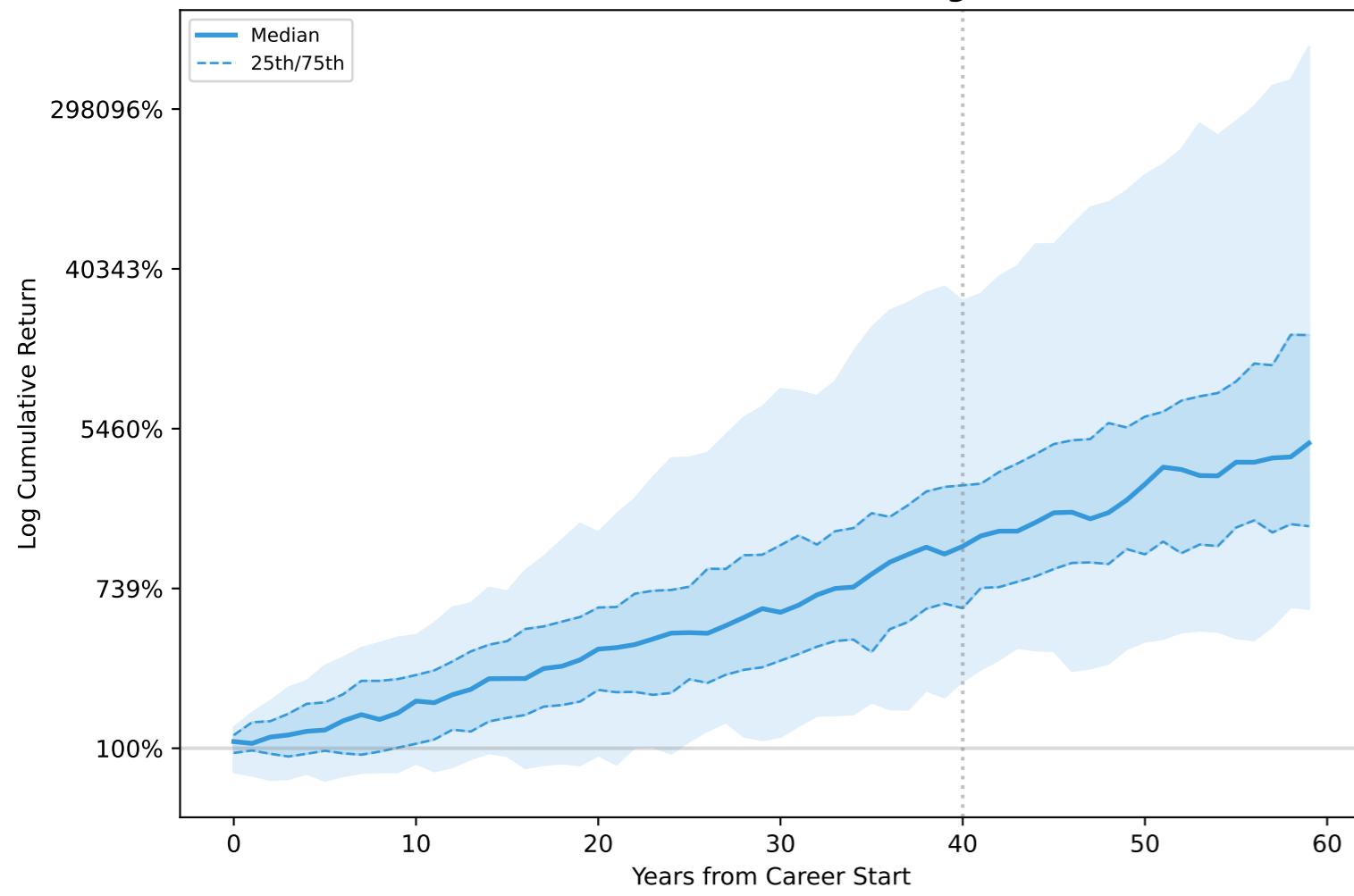
## Terminal Values at Age 84

**Financial Wealth (\$k):**  
 5th percentile: \$ 544  
 25th percentile: \$ 1,601  
 Median: \$ 2,998  
 75th percentile: \$ 6,913  
 95th percentile: \$ 75,529

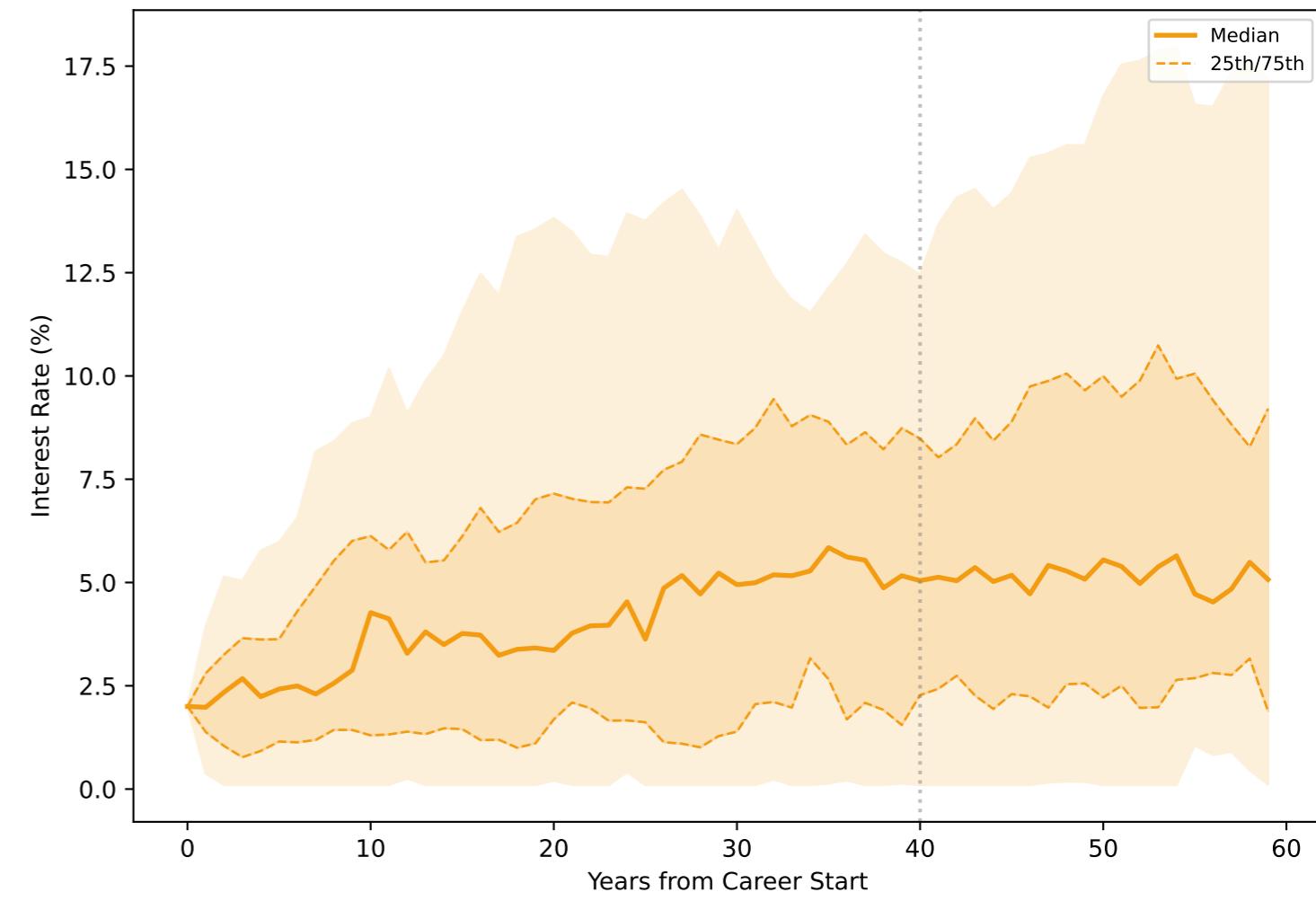
**Annual Consumption (\$k):**  
 5th percentile: \$ 105  
 25th percentile: \$ 163  
 Median: \$ 239  
 75th percentile: \$ 451  
 95th percentile: \$ 4,180

Runs depleted (FW < \$10k): 0 of 50  
 Default Rate: 0.0%

Cumulative Stock Returns (Log Scale)

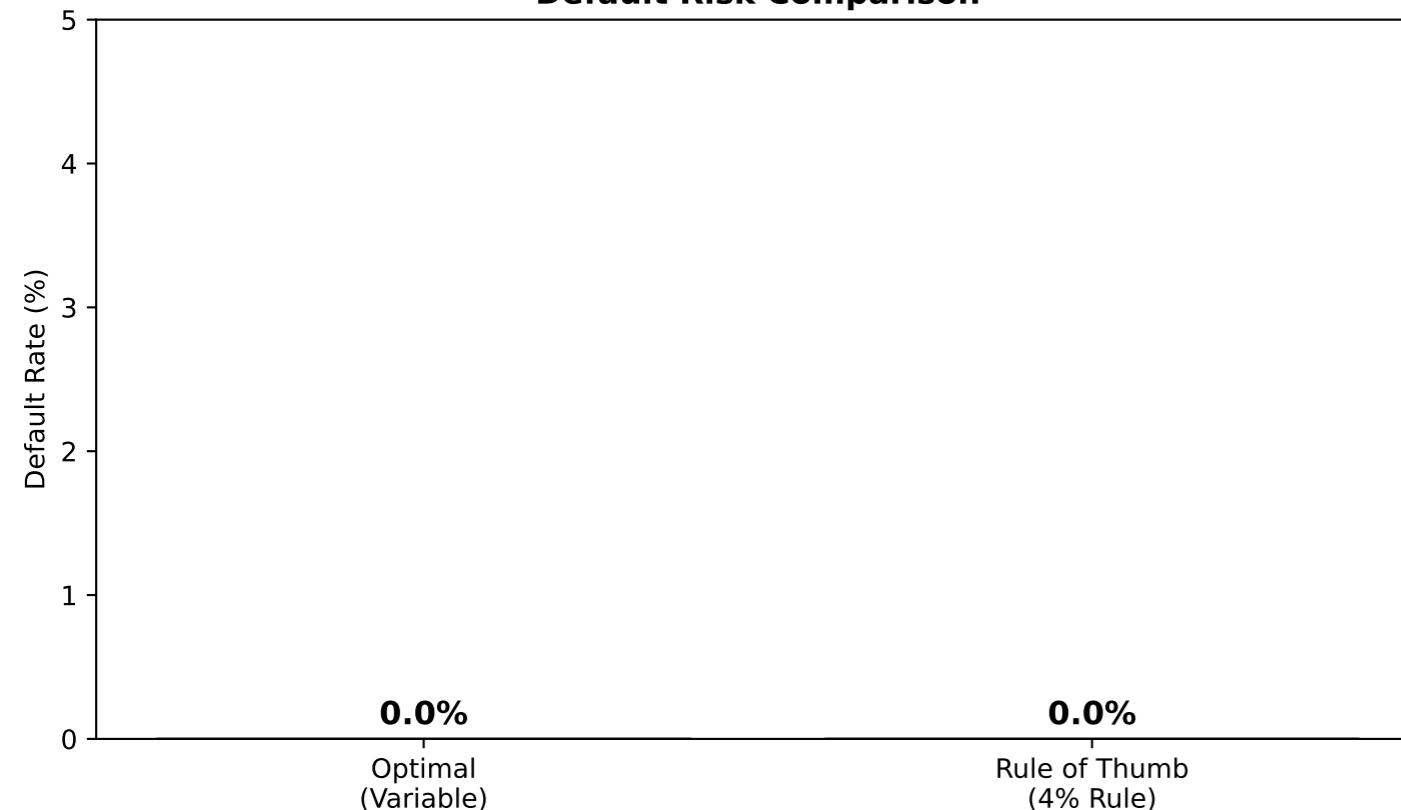


Interest Rate Paths (%)

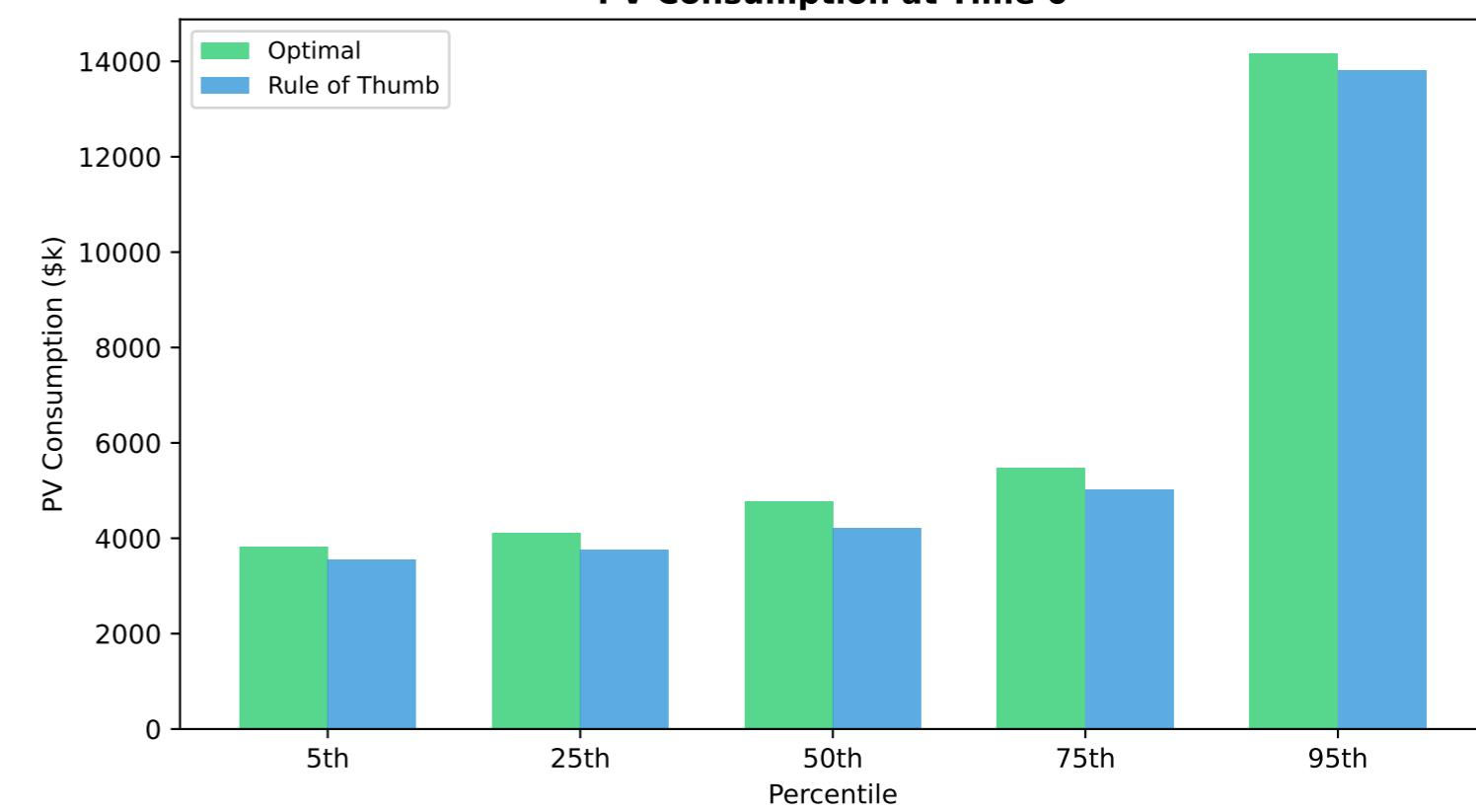


# PAGE 3a: TEACHING SCENARIO - Normal Market Conditions

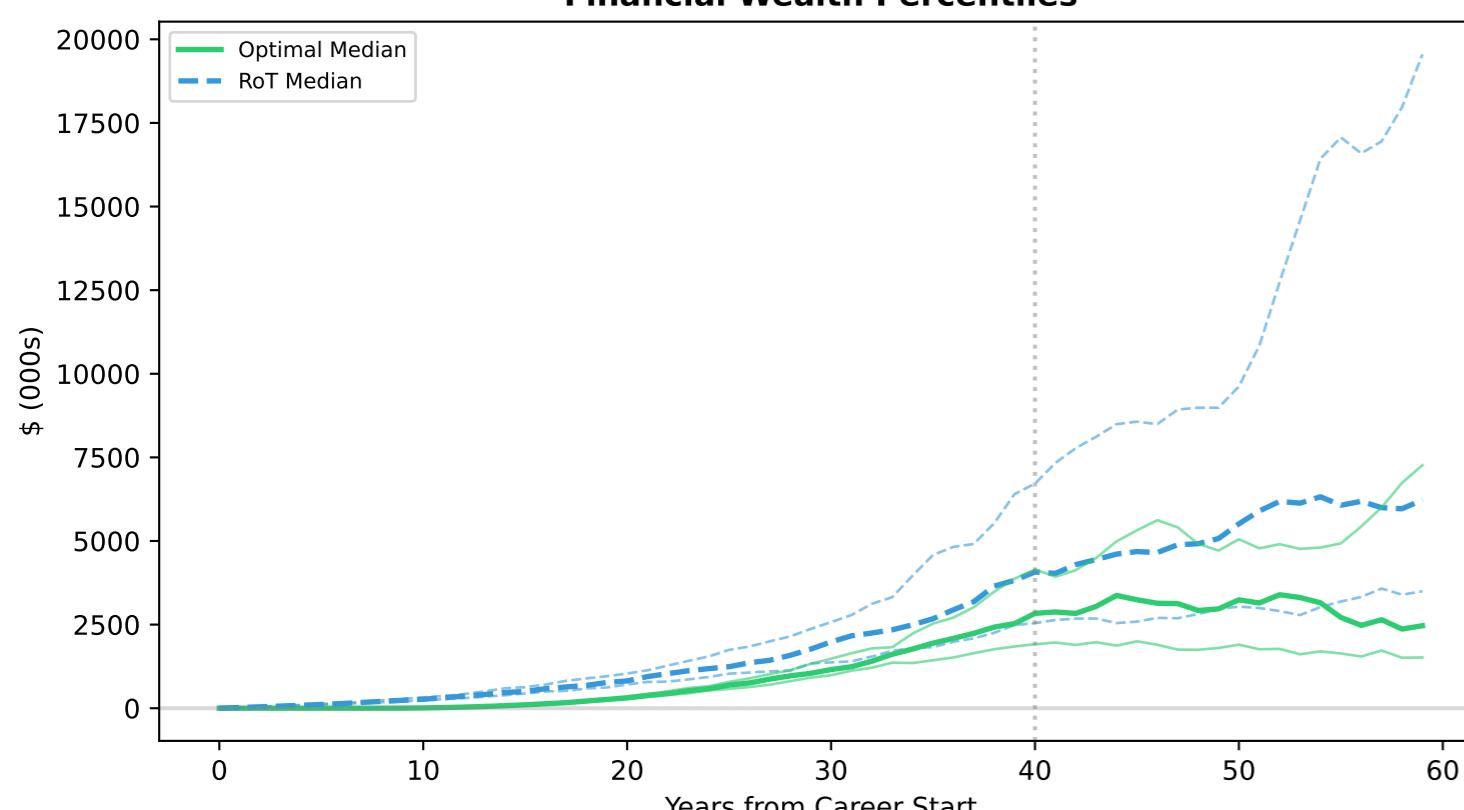
**Default Risk Comparison**



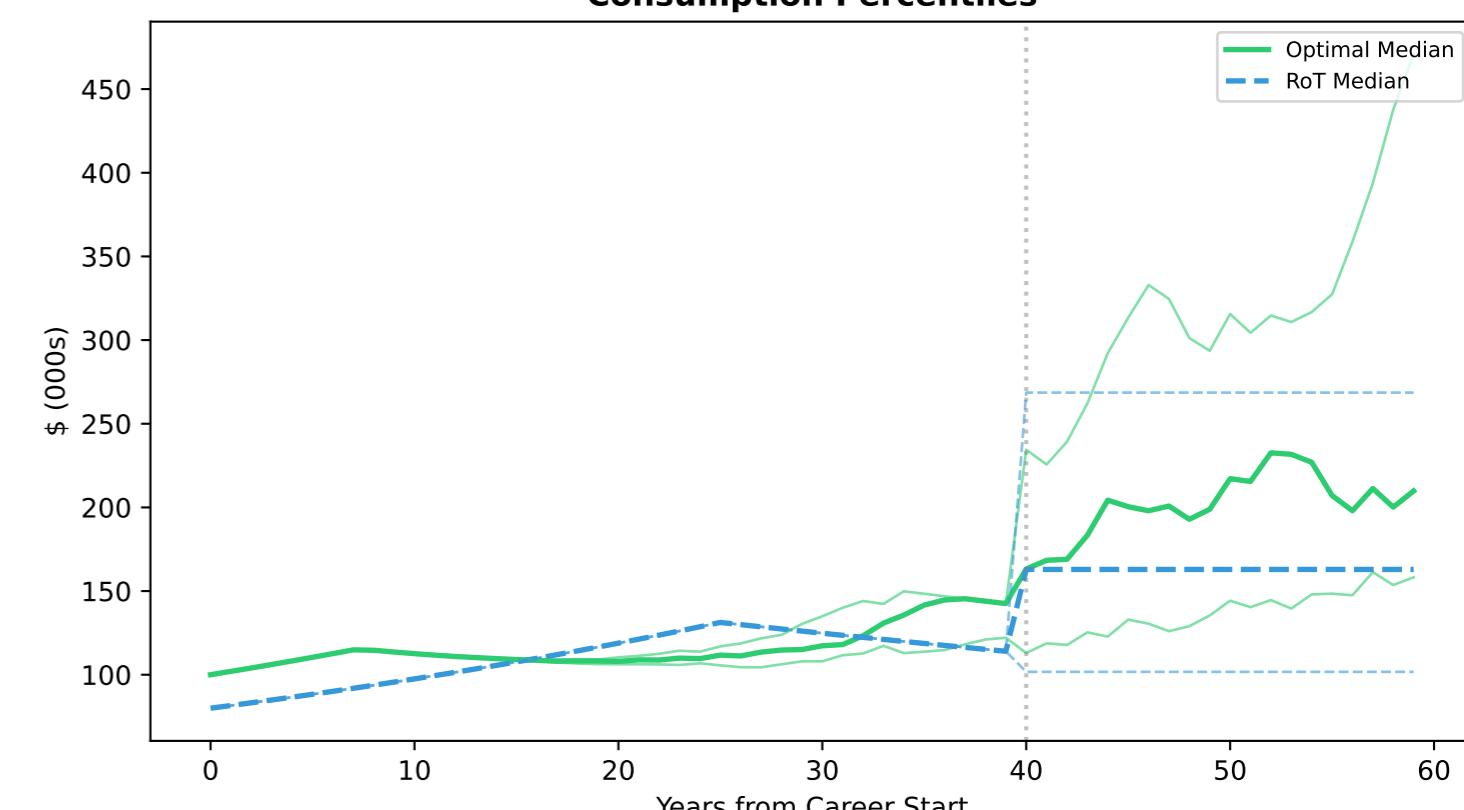
**PV Consumption at Time 0**



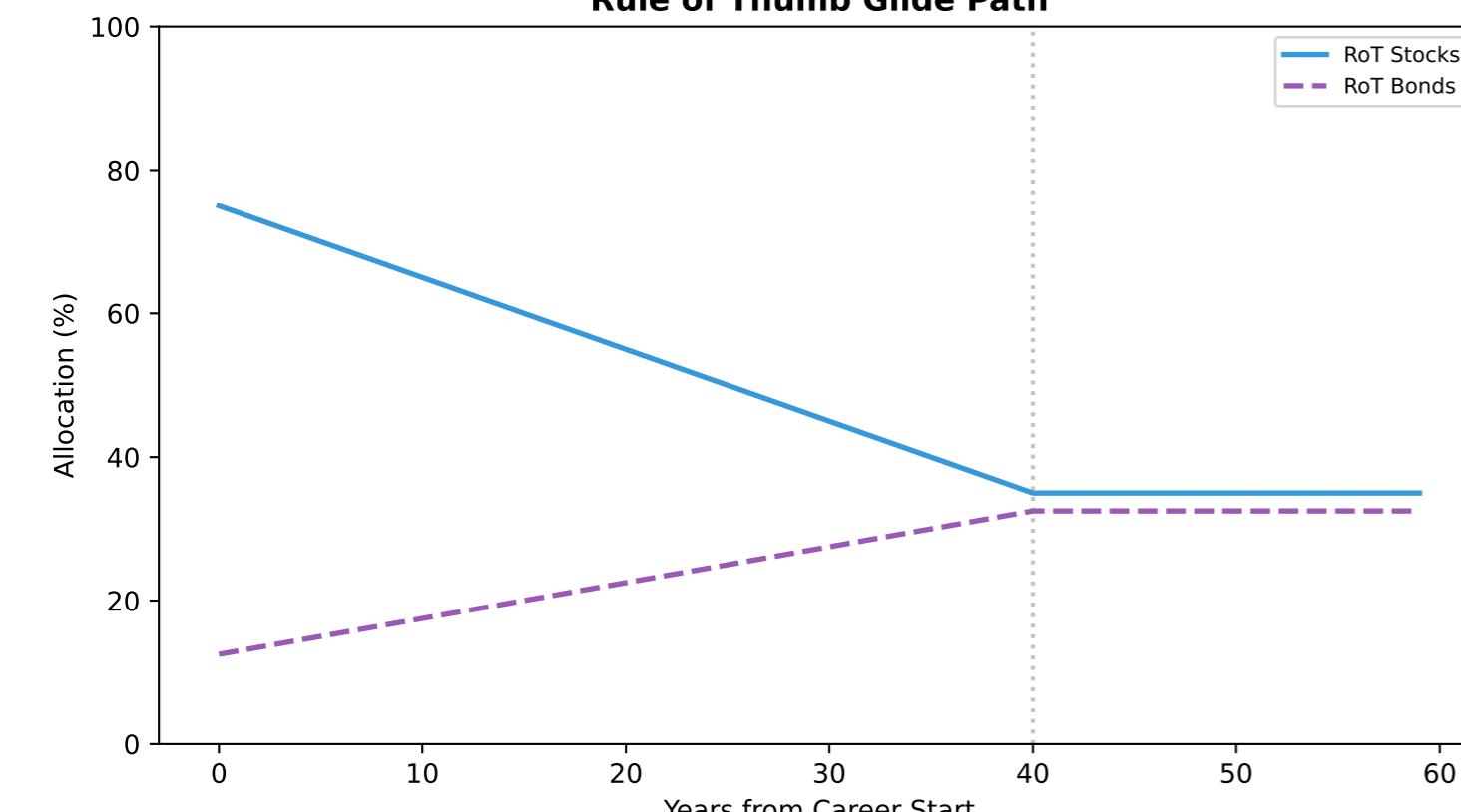
**Financial Wealth Percentiles**



**Consumption Percentiles**



**Rule of Thumb Glide Path**



## Strategy Comparison Summary

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Scenario: Normal Market Conditions

Default Rates:  
Optimal (Variable): 0.0%  
Rule of Thumb (4%): 0.0%

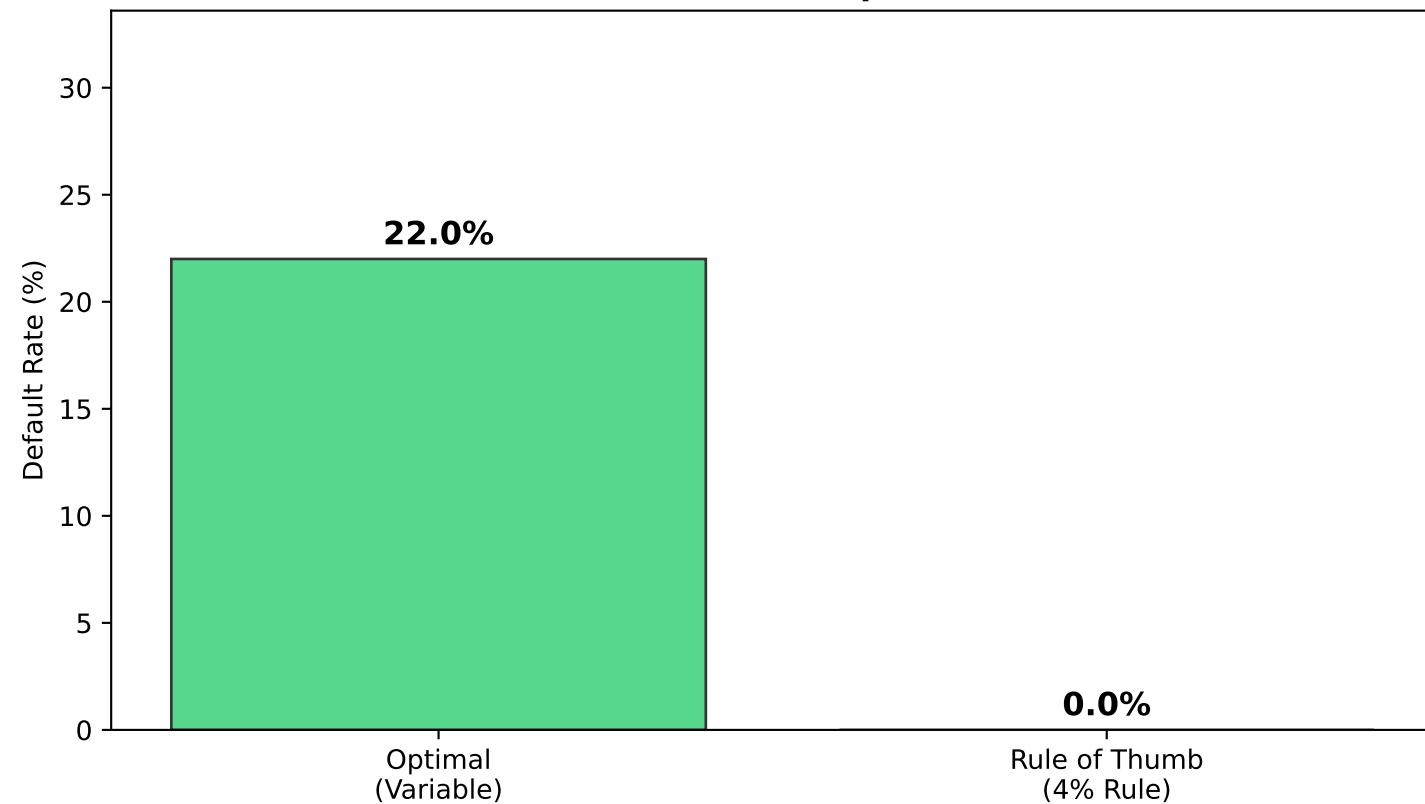
Median Final Wealth (\$k):  
Optimal: \$ 2,467  
Rule of Thumb: \$ 6,232

Median PV Consumption (\$k):  
Optimal: \$ 4,770  
Rule of Thumb: \$ 4,212

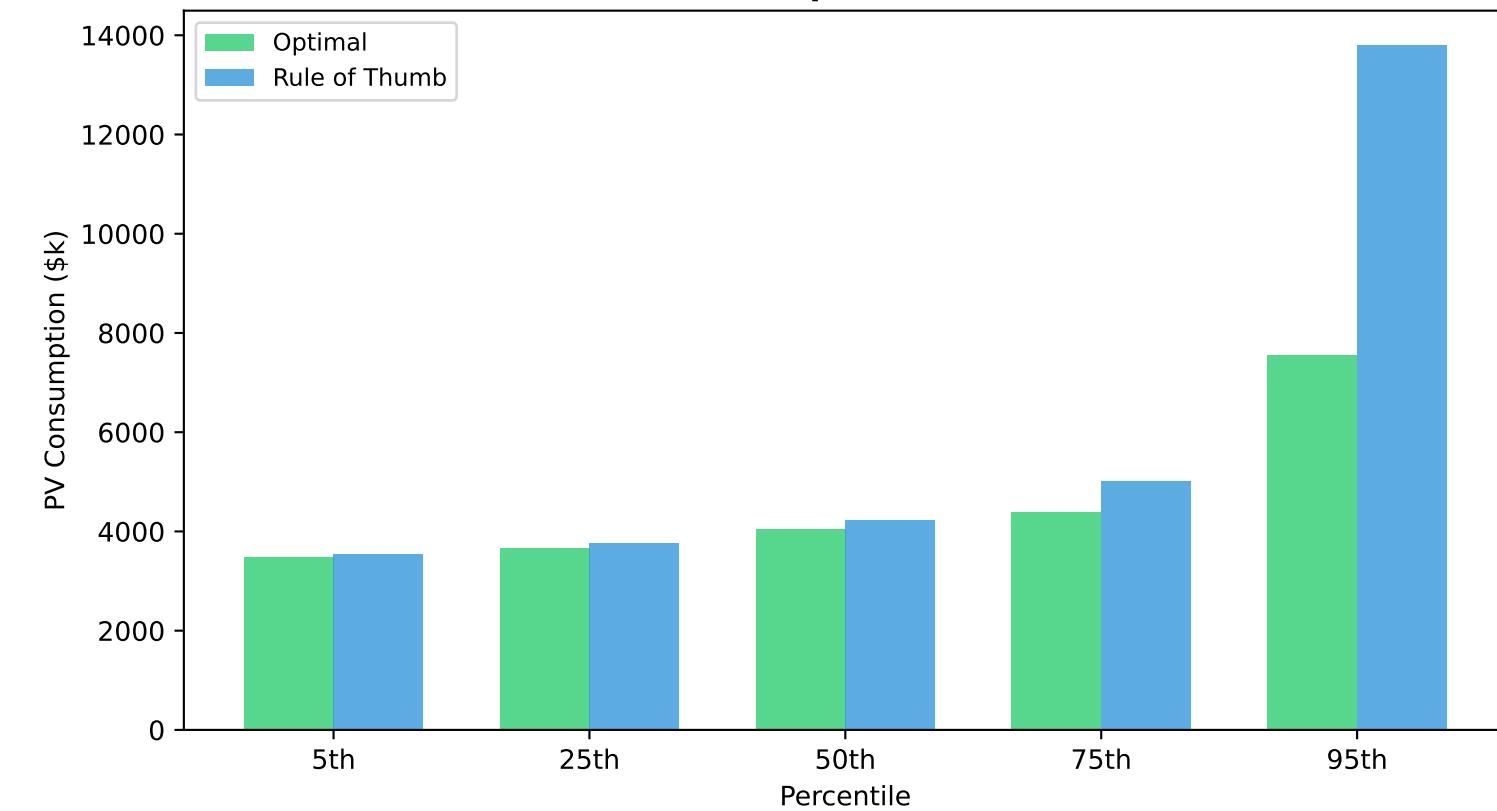
Simulations: 50

## PAGE 3b: TEACHING SCENARIO - Sequence Risk (Bad Early Returns)

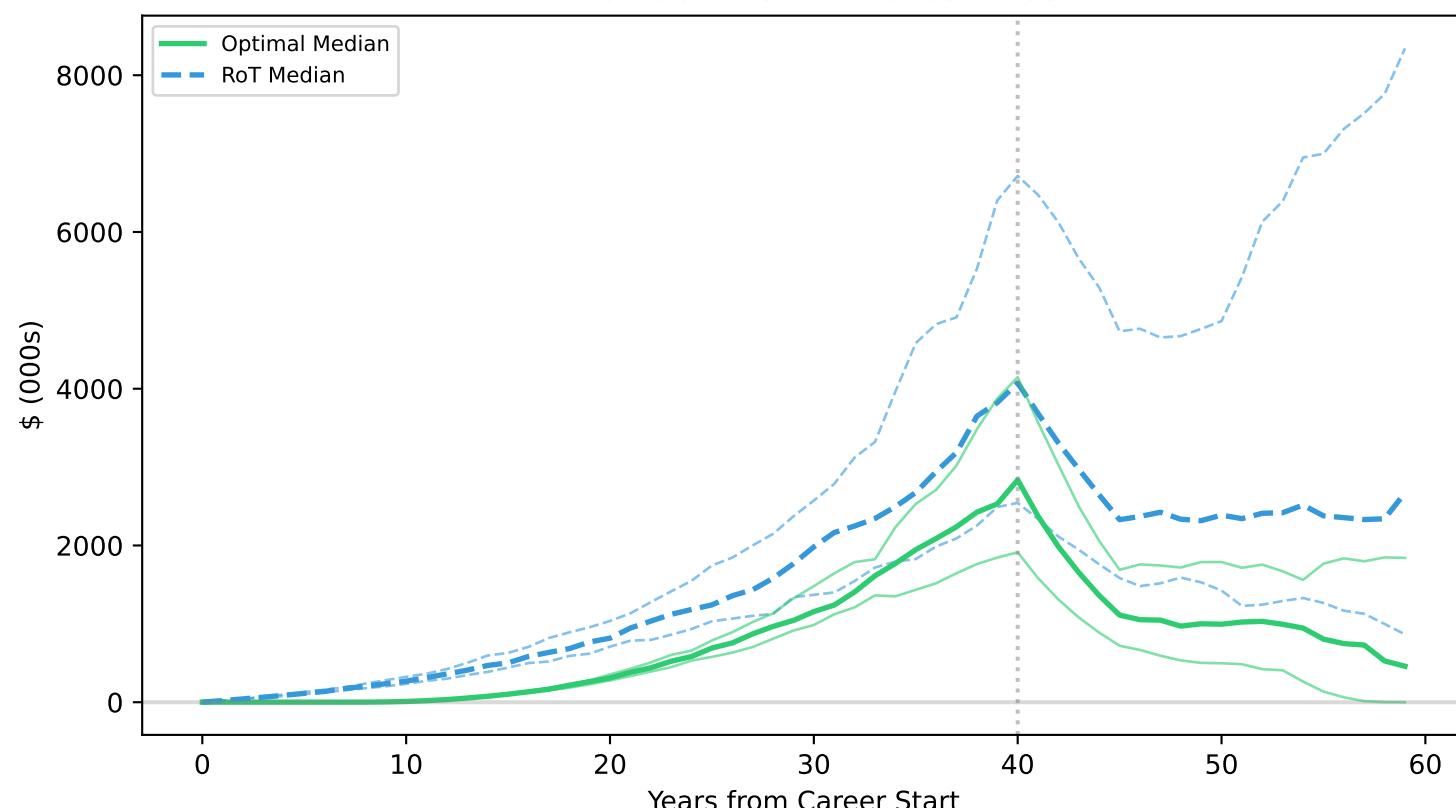
**Default Risk Comparison**



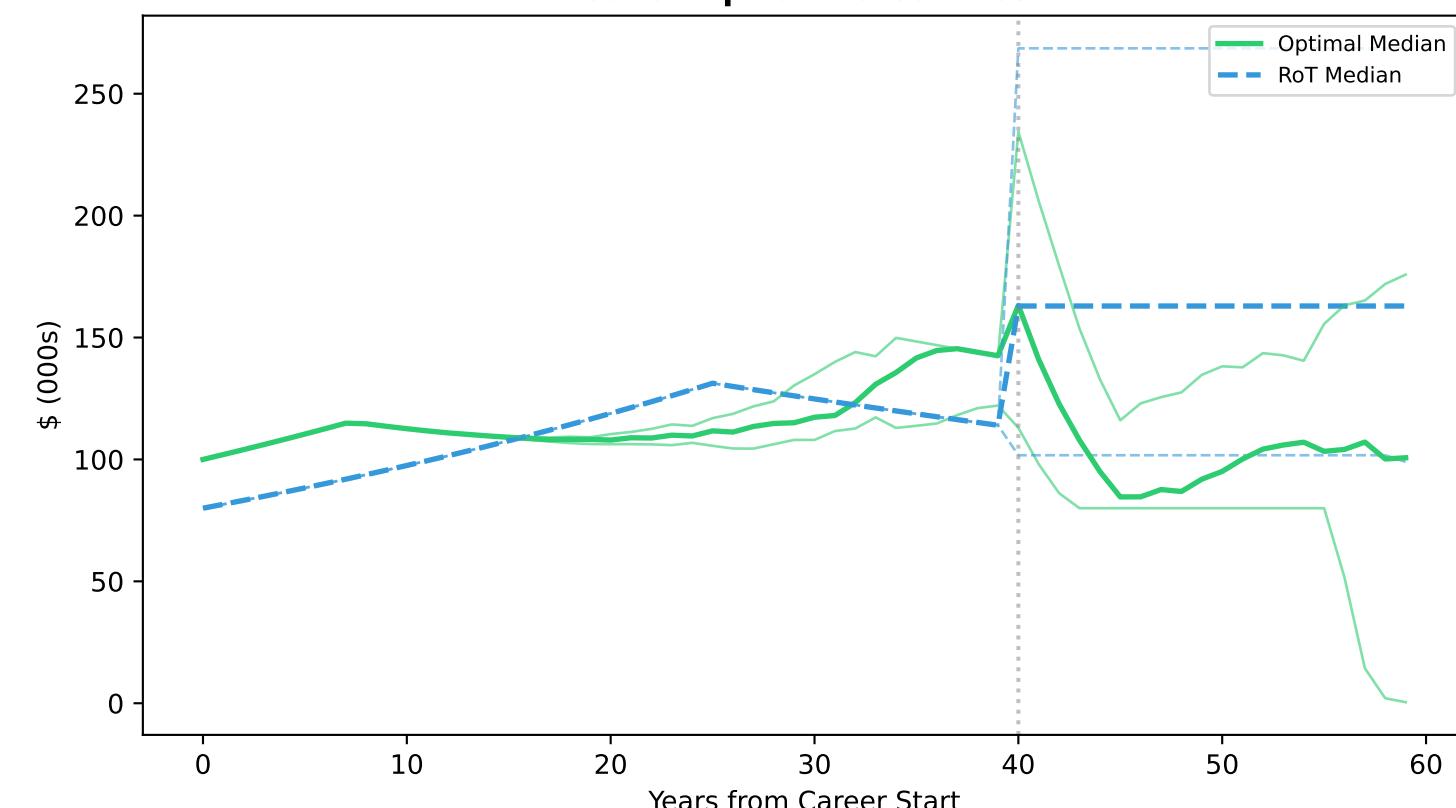
**PV Consumption at Time 0**



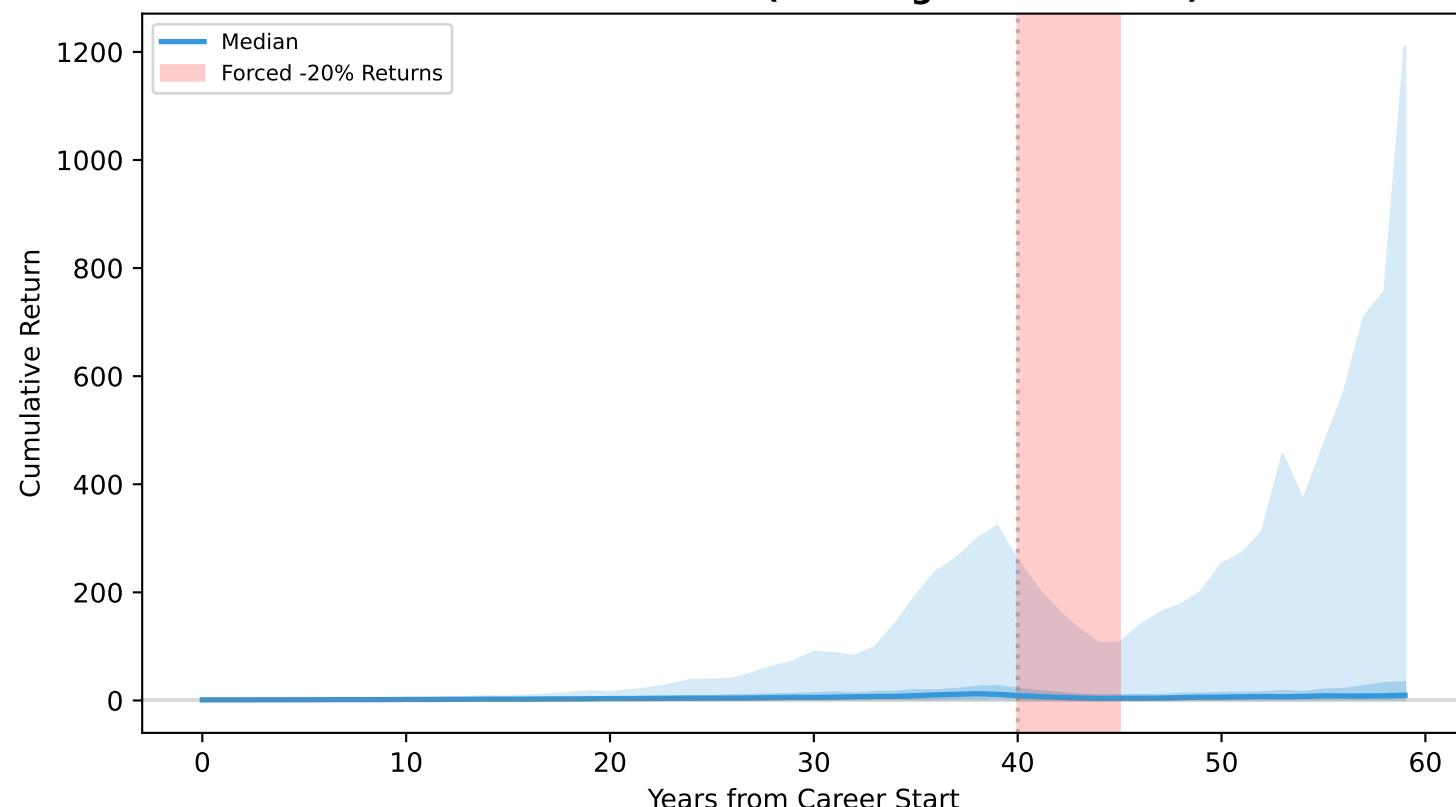
**Financial Wealth Percentiles**



**Consumption Percentiles**



**Stock Return Paths (Showing Stress Period)**



### Strategy Comparison Summary

Scenario: Sequence Risk (Bad Early Returns)

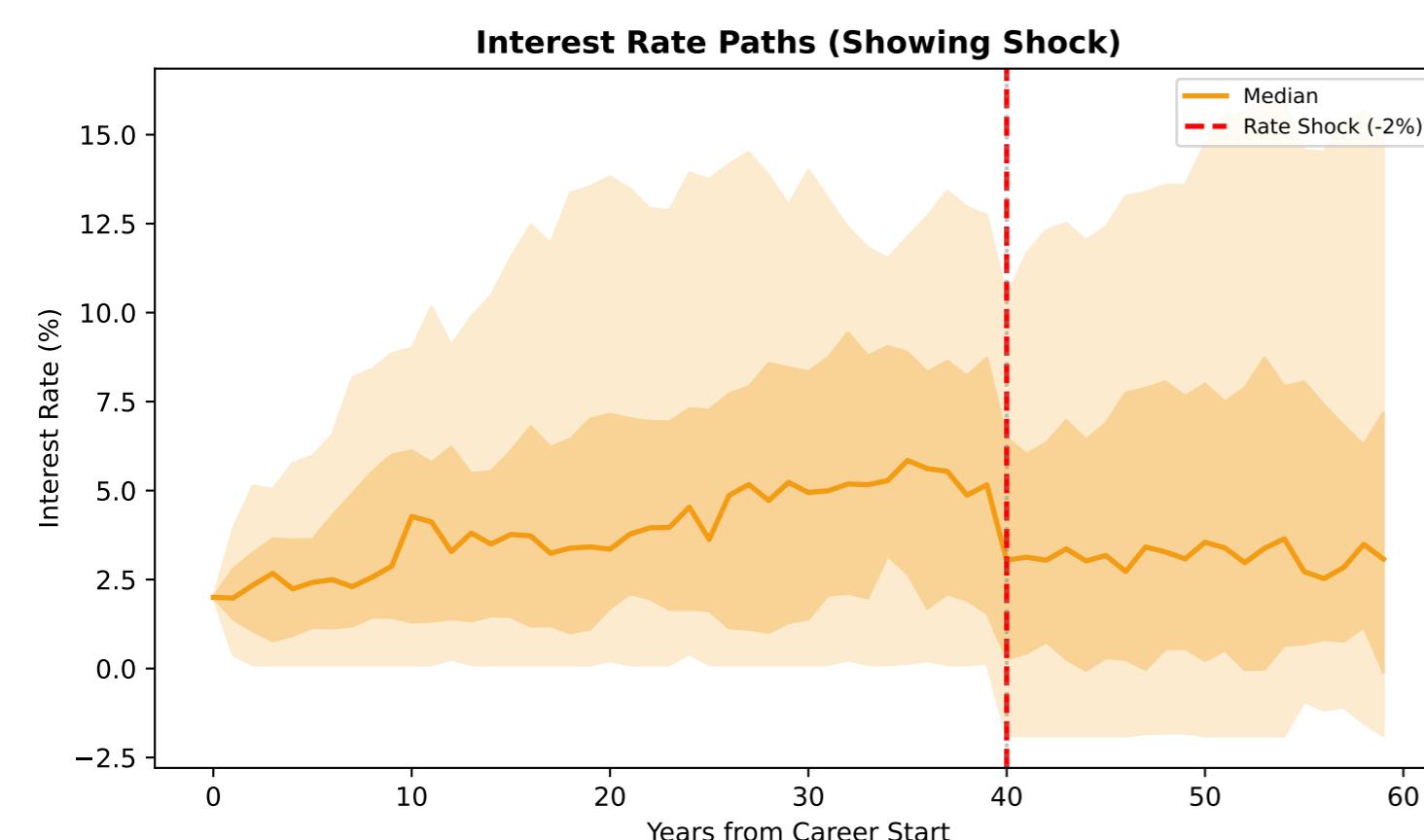
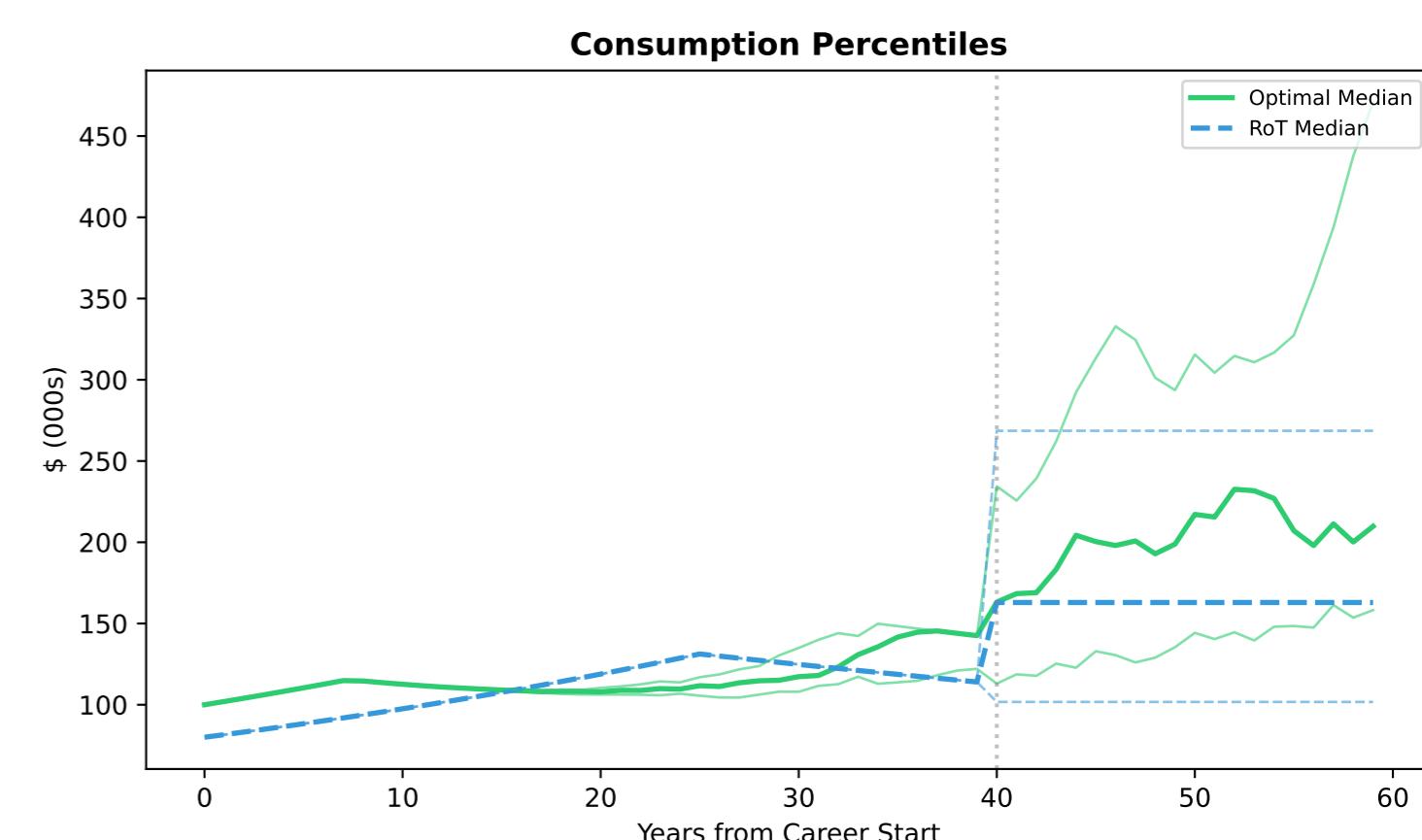
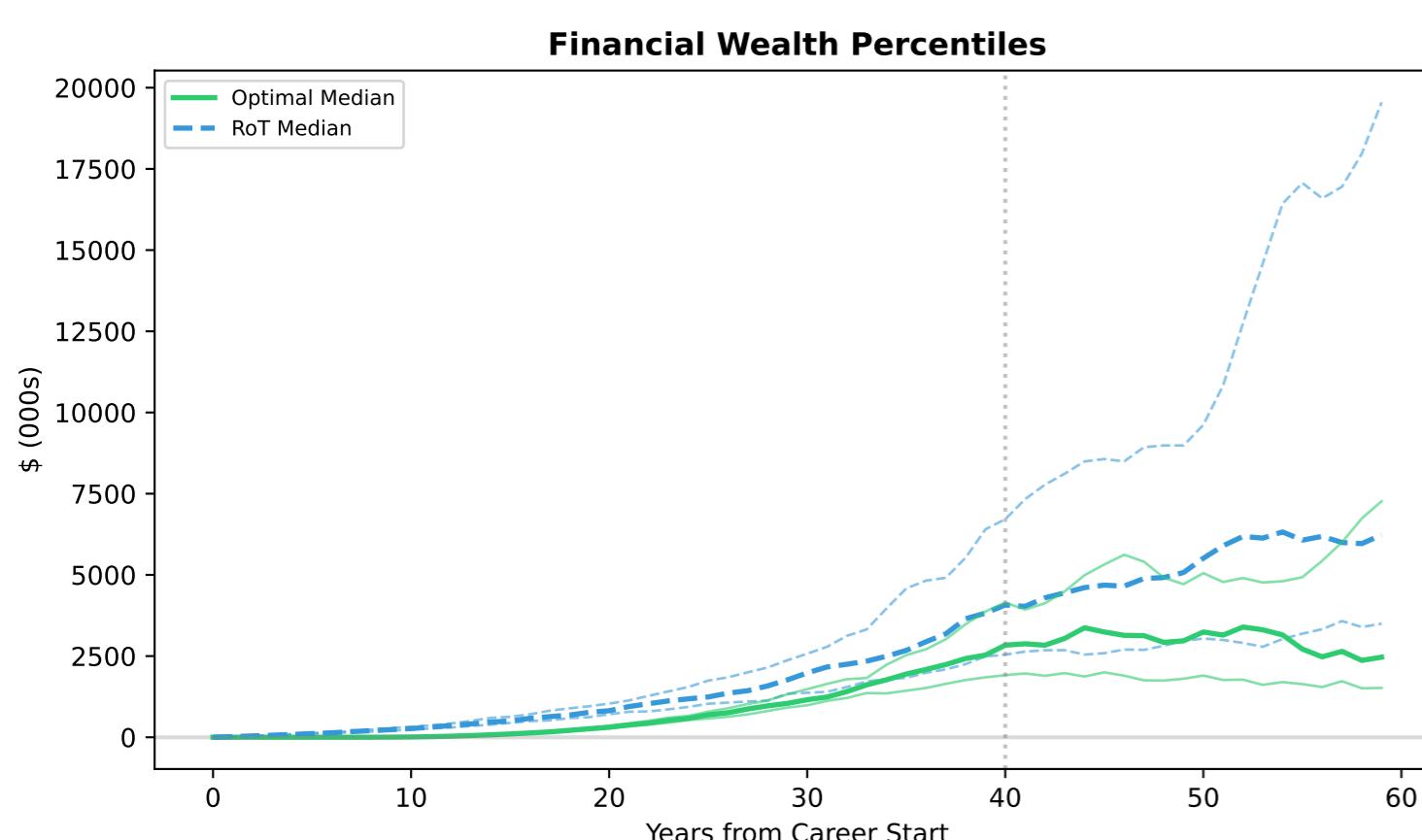
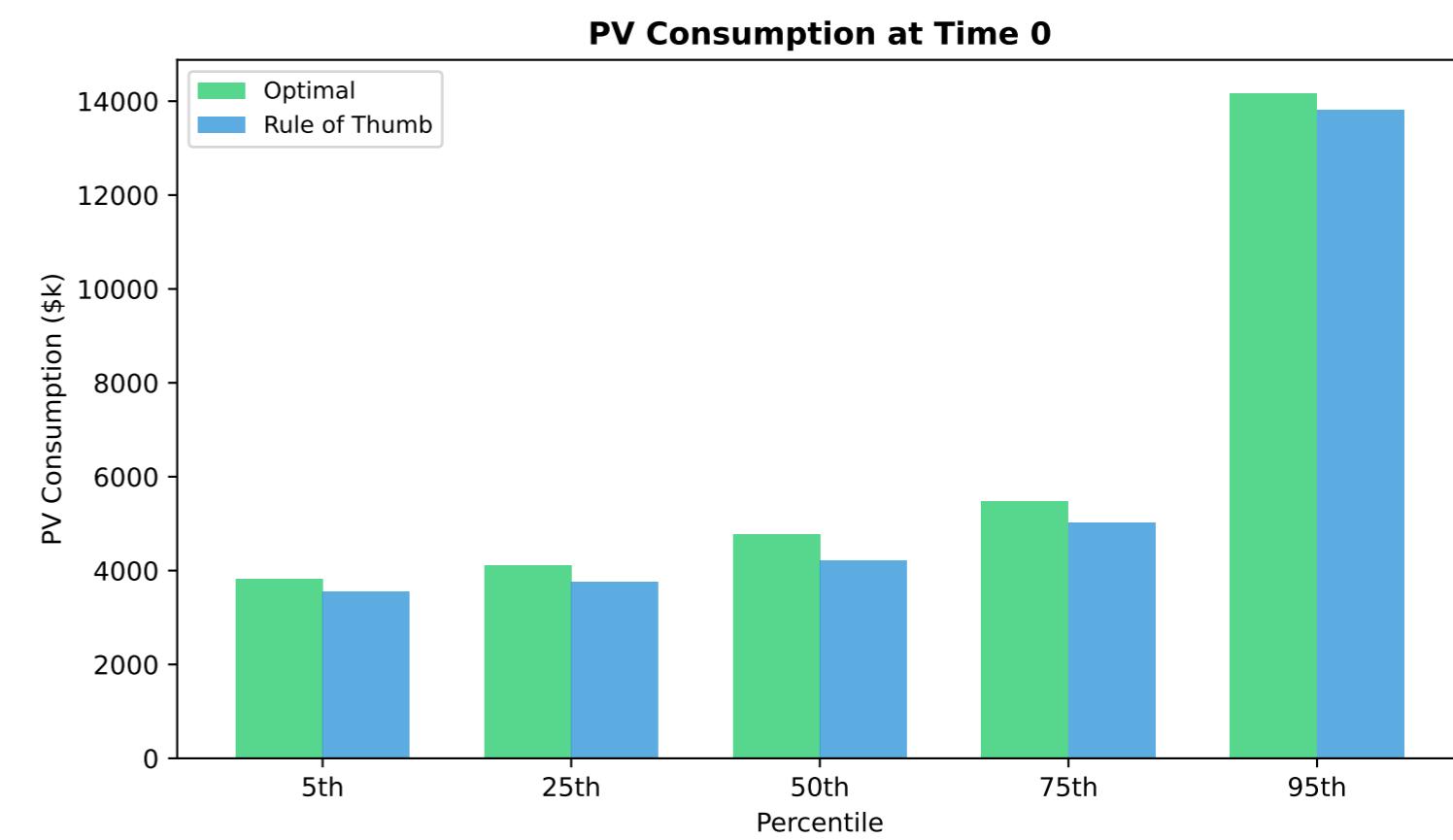
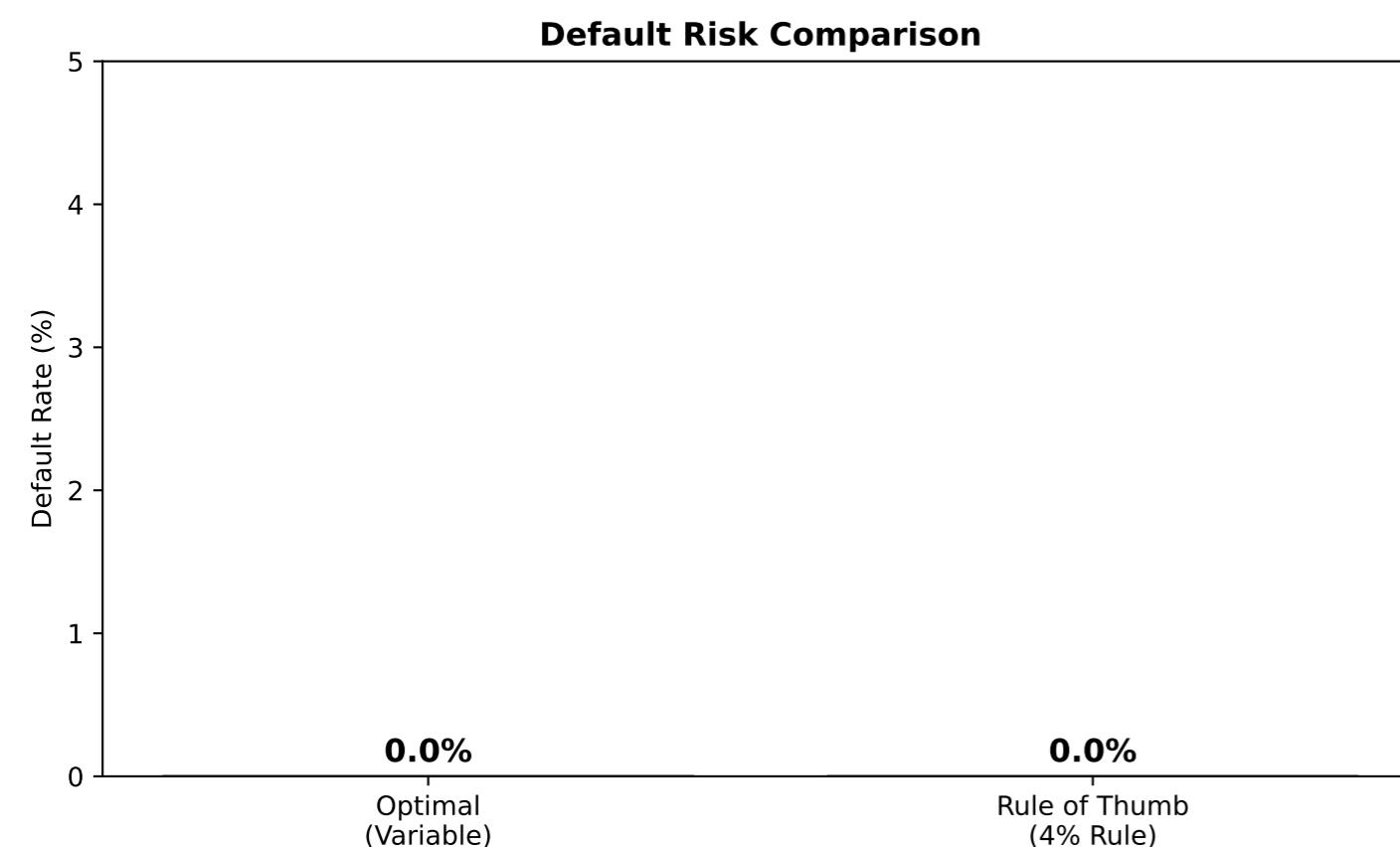
Default Rates:  
Optimal (Variable): 22.0%  
Rule of Thumb (4%): 0.0%

Median Final Wealth (\$k):  
Optimal: \$ 459  
Rule of Thumb: \$ 2,672

Median PV Consumption (\$k):  
Optimal: \$ 4,046  
Rule of Thumb: \$ 4,212

Simulations: 50

# PAGE 3c: TEACHING SCENARIO - Interest Rate Shock (at age 65)



Strategy Comparison Summary		
<hr/>		
Scenario:	Interest Rate Shock (at age 65)	
Default Rates:		
Optimal (Variable):	\$	0.0%
Rule of Thumb (4%):	\$	0.0%
Median Final Wealth (\$k):		
Optimal:	\$	2,467
Rule of Thumb:	\$	6,232
Median PV Consumption (\$k):		
Optimal:	\$	4,770
Rule of Thumb:	\$	4,212
Simulations:	50	

## Lifecycle Investment Strategy Parameters

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### Age Parameters:

- Career Start: 25
- Retirement Age: 65
- Planning Horizon: 85

### Income Parameters:

- Initial Earnings: \$100k
- Earnings Growth: 2.0%
- Peak Earnings Age: 50

### Subsistence Expense Parameters:

- Base Expenses: \$60k
- Retirement Expenses: \$80k

### Initial Wealth:

- Starting Financial Wealth: \$1k

### Consumption Model:

- Total Consumption = Subsistence + Rate x Net Worth
- Net Worth = Human Capital + Financial Wealth - PV(Future Expenses)
- Consumption Rate = Median Return + 1.0pp

### Human Capital Allocation:

- Stock Beta: 0.10
- Bond Duration: 7.0 years (used for HC decomposition and MV optimization)

### Mean-Variance Optimization (Full VCV):

- Risk-Free Rate ( $r_{\bar{r}}$ ): 2.0%
- Stock Excess Return ( $\mu_s$ ): 4.0%
- Bond Excess Return ( $\mu_b$ ): 0.50%
- Stock Volatility ( $\sigma_s$ ): 18%
- Rate Shock Volatility ( $\sigma_r$ ): 1.2%
- Rate/Stock Correlation ( $\rho$ ): -0.20
- Risk Aversion ( $\gamma$ ): 2.0
- Allocation Source: Mean-Variance Optimization (Full VCV)
- $w^* = (1/\gamma) * \Sigma^{-1} * \mu$  (Full VCV Merton solution)

### VCV-Based Asset Return Models:

- Stock:  $R_s = r + \mu_s + \sigma_s * \epsilon_s$
- Bond:  $R_b = r + \mu_b - D * \sigma_r * \epsilon_r$
- Bond Vol:  $D * \sigma_r = 8.4\%$
- Cov( $R_s, R_b$ ):  $-D * \sigma_s * \sigma_r * \rho = 0.302\%$

### Target Total Wealth Allocation (from MV):

- Stocks: 60.9%
- Bonds: 9.3%
- Cash: 29.8%

### Key Insights:

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1. Portfolio allocation is derived from full Merton solution:  $w^* = (1/\gamma) * \Sigma^{-1} * \mu$
2. The VCV matrix accounts for bond return volatility from duration and rate shock correlation with stocks.
3. Changing  $\gamma$ ,  $\mu$ ,  $\sigma$ ,  $\rho$ , or duration allows studying how portfolios respond to assumptions.
4. Human capital is treated as implicit asset holdings, and financial portfolio adjusts to reach total targets.