## Bigram LLM Model

August 8, 2023

## 1 Bigram Model

The "Attention Is All You Need" paper introduced the revolutionary Transformer architecture, which has since become a cornerstone in modern NLP. This project aims to leverage the Transformer's attention mechanisms to build a bigram language model that predicts the next word in a sentence given the previous words.

```
[]: # Checking CUDA (GPU)
  !nvidia-smi
  Fri Apr 14 10:29:18 2023
  +----+
  |-----
             Persistence-M | Bus-Id Disp.A | Volatile Uncorr. ECC |
  | Fan Temp Perf Pwr:Usage/Cap| Memory-Usage | GPU-Util Compute M. |
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    0 Tesla T4
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  | Processes:
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    No running processes found
  +-----+
[]: import torch
  import torch.nn as nn
  from torch.nn import functional as F
  torch.cuda.is_available()
```

[ ]: True

## 2 Preprocessing and Data Loading

```
[]: # Download Data
     !wget https://raw.githubusercontent.com/karpathy/char-rnn/master/data/
      →tinyshakespeare/input.txt
     filename = '/content/drive/MyDrive/Colab Notebooks/content/shakespeareInputLLM.
     with open(filename, 'r', encoding='utf-8') as f:
         text = f.read()
[]: # Create vocabulary
     torch.manual_seed(1337)
     chars = sorted(list(set(text)))
     vocab size = len(chars)
     # create a mapping from characters to integers
     stoi = { ch:i for i,ch in enumerate(chars) }
     itos = { i:ch for i,ch in enumerate(chars) }
     encode = lambda s: [stoi[c] for c in s] # encoder: take a string, output a list_{\sqcup}
      ⇔of integers
     decode = lambda 1: ''.join([itos[i] for i in 1]) # decoder: take a list of
      ⇒integers, output a string
[]: # Train and test splits
     data = torch.tensor(encode(text), dtype=torch.long)
     n = int(0.9*len(data)) # first 90% will be train, rest val
     train data = data[:n]
     val_data = data[n:]
[]: # Data loading
     def get_batch(split):
         \# generate a small batch of data of inputs x and targets y
         data = train_data if split == 'train' else val_data
         ix = torch.randint(len(data) - block_size, (batch_size,))
         x = torch.stack([data[i:i+block_size] for i in ix])
         y = torch.stack([data[i+1:i+block_size+1] for i in ix])
         x, y = x.to(device), y.to(device) # sending data to device (cpu or gpu)
         return x, y
[]: | # Define hyperparameters
     batch_size = 64 # how many independent sequences will we process in parallel?
     block size = 256 # what is the maximum context length for predictions?
     max_iters = 5000
     learning rate = 3e-4 #self-attention can't tolerate high lr
     device = 'cuda' if torch.cuda.is_available() else 'cpu' # if you have gpu, run_
      \hookrightarrow on it
     eval_interval = 500
```

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eval_iters = 200
n_embd = 384
n_head = 6
n_layer = 6
dropout = 0.2
```

```
[]: # Let's estimate the loss every few epochs
     @torch.no_grad()
     def estimate_loss():
         out = \{\}
             Instead of evaluating the model every iter,
             we Evaluate every eval_interval based on what the model has been ⊔
      \hookrightarrow trained so far
         model.eval() # Switch to Evaluation mode
         for split in ['train', 'val']:
             losses = torch.zeros(eval_iters)
             for k in range(eval_iters):
                 X, Y = get_batch(split)
                 logits, loss = model(X, Y)
                 losses[k] = loss.item()
             out[split] = losses.mean()
         model.train() # Switch to Training mode
         return out
```

## 3 Transformer Architecture

```
[]: # Self-Attention
class Head(nn.Module):
    """ one head of self-attention """

def __init__(self, head_size):
    super().__init__()
    self.head_size = head_size
    self.key = nn.Linear(n_embd, head_size, bias=False)
    self.query = nn.Linear(n_embd, head_size, bias=False)
    self.value = nn.Linear(n_embd, head_size, bias=False)
    self.register_buffer('tril', torch.tril(torch.ones(block_size,_u))) #tril is not a parameter to be optimized

self.dropout = nn.Dropout(dropout)

def forward(self, x):
    B, T, C = x.shape
    k = self.key(x) # (B, T, head_size)
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q = self.query(x) # (B, T, head_size)
        v = self.value(x) # (B, T, head_size)
        # compute attention scores ("affinities")
        wei = (q @ k.transpose(-2, -1)) * self.head_size**-0.5 # (B, T, )
 \hookrightarrow head_size) @ (B, head_size, T) -> (B, T, T) # Notice it has changed to \sqcup
 ⇔(Block_size, BLock_size)
        wei = wei.masked_fill(self.tril[:T, :T] == 0, float('-inf')) # in lower__
 → traiangular matrix filled with 1's on lower left and 0's on upper right, well
 →are replacing 0's with '-inf' # (B, T, T)
        wei = F.softmax(wei, dim=-1) # (B, T, T)
        wei = self.dropout(wei)
        # perform weighted aggregation of values
        out = wei @ v # (B, T, T) @ (B, T, head_size) -> (B, T, head_size) ==_
 \hookrightarrow (B, T, n_embd) if num_heads = 1
        return out
class MultiHeadAttention(nn.Module):
    """ multiple heads of self-attention in parallel """
    def __init__ (self, num_heads, head_size):
        super(). init ()
        self.heads = nn.ModuleList([Head(head_size) for _ in range(num_heads)])
        self.proj = nn.Linear(n embd, n embd)
        self.dropout = nn.Dropout(dropout)
    def forward(self, x):
        out = torch.cat([h(x) for h in self.heads], dim=-1) # (B, T, ___
 \Rightarrowhead_size*4) == (B, T, n_embd)
        out = self.proj(out) # we are doing Linear transformation of the output ⊔
 \hookrightarrow from self-attention
        out = self.dropout(out)
        return out
class FeedForward(nn.Module):
    """ Simple Linear Layer followed by Non-Linearity"""
    def __init__(self, n_embd):
        super().__init__()
        self.net = nn.Sequential(
            nn.Linear(n embd, 4* n embd), # making ouput of Linear 4 times, as ...
 ⇔suggested in paper
            nn.ReLU(),
            nn.Linear(4 * n_embd, n_embd), # self.proj # here again making_
 →ouput of Linear n_embd, as suggested in paper
            nn.Dropout(dropout)
```

```
def forward(self, x):
        return self.net(x)
class Block(nn.Module):
    """ Transformer Decoder Block: communication followed by computation """
    def __init__(self, n_embd, n_head):
        super().__init__()
        \# n_{embd}: embedding dimension, n_{embd}: the number of heads we'd like
        # Self Attention
        head_size = n_embd // n_head
        self.sa_heads = MultiHeadAttention(n_head, head_size)
        # Feed Forward
        self.ffwd = FeedForward(n_embd)
        # Layer Norms
        self.ln1 = nn.LayerNorm(n_embd) # making Unit Gaussians
        self.ln2 = nn.LayerNorm(n_embd)
    def forward(self, x):
        x = x + self.sa_heads(self.ln1(x)) # in original paper the layernorm is_{\square}
 →applied after the computation, though overtime it has become more common tou
 →apply it before the computaion
        x = x + self.ffwd(self.ln2(x))
        return x
class BigramLanguageModel(nn.Module):
    '''super simple bigram model - Decoder-only Transformer'''
    def __init__(self):
        super().__init__()
        # Each word or token will be represented by an n_embd-dimensional \sqcup
 ⇔embedding vector.
        self.token_embedding_table = nn.Embedding(num_embeddings=vocab_size,_
 →embedding_dim=n_embd)
        # We don't just want to encode the identity of token, but also its_\sqcup
 \rightarrowposition
        self.position_embedding_table = nn.Embedding(num_embeddings=block_size,_
 →embedding_dim=n_embd)
        # Decoder Block Component
        self.blocks = nn.Sequential(*[Block(n embd, n head=n head) for _ in_
 →range(n_layer)])
        # Layer Norm
        self.ln_f = nn.LayerNorm(n_embd) # final layer norm
        # Applies a linear transformation to the incoming data: :math: y = x C_{\sqcup}
 \hookrightarrow W.T + b
        self.lm_head = nn.Linear(in_features=n_embd, out_features=vocab_size)
```

```
def forward(self, idx, targets=None):
      B, T = idx.shape
       # idx and targets are both (B,T) tensor of integers
      tkn_emb = self.token_embedding_table(idx) # (B,T,C)
       # range(0, T):: Every position will have n_embd-dimensional embedding_
⇒vector.
      pos_emb = self.position_embedding_table(torch.arange(T, device=device))__
\hookrightarrow# (T,C)
       # x now, not just hold token identity but also its position
      x = tkn_emb + pos_emb # (B, T, C)
       # Block component
      x = self.blocks(x) # (B, T, C)
       # final layer norm
      x = self.ln_f(x) # (B, T, C)
       # Making Logits
      logits = self.lm_head(x) # (B, T, vocab_size)
       if targets is None:
           loss = None
       else:
           B, T, C = logits.shape # (B, T, vocab_size)
           logits = logits.view(B*T, C) # (B*T, vocab_size)
           targets = targets.view(B*T)
           loss = F.cross_entropy(logits, targets)
      return logits, loss
  def generate(self, idx, max_new_tokens):
       # idx is (B, T) array of indices in the current context
       for _ in range(max_new_tokens):
           # as we are implementing position embedding (pos emb), we can t_{\sqcup}
→include context more than block_size
           # crop idx to the last block size token
           idx_cond = idx[:, -block_size:] # (B, block_size) == (B, T)
           # get the predictions
           logits, _ = self(idx_cond) #forward()
           # focus only on the last time step
           logits = logits[:, -1, :] # becomes (B, 1, C) == (B, C)
           # apply softmax to get probabilities
           probs = F.softmax(logits, dim=-1) \# (B, 1, C) == (B, C)
```

```
# sample from the distribution
             idx_next = torch.multinomial(probs, num_samples=1) # (B, 1)
             # append sampled index to the running sequence
             idx = torch.cat((idx, idx_next), dim=1) # (B, T+1)
        return idx
# Build Model
model = BigramLanguageModel()
m = model.to(device)
# create a PyTorch optimizer
optimizer = torch.optim.AdamW(model.parameters(), lr=learning_rate)
# Epochs
for iter in range(max_iters):
    # After every eval interval iters, evaluate the loss on train and val sets
    if (iter % eval_interval == 0) or (iter==max_iters-1):
        losses = estimate_loss()
        print(f"step {iter}: train loss {losses['train']:.4f}, val loss⊔

{losses['val']:.4f}")
    # sample a batch of data
    xb, yb = get_batch('train') # (B, T)
    # train model
    logits, loss = model.forward(xb, yb)
    optimizer.zero_grad(set_to_none=True)
    loss.backward()
    optimizer.step()
# Generate next word using the model
context = torch.zeros((1, 1), dtype=torch.long, device=device) # (B=1, T=1)
print(decode(m.generate(context, max_new_tokens=500)[0].tolist()))
step 0: train loss 4.2846, val loss 4.2820
step 500: train loss 1.8865, val loss 2.0023
step 1000: train loss 1.5361, val loss 1.7221
step 1500: train loss 1.3948, val loss 1.6038
step 2000: train loss 1.3077, val loss 1.5490
step 2500: train loss 1.2523, val loss 1.5153
step 3000: train loss 1.2010, val loss 1.4894
```

step 3500: train loss 1.1587, val loss 1.4800 step 4000: train loss 1.1222, val loss 1.4800 step 4500: train loss 1.0853, val loss 1.4736 step 4999: train loss 1.0494, val loss 1.4913

```
But with price of a breast sast-creature.
    Of whom, Cariolanus: of God! what's Romeo?
    Third Consciden:
    Mistress, let's proceed. Go to me, go: I say.
    CAMILLO:
    By my lord, I'll braw a light:
    I have bore alone death.
    SLY:
    If you would I wish vengeance me when I was off
    these advancementary; this to fled till
    I clear thee join till ar outrain, thou art to me;
    And, not many hath punishmen.
    SLY:
    They Gentleman, I have deliver'd by thus leave
    He known I dissevel to you!
    Lord:
    Lords, am I though for
[]: print("Total Number of Parameters:", sum(p.numel() for p in m.parameters()))
    Total Number of Parameters: 10788929
[]: # Save the model
     PATH = '/content/drive/MyDrive/Colab Notebooks/content/BigramModel.pth'
     torch.save(m, PATH)
[]:
```