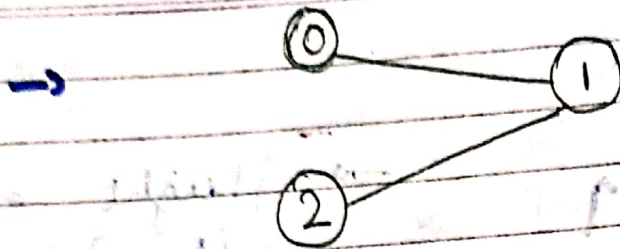


## HOW TO REPRESENT TREES AND GRAPHS IN CODE

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→ Adjacency Matrix : In this we create a  $V \times V$  ( $V = \text{Vertex}$ ) matrix.

→ Adjacency Matrix of Undirected graph:



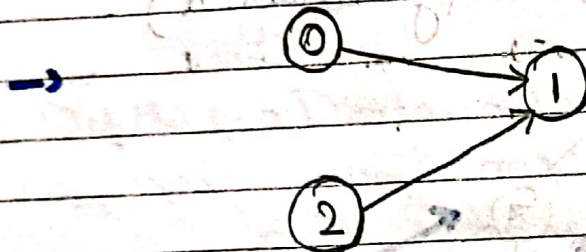
$V=3, E=2$

	0	1	2
0	0	1	0
1	1	0	1
2	0	1	0

If  $i, j$  is connected:  
 $a[i][j] = 1$

else:  
 $a[i][j] = 0$

→ Adjacency matrix of directed graph:



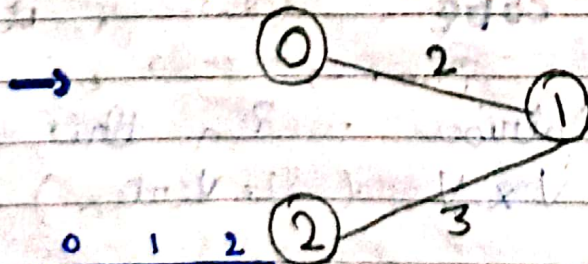
$V=3, E=2$

	0	1	2
0	0	1	0
1	0	0	0
2	0	1	0

If  $i, j$  is connected:  
 $a[i][j] = 1$

else:  
 $a[i][j] = 0$

→ Adjacency matrix of undirected weighted graph:



$V=3, E=2$

	0	1	2
0	0	2	0
1	2	0	3
2	0	3	0

If  $i, j$  is connected:  
 $a[i][j] = \text{weight}$

else:  
 $a[i][j] = 0$



→ General input we get in graph's questions:

First line contains  $n, m$ , where  $n$  = vertices,  $m$  = edges.

Then the following  $m$  lines contains configurations (connections) of edges.

e.g.:

$n$	$m$
1	2
2	3
3	4

Here,  $n = 4$  &  $m = 3$   
(It denotes an edge b/w 1 & 2)

### ADJACENCY MATRIX

### CODE

CONST int N = 1e3 + 10; → Let's suppose we can have a max of  $10^3$  vertices.

→ Initializing an Adjacency matrix of  $N, N$ .  
And as it is declared globally, it will automatically be initialized with all 0 values.

```
int GRAPH[N][N];
```

```
int MAIN()
```

```
{
```

```
    int n, m; → vertices and edges resp.
```

```
    cin >> n >> m;
```

```
for (int i = 1; i ≤ m; i++) {
```

```
    int v1, v2;
```

```
    cin >> v1 >> v2;
```

→ Undirected graph

```
    graph[v1][v2] = 1;
```

```
    graph[v2][v1] = 1;
```

```
}
```

→ But, there is an issue with this approach:

→  $O(N^2)$  space complexity.

→ And if we get a  $N$  with  $10^5$  then  $N \times N$  will be  $10^{10}$ , which is out of limit for an array, an array can store a maximum of  $10^6 - 10^7$  capacity of values.

→ So, to represent large capacity of  $N$ , we use Adjacency lists.

```
return 0;
```

```
}
```

INPUT :

6 9

1 3

1 5

3 5

3 4

3 6

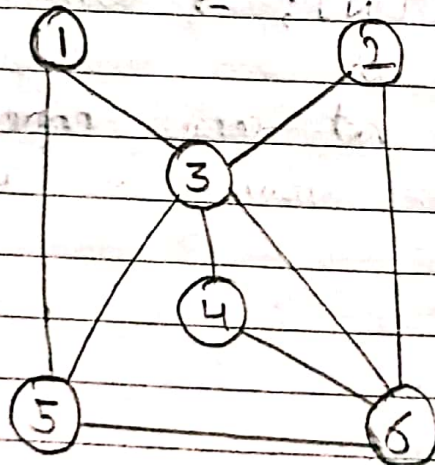


3 2  
2 6  
4 6  
5 6

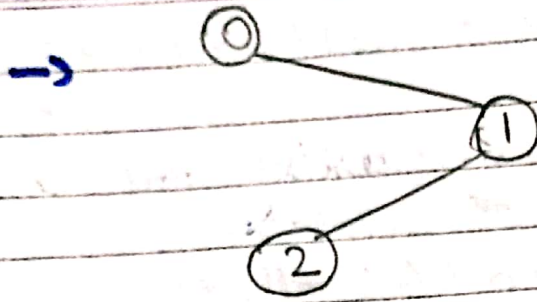
Output:

0 0 1 0 1 0  
0 0 1 0 0 1  
1 1 0 1 1 1  
0 0 1 0 0 1  
1 0 1 0 0 1  
0 1 1 1 1 0

→ It will look something like this:



→ Adjacency list: In this if a graph has  $V$  vertices, then it will contain  $V$  no. of lists (e.g: If 3 vertices then 3 lists) And each list will contain its connected vertices (edges).



Its adjacency list will be:

0 → 1

1 → 0, 2

2 → 1

(Its space complexity is  $O(V+E)$ )

### ADJACENCY LIST

### CODE

const int N = 1e3 + 10;  
vector<int> GRAPH[N]; → Vector of arrays  
Here, GRAPH[0] is an array which  
will contain its connected edges.

```
int main()
{
```

```
    int n, m;
```

```
    cin >> n >> m;
```

```
    for (int i=1; i<=m; i++)
    {
```

```
        int v1, v2;
```

```
        cin >> v1 >> v2;
```

```
        GRAPH[v1].pb(v2);
```

```
        GRAPH[v2].pb(v1);
```



→ Time Complexity  $\Rightarrow O(N + M)$

```
    RETURN 0;
}
```

**NOTE:** If we have to store weighted undirected graph in Adjacency list, then we will do slight changes in our previous code:

→ Now we will take vector of pair instead of vector of arrays:

```
VECTOR < PAIR < INT, INT > > GRAPH[N];
```

→ And we will store pairs now with weights like this:

```
GRAPH[V1].PB ({ V2, wt });
GRAPH[V2].PB ({ V1, wt });
```