

UMEÅ UNIVERSITY
Department of computer science
Lab report

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Laboratory 5
Modelling and Simulation 7.5hp

ODE using GSL-library

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1 Exercise 1

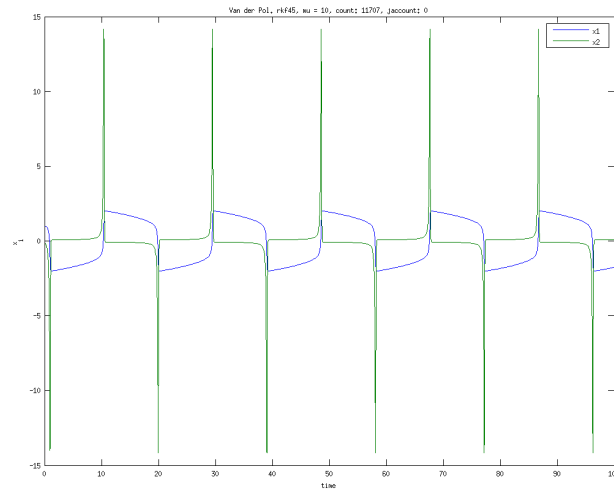


Figure 1: Van der Pol model. Solved using rkf45 with parameter $\mu = 10$.

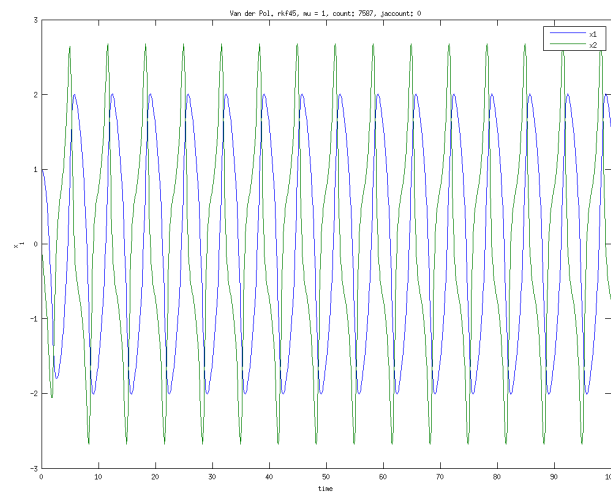


Figure 2: Van der Pol model. Solved using rkf45 with parameter $\mu = 1$.

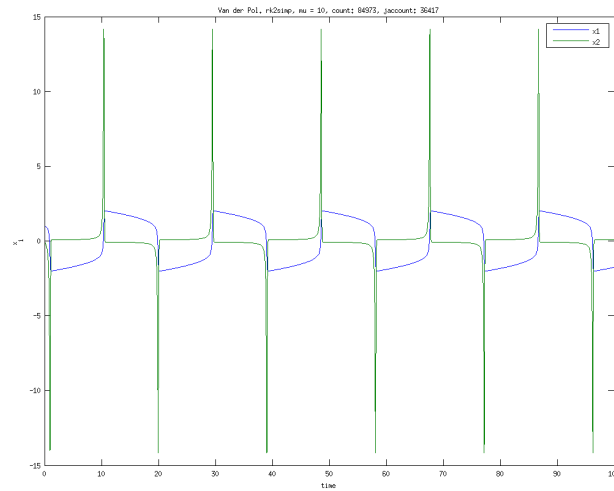


Figure 3: Van der Pol model. Solved using rk2simp with parameter $\mu = 10$.

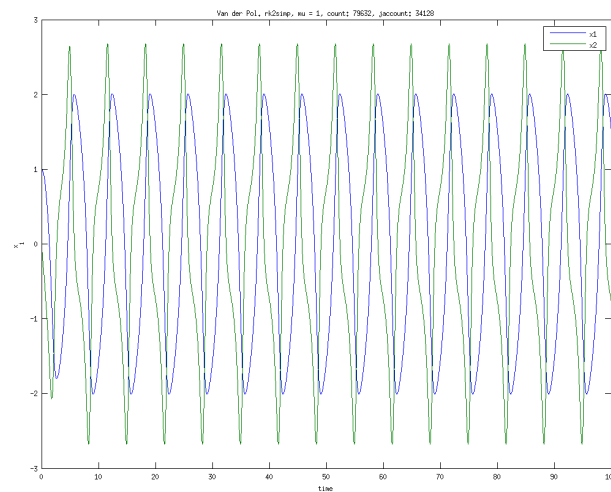


Figure 4: Van der Pol model. Solved using rk2simp with parameter $\mu = 1$.

2 Exercise 2

The efficiency was about double as fast in the C implementation compared with the matlab implementation. And in the C implementation the rk4imp was better. The times were: 0.92 seconds from matlab using ode23s; 0.623 seconds in C using rk2imp; and 0.419 seconds in C using rk4imp.

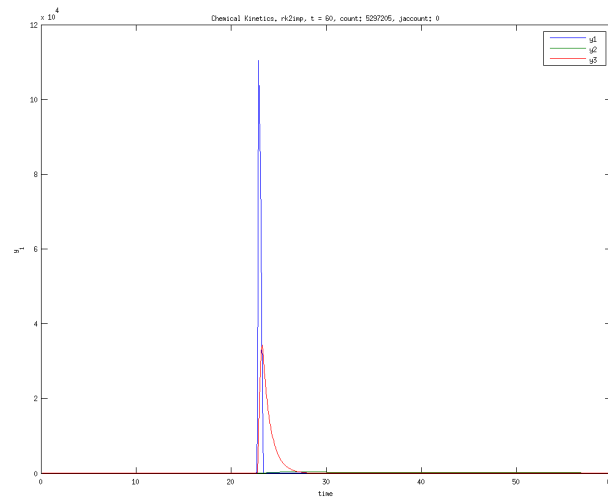


Figure 5: Chemical kinetics. Solved using rk2imp integrating from $t = 0$ to $t = 60$.

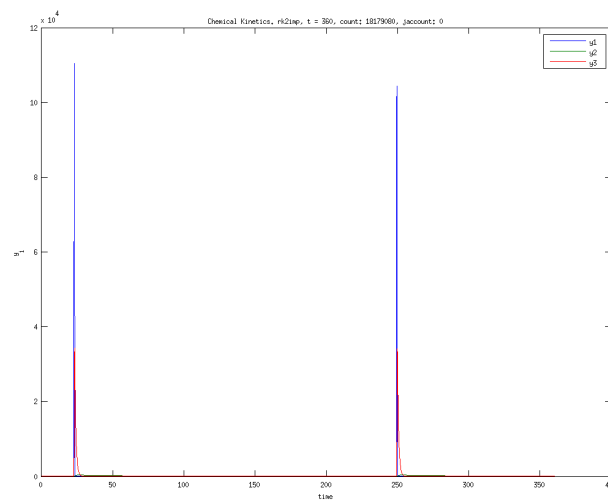


Figure 6: Chemical kinetics. Solved using rk2imp integrating from $t = 0$ to $t = 360$.

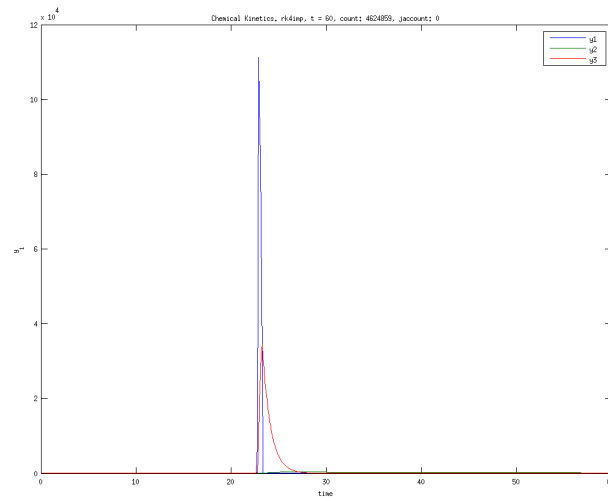


Figure 7: Chemical kinetics. Solved using rk4imp integrating from $t = 0$ to $t = 60$.

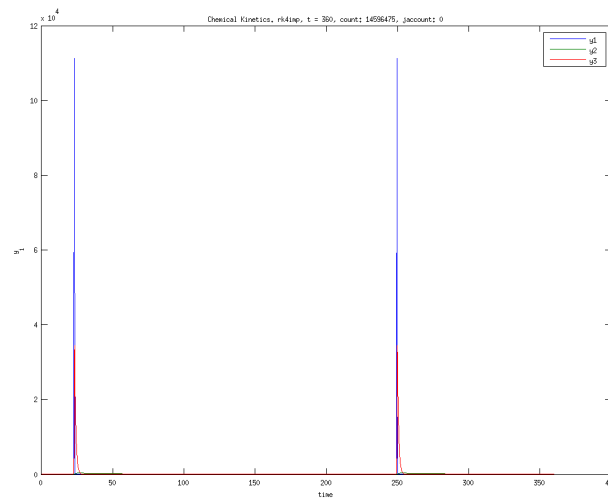


Figure 8: Chemical kinetics. Solved using rk4imp integrating from $t = 0$ to $t = 360$.

3 Exercise 3

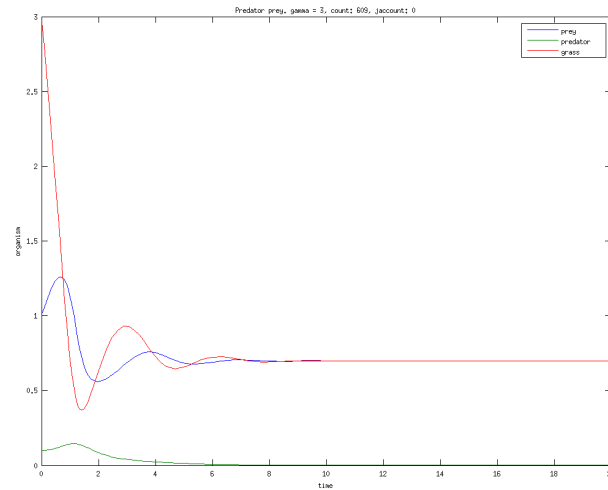


Figure 9: Predator prey. Solved using rkf45 with parameter $\gamma = 3$.

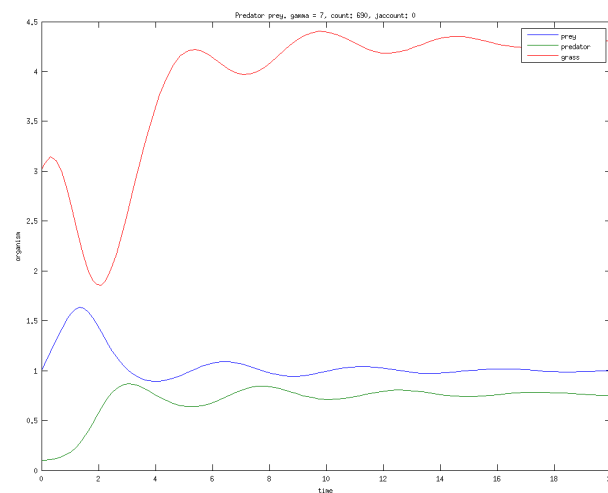


Figure 10: Predator prey. Solved using rkf45 with parameter $\gamma = 7$.

Lower gamma reaches steady state faster. Higher gamma increases predator population more than prey. At $\gamma=3$ the predator population actually dies out. This is using the extra term with g_{\max} .

If we leave out the g_{\max} term in the grass equation. The grass will grow without bounds for large enough gamma, see fig. 11

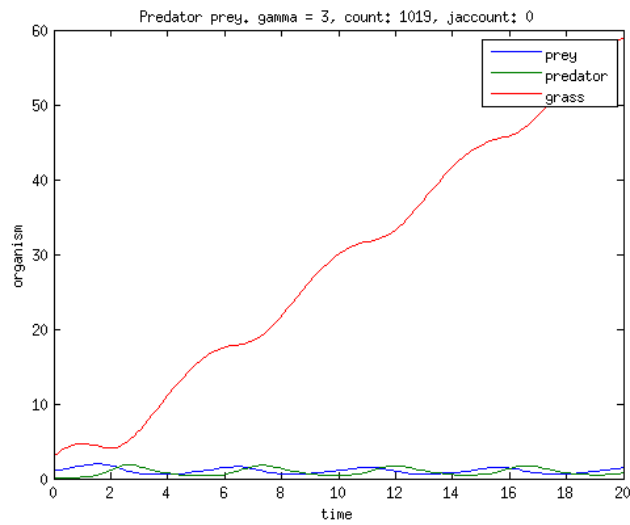


Figure 11: Predator prey. Solved using rkf45 with parameter $\gamma = 7$ but without gmax term in the grass equation.

4 Exercise 4

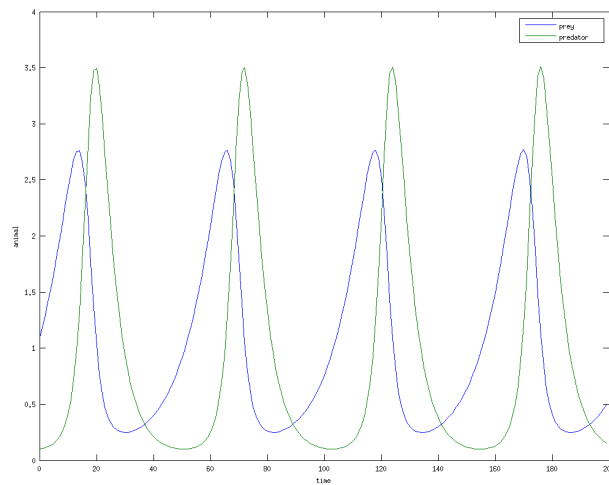


Figure 12: A predator-prey model. Solved using symplectic Euler A.