

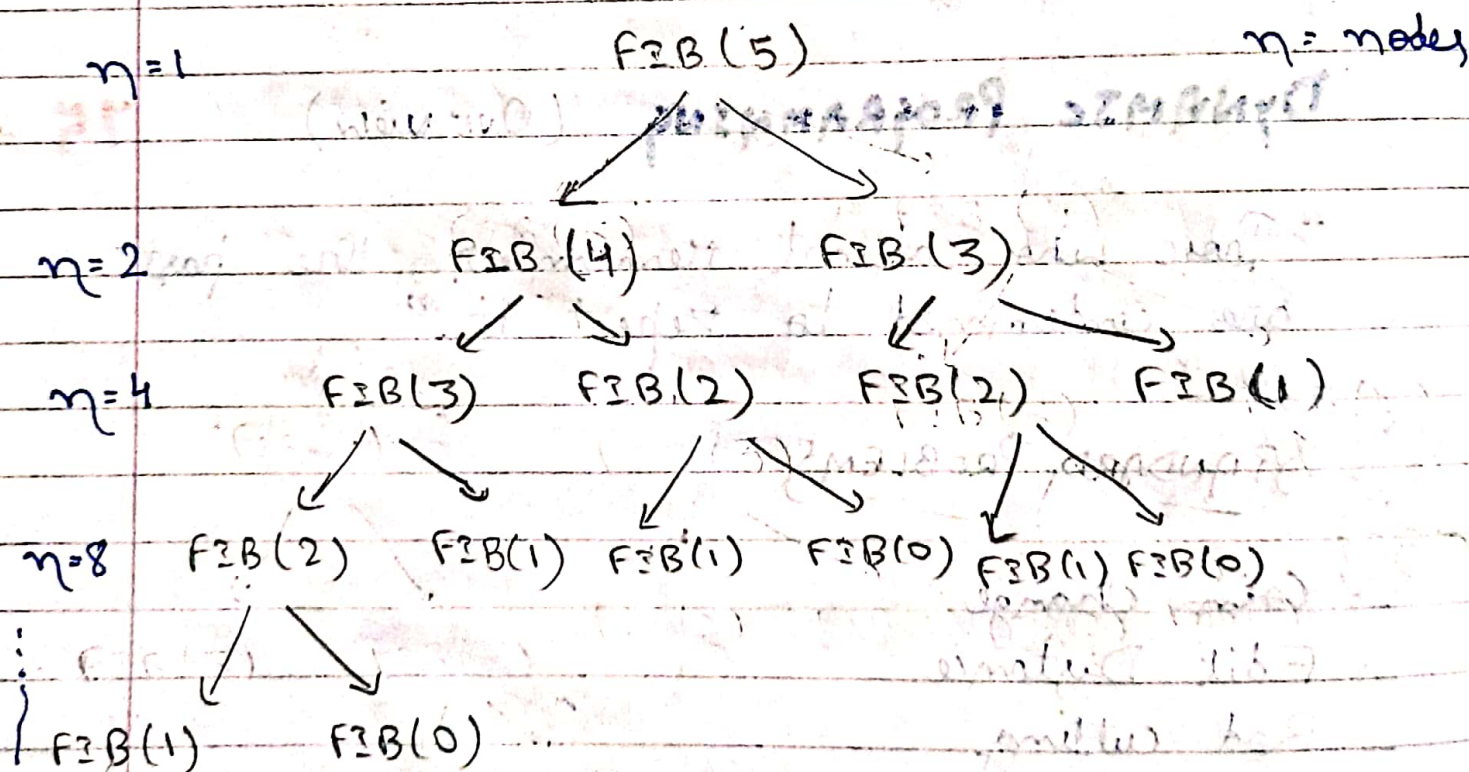
INTRODUCTION TO DYNAMIC PROGRAMMING ...

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FIBONACCI SERIES: 0 1 1 2 3 5 8

In the simple recursive function of Fibonacci series ($FIB(n)$).
 $FIB(n)$ gives n^{th} Fibonacci number.

Its Recursion Tree: For: $FIB(5)$



Here, we can see no. of calls in this Recursion tree is increasing exponentially

$$1, 2, 4, 8, \dots, 2^{n-1}$$
$$S_n = 1(2^n - 1)$$
$$S_n = \frac{2^n - 1}{2 - 1}$$

∴ It's Time complexity is: $O(2^n)$

∴ We can compute till $n=20$ in normal recursive function of Fibonacci series, ~~or~~ if we Tse n any more it will give TLE.

→ But with Dynamic Programming using memoisation technique, we will reduce P.C ~~to~~ to $O(n)$.

→ In this technique we try to remember what we have computed by far and use it for further computation, instead calculating the whole thing again.

e.g: Let's suppose we are computing $FIB(5)$, in its recursion tree we can see we are computing $FIB(3)$ twice, but we will only compute it once and store it to use it further directly.

∴ With DP we can compute n upto 10^6

→ Top Down Approach: Bade problems ko chote mai todke use solve krna, usually with recursion.

→ Bottom Up Approach: Chote problems ko compute krte hue use bdi problems solve krna.

CODE

```
CONST INT N = 1e5 + 10;
INT DP[N];
```

→ Top Down Approach

```
INT FIB (INT n)
{
```

```
    IF (n == 0) RETURN 0;
```

```
    IF (n == 1) RETURN 1;
```

```
    IF (DP[n] != -1) RETURN DP[n];
```

```
    → memoize
    RETURN DP[n] = FIB(n-1) + FIB(n-2);
```

```
}
```

```
INT MAIN ()
{
```

```
    MEMSET (DP, -1, sizeof (DP)); // memset
    // function to store array with same
    // default value here with -1
```

```
    INT n;
```

```
    CIN >> n;
```

```
    cout << FIB (n) << "\n";
```

```
    RETURN 0;
```

```
}
```