



Puzzle requirements

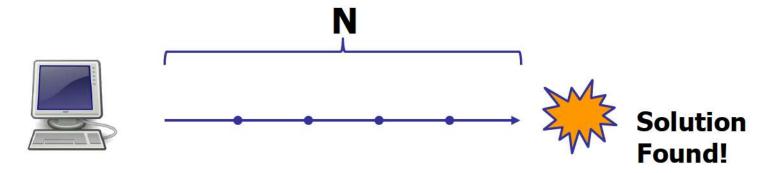
- Cheap to Verify
- Adjustable difficulty

. . .

- Chance of winning is proportional to hashpower
 - Large players get only proportional advantage
 - Even small players get proportional compensation

Bad puzzle: a sequential puzzle

Consider a puzzle that takes N steps to solve a "Sequential" Proof of Work





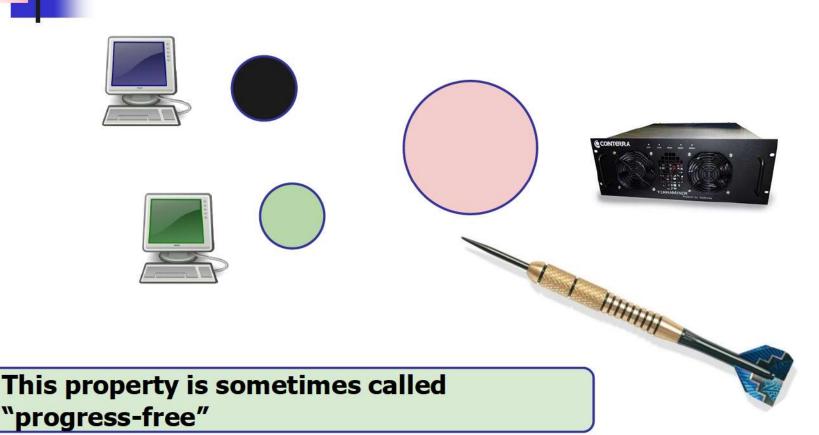
Bad puzzle: a sequential puzzle

Problem: fastest miner **always** wins the race!





Good puzzle → Weighted sample



ASIC resistance - Why? (1 of 2)

Goal: Ordinary people with idle laptops, PCs, or even mobile phones can mine!

Lower barrier to entry

Approach: reduce the gap between custom hardware and general purpose equipment



ASIC resistance - Why? (2 of 2)

Goal: Prevent large manufacturers from

dominating the game

"Burn-in" advantage In-house designs

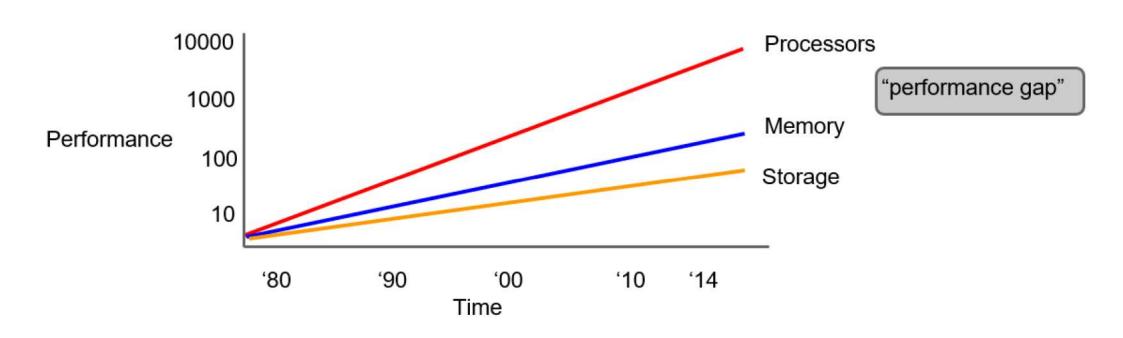


Approach: reduce the "gap" between future hardware and the custom ASICs we already have



Memory hard puzzles

Premise: the cost and performance of memory is more stable than for processors





Colin Percival, 2009

Memory hard hash function

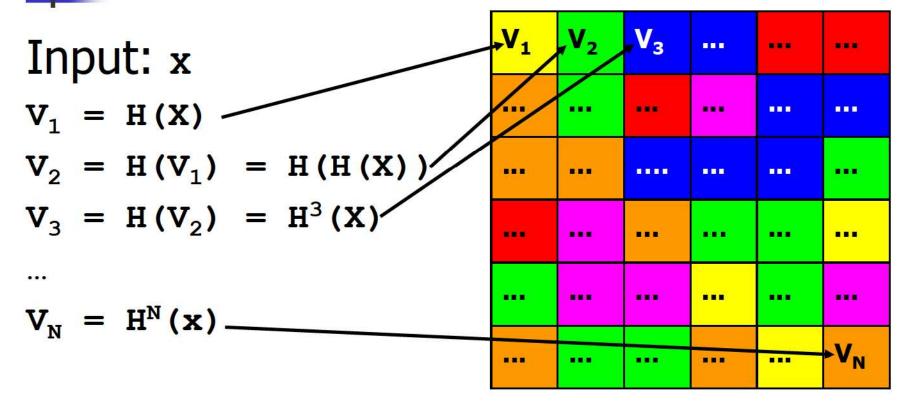
Constant time/memory tradeoff

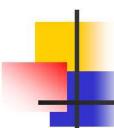
- Most widely used alternative Bitcoin puzzle
- Also used elsewhere in security (PW-hashing)

- 1. Fill memory with random values
- 2. Read from the memory in random order



scrypt - step 1 of 2 (write)





scrypt - step 2 of 2 (read)

Input: X

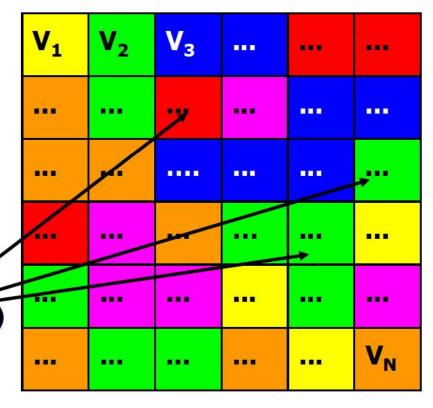
$$A := H^{N+1}(X)$$

For N iterations:

 $i := A \mod N$

 $A := H(A \times \nabla_i)$

Output: A





scrypt - time/memory tradeoff

Why is this memory-hard? Reduce memory by half, 1.5x the # steps

V ₁	V ₃		V ₅		
•••	***		•••		Need to access V _i where <i>i</i> is even?
•••	••••		•••		
***	V _{i-1}	V_{i}			Access V _{i-1}
					Compute $V_i = H(V_{i-1})$
•••					



Disadvantages:

Also requires N steps, N memory to check

Is it actually ASIC resistant? scrypt ASICs are already available

Future: PW-hashing research



http://zeusminer.com/



Cuckoo hash cycles

John Tromp, 2014

Memory hard puzzle that's cheap to verify

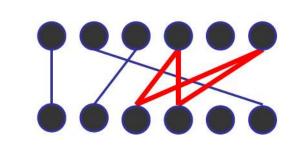
Input: X

For i = 1 to E:

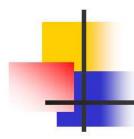
$$a := H_0(X + i)$$

$$b := i + H_1(X + i)$$

edge (a mod N, b mod N)



Is there a cycle of size K? If so, Output: X, K edges



Even more approaches

More complicated hash functions
X11: 11 different hash functions combined

Moving target
Change the puzzle periodically



Recovering wasted work

Recall:

between 150 MW - 900 MW power (as of mid-2014)

Natural question:

Can we recycle this and do something useful?





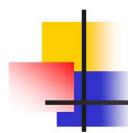
Sunny King, 2013

Puzzle based on finding large prime numbers

Cunningham chain:

```
p_1, p_2, ... p_n where p_i = 2 p_{i-1} + 1
Each p_i is a large (probable) prime
```

For instance: p₁ is divisible by H(prev || mrkl_root || nonce)



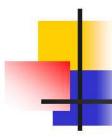
Primecoin



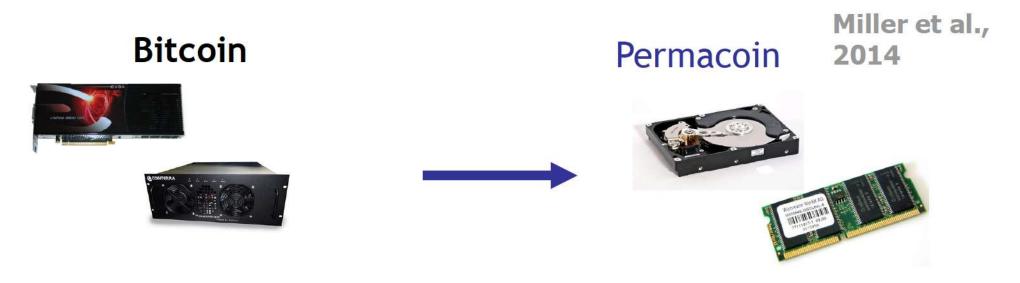
Many of the largest known Cunningham chains have come from Primecoin miners

Hard problem? Studied by others (e.g., PrimeGrid)

Usefulness? Maybe - at least one known use



Permacoin - Mining with storage



Side effect:

Massively distributed, replicated storage system

Permacoin

Assume we have a large file **F** to store

For simplicity: **F** is chosen globally, at the beginning, by a trusted dealer

Each user stores a *random subset* of the file

Storage-based puzzle

1. Build a Merkle tree, where each leaf is a segment of the file

 F_2 F_4

2. Generate a public signing key pk, which determines a random subset of file segments

F₁ F₂ F₄ F₅

- 3. Each mining attempt:
- a) Select a random nonce
- b) h1 := H(prev || mrkl_root || PK || nonce)
- c) h1 selects k segments from subset
- d) h2 := H(prev || mrkl root || PK || nonce || F)
- e) Winner if h2 < TARGET

