



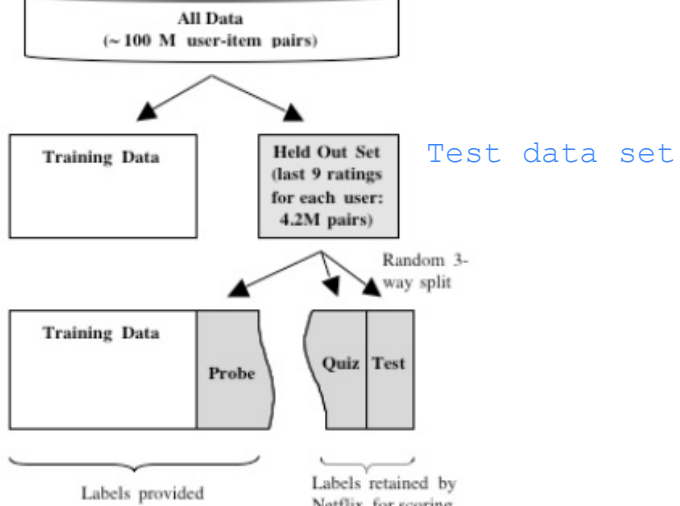
# Cross validation

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```

graph LR
    A["All Data  
(~ 100 M user-item pairs)"] --> B["Training Data  
(100 M user-item pairs)"]
    A --> C["Test Data  
(100 M user-item pairs)"]
    B --> D["Training Data  
(100 M user-item pairs)"]
    B --> E["Validation Data  
(100 M user-item pairs)"]
  
```



# Key idea

1. Accuracy on the training set (resubstitution accuracy) is optimistic
2. A better estimate comes from an independent set (test set accuracy)
3. But we can't use the test set when building the model or it becomes part of the training set
4. So we estimate the test set accuracy with the training set. using Cross validation

# Cross-validation

*Approach:*

1. Use the training set
2. Split it into training/test sets `i.e. we split it again!`
3. Build a model on the training set `a subset of the original training set`
4. Evaluate on the test set `a subset of the original training set`
5. Repeat and average the estimated errors

*Used for:* `so the original test set is never used.`

1. Picking variables to include in a model
2. Picking the type of prediction function to use
3. Picking the parameters in the prediction function
4. Comparing different predictors

# Random subsampling

this is only still  
from the original  
training set

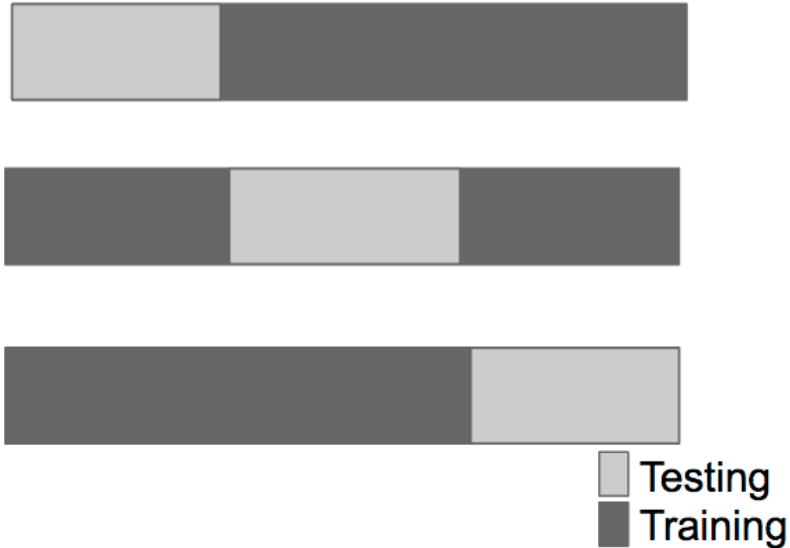
different runs,  
in the end:  
averaging the  
errors



Testing  
Training

# K-fold

break training set up into k equal sized sets.





# Leave one out



predict only one in  
each run.



 Testing  
 Training

# Considerations

- For time series data data must be used in "chunks" because time  $t$  might depend on time  $t-1$  (or  $-2, \dots$ )
- For k-fold cross validation
  - Larger  $k$  = less bias, more variance bias=ungenaues Modell – under fitting
  - Smaller  $k$  = more bias, less variance variance=zu genaues Modell – over fitting
- Random sampling must be done *without replacement*
- Random sampling with replacement is the *bootstrap*
  - Underestimates of the error
  - Can be corrected, but it is complicated ([0.632 Bootstrap](#))
- If you cross-validate to pick predictors estimate you must estimate errors on independent data.