

## → Time complexity

3

Generally in coding contests : no. of iterations  
in 1 sec  $\Rightarrow 10^7 - 10^8$

$\therefore 10^7 \rightarrow 1 \text{ sec}$

$10^8 \rightarrow 10 \text{ sec}$

$10^9 \rightarrow 100 \text{ sec}$

$10^{10} \rightarrow 1000 \text{ sec}$

$10^{11} \rightarrow 10000 \text{ sec}$

```

→ INT x; // O(1)
   INT sum = 0; // O(1)
   sum = x * x; // O(1)

```

No. of iterations = 3  $\therefore O(1) + O(1) + O(1)$   
 $\Rightarrow O(3) \approx O(1)$

```

→ INT x; // O(1)
   INT sum = 0; // O(1)
   sum = x * x; // O(1)
   INT n; // O(1)
   cin >> n; // O(1)
   for (INT i = 0; i < n; ++i) {
       INT y; // O(n)
       y = 5; // O(n)
       y++; // O(n)
   }
}

```

Total time complexity:  $O(5) + O(3n) \approx O(n)$

```

→ for (INT i = 0; i < n; ++i) {
    cin >> temp; // O(n)
}
for (INT i = 0; i < n; ++i) {
    cin >> temp2; // O(n)
}
for (INT i = 0; i < n; ++i) {
    cin >> temp3; // O(n)
}

```



Total time complexity :  $O(n) + O(n) + O(n) \approx O(n)$

```

-> FOR (int i=0; i<n; ++i) {
    FOR (int i=0; i<n; ++i) {
        C[N][i] // O(n^2)
    }
}

```

Total time complexity :  $O(n^2)$

```

-> int n;
    cin >> n; // let n = 10^5
    while (n > 0) {
        n = n/2;
    }

```

Total time complexity : e.g :  $n = 10$   
 $10 \rightarrow 5 \rightarrow 2 \rightarrow 1 \rightarrow 0$   
 3 Iterations

If  $n = 20$

$20 \rightarrow 10 \rightarrow 5 \rightarrow 2 \rightarrow 1 \rightarrow 0$   
 4 Iterations

If  $n = 100$

$100 \rightarrow 50 \rightarrow 25 \rightarrow 12 \rightarrow 6 \rightarrow 3 \rightarrow 1 \rightarrow 0$   
 6 Iterations

Let  $a$  is the no. of times we can divide  $n$  to make it zero (0).

$$2^a = n$$

$$\log_2(2^a) = \log_2(n)$$

$$a \log_2 2 = \log_2(n)$$

$\therefore a = \log_2(n)$   $\rightarrow$  This is the best time complexity we can have.

eg if  $n = 10^5$

$$\begin{aligned}\therefore \log_2(10^5) &= 5 \times \log_2(10) \\ &= 5 \times 3 \\ &= \underline{\underline{15 \text{ iterations}}}\end{aligned}$$